## Structure in the Universe

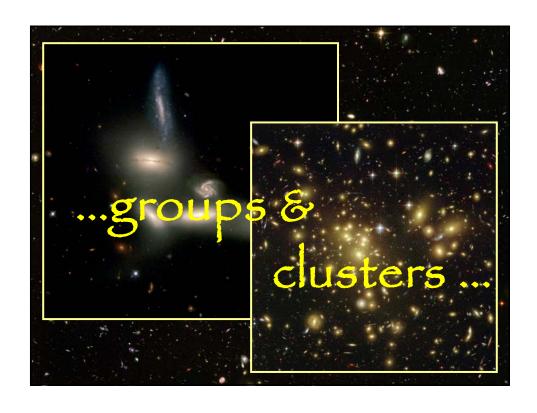






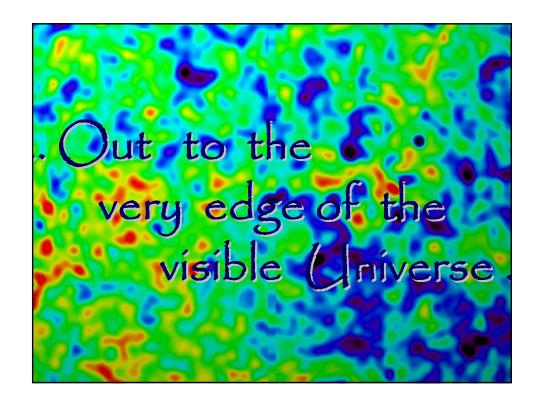






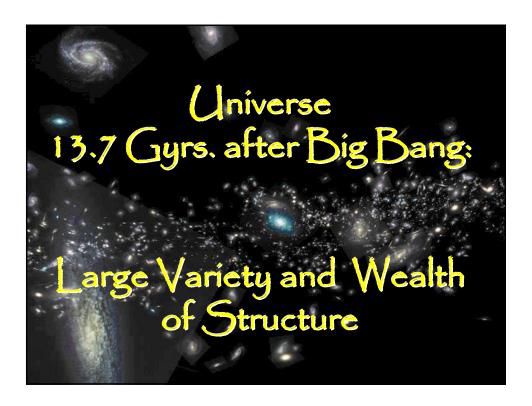






### Central Theme: Cosmic Enigma

### Universe 379,000 years after Big Bang almost perfectly smooth Microwave Background Radiation, surface of last scattering of cosmic photons is almost perfectly isotropic, all around the same temperature: T=2.725 K

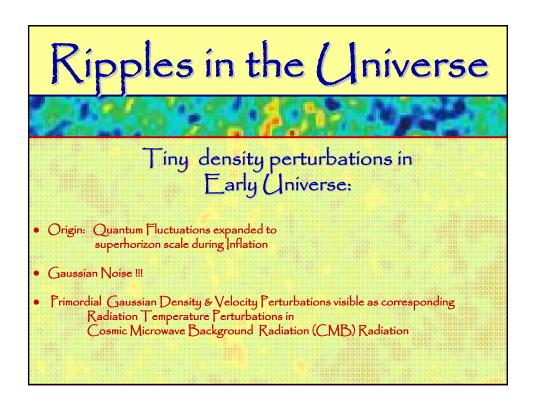


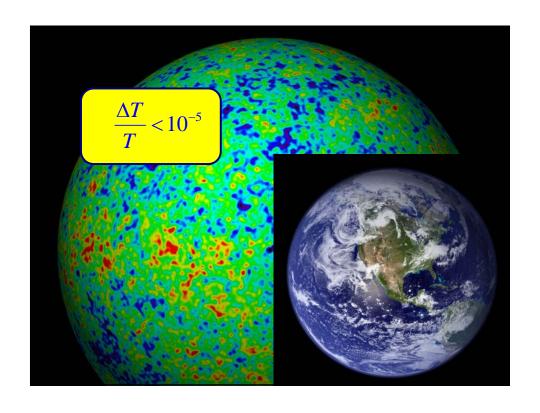
### The Early Universe:

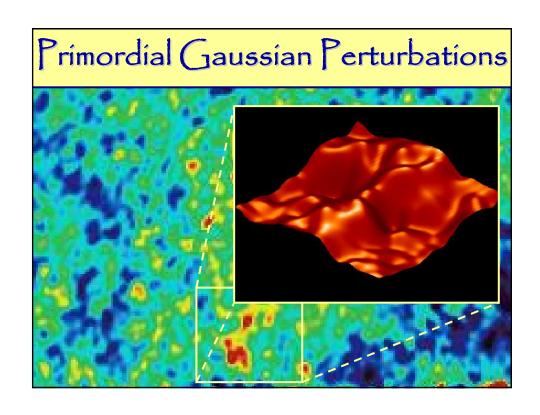
Almost perfectly homogeneous and isotropic, without any discernable structure ...

How did the present wealth and variety of structure emerge out of an almost featureless, pristine early Universe ?????

### Cosmic Paradigm: Gravitational Instability







### Cosmic Structure Formation

After decoupling, density perturbations in the matter distribution gradually develop into forming structures by means of the "gravitational instability" mechanism. The origin of these density perturbations is still an unsettled issue. Their presence, however, has been proven beyond doubt: their imprint in the CMB beautifully confirmed by COBE and WMAP.

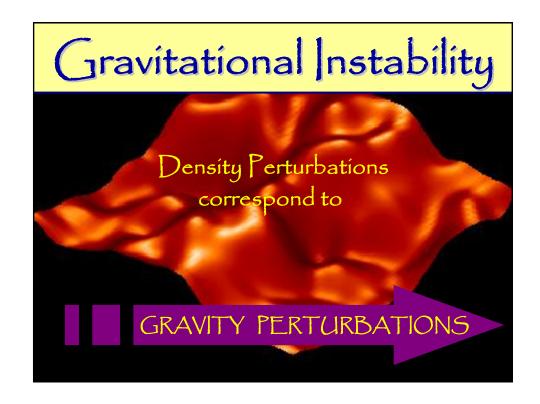
Hidden in the depths of the very first instances of the early universe, at present the most viable suggestion is that it concerns quantum fluctuations blown up to macroscopic proportions in an inflationary phase of cosmic expansion.

In the later phases of more "quiescent" cosmic expansion, density fluctuations, frozen while they have the superhorizon scale assumed in inflation, gradually enter the horizon (i.e they are overtaken).

From that instant on they can start growing!

$$\delta(\mathbf{x},t) \equiv rac{
ho(\mathbf{x},t) - ar{
ho}(t)}{ar{
ho}(t)}$$

$$\delta(\mathbf{x}) = \int \frac{d\mathbf{k}}{(2\pi)^3} \hat{\delta}(\mathbf{k}) e^{-i\mathbf{k}\cdot\mathbf{x}}$$



Gravitational Instability

GRAVITY PERTURBATIONS

$$\mathbf{g}(\mathbf{r},t) = -\frac{1}{a}\nabla\phi = \frac{3\Omega H^2}{8\pi}\int \mathrm{d}\mathbf{x}'\,\delta(\mathbf{x}',t)\frac{(\mathbf{x}'-\mathbf{x})}{|\mathbf{x}'-\mathbf{x}|^3}$$

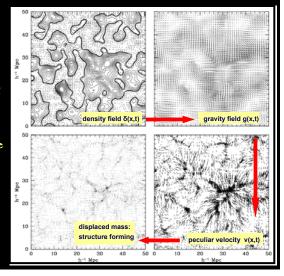


The gravity perturbations induce cosmic flows of matter. High density regions start to contract and finally collapse, assembling more and more matter from their surroundings.

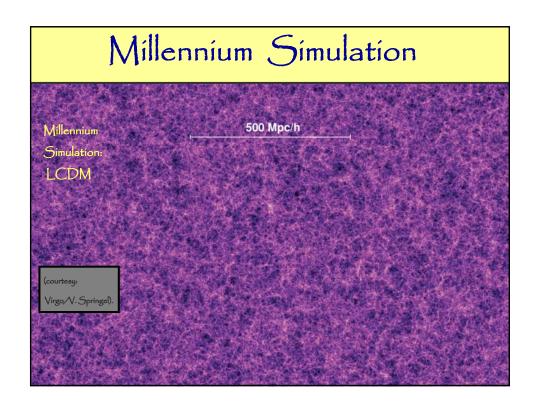
By contrast, as matter is moving out of them, low density regions turn into empty void regions.

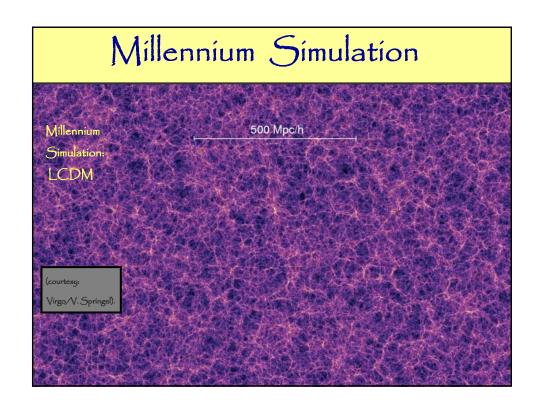
Gradually, dependent on scale, we see the emergence of cosmic structures.

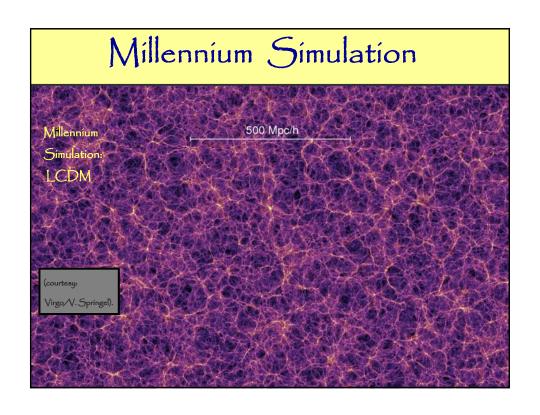
These days we can simulate the characteristics of the process through large computer simulations. Succesfull confrontation with the observational reality has given confidence in our understanding.



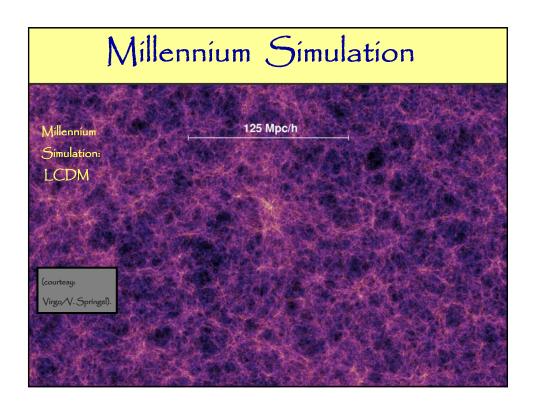
# Millennium Simulation Millennium 500 Mpc/h Simulation: LCDM (courtesy: Virgo/V. Springel).



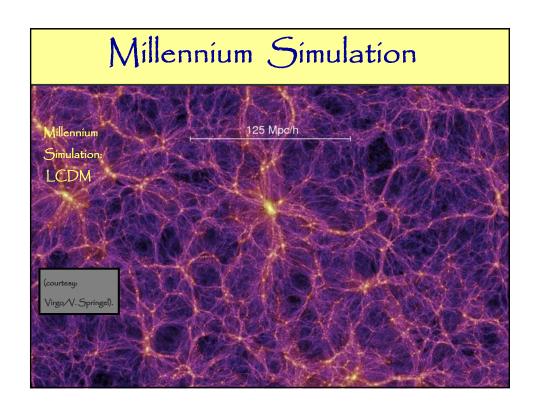


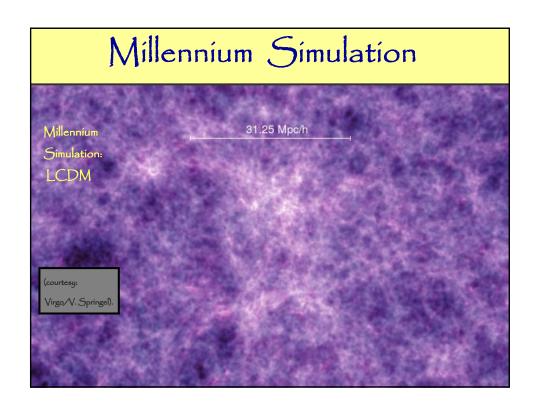


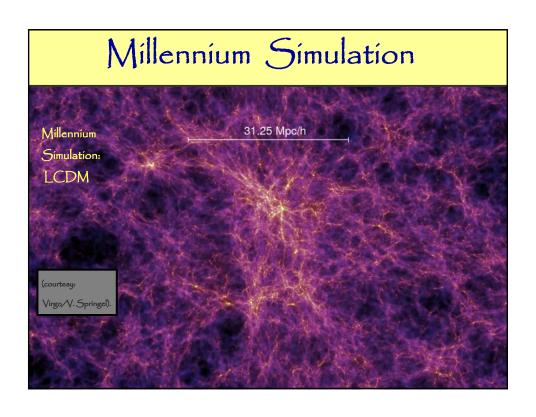
# Millennium Simulation Millennium 125 Mpc/h Simulation; LCDM (courtesy: Virgo/V. Springel).



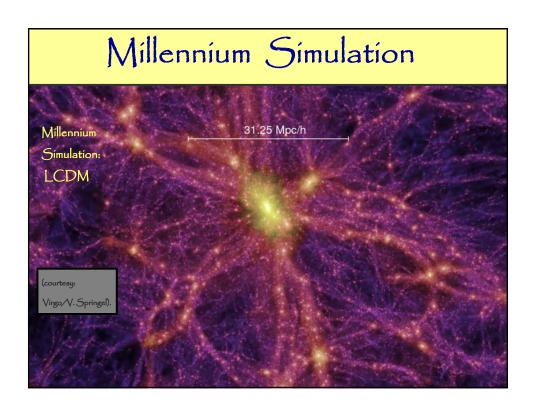
# Millennium Simulation Millennium 125 Mpc/n Simulation: LCDM (courtesy: Virgo/V. Springel).





