

FRW Dynamics

In a FRW Universe, densities are in the order of the critical density, the density at which the Universe has a flat curvature

$$\rho_{crit} = \frac{3H_0^2}{8\pi G} = 1.8791h^2 \times 10^{-29} g cm^{-3}$$

$$\rho_0 = 1.8791 \times 10^{-29} \,\Omega h^2 \, g \, cm^{-3}$$
$$= 2.78 \times 10^{11} \,\Omega h^2 \qquad M_{\odot} Mpc^{-3}$$

FRW Dynamics

In a matter-dominated Universe, the evolution and fate of the Universe entirely determined by the (energy) density in units of critical density:

$$\Omega$$
 \equiv $rac{
ho}{
ho_{crit}}$

Arguably, Ω is the most important parameter of cosmology !!!

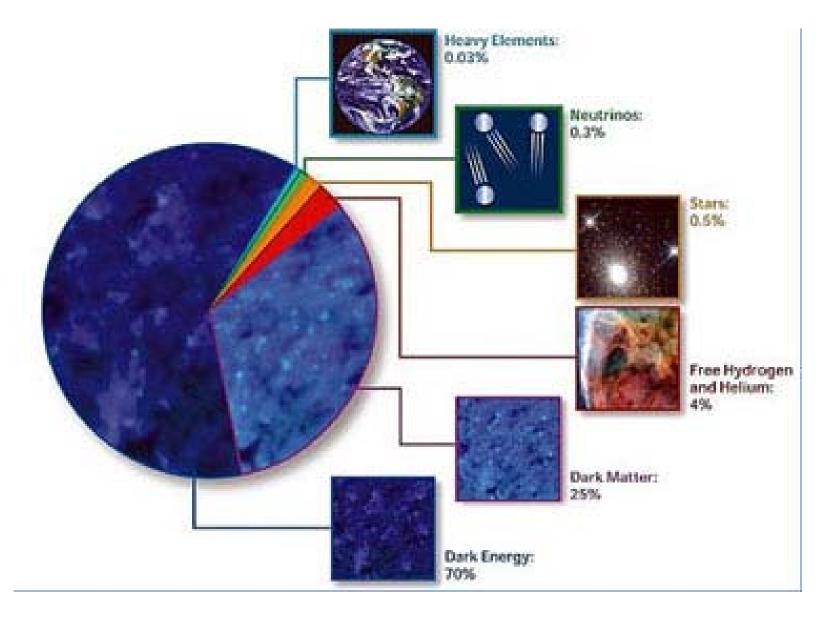
Present-day
Cosmic Density:

$$\rho_0 = 1.8791 \times 10^{-29} \,\Omega h^2 \, g \, cm^{-3}$$
$$= 2.78 \times 10^{11} \,\Omega h^2 \quad M_{\odot} Mpc^{-3}$$

what the Universe exists of:

Cosmic Constituents

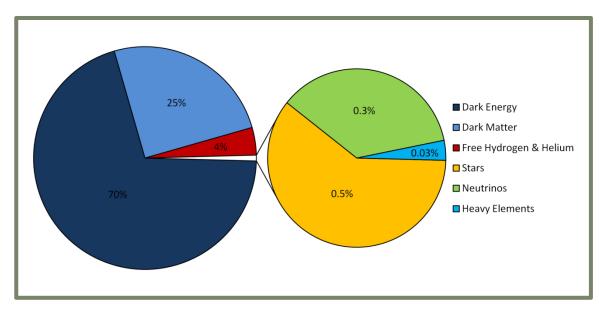
Cosmic Components



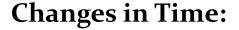
Cosmic Energy Inventarisation

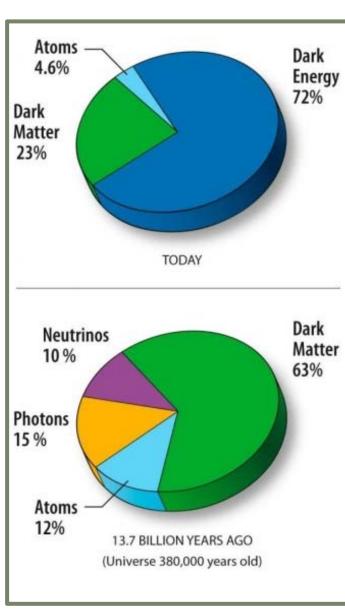
| 1 1.1 1.2 1.3 | dark sector dark energy dark matter primeval gravitational waves | | 0.72 ± 0.03 0.23 ± 0.03 $\lesssim 10^{-10}$ | 0.954 ± 0.003 |
|---|---|--|---|--|
| 2 2.1 2.2 2.3 | primeval thermal remnants electromagnetic radiation neutrinos prestellar nuclear binding energy | | $10^{-4.3\pm0.0}$ $10^{-2.9\pm0.1}$ $-10^{-4.1\pm0.0}$ | 0.0010 ± 0.0005 |
| 3 3.1 3.1a 3.1b | baryon rest mass warm intergalactic plasma virialized regions of galaxies intergalactic intracluster plasma | $0.024 \pm 0.005 \\ 0.016 \pm 0.005$ | 0.040 ± 0.003 0.0018 ± 0.0007 | 0.045 ± 0.003 |
| 3.3 3.4 | main sequence stars | spheroids and bulges disks and irregulars | $0.0015 \pm 0.0004 \\ 0.00055 \pm 0.00014$ | |
| 3.5 3.6 3.7 3.8 3.9 3.10 | white dwarfs neutron stars black holes substellar objects HI + HeI molecular gas | | $egin{array}{c} 0.00036 \pm 0.00008 \\ 0.00005 \pm 0.00002 \\ 0.00007 \pm 0.00002 \\ 0.00014 \pm 0.00007 \\ 0.00062 \pm 0.00010 \\ 0.00016 \pm 0.00006 \end{array}$ | 1 |
| 3.11 3.12 3.13 | planets condensed matter sequestered in massive black holes | | $10^{-6} 10^{-5.6 \pm 0.3} 10^{-5.4} (1 + \epsilon_n)$ | sterren slechts ~0.1% energie Heelal |
| 4 4.1 4.2 4.3 | primeval gravitational binding energy virialized halos of galaxies clusters large-scale structure | | $-10^{-7.2} \\ -10^{-6.9} \\ -10^{-6.2}$ | -10 ^{-6.1±0.1} |

