

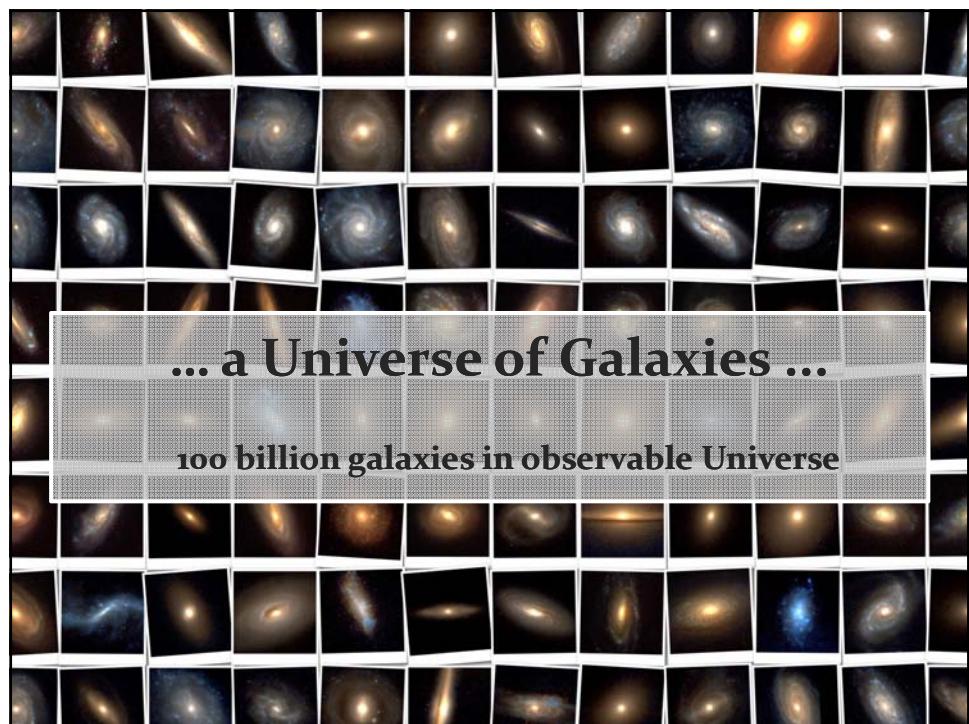
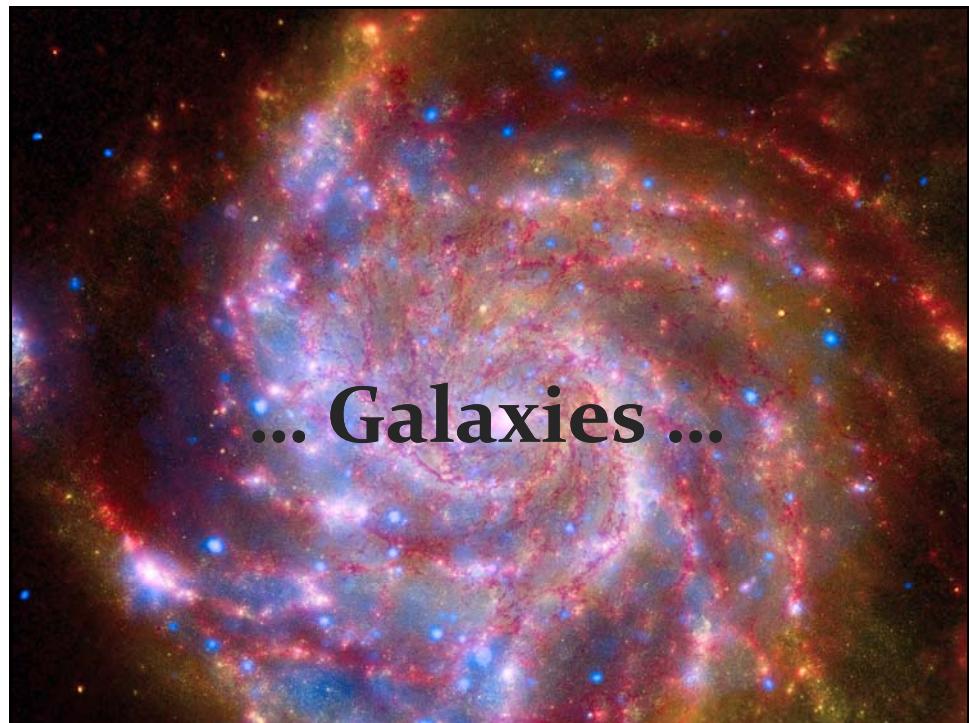
# Cosmic Web: Galaxies along spatial patterns

## Map of the Universe

How to map the structures and patterns in the Universe ?

- Use galaxies as beacons
- Map of Galaxy positions
- Tracing of structures from distribution of galaxies

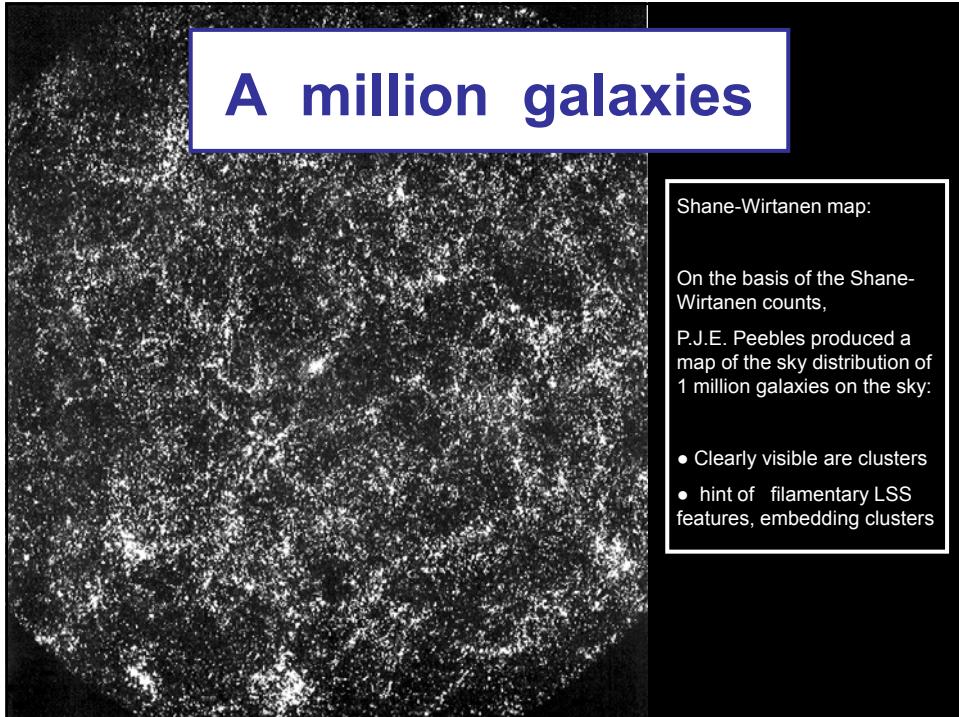


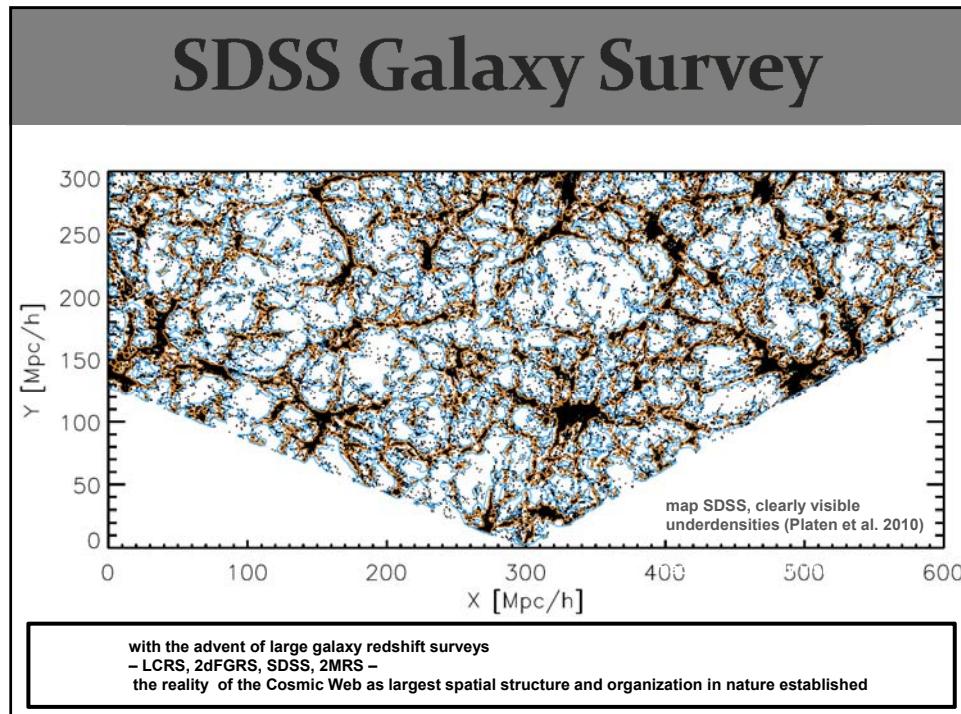
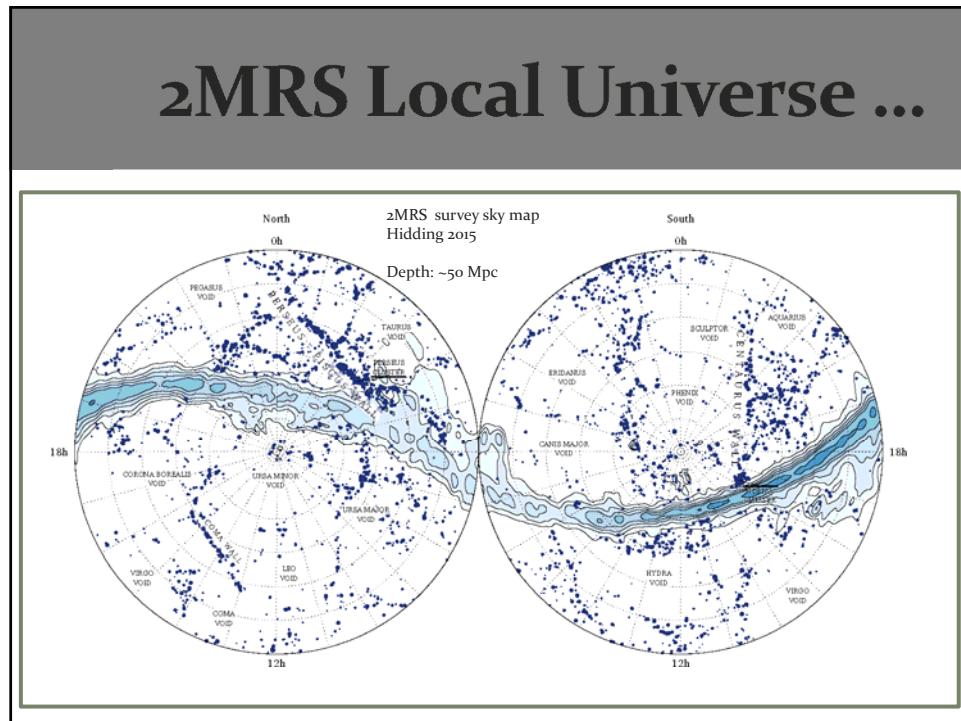