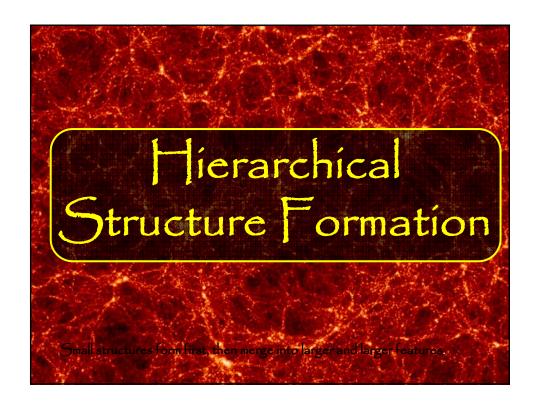


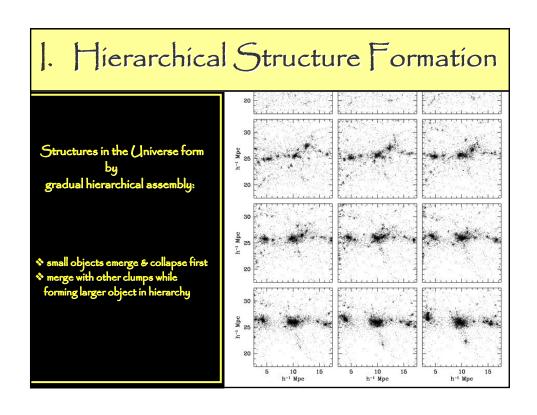
# Millennium Simulation Millennium 31.25 Mpc/h Simulation: LCDM (courtesy: Virgo/V. Springel).

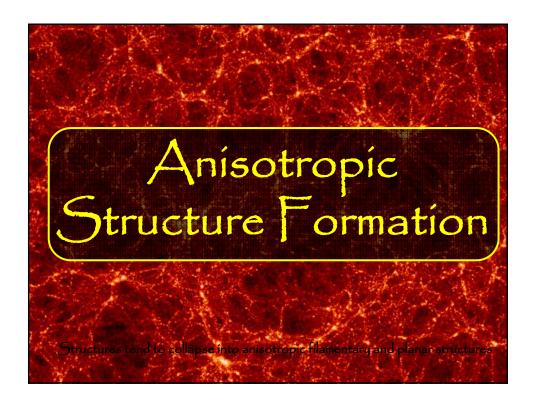


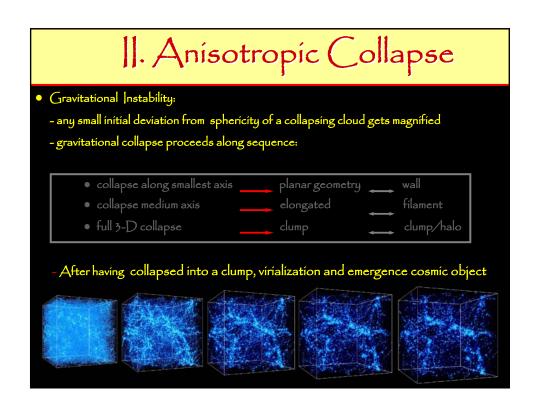
## Caravitational Instability Perturbation Development: Generation: Generation:

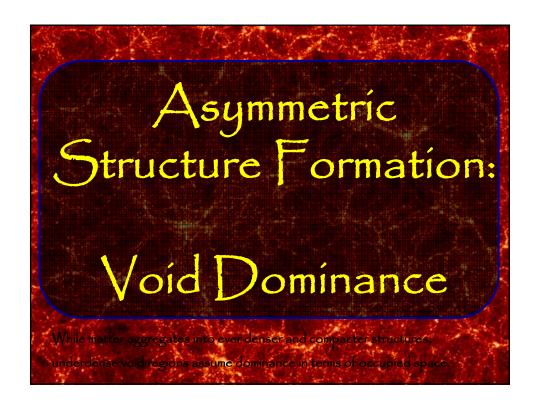
### Cosmic Structure Formation Once the first linear phase of structure formation has passed, we start to recognize the emergence of genuine cosmic structures. Three generic properties nonlinear structure formation: • hierarchical structure formation • anisotropic collapse • void formation: asymmetry overdense vs. underdense

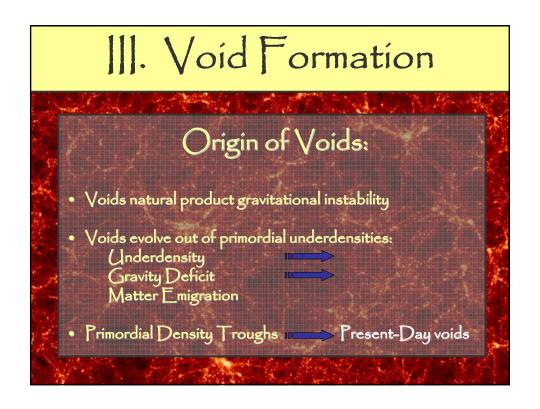






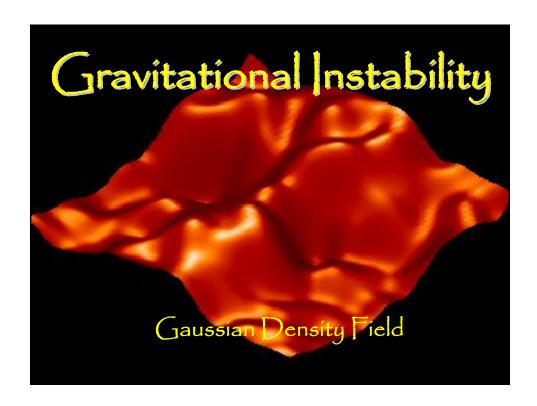






### Structure Formation: Power Spectrum

### Gravitational Instability $\delta(\mathbf{x},t) \equiv \frac{\rho(\mathbf{x},t) - \bar{\rho}(t)}{\bar{\rho}(t)}$ $\delta(\mathbf{x}) = \int \frac{\mathrm{d}\mathbf{k}}{(2\pi)^3} \hat{\delta}(\mathbf{k}) \, \mathrm{e}^{-\mathrm{i}\mathbf{k}\cdot\mathbf{x}}$ ting density perturbations in the early universe



### Gaussian Perturbations

$$\mathcal{P}_{N} = \frac{\exp\left[-\frac{1}{2} \sum_{i=1}^{N} \sum_{j=1}^{N} f_{i} (\mathsf{M}^{-1})_{ij} f_{j}\right]}{[(2\pi)^{N} (\det \mathsf{M})]^{1/2}} \prod_{i=1}^{N} \mathrm{d}f_{i}$$

$$M_{ij} \equiv \langle f(\mathbf{x}_i) f(\mathbf{x}_j) \rangle = \xi(\mathbf{x}_i - \mathbf{x}_j) = \xi(|\mathbf{x}_i - \mathbf{x}_j|)$$

Gaussian perturbations represent the simplest stochastic field of fluctuations imaginable. It is fully and completely characterized by its second-order moment, the autocorrelation function  $\xi(r)$ .

In fact, by concentrating on the contributions of the various scales and describing the field in terms of its Fourier components, we directly see that the

FUNDAMENTAL function fully characterizing the Gaussian field

### Power Spectrum P(k)

$$(2\pi)^3 P(k_1) \, \delta_{\rm D}(\mathbf{k}_1 - \mathbf{k}_2) = \langle \hat{f}(\mathbf{k}_1) \hat{f}^*(\mathbf{k}_2) \rangle$$

Arguably, the power spectrum is the single most important function for our understanding of the cosmic structure formation process.

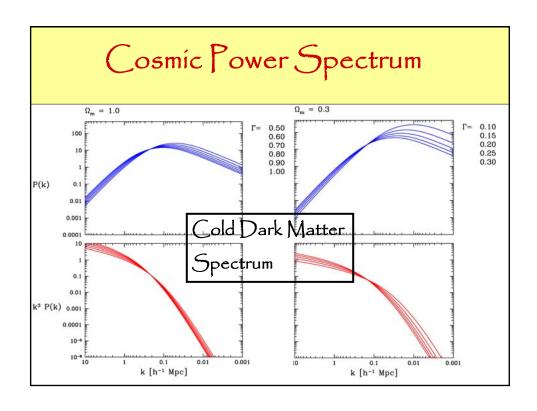
### Power Spectrum

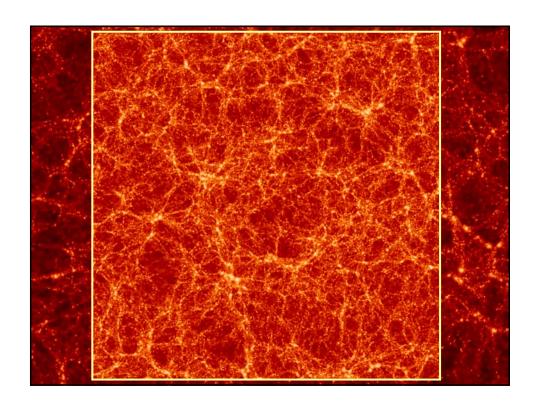
- Direct Characterization of contribution on different scales to inhomogeneous matter distribution
- First direct measure of inhomogeneities in spatial matter distribution
- Along with its Fourier transform, the autocorrelation function  $\xi(r)$
- For Gaussian primordial field, full characterization of density field
- Directly related to potential and velocity perturbations
- Encapsulates all relevant physical processes in early Universe affecting the primordial evolution density/potential/velocity perturbations
- Highly sensitive to constituency of Universe (nature dark matter, etc.)
- This is what the early (inflationary) Universe gives us !!!

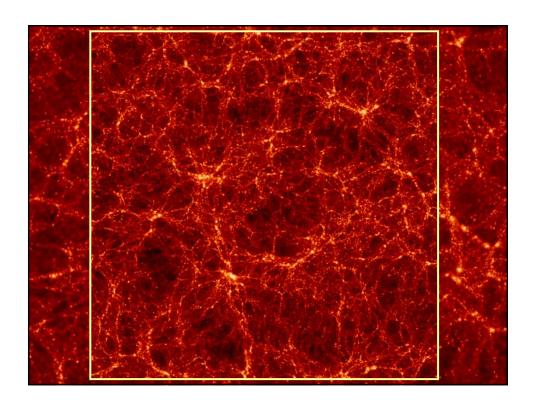
### Cosmic Power Spectrum

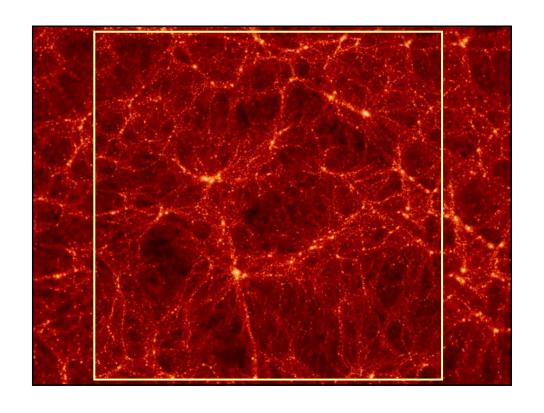
$$P(k) \propto \frac{k^n}{\left[1 + 3.89q + (16.1q)^2 + (5.46q)^3 + (6.71q)^4\right]^{1/2}} \times \frac{\left[\ln(1 + 2.34q)\right]^2}{(2.34q)^2},$$

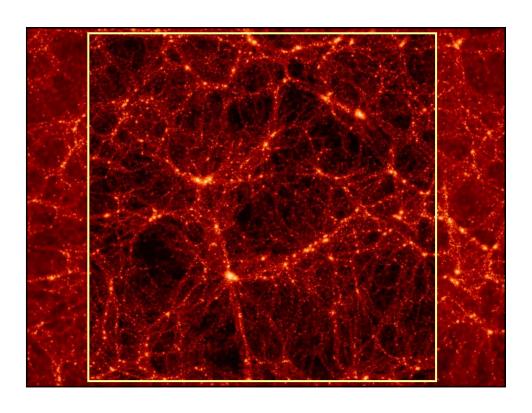
Cold Dark Matter Spectrum  $q = k/\Gamma$   $\Gamma = \Omega_0 h \exp(-\Omega_b - \Omega_b/\Omega_0)$ 