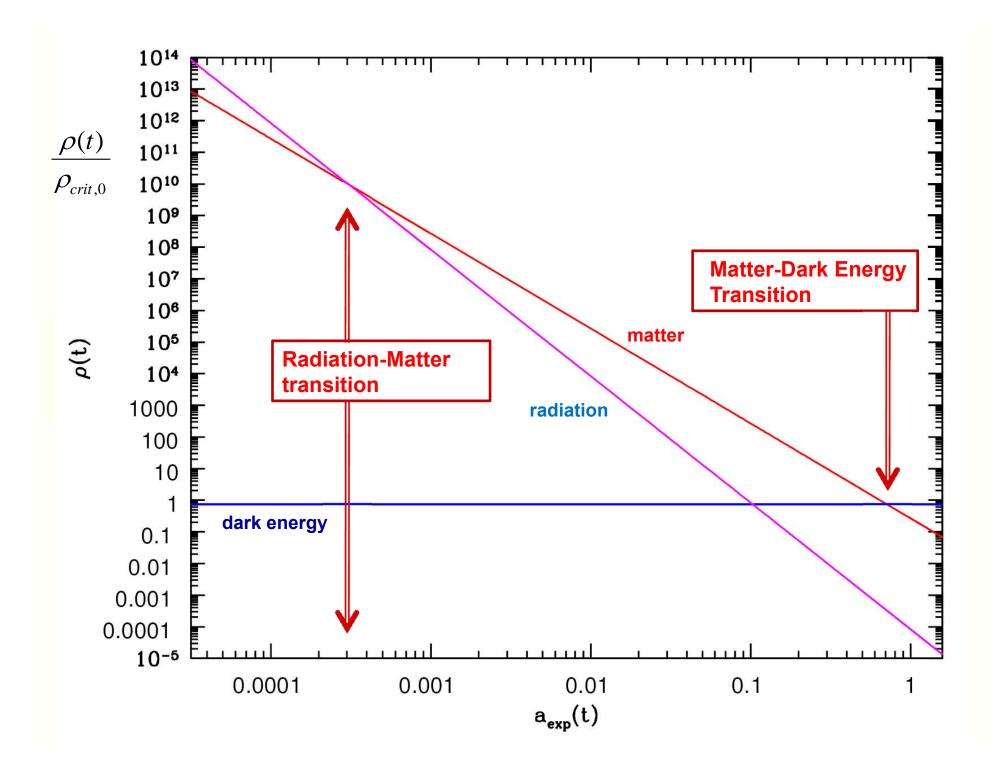
Cosmic Constitution

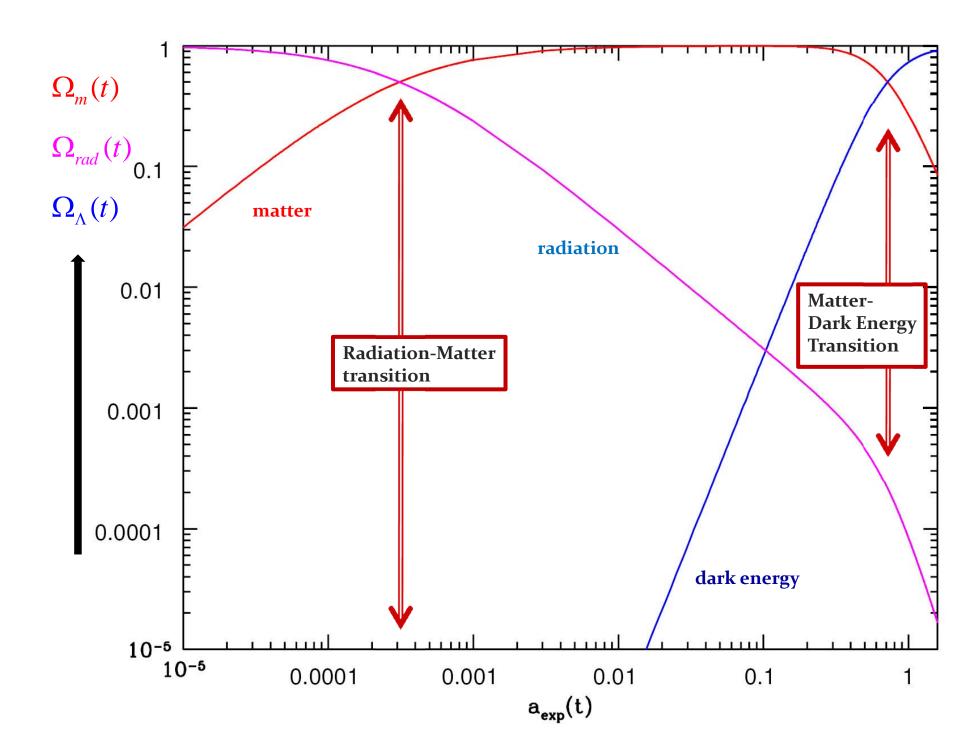


Cosmic Pie Diagram









Dark Matter

Matter

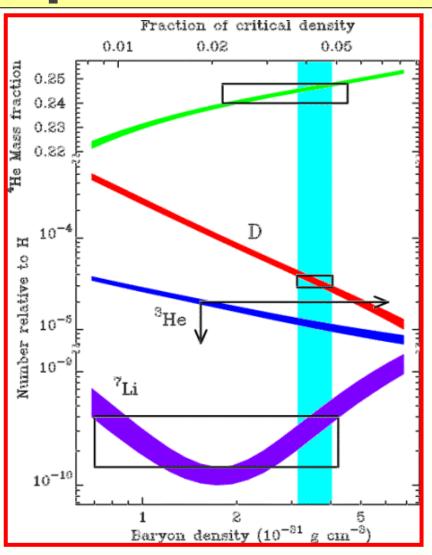
- Baryonic Matter
- Nonbaryonic Dark Matter