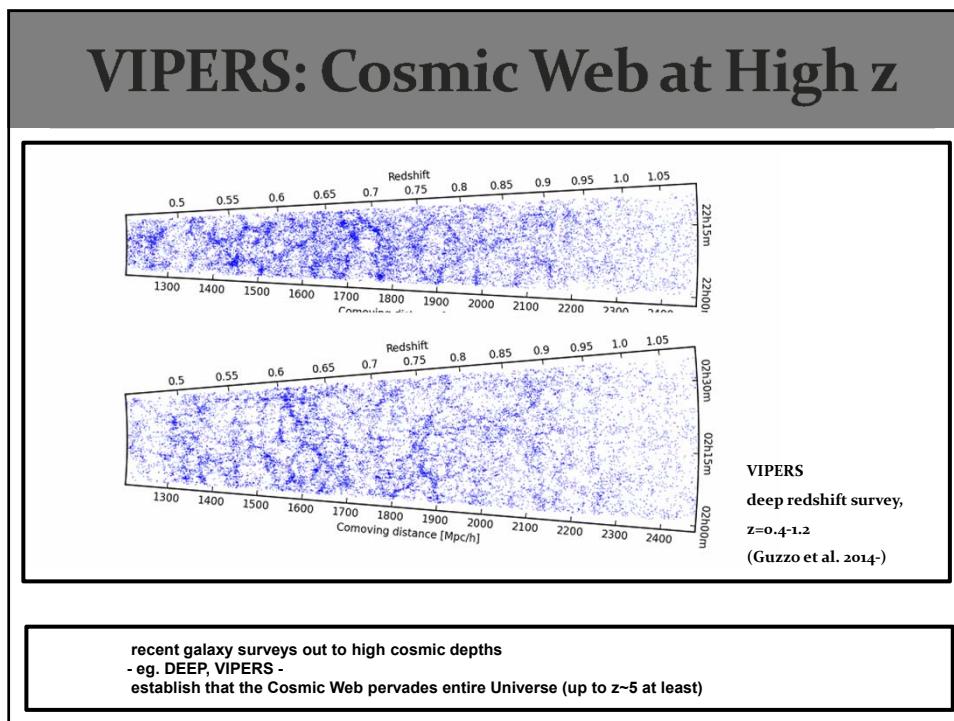
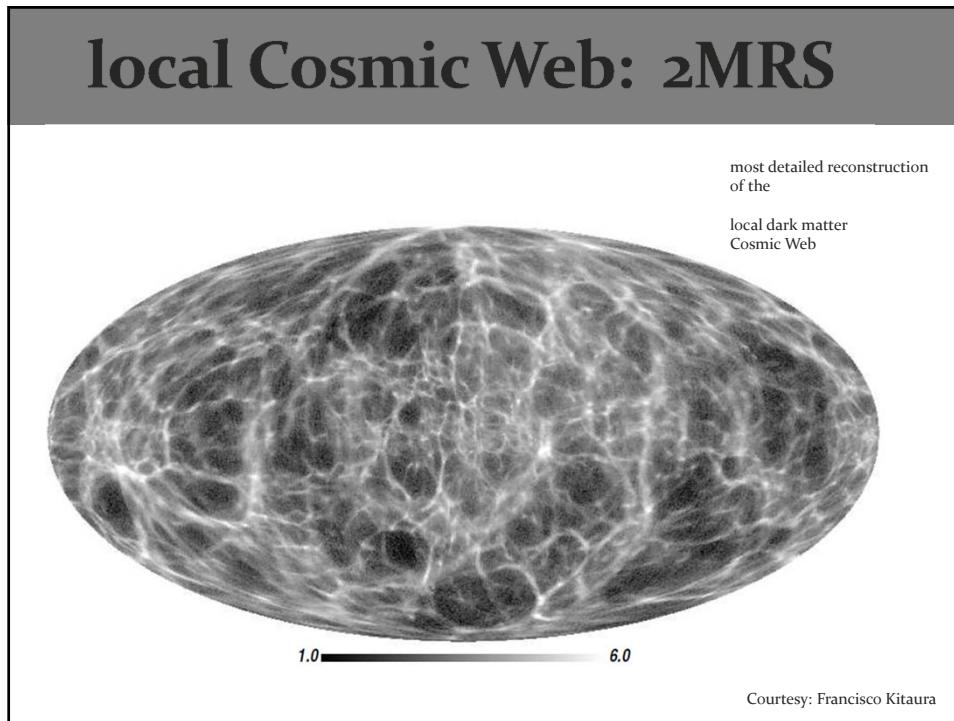
# Clusters of Galaxies



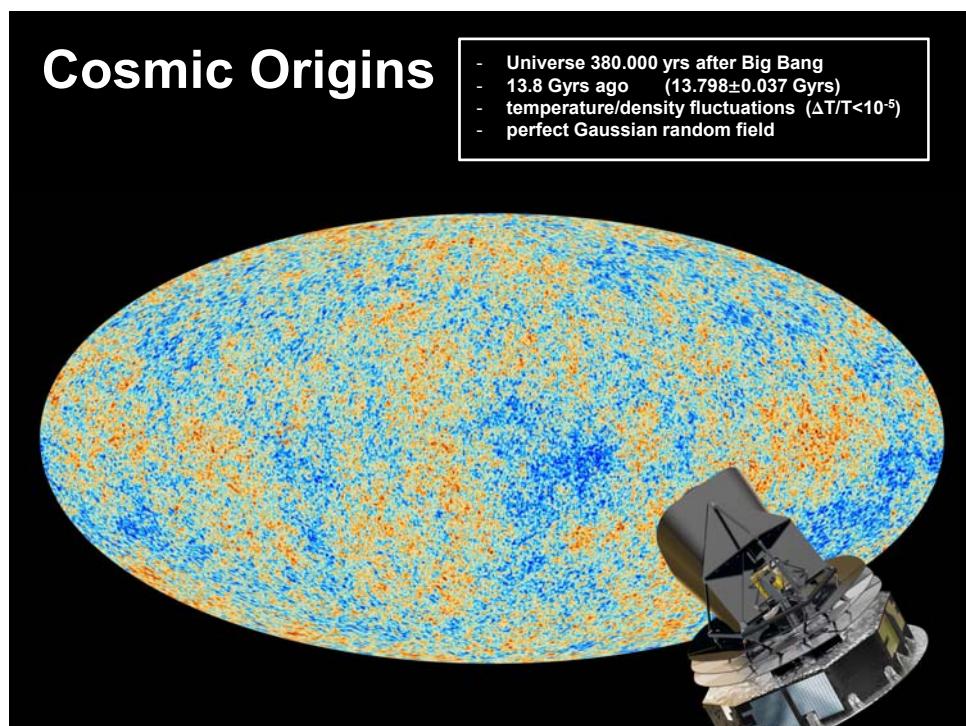
A million galaxies

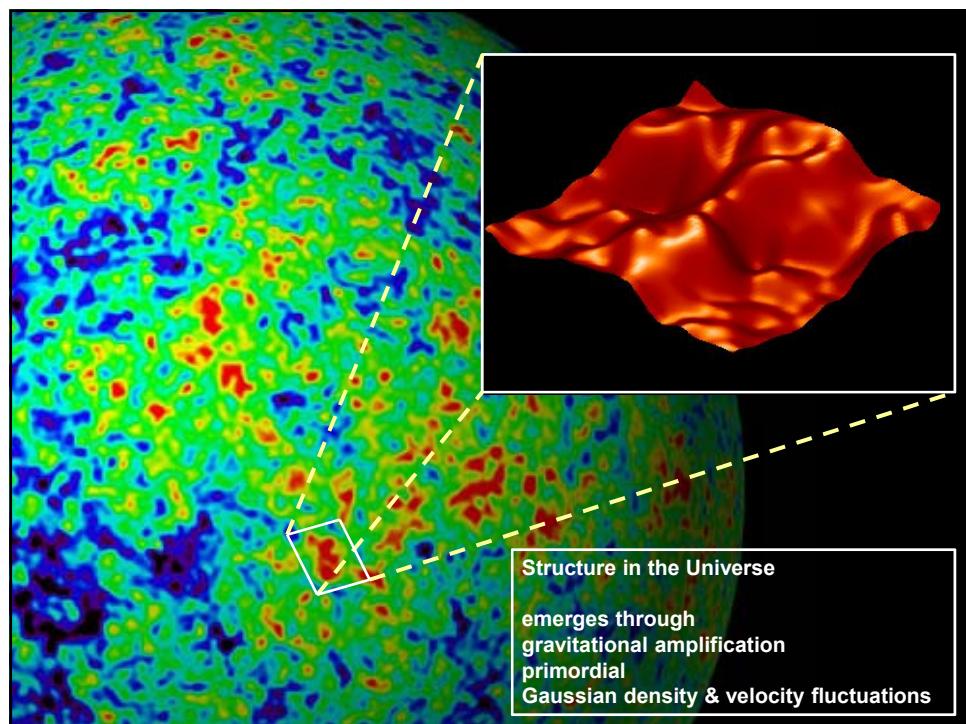
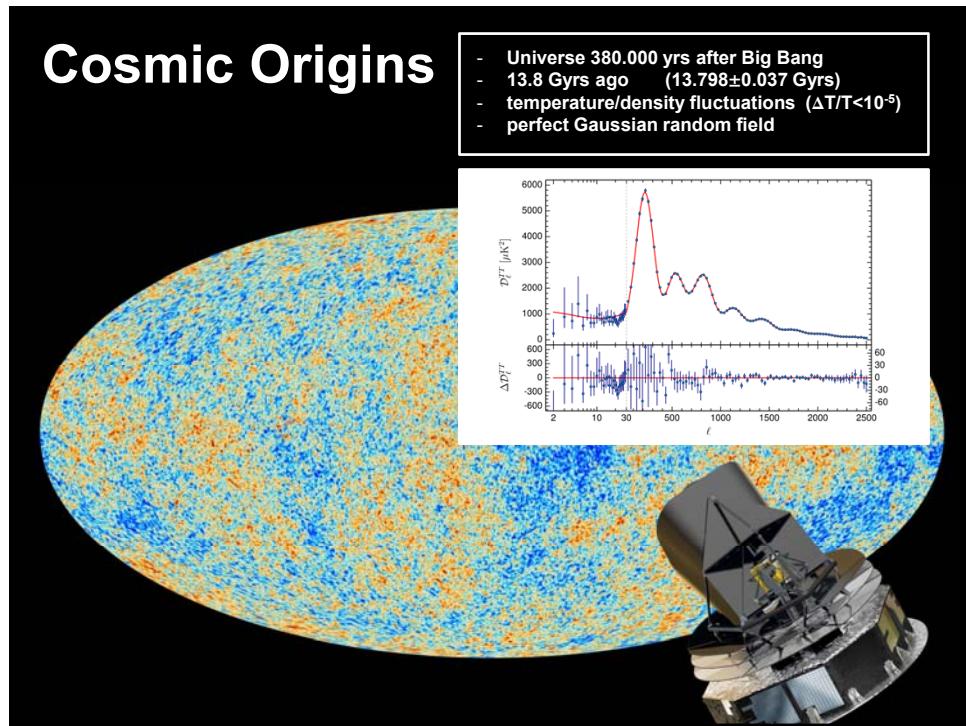