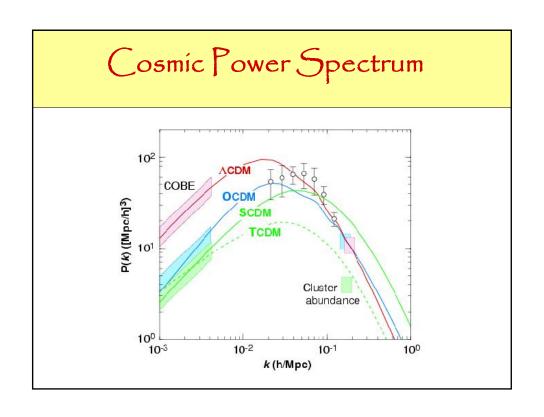


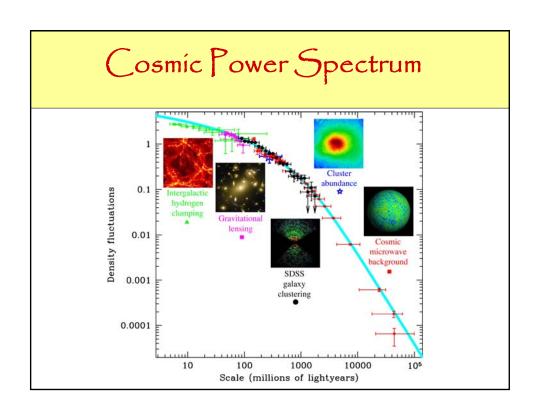


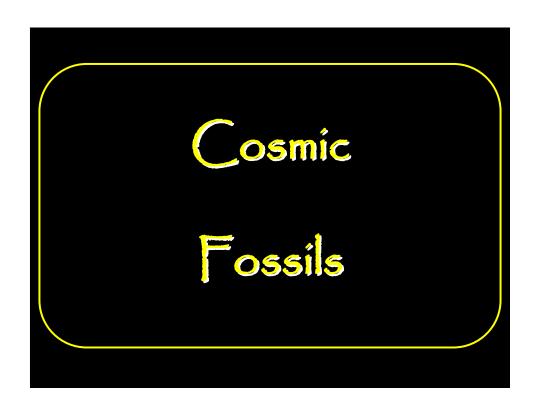


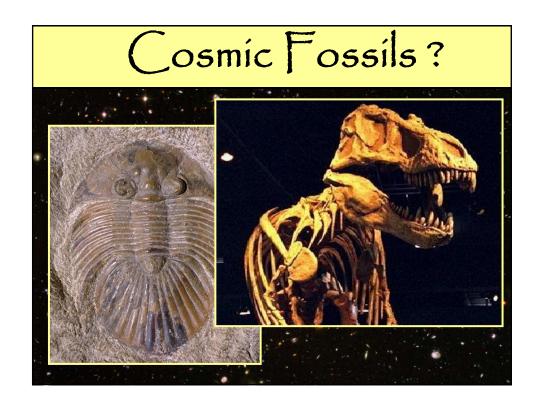


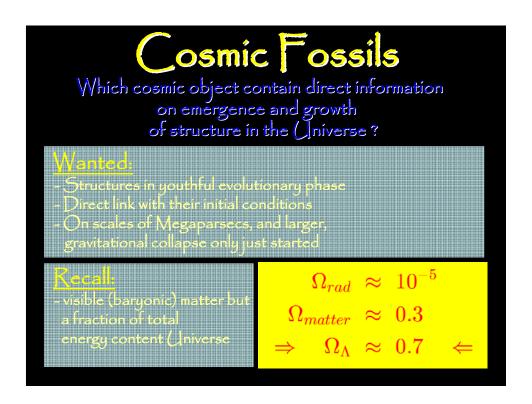


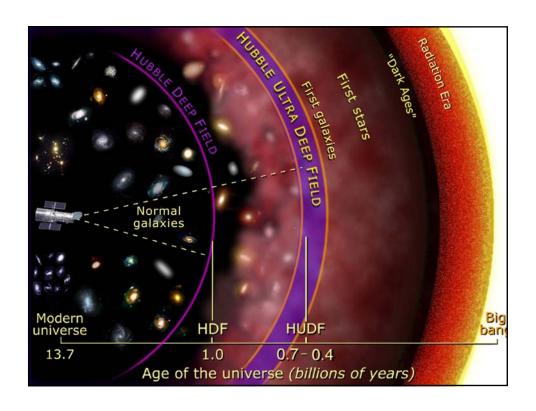












# Primordial Conditions: - temporature fluctuations in microwave background radiation - polarization Cosmic Microwave Background - treasure trove cosmological information Dynamics: - cosmic velocity flows - very difficult in practice, due to large uncertainties in distance estimate/measurements of galaxies, and hence the estimated deviations from Mubble expansion. Mass Distribution: - gravitational lensing of light by cosmic matter distribution - very promising, just started to yield significant results ...



• Clusters of Calaxies

- spatial distribution tracer Cosmic Web

- internal structure dictated by primordial perturbations

- Hot intracluster gas (10<sup>7-8</sup> K) - accurate tracer potential cluster

- easily observable via X-rays

• Caseous Cosmic Web

- Baryonic gas traces the Cosmic Web:

Lya forest neutral hydrogen gas, mostly at high z

WHM shock-heated gas settled in cosmic web

• Distribution & Physical State Gas @ Dark Ages

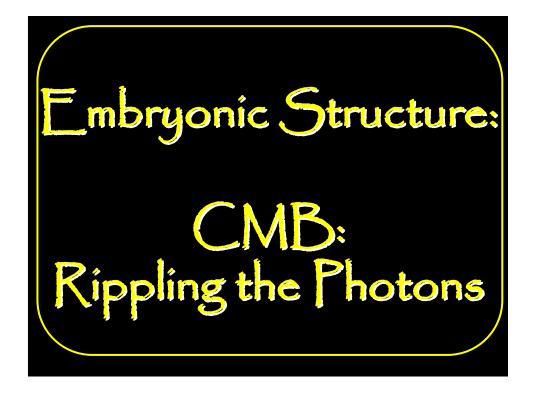
- First Stars & Galaxies

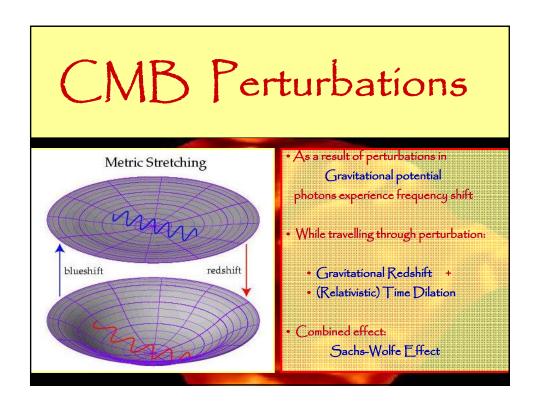
- Reionization of baryonic gas: very sensitive measure cosmology

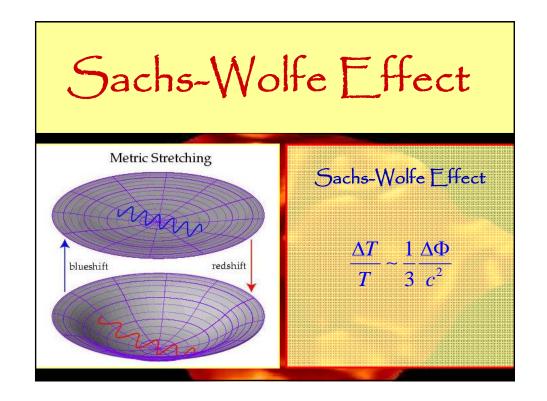
• Structure of Galaxies

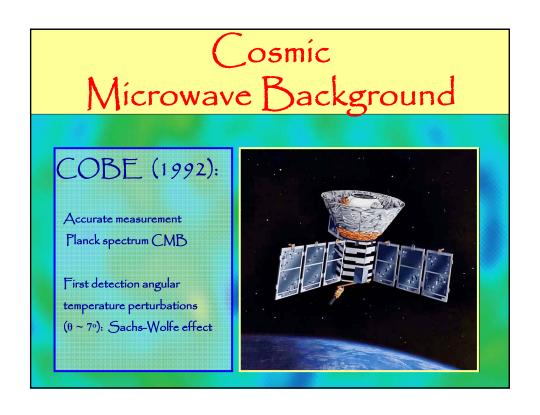
- Mass distribution galaxies

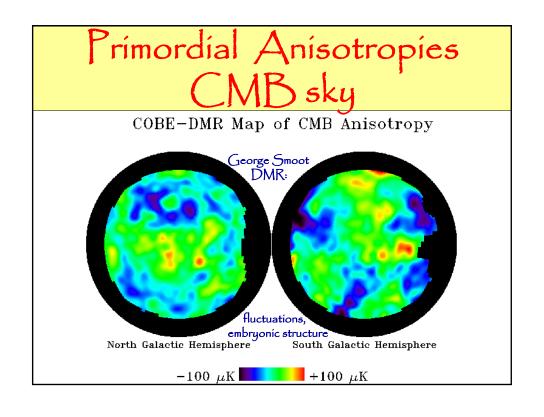
- Internal phase-space structure galaxy haloes

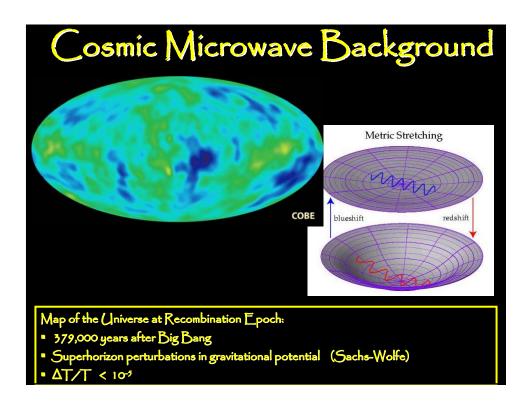


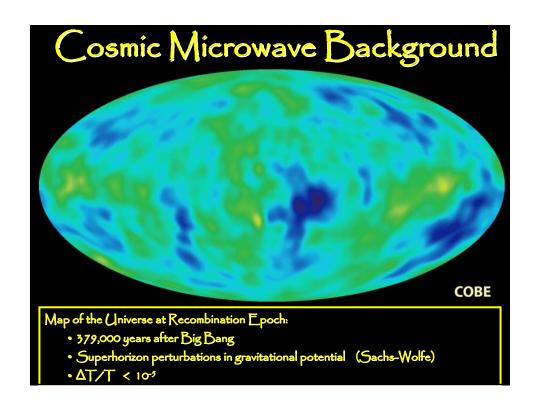


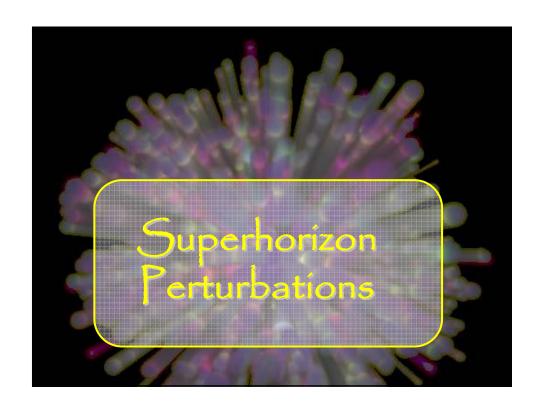


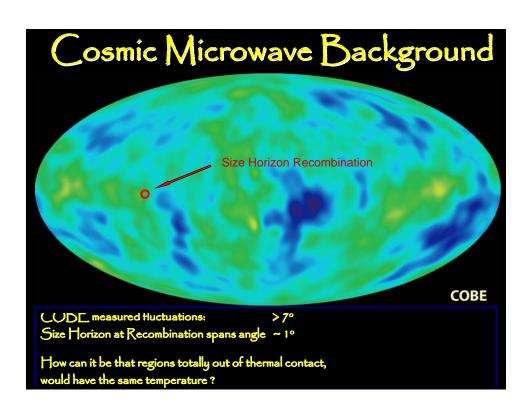


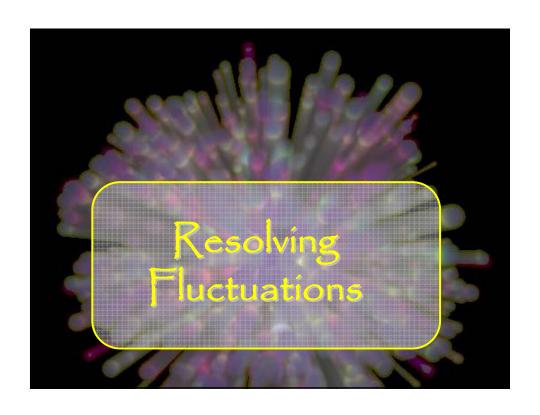


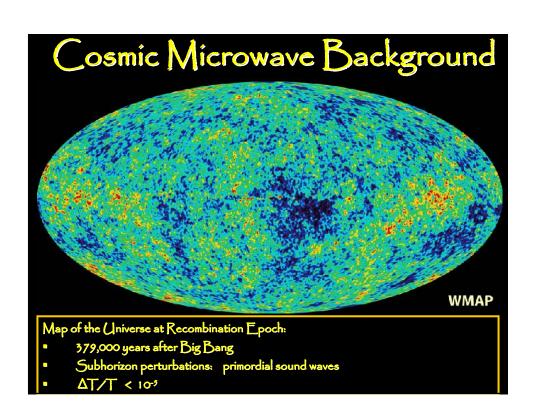




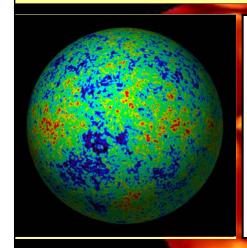








#### Temperature Anisotropies

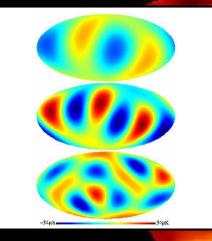


Temperature Perturbations in terms of Spherical Harmonics:

$$T(\theta,\phi) = \sum_{l,m} a_{lm} Y_l^m(\theta,\phi)$$

$$\phi \sim \frac{\pi}{l} \sim \frac{180^{\circ}}{l}$$

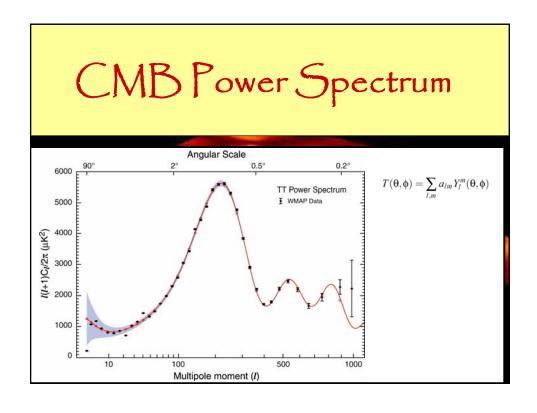
#### Temperature Anisotropies

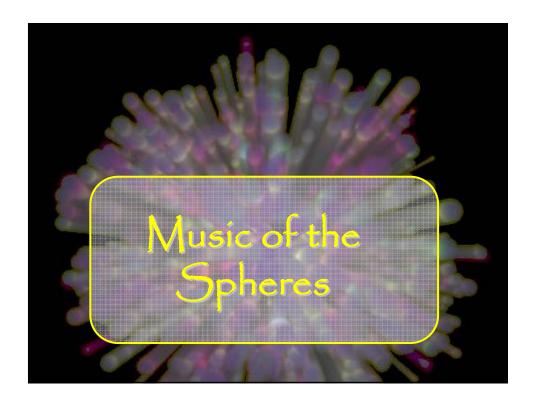


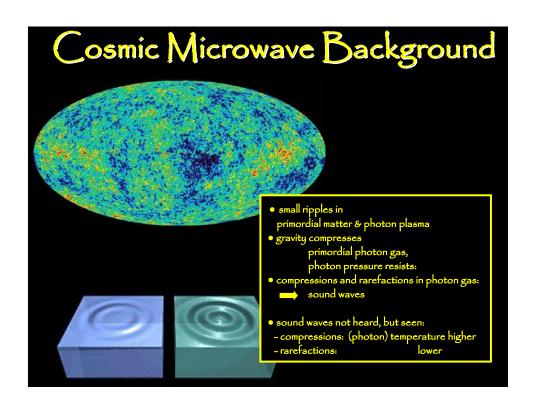
Temperature Perturbations in terms of Spherical Harmonics:

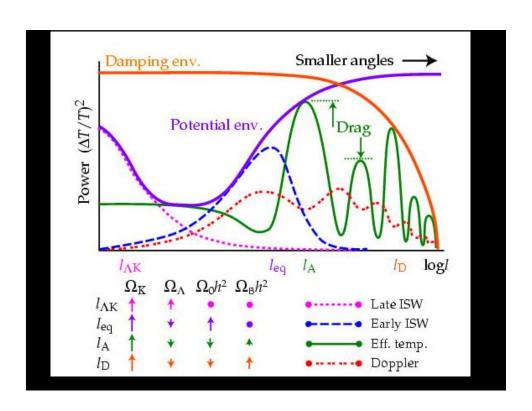
$$T(\theta,\phi) = \sum_{l,m} a_{lm} Y_l^m(\theta,\phi)$$

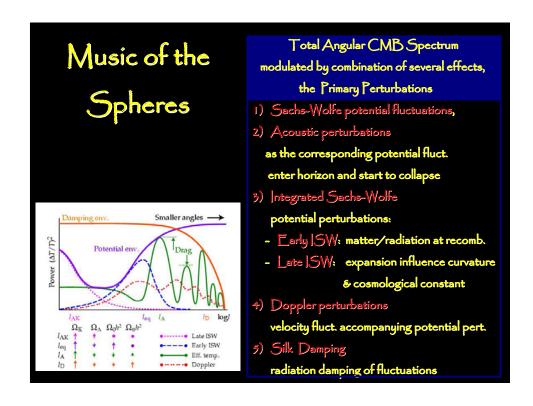
$$\phi \sim \frac{\pi}{l} \sim \frac{180^{\circ}}{l}$$

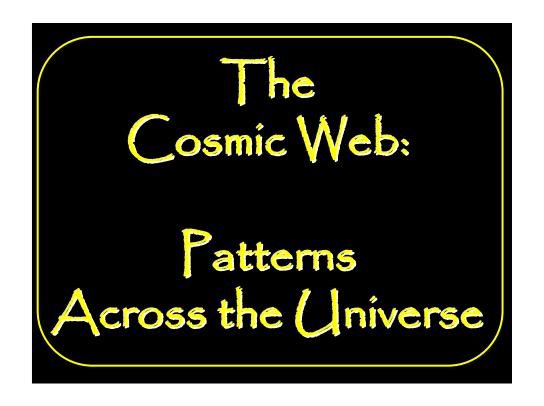




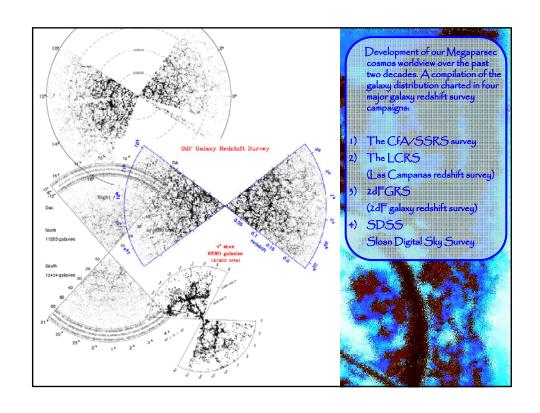








# A Universe of Galaxies Used as point tracers of underlying cosmic density field. Intention is to map this cosmic matter field on Megaparsec scales. \*LSS\* still reflects conditions primordial Universe: Cosmic Fossil

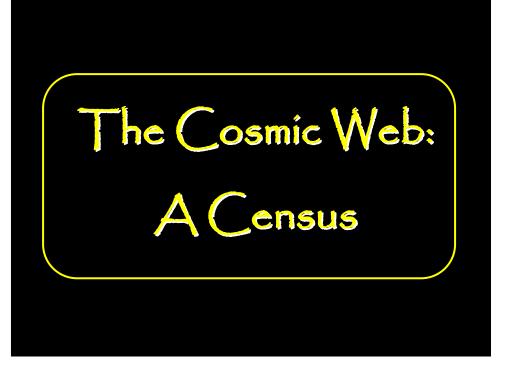


Over the past two decades we have witnessed a paradigm shift in our perception of the Megaparsec scale structure in the Universe. As increasing elaborate galaxy redshift surveys charted ever larger regions in the nearby Universe, an intriguingly complex and salient foamlike network came to unfold and establish itself as the quintessential characteristic of the cosmic matter and galaxy distribution.

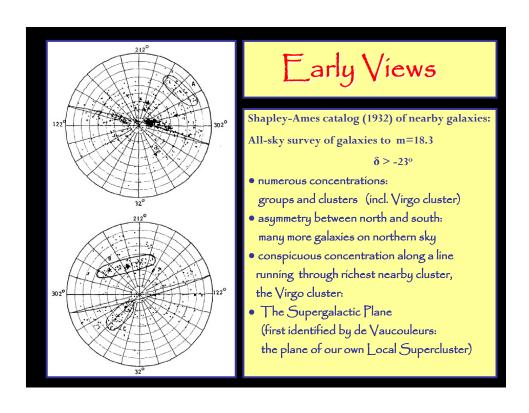
In a great many physical systems, the spatial organization of matter is one of the most readily observable manifestations of the forces and processes forming and moulding them. Richly structured morphologies are usually the consequence of the complex and nonlinear collective action of basic physical processes.

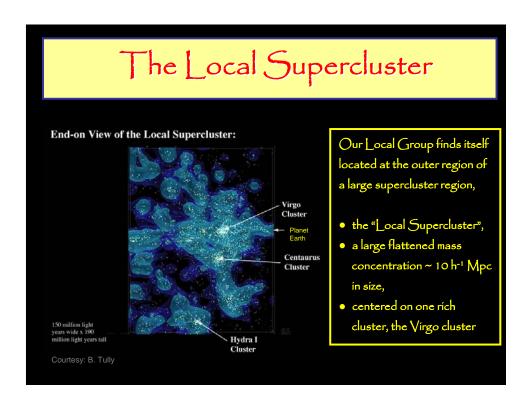
The vast Megaparsec cosmic web is undoubtedly one of the most striking examples of complex geometric patterns found in nature. In its own right, the vast dimensions and intricate composition of the cosmic foam make it one of the most imposing and intriguing patterns existing in the Universe. Its wide-ranging Importance stems from its status as a cosmic fossil. On a scale of tens up to a few hundred Megaparsecs It is still relatively straightforward to relate the configuration at the present cosmic epoch to that of the primordial matter distribution from which it emerged. With the cosmic foam seemingly representing this phase, it assumes a fundamental role in the quest for understanding the origin of all structures in the Universe.

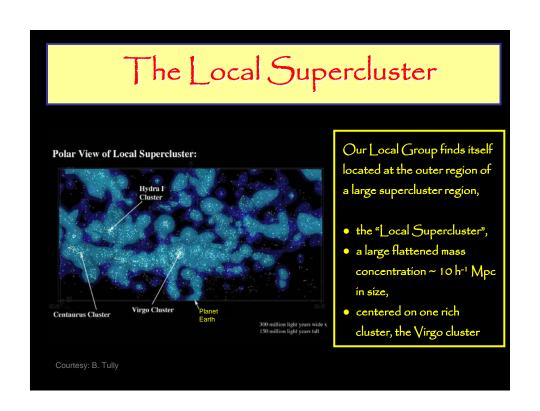
While its complex cellular morphology involves one of the most outstanding and evident aspects of the Cosmic foam, it has also remained one defying simple definitions which may be the cause of it having Remained one of the least addressed aspects. The geometry of the cosmic foam may be described as a nontrivial stochastic assembly of various anisotropic and asymmetric elements. A major deficiency in the vast majority of studies on the large scale distribution of galaxies has been the lack of suitable quantitative and statistical characterizations of the truly fundamental aspects of the comsic foam geometry.

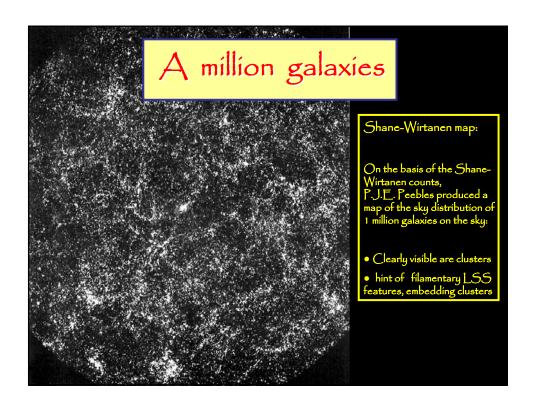


## Sky Maps: world all around us









#### APM survey

• Sky map:

 $2 \times 10^6$  galaxies

17 < m < 20.5

· Uniformly defined

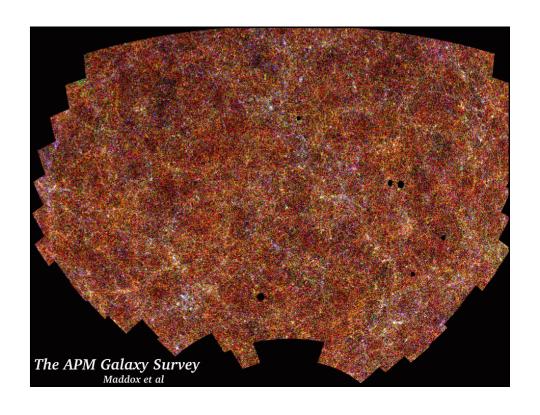
• Sky region: 4300 sq. deg

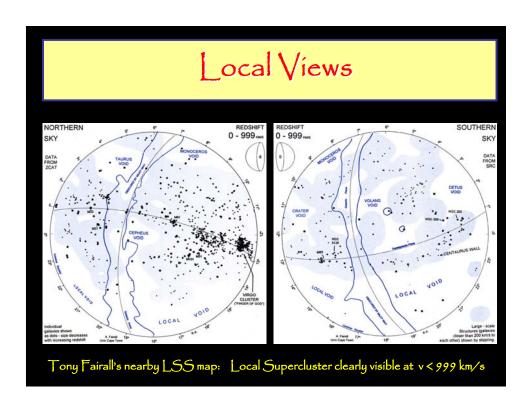
4300 sq. deg. 185 UK Schmidt plates, 6° x 6°

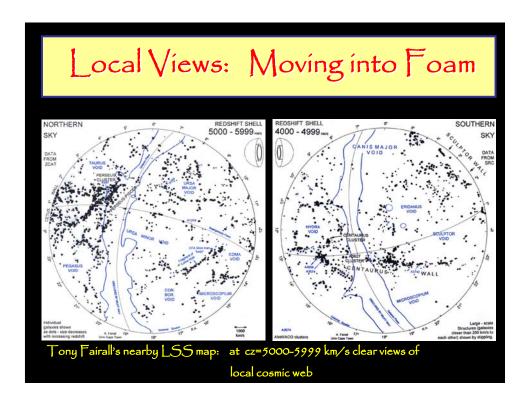
• Large inhomogeneities, hints of weblike patterns, with clusters at densest regions.

courtesy:

S. Maddox, G. Efstathiou, W. Sutherland, D. Loveday





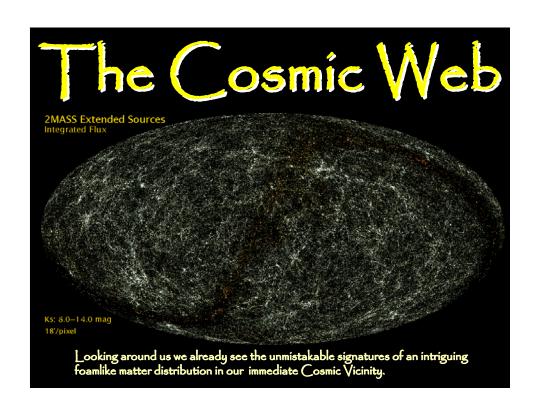


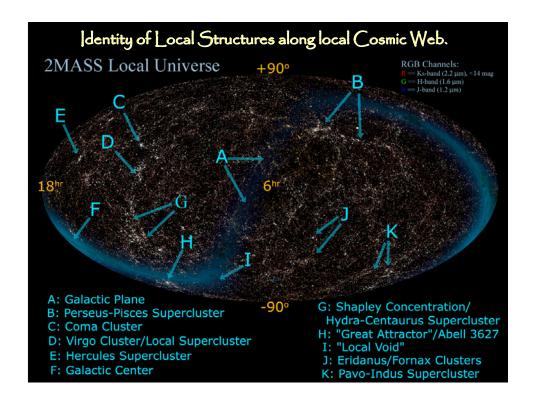
#### 2MASS survey

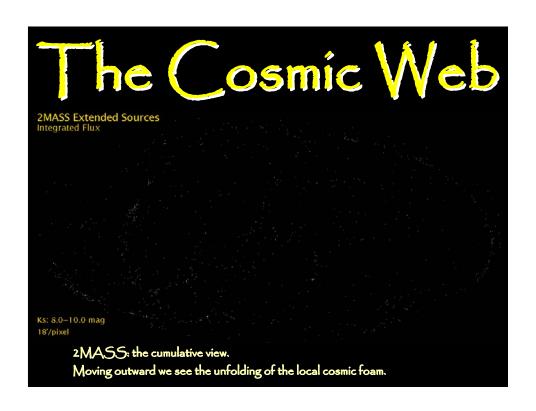
- 2MASS all-sky survey: ground-based near-infrared survey whole sky, J(1.2  $\mu$ m), H(1.6  $\mu$ m), K(2.2  $\mu$ m)
- 2MASS extended source catalog (XSC):
   1.5 million galaxies
- unbiased sample nearby galaxies
- photometric redshifts: depth in 2MASS maps, "cosmic web" of (nearby) superclusters spanning the entire sky.