Baryonic Matter

The amount of baryonic matter in the Universe is (by now) very well determined, by two independent determinations:

- 1) Primordial Nucleosynthesis
- Acoustic Oscillations in CMB power spectrum,
 2nd peak (CMB)

Baryonic Matter: primordial nucleosynthesis



From measured light element abundances:

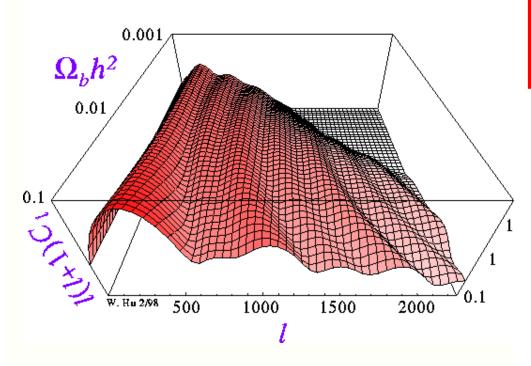
$$\eta \equiv \frac{n_B}{n_\gamma}$$



$$0.005 \lesssim \Omega_b h^2 \lesssim 0.026$$

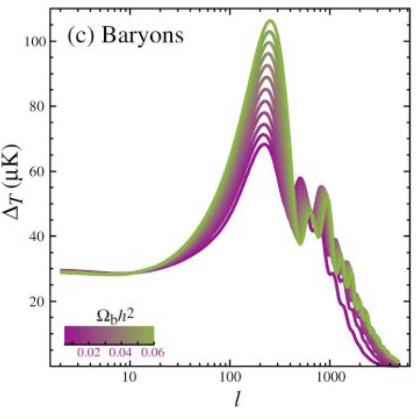
Baryonic Matter: CMB

Baryon-Photon Ratio in the CMB



 $\Omega_b h^2 \approx 0.0224 \pm 0.0009$ $\Omega_b \approx 0.044 \pm 0.004$

Due to baryon drag in the primordial baryon-photon gas, 2nd peak in CMB spectrum is suppressed:



Baryonic Matter

Cosmic Baryons

| 3 | baryon rest mass | | | 0.045 ± 0.003 |
|------|------------------------------------|----------------------|-----------------------------|-------------------|
| 3.1 | warm intergalactic plasma | | 0.040 ± 0.003 | |
| 3.1a | virialized regions of galaxies | 0.024 ± 0.005 | | |
| 3.1b | intergalactic | 0.016 ± 0.005 | | |
| 3.2 | intracluster plasma | | 0.0018 ± 0.0007 | |
| 3.3 | main sequence stars | spheroids and bulges | 0.0015 ± 0.0004 | |
| 3.4 | | disks and irregulars | 0.00055 ± 0.00014 | |
| 3.5 | white dwarfs | | 0.00036 ± 0.00008 | |
| 3.6 | neutron stars | | 0.00005 ± 0.00002 | |
| 3.7 | black holes | | 0.00007 ± 0.00002 | |
| 3.8 | substellar objects | | 0.00014 ± 0.00007 | |
| 3.9 | HI + HeI | | 0.00062 ± 0.00010 | |
| 3.10 | molecular gas | | 0.00016 ± 0.00006 | |
| 3.11 | planets | | 10^{-6} | |
| 3.12 | condensed matter | | $10^{-5.6\pm0.3}$ | |
| 3.13 | sequestered in massive black holes | | $10^{-5.4}(1 + \epsilon_n)$ | |

Baryonic Matter

Note:

- STARS are but a fraction of the total amount of baryonic matter
- There is still a large amount of undetected baryonic matter:
 - hiding as warm Intergalactic Gas (WHIM) ?

| 3 | baryon rest mass | | | 0.045 ± 0.003 |
|------|------------------------------------|----------------------|---------------------------|-------------------|
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Non-baryonic DM: candidates