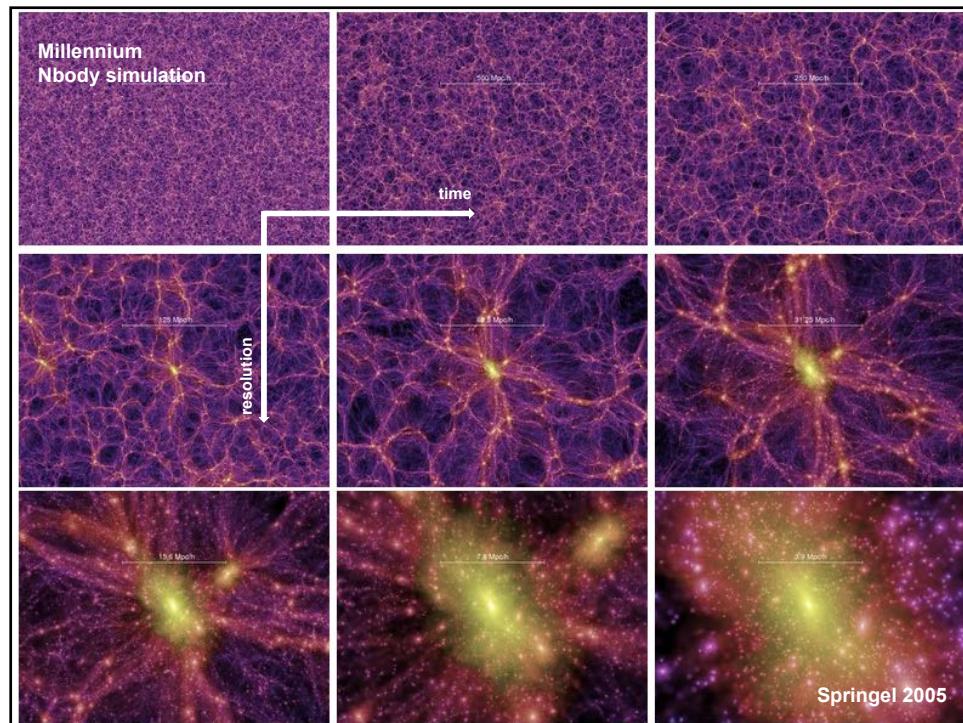
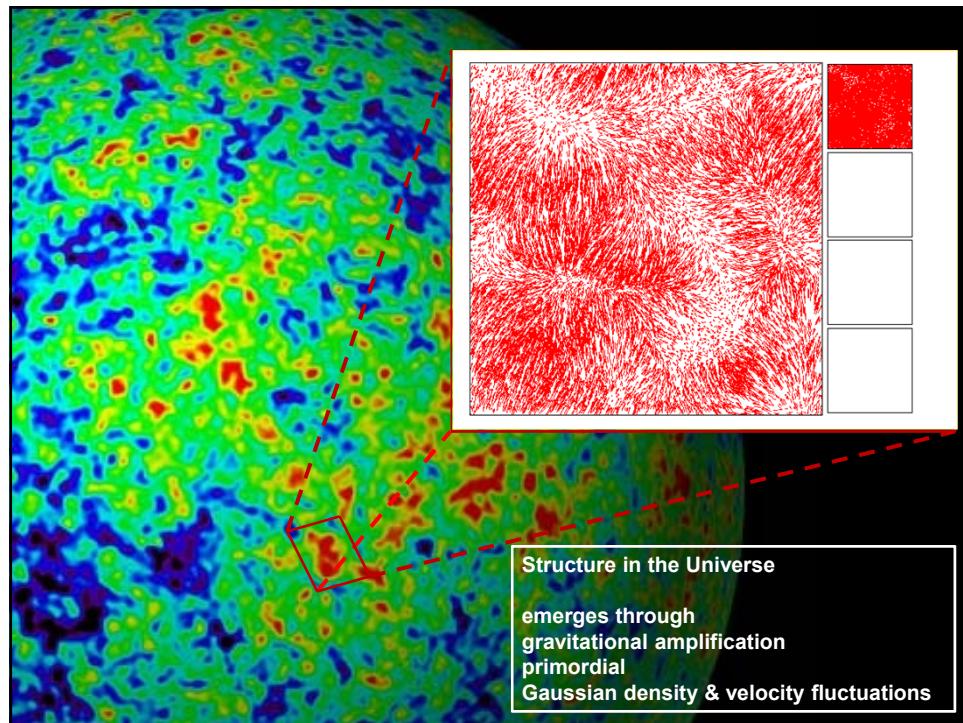


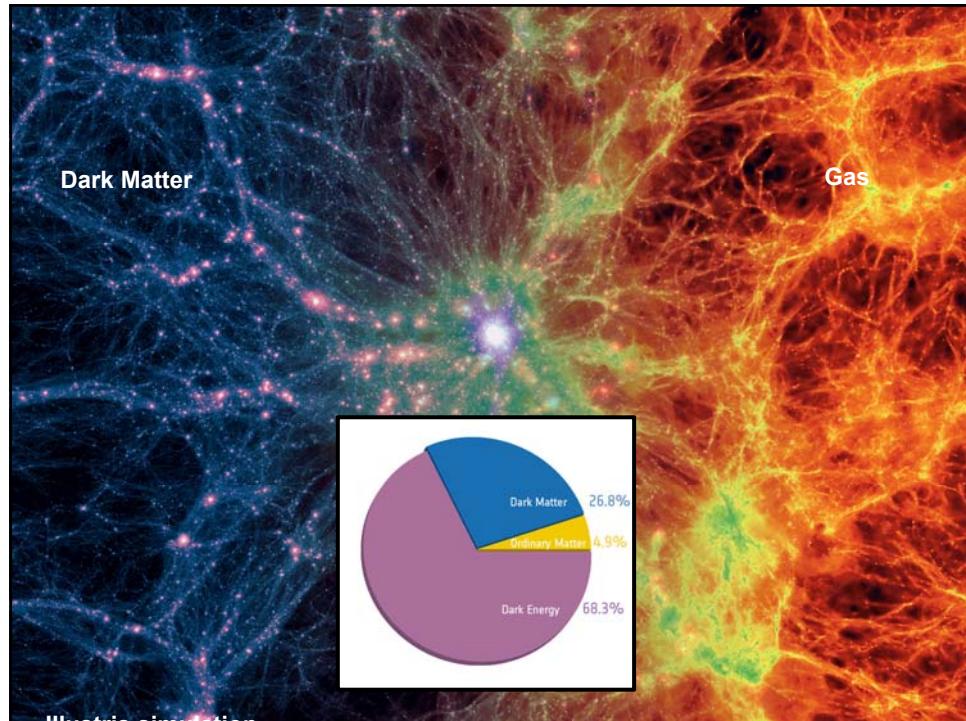


# Cosmic Structure Formation: Gravitational Instability

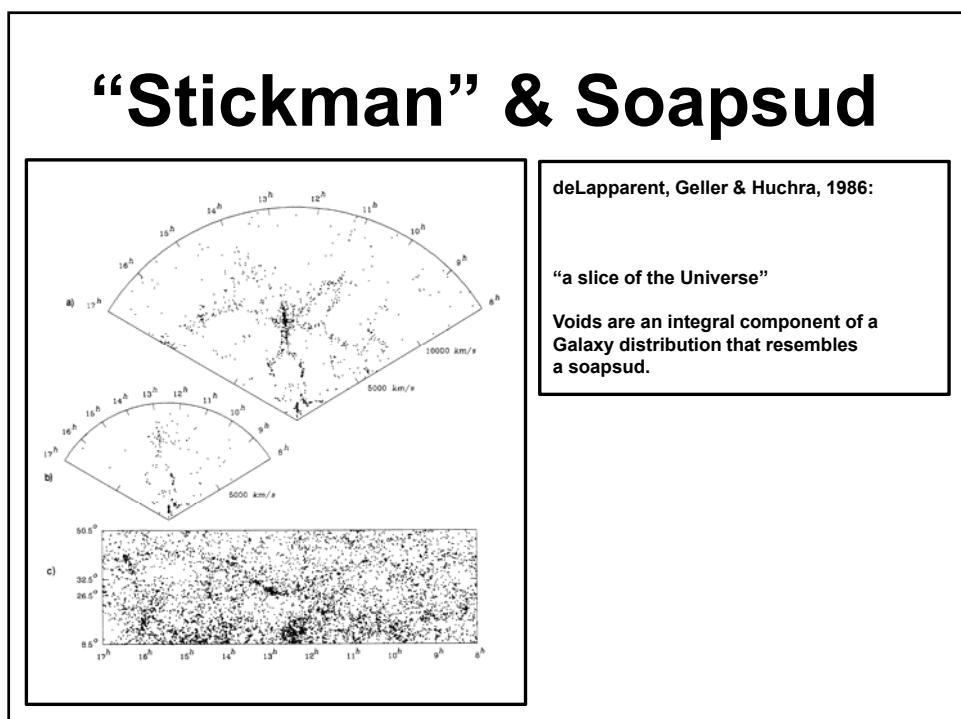
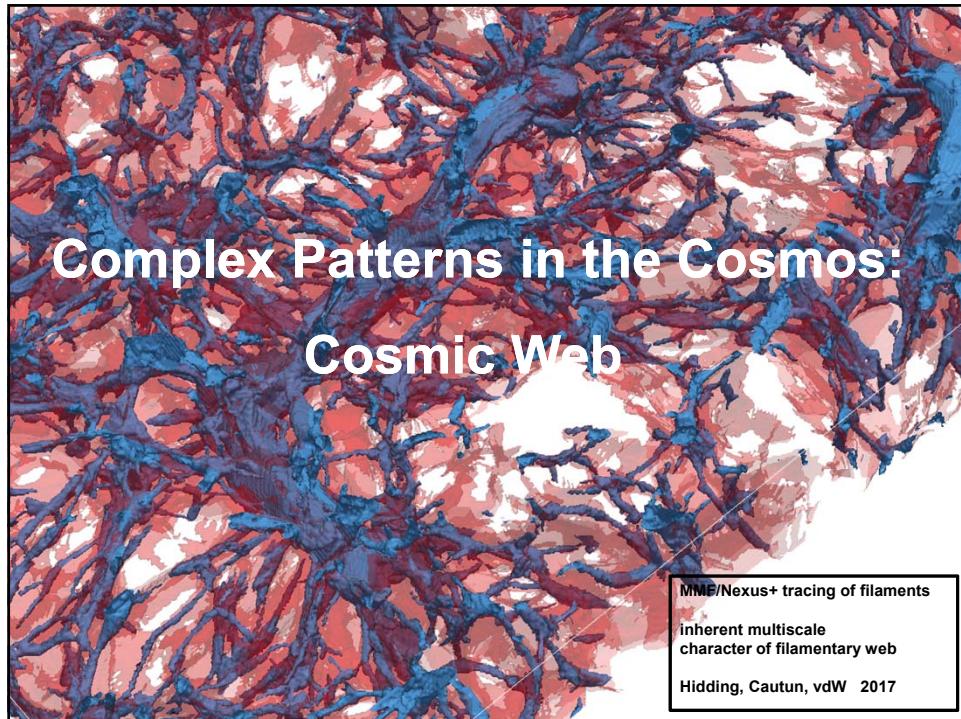