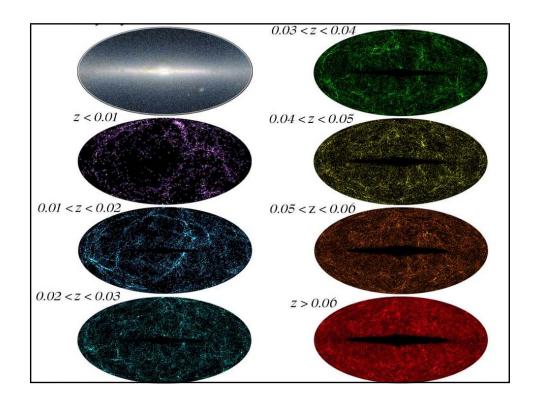
courtesy:

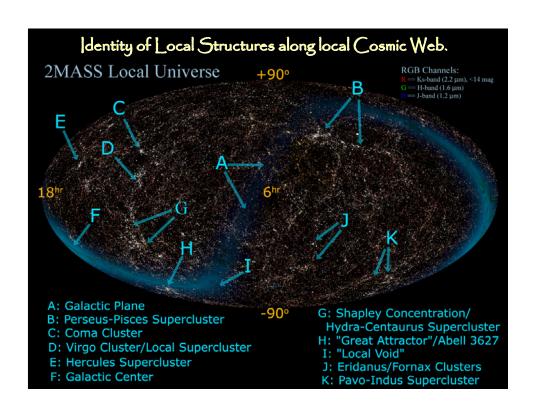
T. Jarrett









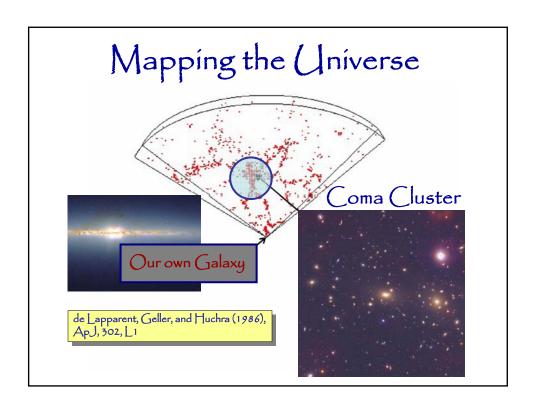


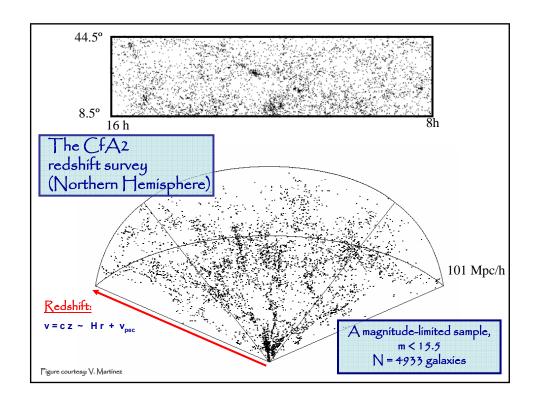
### Maps of the Local Universe

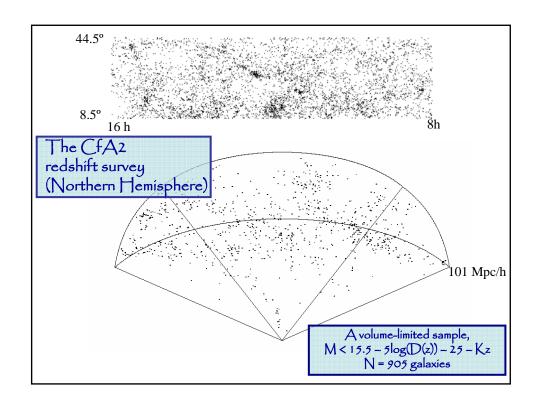
The Cosmic Web Revealed:

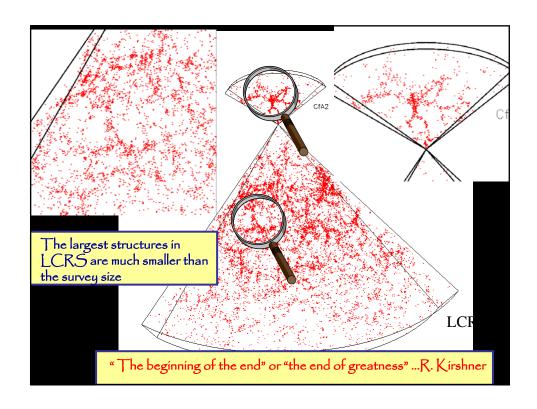
The CfA2 and SDSS survey slices

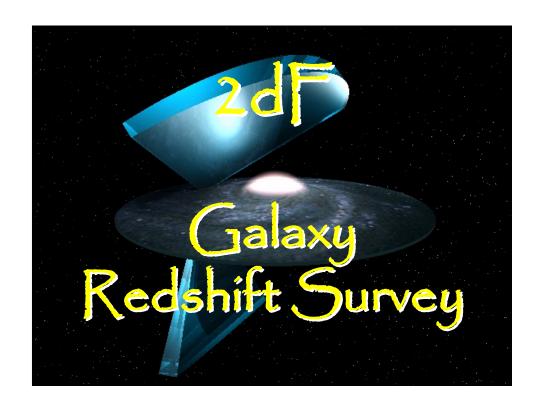
(de Lapparent, Geller, Huchra, ...

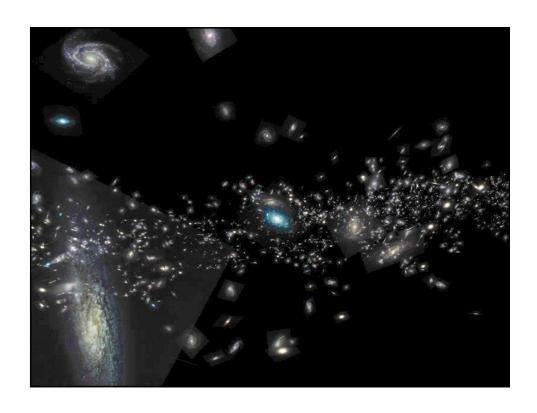


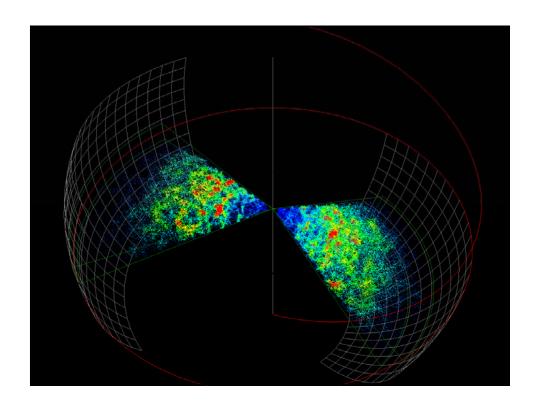


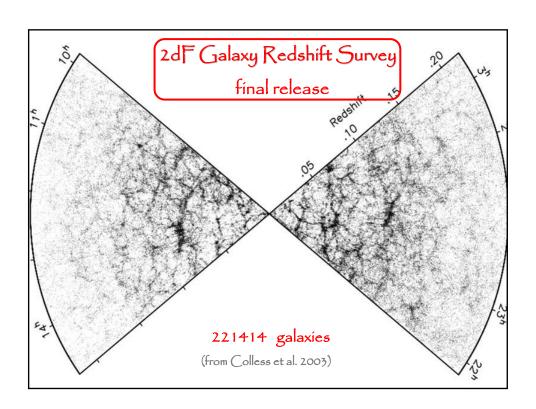












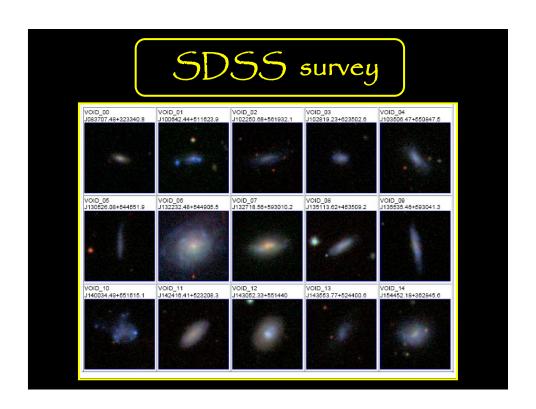
#### SDSS survey

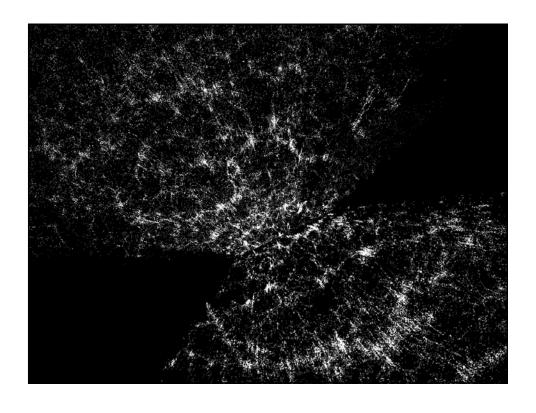
- Largest and most systematic (digital!) sky survey in history of astronomy.

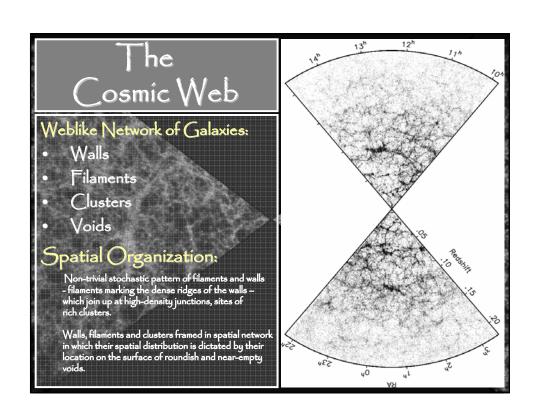
  Images sky in 5 photometric bands!!!!

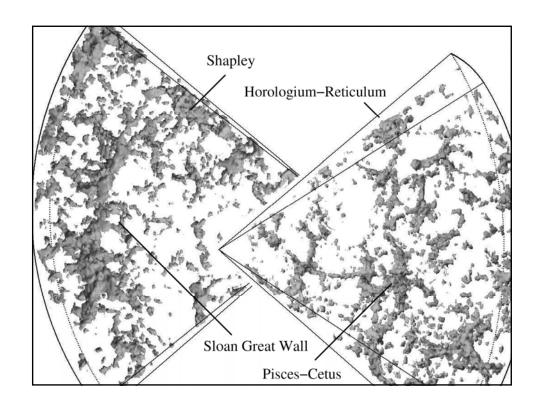
- Down to apparent magnitude r~23.1 Covers ~ 25% of the sky: 8452 sq. deg. With 2dFGRS, the SDSS will produce the most extensive map of the
- spatial structure of our cosmic neighbourhood.

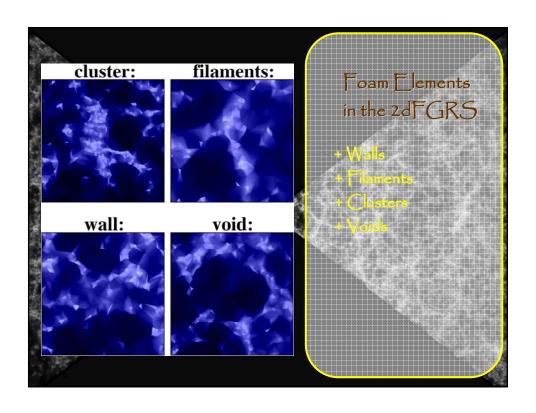
   Million galaxies subsequently selected for measuring redshift z: electromagnetic spectrum
- Total:
  - 108 stars, 108 galaxies, 105 quasars sky survey: spectroscopy: 106 galaxies, 105 quasars, 105 stars