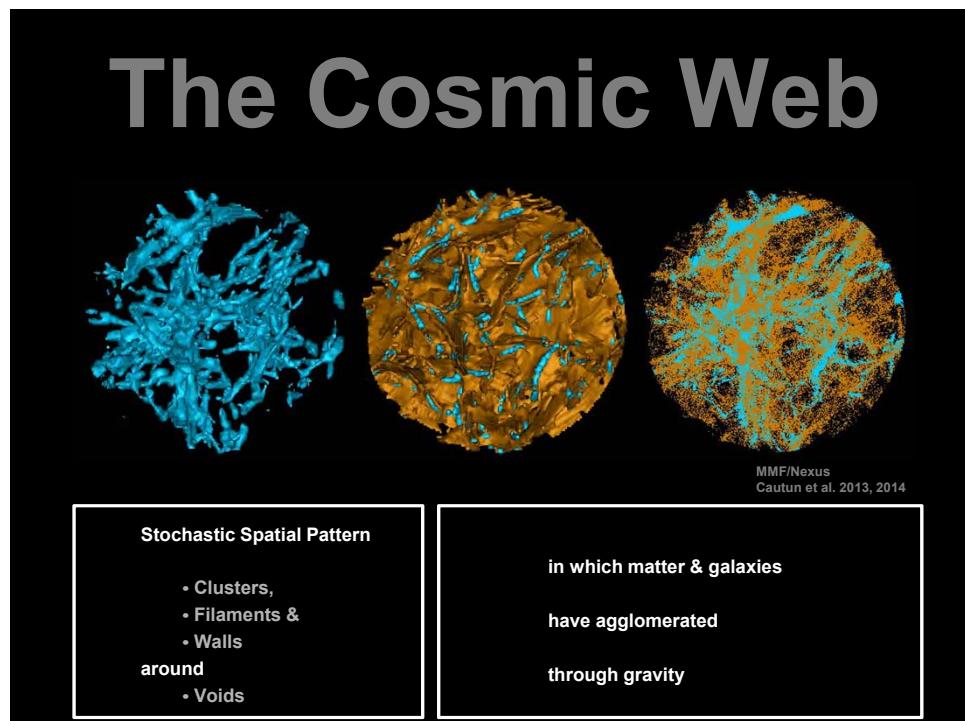
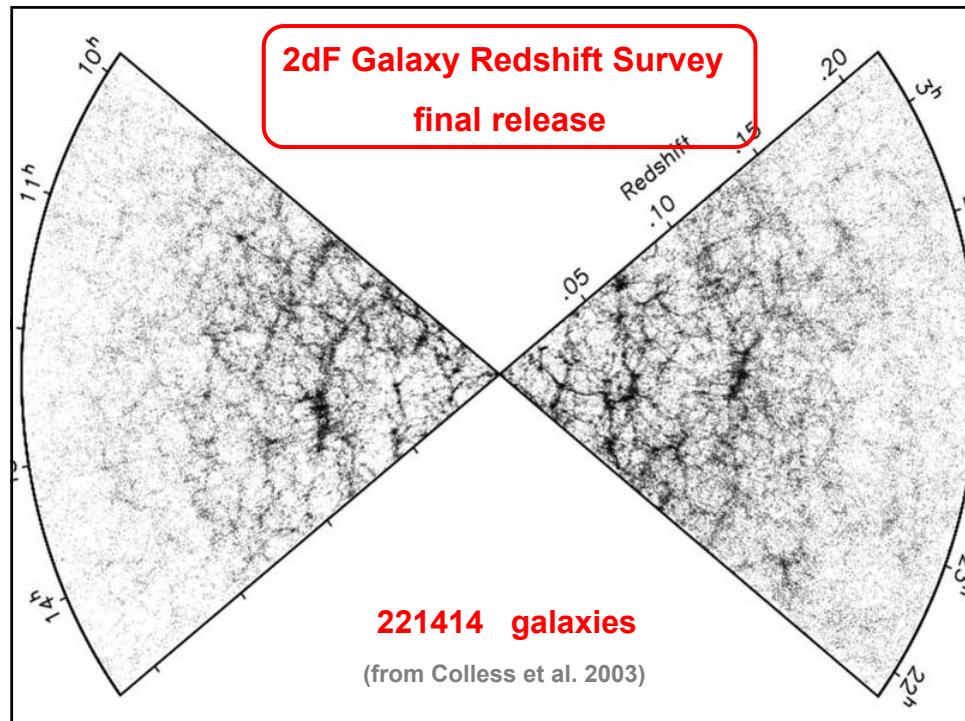






# Cosmic Structure Formation: Cosmic Web

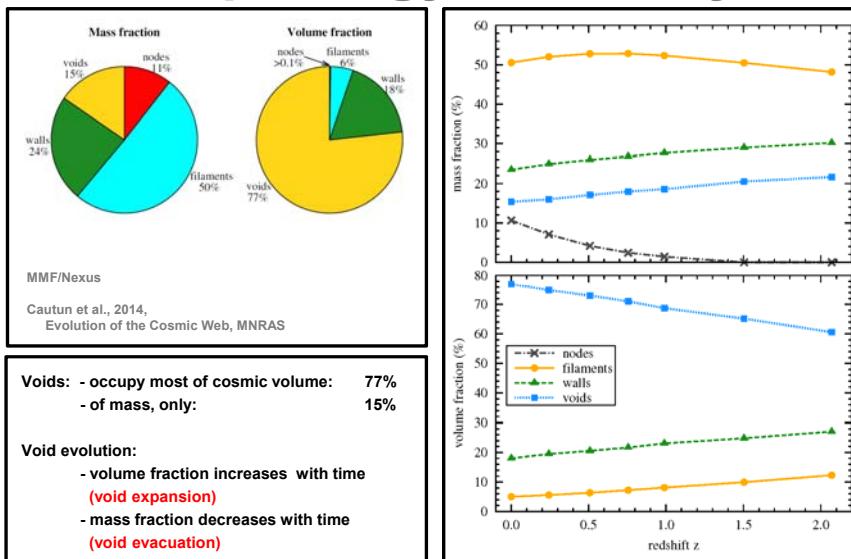


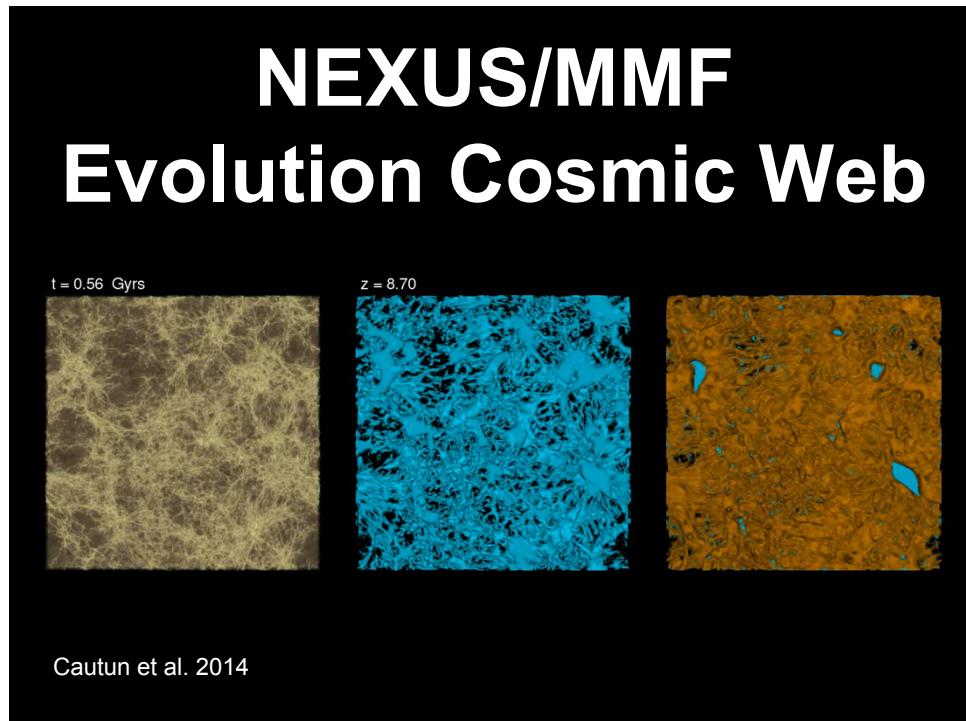


# Cosmic Web Characteristics

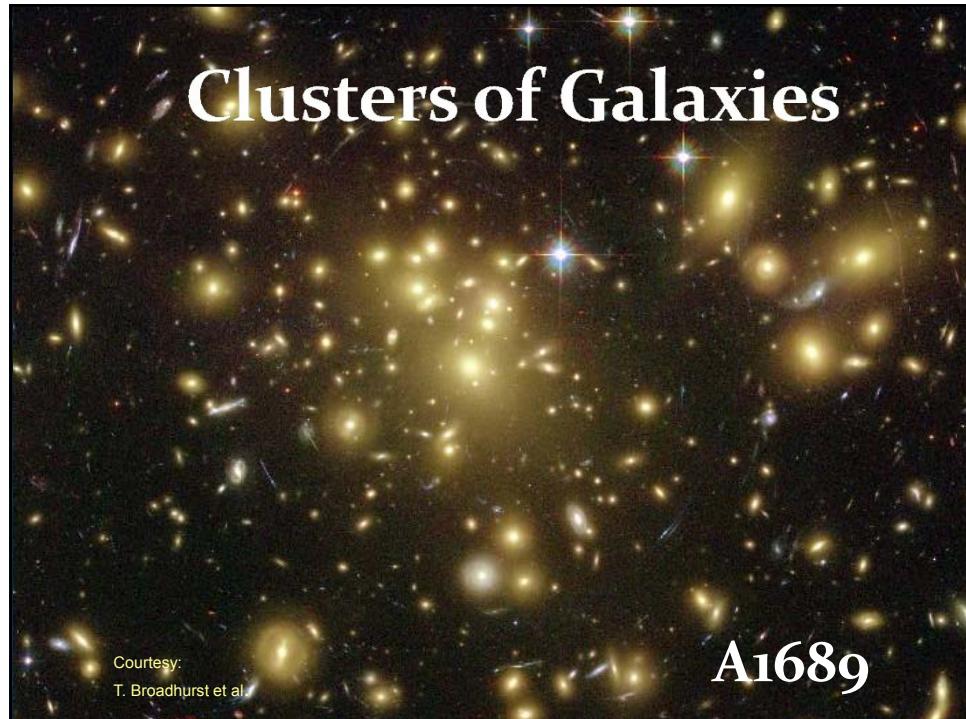
- **anisotropic structure:**
  - filaments dominant structural feature
  - sheets/walls
  - elongated
  - flattened
- **multiscale nature**
  - structure on wide range of scales ( $\sim 0.1\text{-}100\text{s Mpc}$ )
  - structures have wide range of densities
- **overdense-underdense asymmetry**
  - voids: underdense, large & roundish
  - filaments & walls: overdense, flattened/elongated
  - clusters: dense, massive & compact nodes
- **complex spatial connectivity**
  - all structural features connected in a complex, multiscale weblike network

# Cosmic Web Morphology Inventory





**Cosmic  
Structure Formation:  
Clusters, Filaments & Voids**

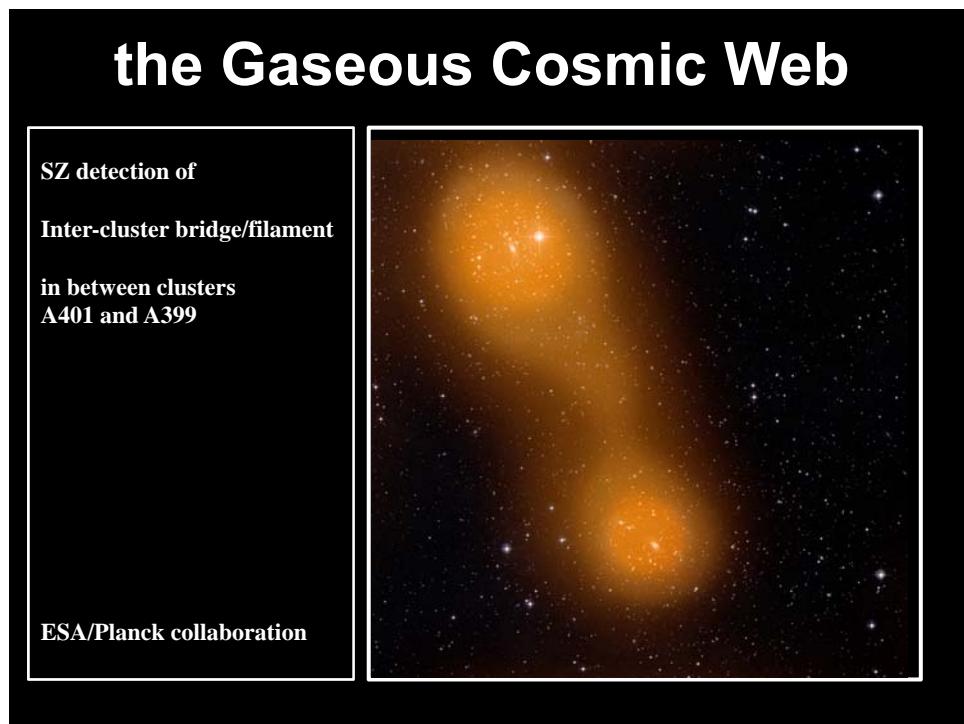
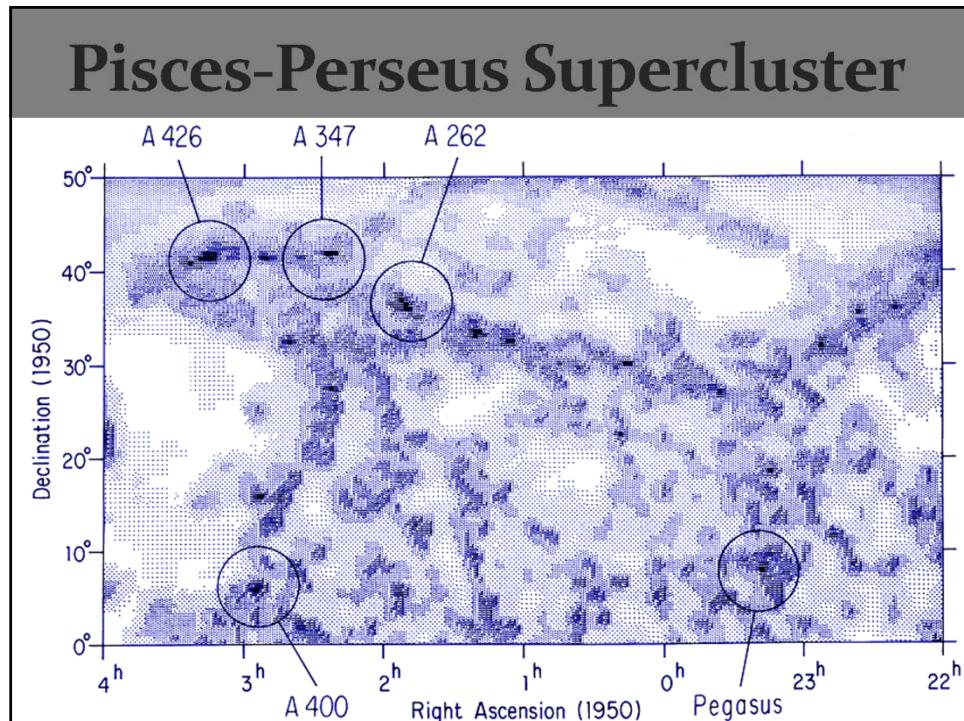


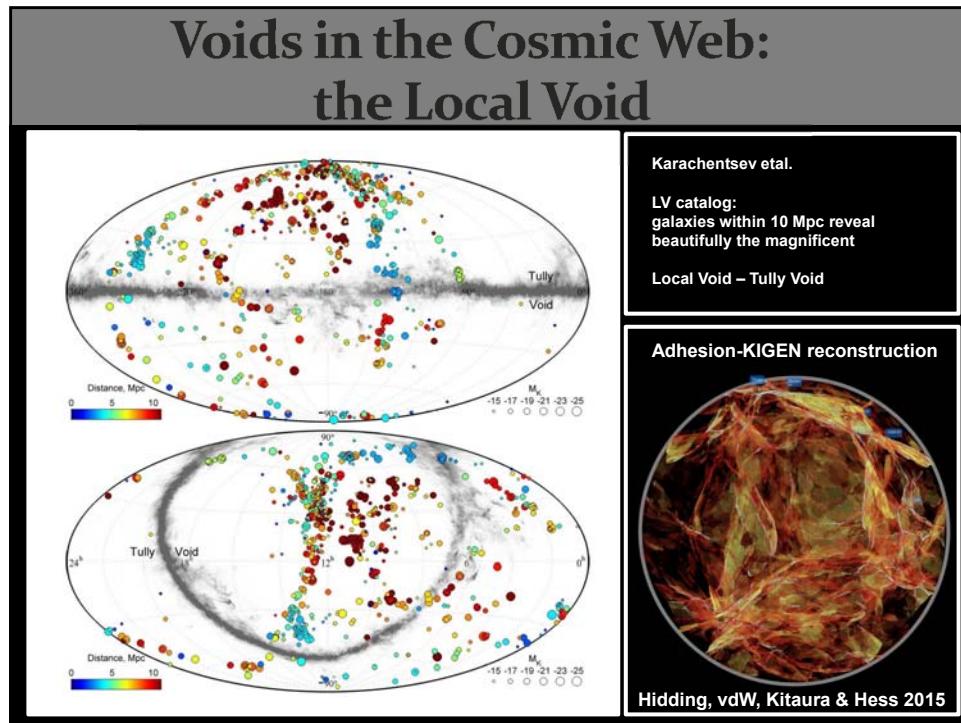
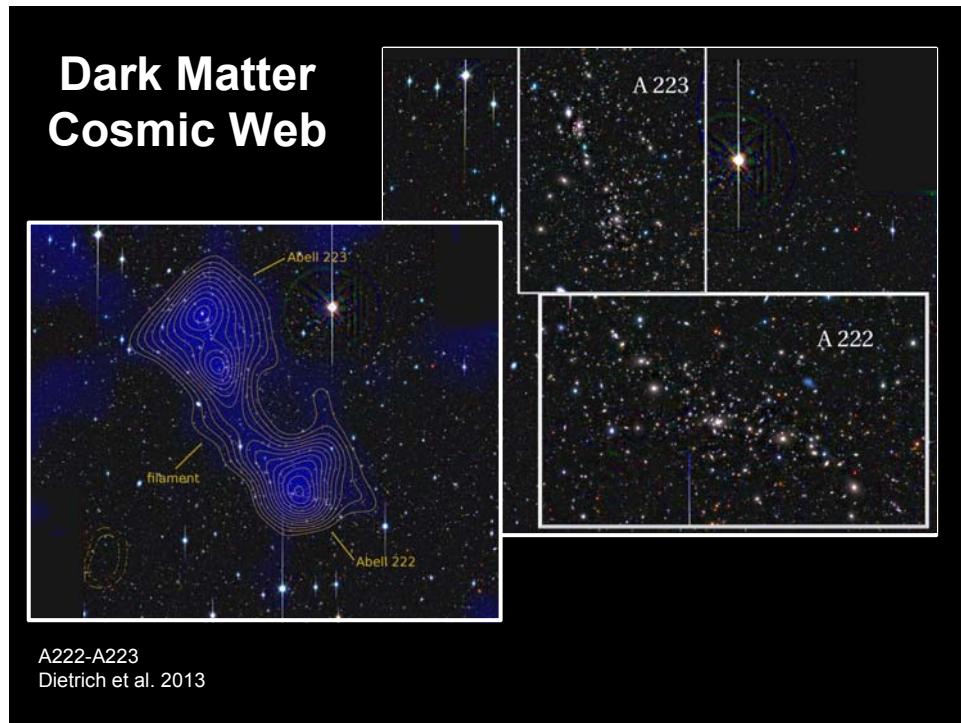
## Voids & Clusters

Einasto, Saar et al. (1990s)

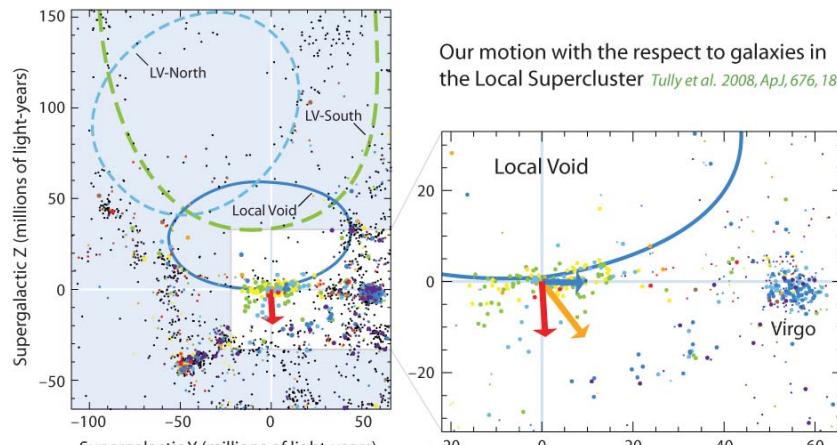
- Superclustering in Abell/APM clusters catalog
- Finding of characteristic scale  $\sim 140$  Mpc, corresponding to large voids in the cluster distribution

Reflex II cluster catalog (Bohringer et al.) reveals same population of voids in cluster distribution.