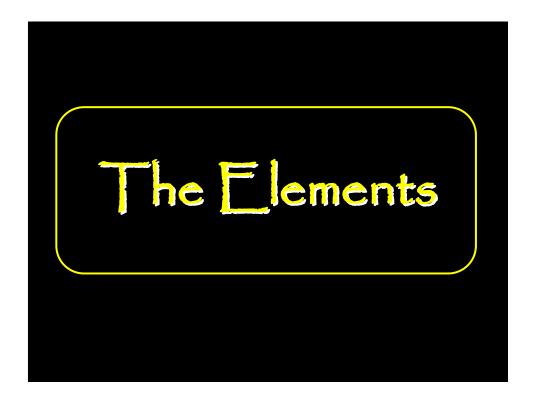


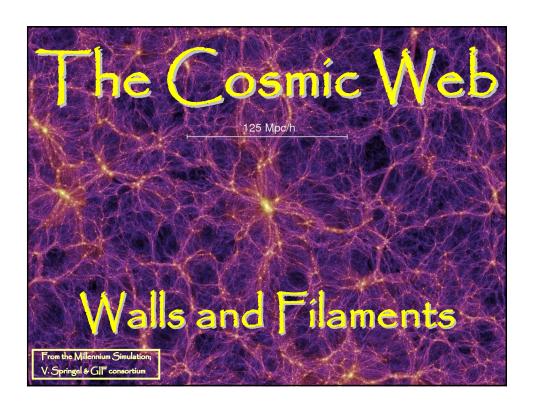


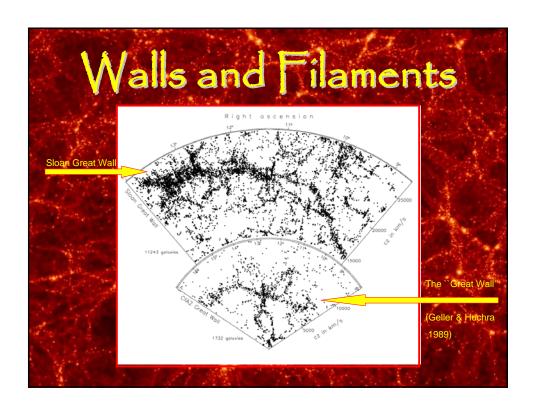


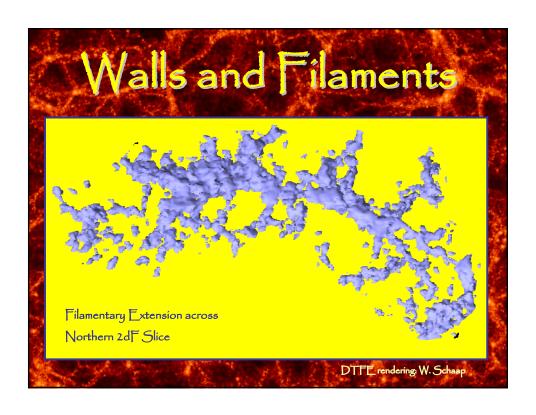


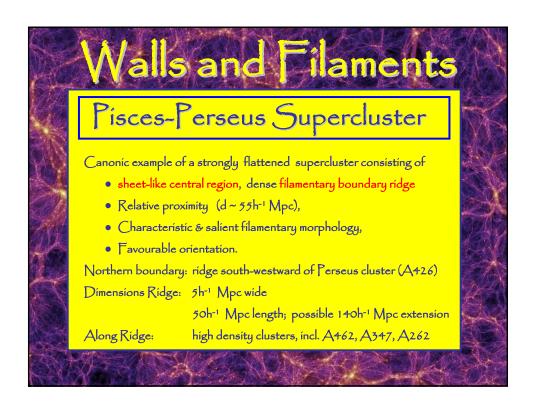


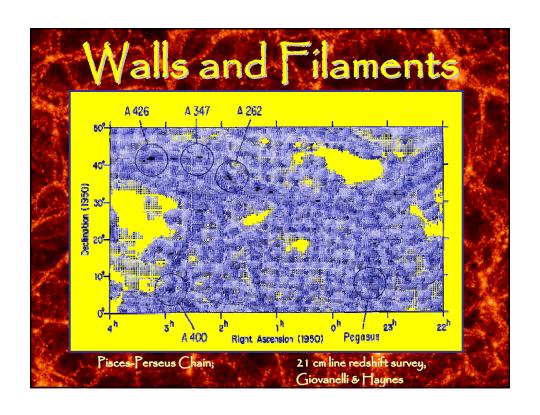


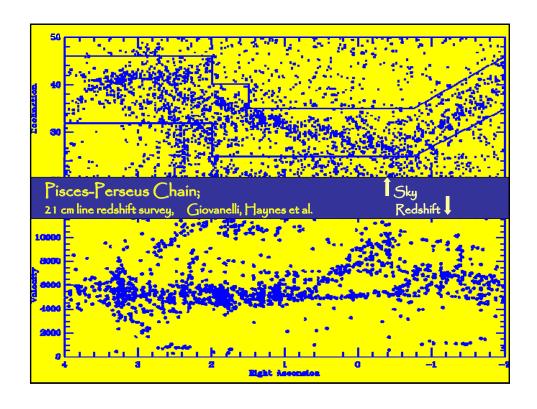


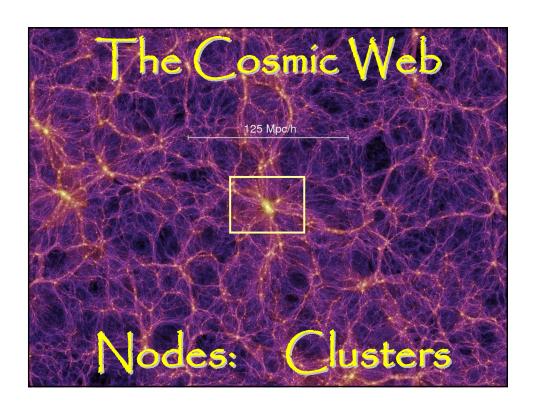


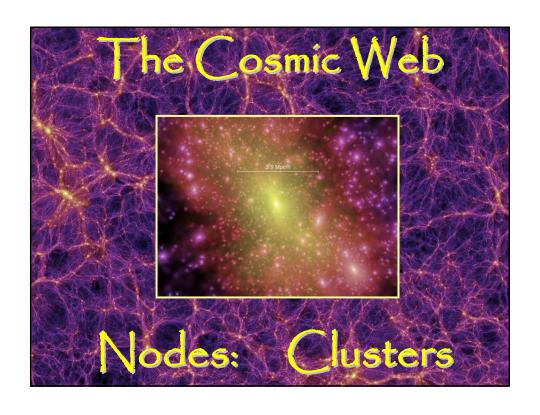


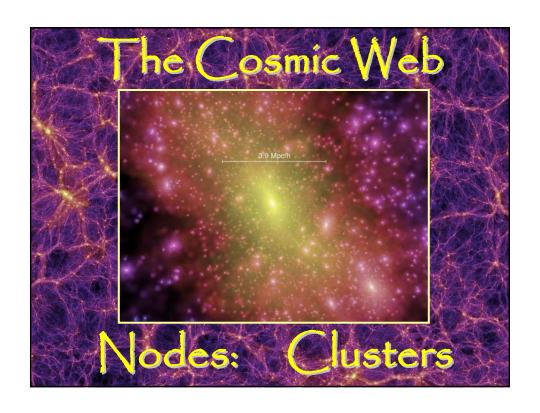


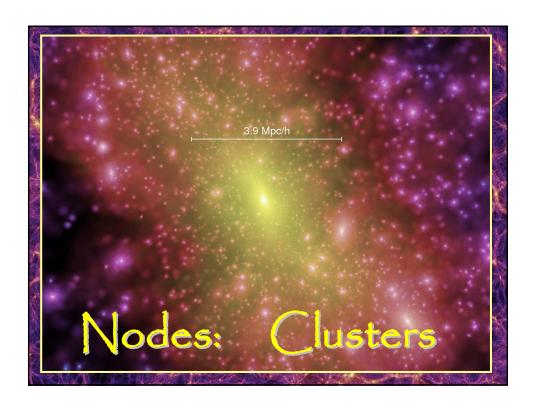


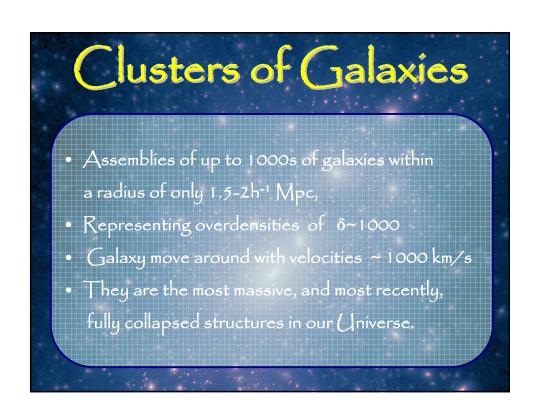


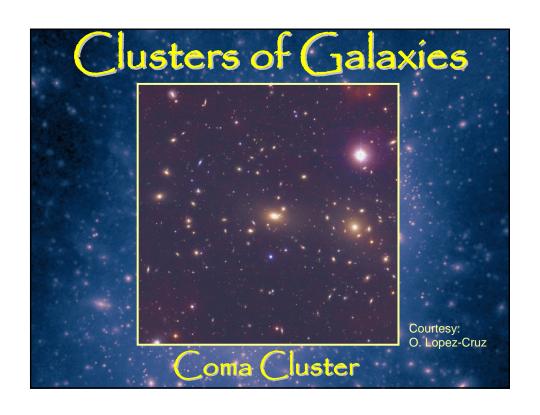


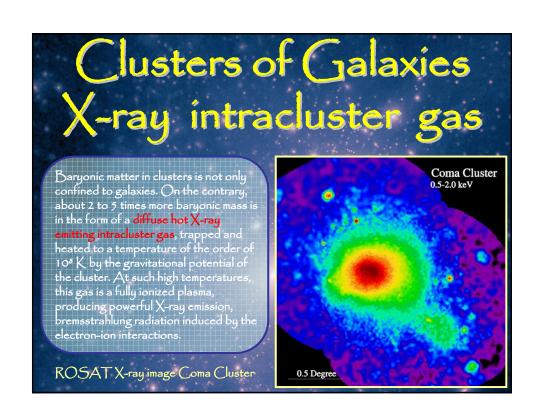


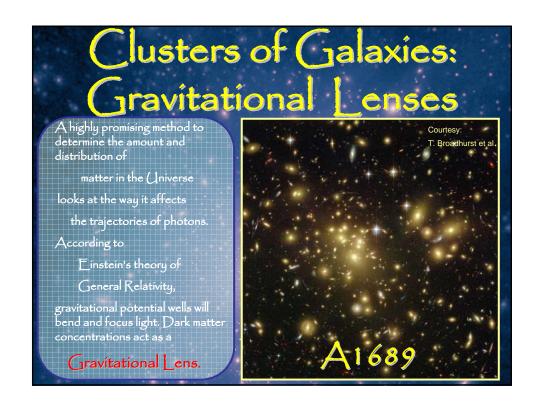


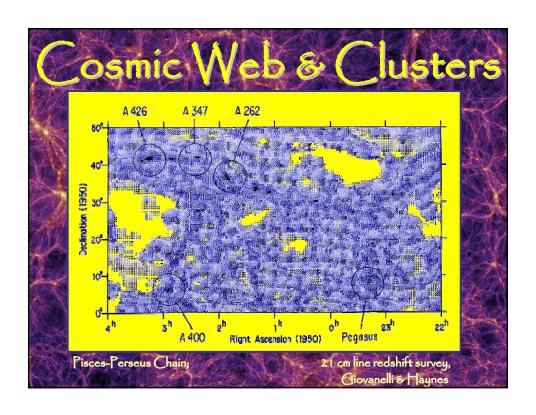


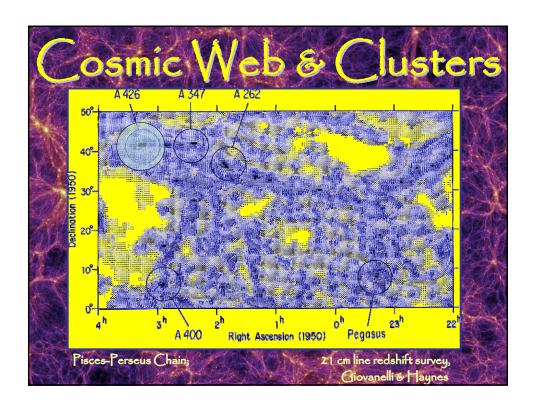


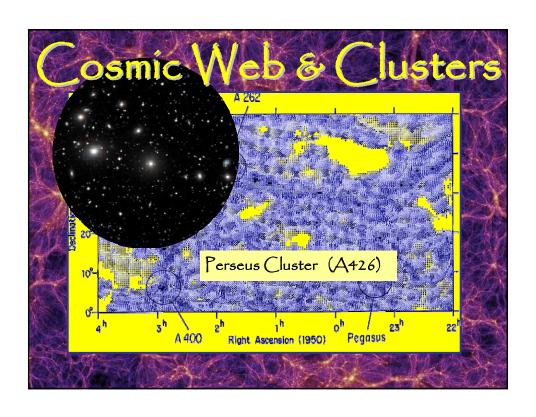


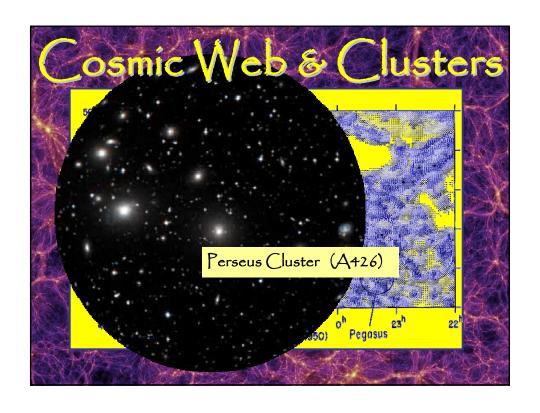


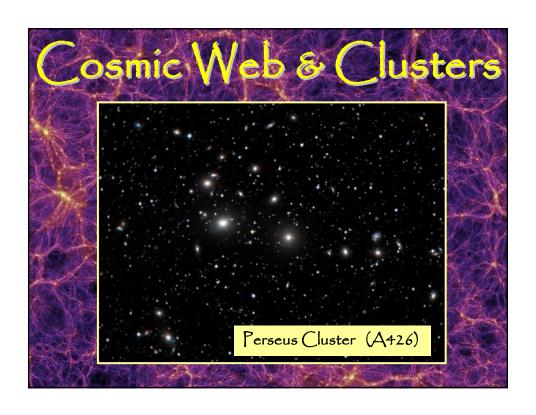


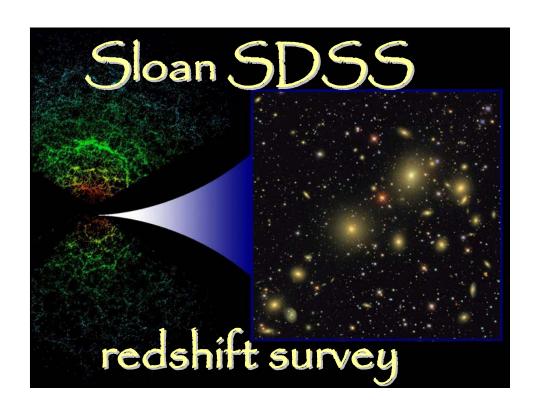


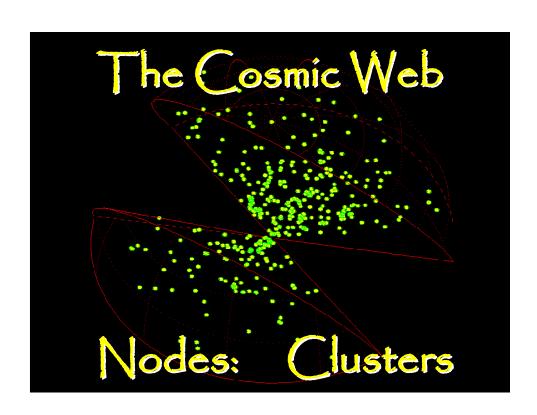


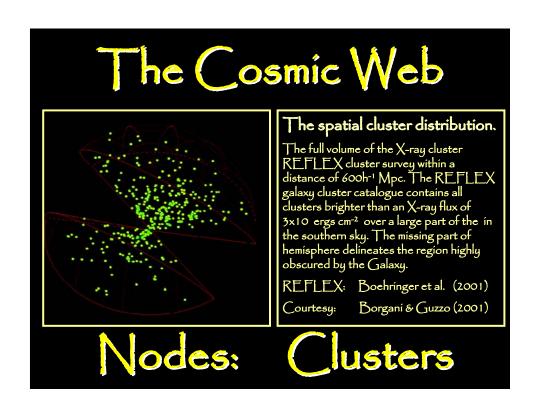


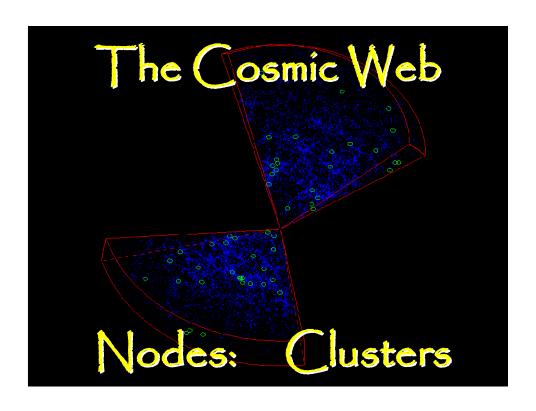


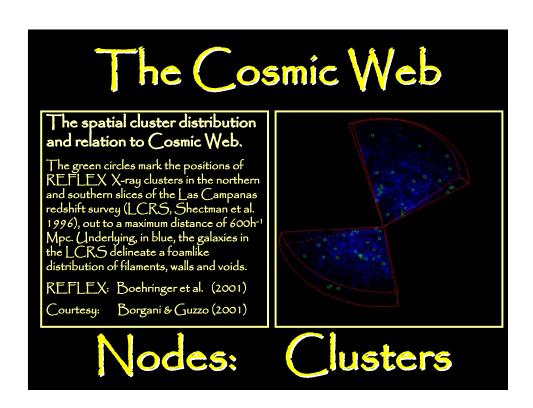


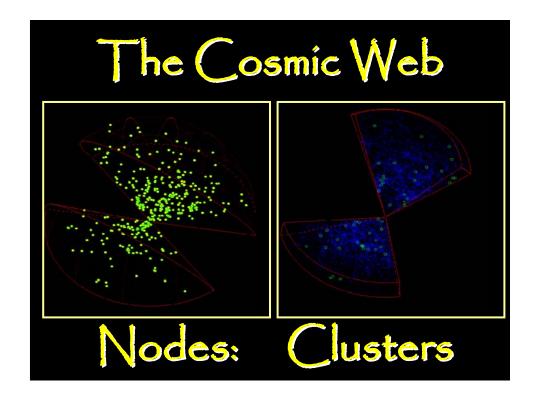


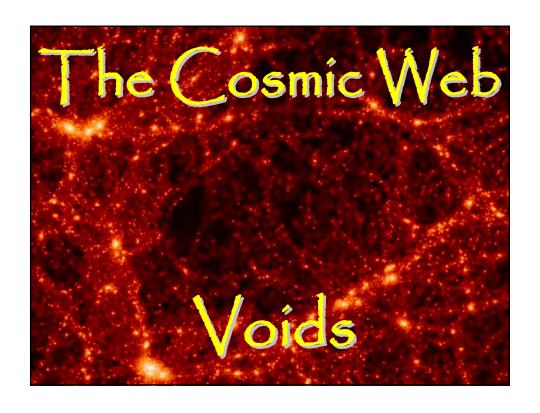


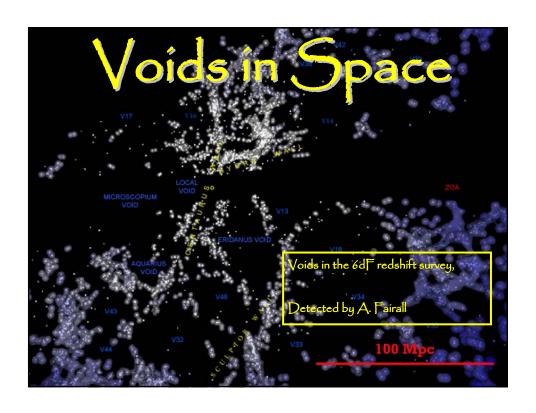


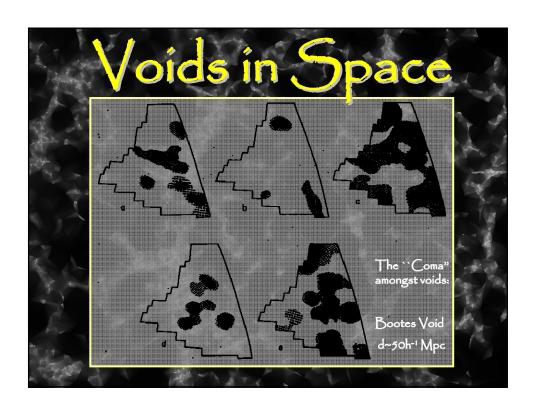