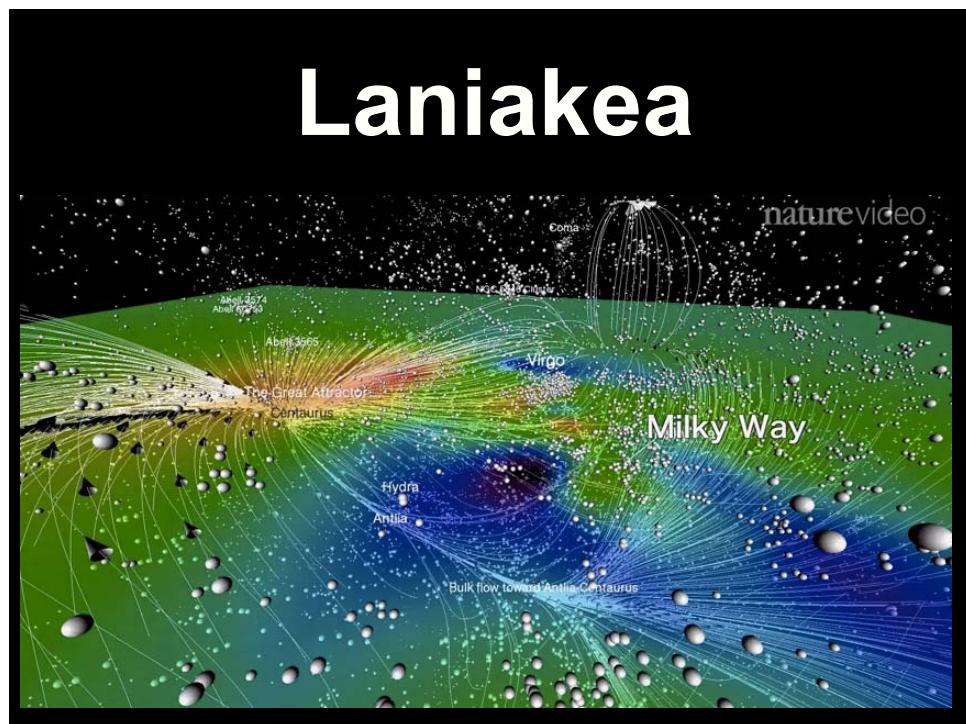
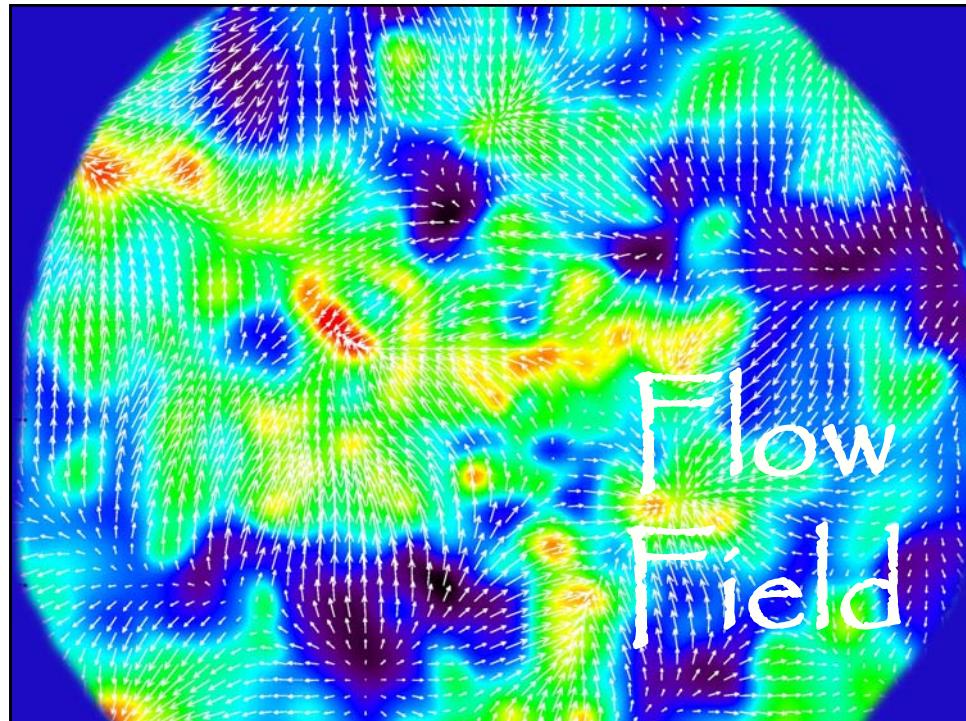
## Push of the Local Void



Our motion with the respect to galaxies in  
the Local Supercluster *Tully et al. 2008, ApJ, 676, 184*

Tully et al. 2008:  
Local Void pushes with  $\sim 260$  km/s against our local neighbourhood

Cosmic  
Structure Formation:  
Dynamics



# Zel'dovich Approximation

$$\vec{x} = \vec{q} + D(t) \vec{u}(\vec{q})$$

$$\vec{u}(\vec{q}) = -\vec{\nabla} \Phi(\vec{q})$$

$$\Phi(\vec{q}) = \frac{2}{3Da^2H^2\Omega} \phi_{lin}(\vec{q})$$

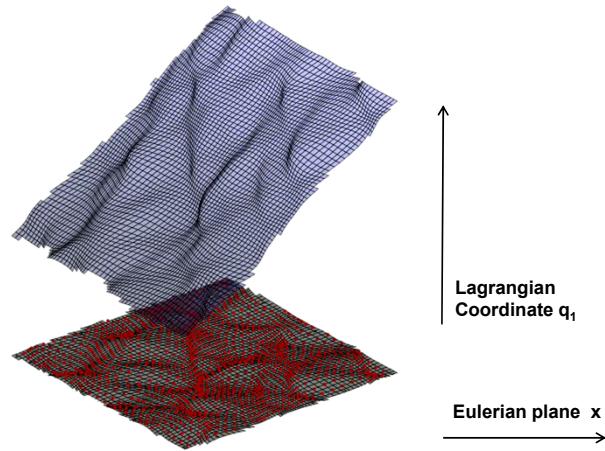
Hierarchical  
Web Evolution:

Adhesion simulation  
buildup Cosmic Web

Johan Hidding  
2012

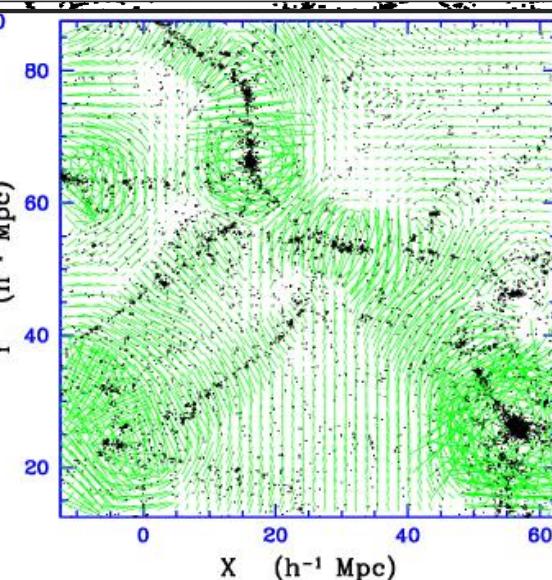
## Phase-Space Dynamics

Dynamical Evolution:  
folding the  
phase-space sheet  $\{q, x\}$



## Tidal Shaping of the Cosmic Web

Tidal Forces  
shape the Cosmic Web



### Formative agent of the Cosmic Web:

Tidal strain induced by the Megaparsec Matter Distribution:

- anisotropic collapse of structures
- connection clusters-filaments:  
clusters main agent for stretching filaments

$$T_{ij}(\vec{r}, t) = \frac{3\Omega H^2}{8\pi} \int d\vec{x} \delta(\vec{x}, t) \left\{ \frac{3(x_i - r_i)(x_j - r_j) - |\vec{x} - \vec{r}|^2 \delta_{ij}}{|\vec{x} - \vec{r}|^5} \right\} - \frac{1}{2} \Omega H^2 \delta(\vec{r}, t) \delta_{ij}$$

**Cosmic  
Structure Formation:  
Computer Simulations**

## 1983: Klypin & Shandarin

- $32^3$  particle in cubic volume
- initial conditions:  
1st time proper cosmological Gaussian conditions:  
Zeldovich approximation
- PM particle-mesh simulation

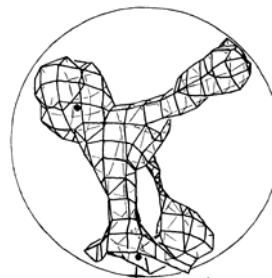
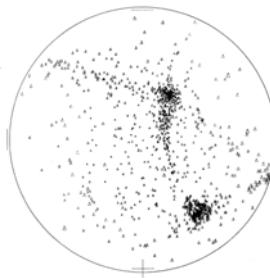
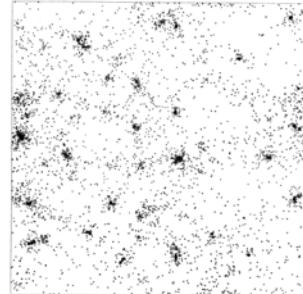
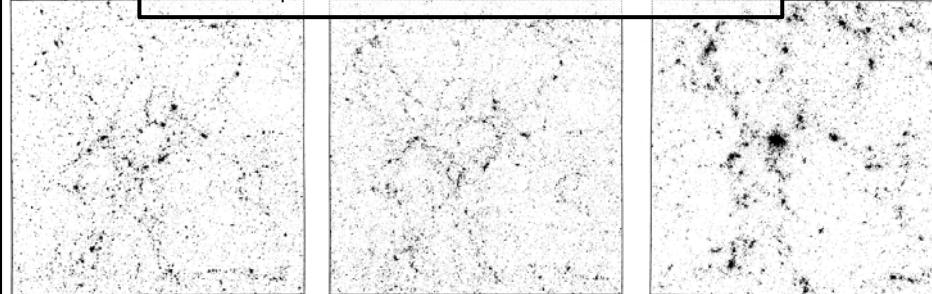


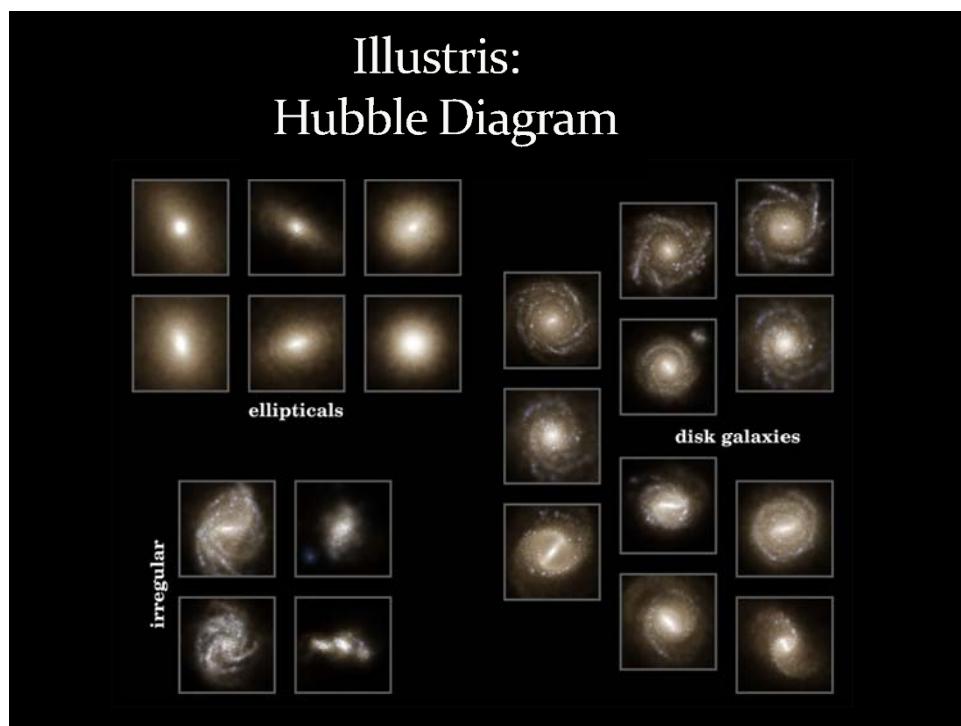
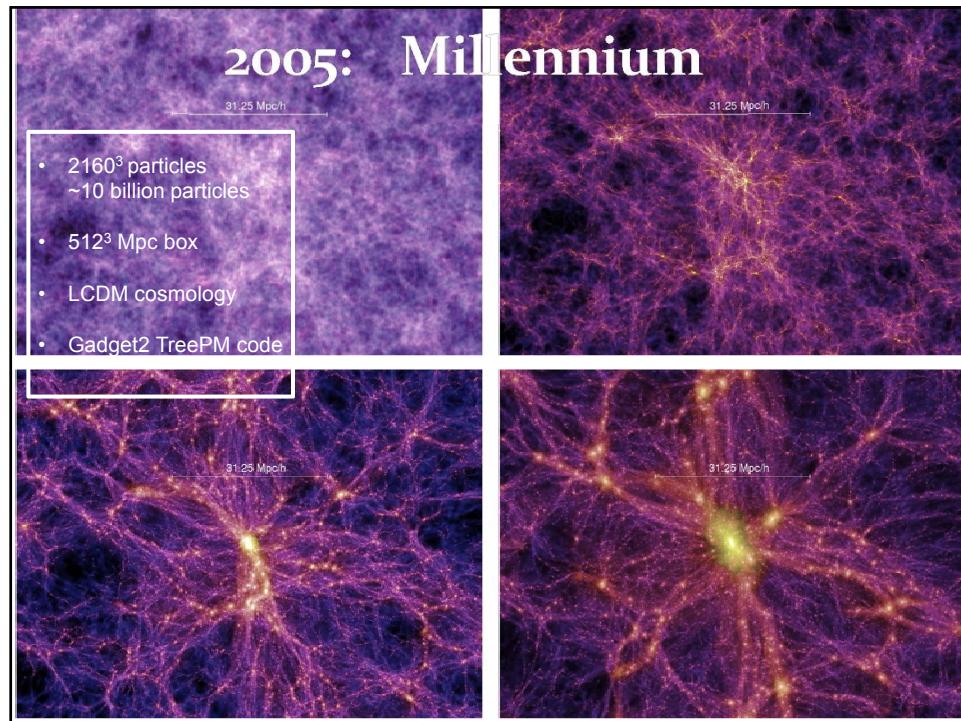
Figure 3. A small fragment of the particle distribution plotted in Fig. 2(b), when  $z = 1.13$  (a). As opposed to Fig. 2 have all particles in the sphere with radius  $R = 4.7 \times 10^8$  Mpc are plotted. Every particle is depicted as a triangle whose size is inversely proportional to distance from an observer. The figure is taken from Klypin & Shandarin (1983).

## 1985-1989:

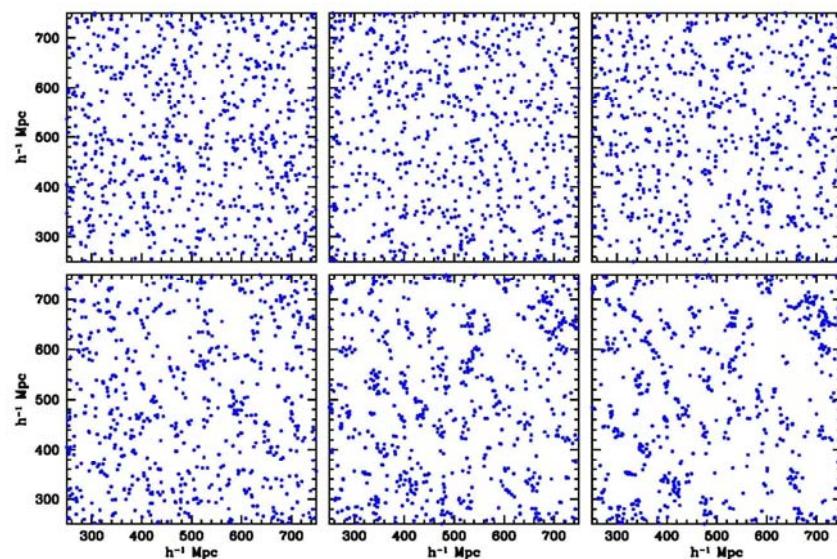
## DEFW, “Gang of Four”

- Davis, Efstathiou, Frenk & White
- HDM does not work: absence older small structure
- CDM simulations,
- $32^3$  particles in cubic box
- P3M particle-particle particle-mesh code
- large range of publications establishes CDM as standard cosmology
- Gruber prize 2011





# Cosmic Structure Formation: Structure Analysis



## only one Universe: Ergodic Theorem

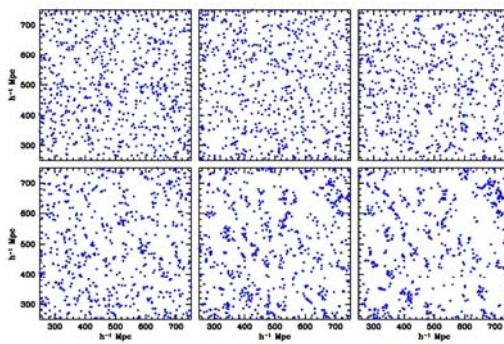
Ensemble Averages



Spatial Averages  
over one realization  
of random field

- Basis for statistical analysis cosmological large scale structure
- In statistical mechanics Ergodic Hypothesis usually refers to time evolution of system, in cosmological applications to spatial distribution at one fixed time

## Correlation Functions



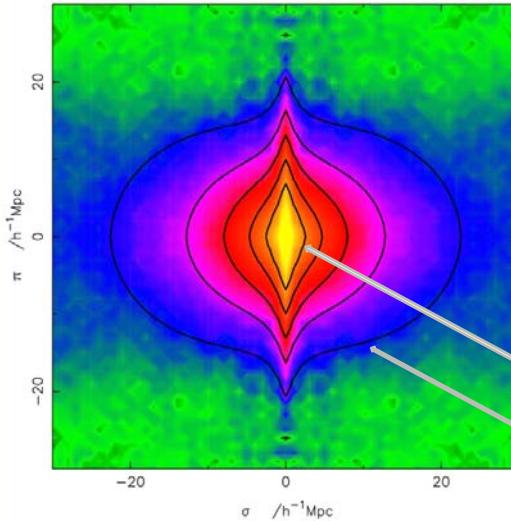
Joint probability that  
in each one of  
the two infinitesimal volumes  
 $dV_1$  &  $dV_2$ ,  
at distance  $r$ ,  
lies a galaxy

Infinitesimal Definition Two-Point Correlation Function:

$$dP(r) = \bar{n}^2 (1 + \xi(r)) dV_1 dV_2$$

mean density

## sky-redshift space 2-pt correlation function $\xi(\sigma, \pi)$



Correlation function determined  
in sky-redshift space:

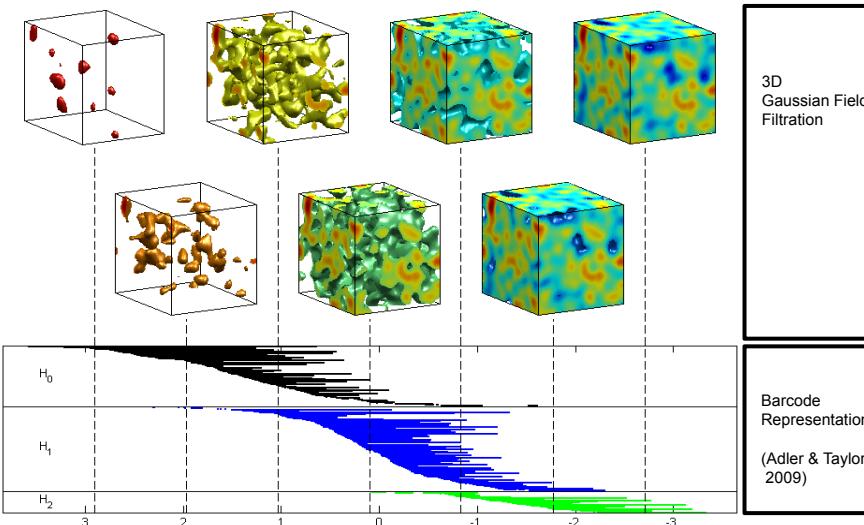
$$\xi(\sigma, \pi)$$

sky position:  $\sigma = (\alpha, \delta)$   
redshift coordinate:  $\pi = cz$

Close distances:  
distortion due to non-linear  
Finger of God  
Large distances:  
distortions due to large-scale  
flows

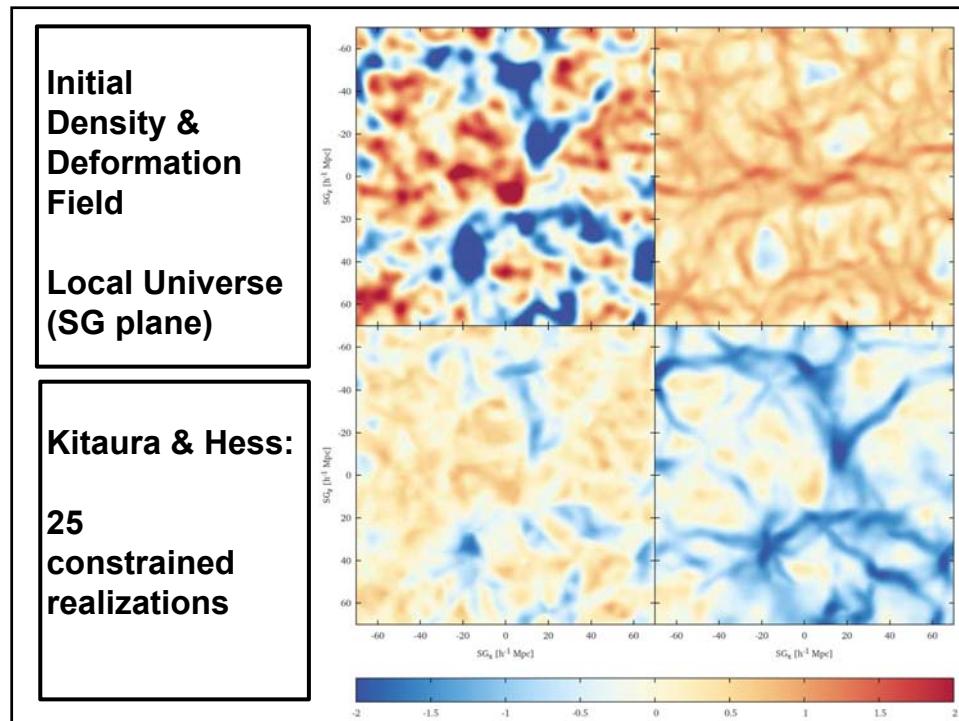
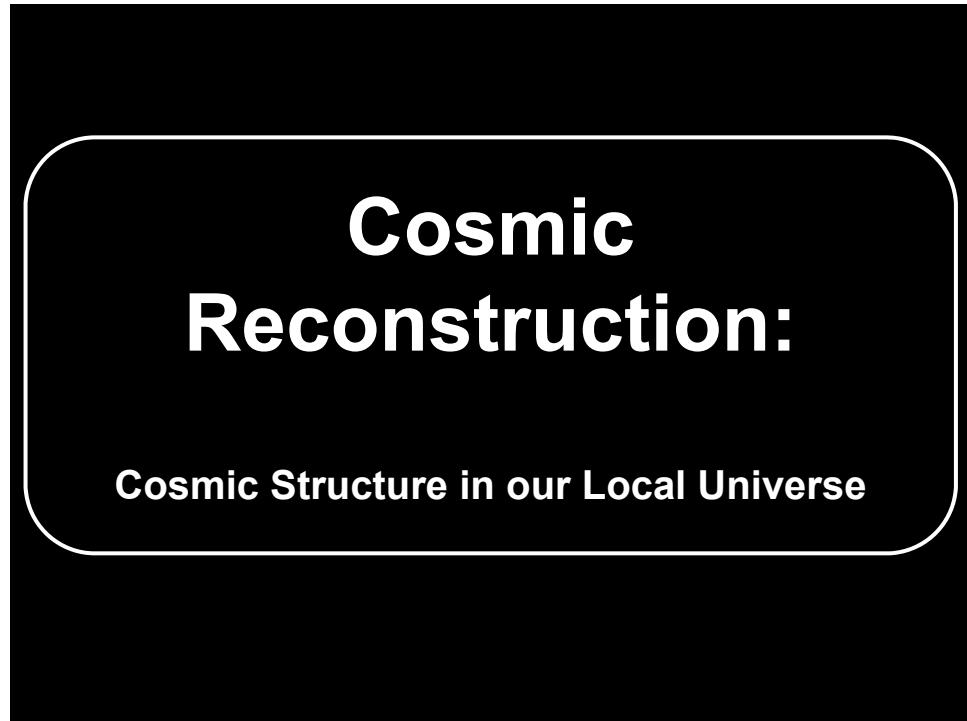
## Persistent Bar Codes