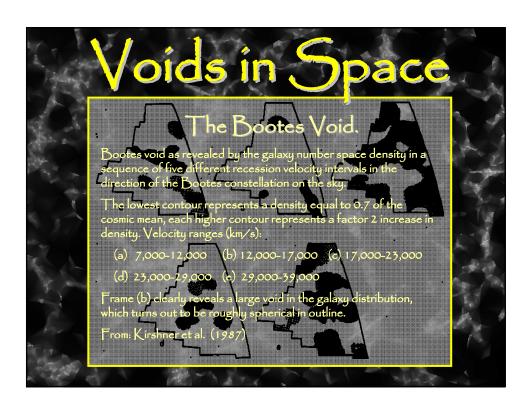


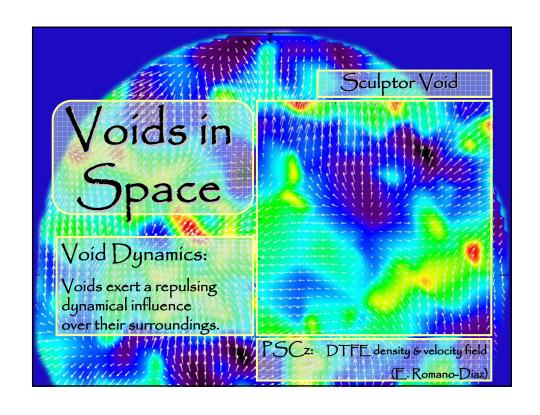


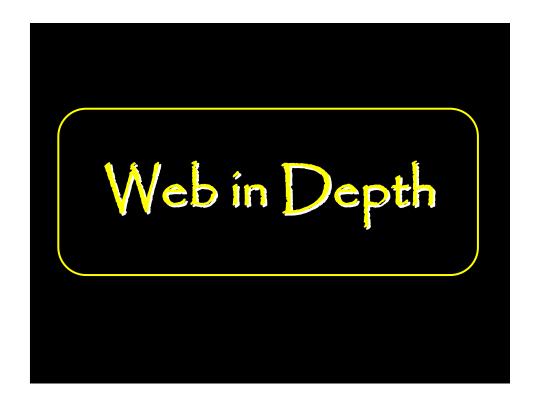




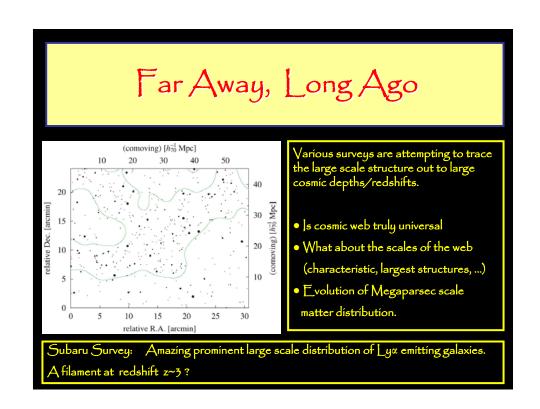




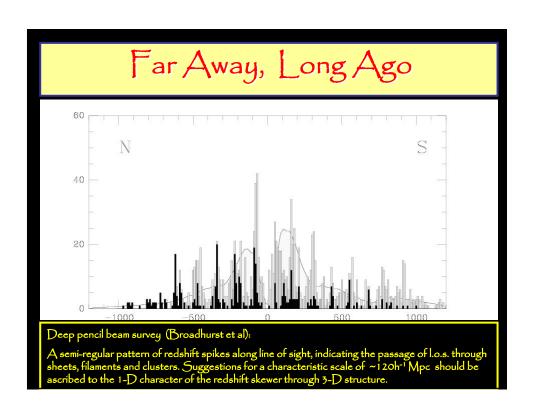




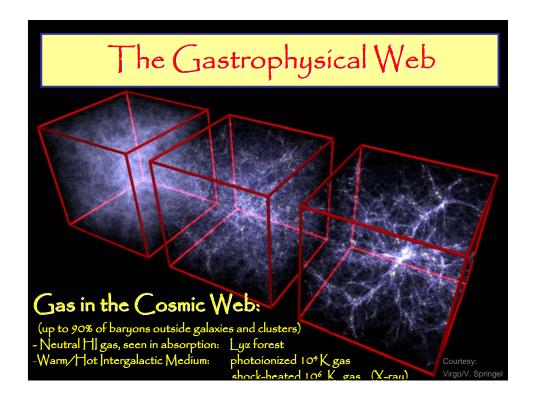


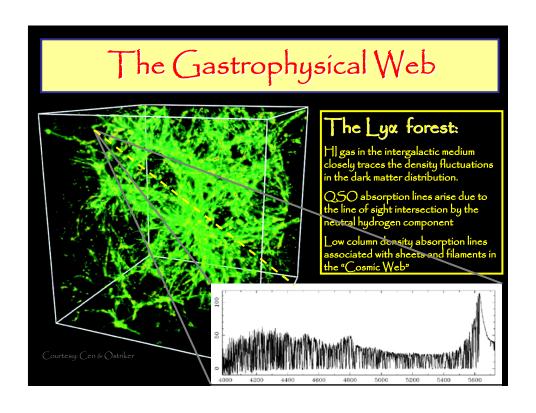


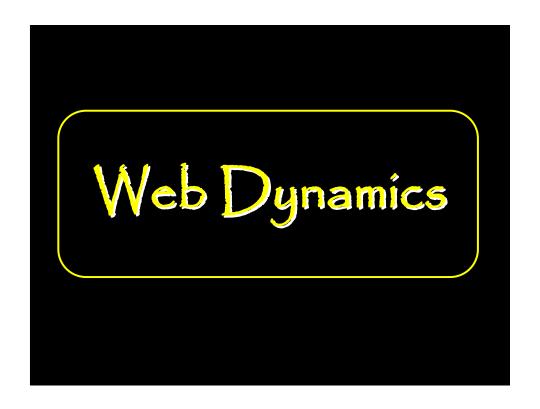


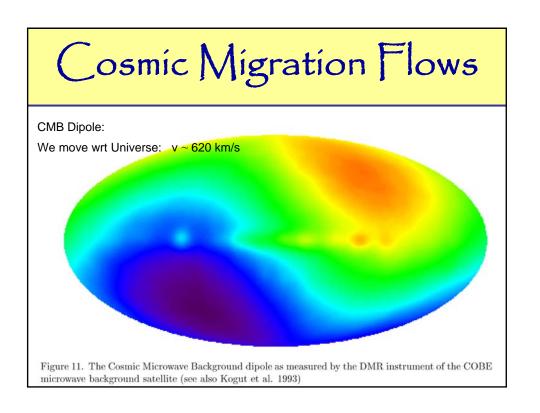


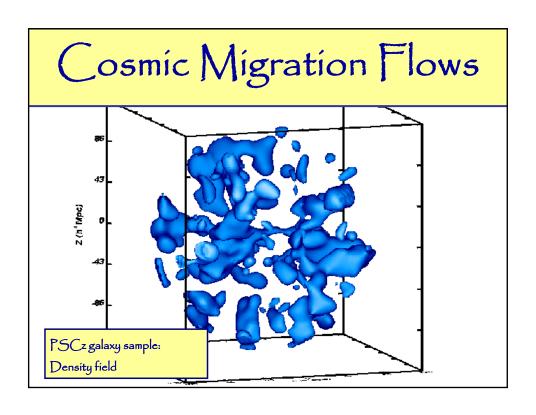








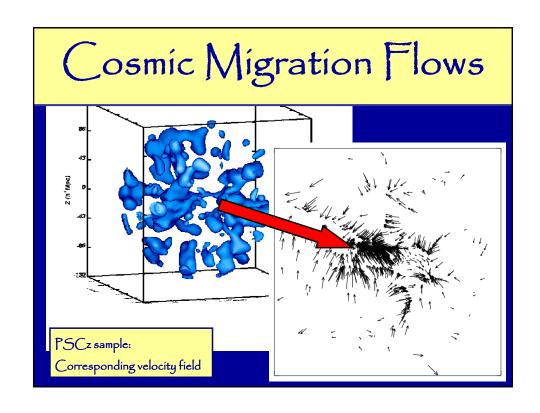


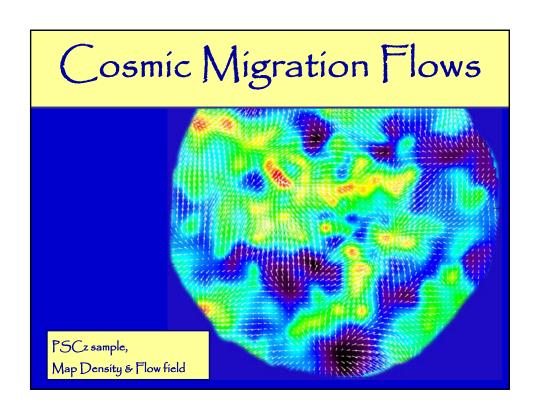


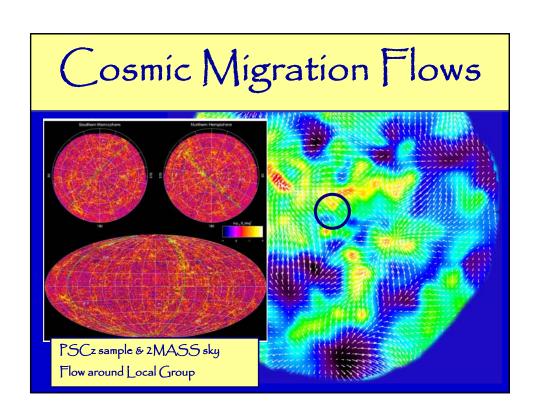
## Cosmic Migration Flows

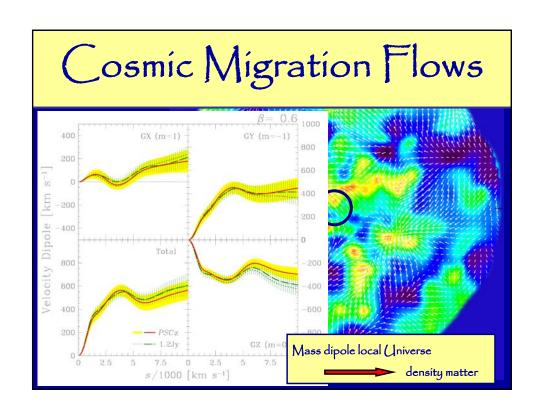
$$\mathbf{v} = \frac{H f}{4\pi G \rho_u} \mathbf{g} = \frac{2 f}{3H\Omega} \mathbf{g}$$

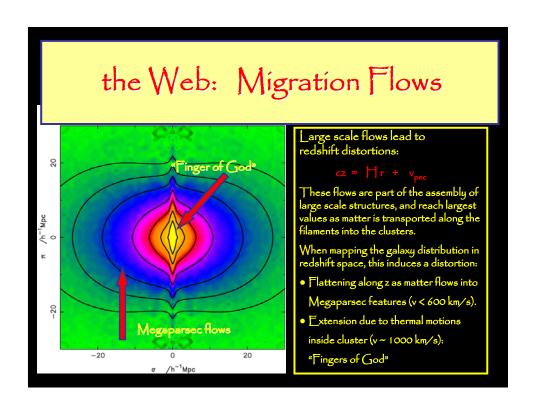
$$\mathbf{v}(\mathbf{x},t) = \frac{H}{4\pi} \frac{f(\Omega_m)}{b} a \int d\mathbf{x}' \frac{\delta_{gal}(\mathbf{x}',t)}{|\mathbf{x}'-\mathbf{x}|^3} \frac{(\mathbf{x}'-\mathbf{x})}{|\mathbf{x}'-\mathbf{x}|^3}$$
(158)



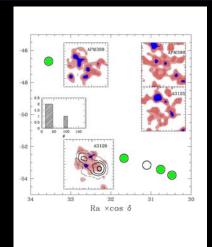








### Web Dynamics: Alignments



Of outmost importance for understanding the dynamical origin of the cosmic web is that of alignments between and around clusters of galaxies.