Persistent Homology: “cycling” over density excursion filtration



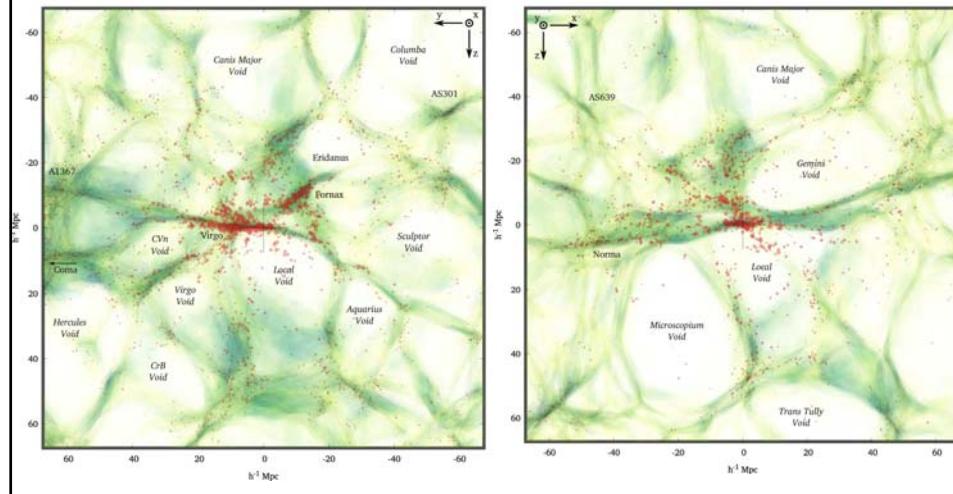
3D  
Gaussian Field  
Filtration

Barcode  
Representation  
(Adler & Taylor  
2009)



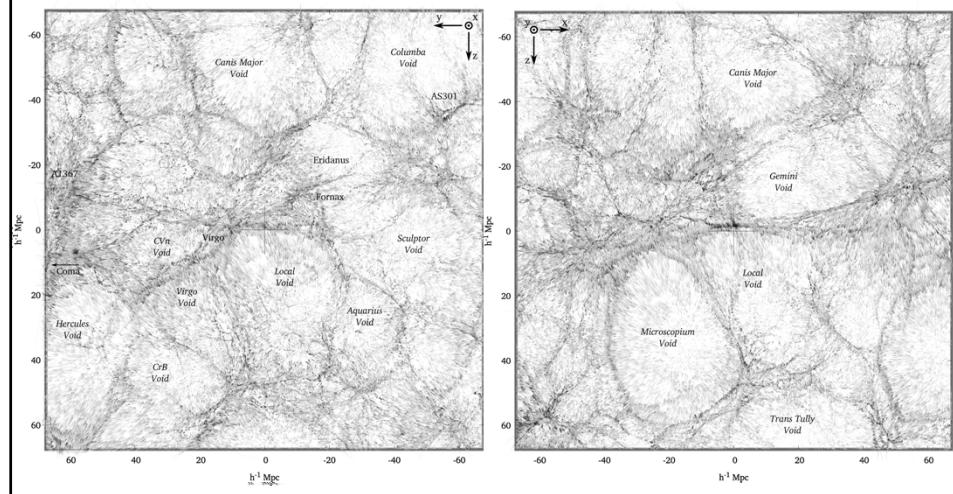
# $\perp$ Supergalactic Plane

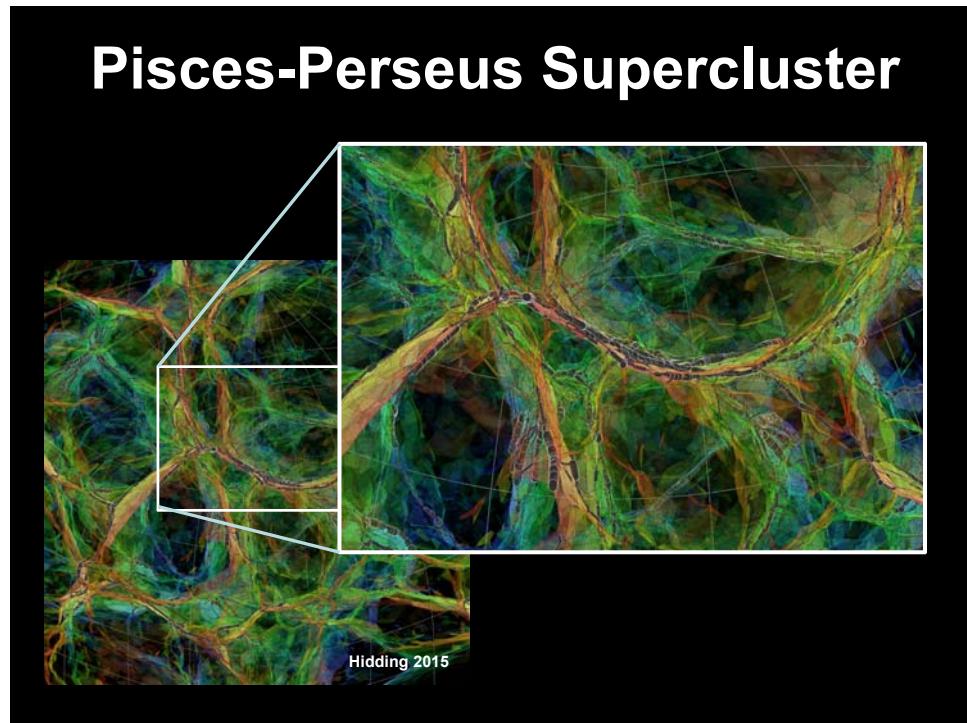
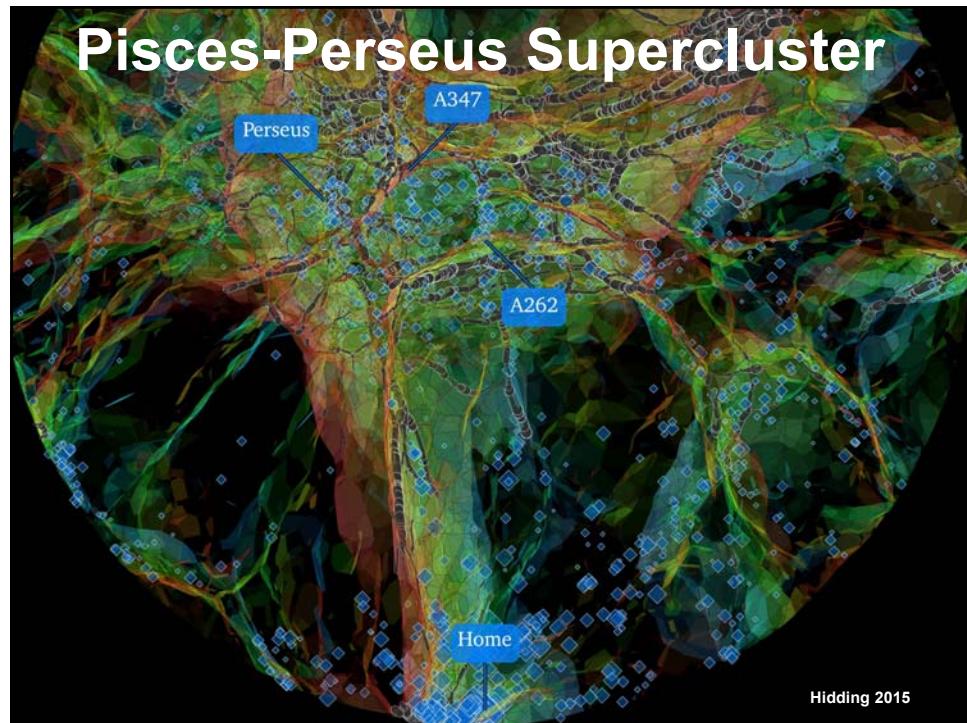
## mean adhesion reconstruction



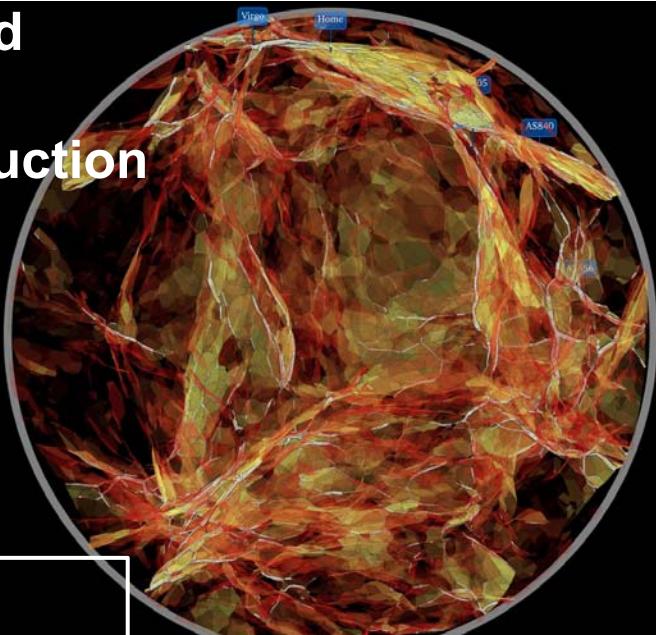
# $\perp$ Supergalactic Plane

## mean adhesion reconstruction





# Local Void Adhesion Reconstruction



Local Void Reconstruction:

Hidding, vdW, Kitaura & Hess 2015