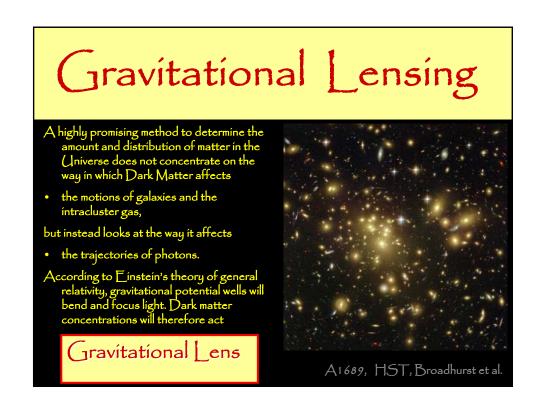
The presence of such alignments is ar indication for the tidal origin of the cosmic web with the clusters as the dominant tidal agents.

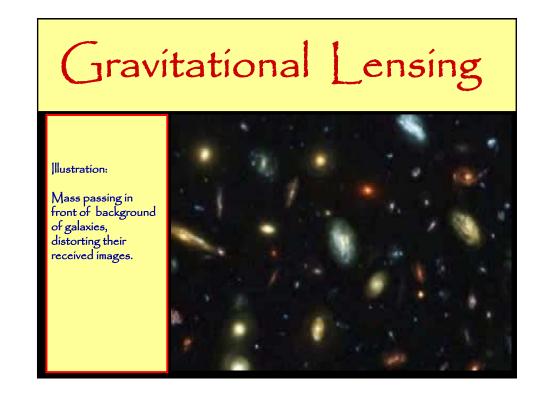
This forms an essential ingredient of the "Cosmic Web" theory of Bond et al.

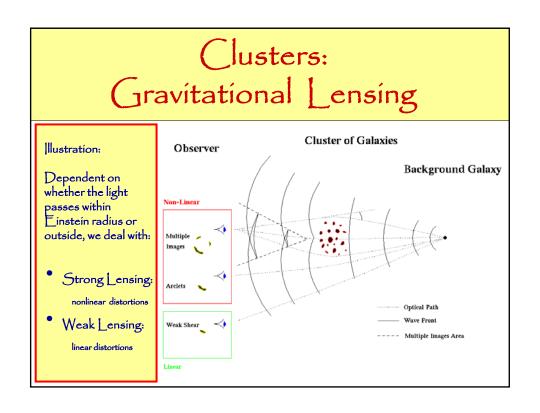
Work by various groups, most notably Plionis and collaborators, indicate that indeed clusters, and galaxies around them, reveal significant alignments.

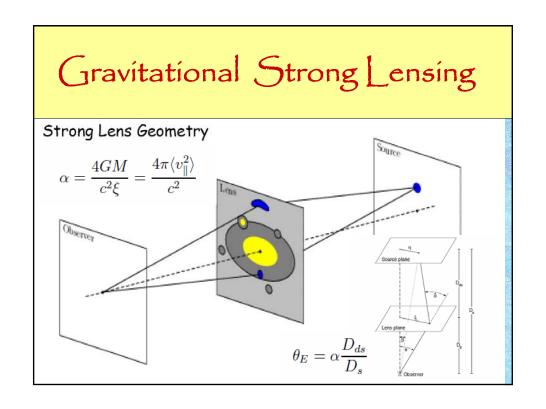
Plionis 2001

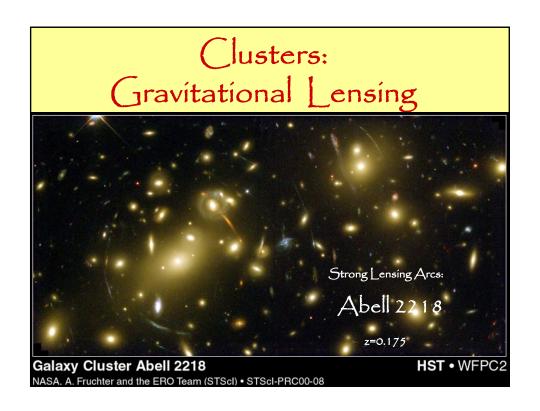


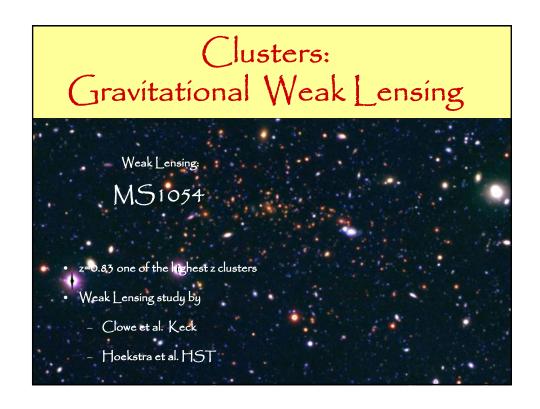




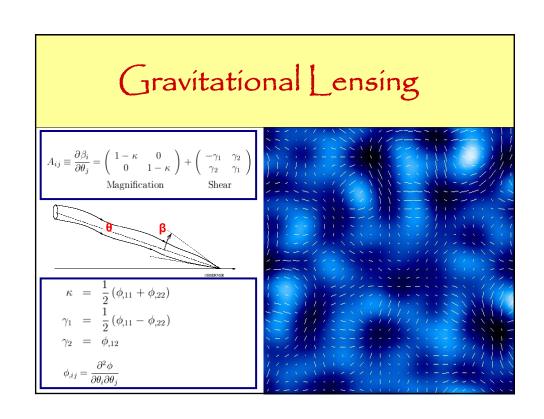








# Gravitational Weak Lensing Lensed Galaxies Shear map + Projected Mass



### Gravitational Lensing

$$\kappa = \frac{1}{2} (\phi_{,11} + \phi_{,22})$$

$$\gamma_1 = \frac{1}{2} (\phi_{,11} - \phi_{,22})$$

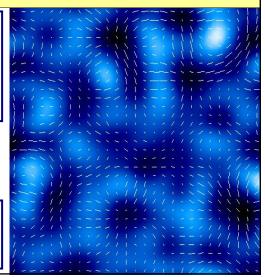
$$\gamma_2 = \phi_{,12}$$

$$\phi_{,ij} = \frac{\partial^2 \phi}{\partial \theta_{,22}}$$

Lensing Potential related to

Peculiar Gravitational Potential

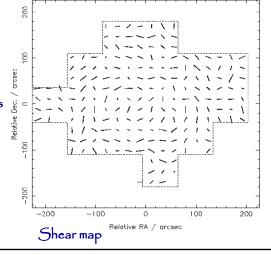
$$\phi(\mathbf{r}) = \frac{2}{c^2} \int_0^r \, dr' \Phi(\mathbf{r}') \left(\frac{1}{r} - \frac{1}{r'}\right)$$

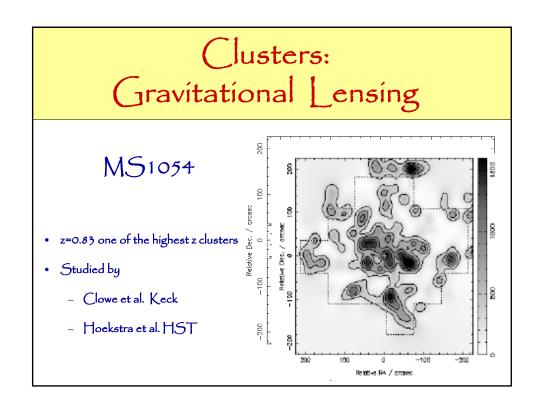


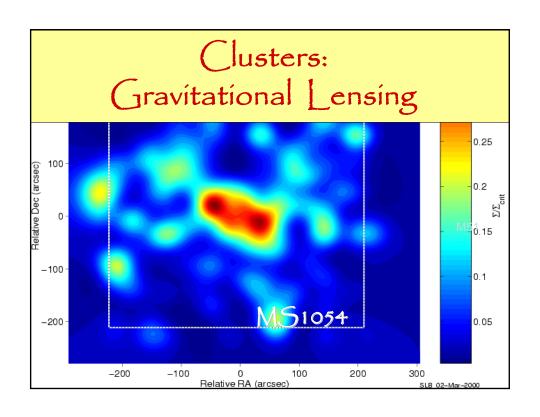
# Clusters: Gravitational Lensing

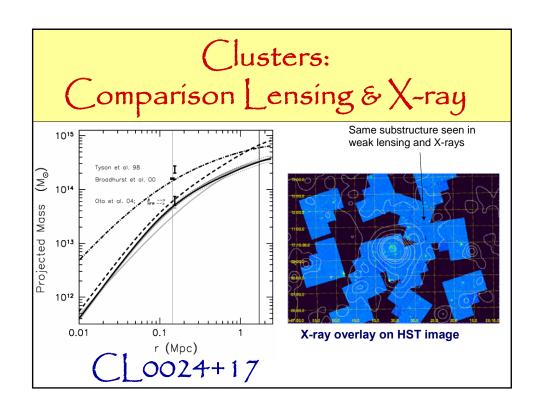
### MS1054

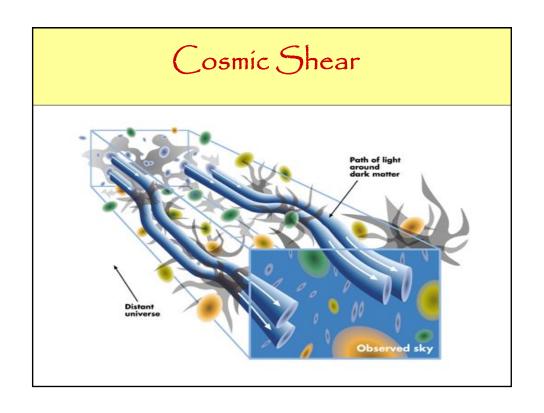
- z=0.83 one of the highest z clusters
- Studied by
  - Clowe et al. Keck
  - Hoekstra et al. HST

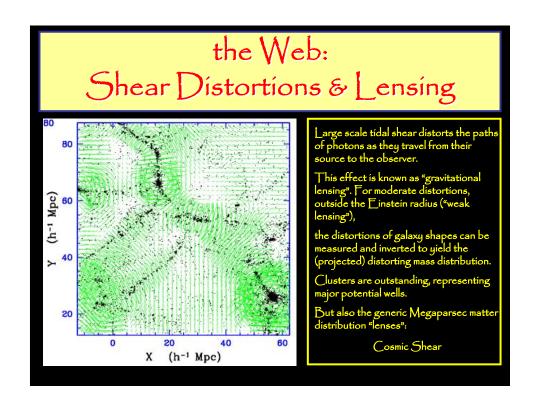


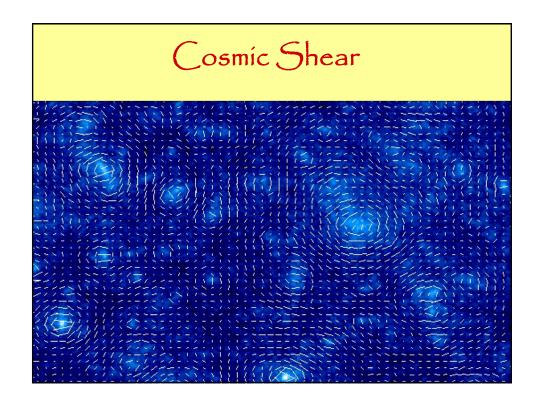


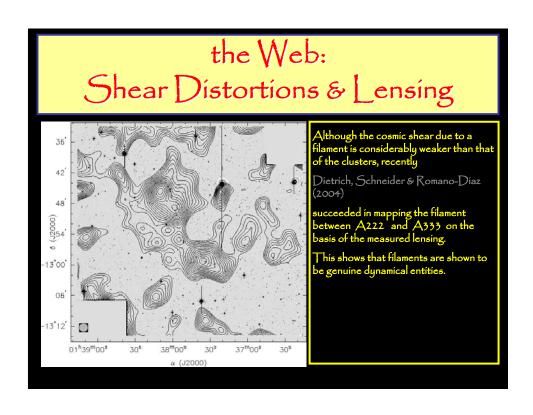


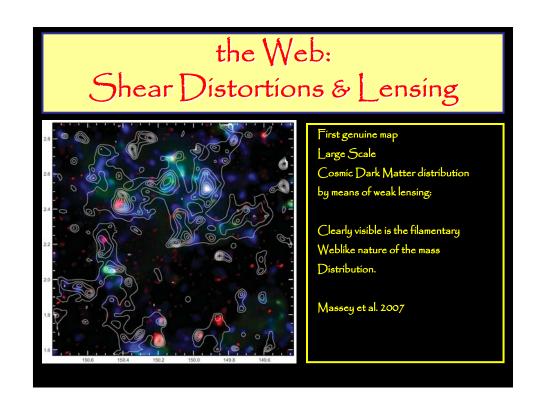




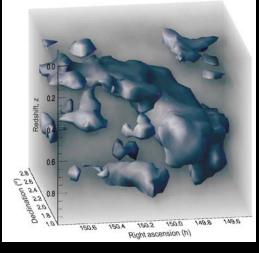








### the Web: Shear Distortions & Lensing



First genuine map
Large Scale
Cosmic Dark Matter distribution
by means of weak lensing:

Clearly visible is the filamentary Weblike nature of the mass Distribution.

Massey et al. 2007