WIMPs: Weakly Interacting Massive Particles

- neutrinos

- sterile neutrinos

- neutralinos

-

MACHOs: Massive astrophysical compact halo object

Modified Gravity: modification of General Relativity

SIMPs ... Strongly Interacting Massive Particles

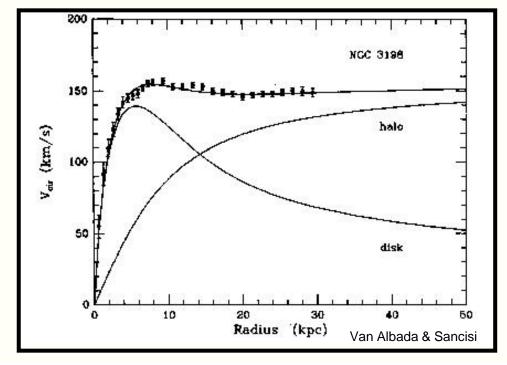
Dark Matter: disk galaxies

• The dark matter in these galactic dark halos will keep the stars and gas clouds in the outer reaches of the spiral galaxies swirling around the galaxy with such high velocities.

$$GM(r)/r = v_c^2$$

 Moreover, the dark matter halos would provide a natural stabilization of the thin and fragile rotating spiral discs, which otherwise are rather unstable structures which would easily be disrupted by "perturbative vibrations".





Clusters of Galaxies: X-ray intracluster gas

Baryonic matter in clusters is not only confined to galaxies:

~ 2 to 5 times more baryonic mass in the form of a diffuse hot X-ray emitting

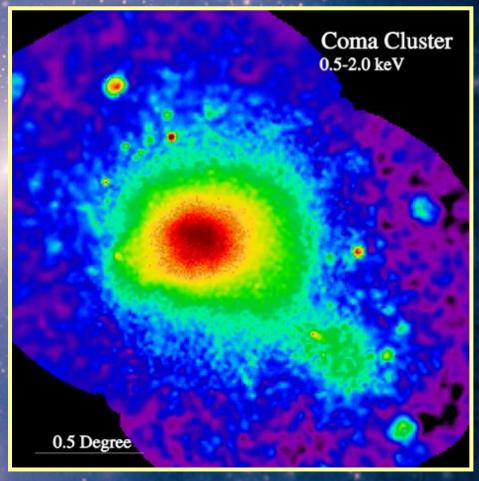
Intracluster Gas,

trapped and heated to a temperature of the order of

 $T \sim 10^8 \ K$

by the gravitational potential of the cluster.

At such high temperatures, this gas is a fully ionized plasma, producing powerful X-ray emission, bremsstrahlung radiation induced by the electron-ion interactions.



ROSAT X-ray image Coma Cluster

Clusters of Galaxies: Gravitational Lenses

A highly promising method to determine the amount and distribution of

matter in the Universe

looks at the way it affects

the trajectories of photons

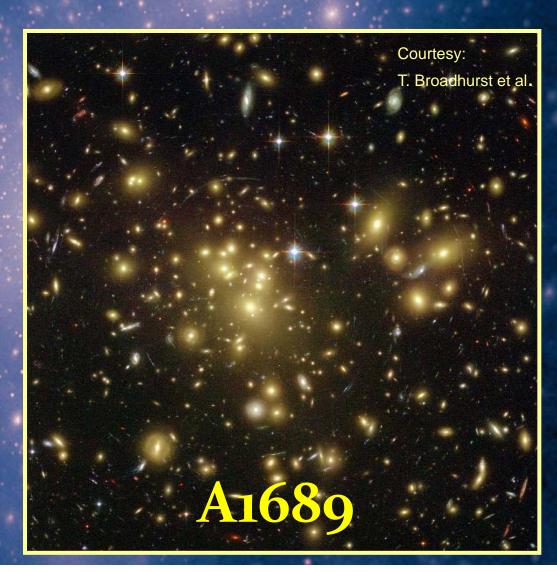
According to

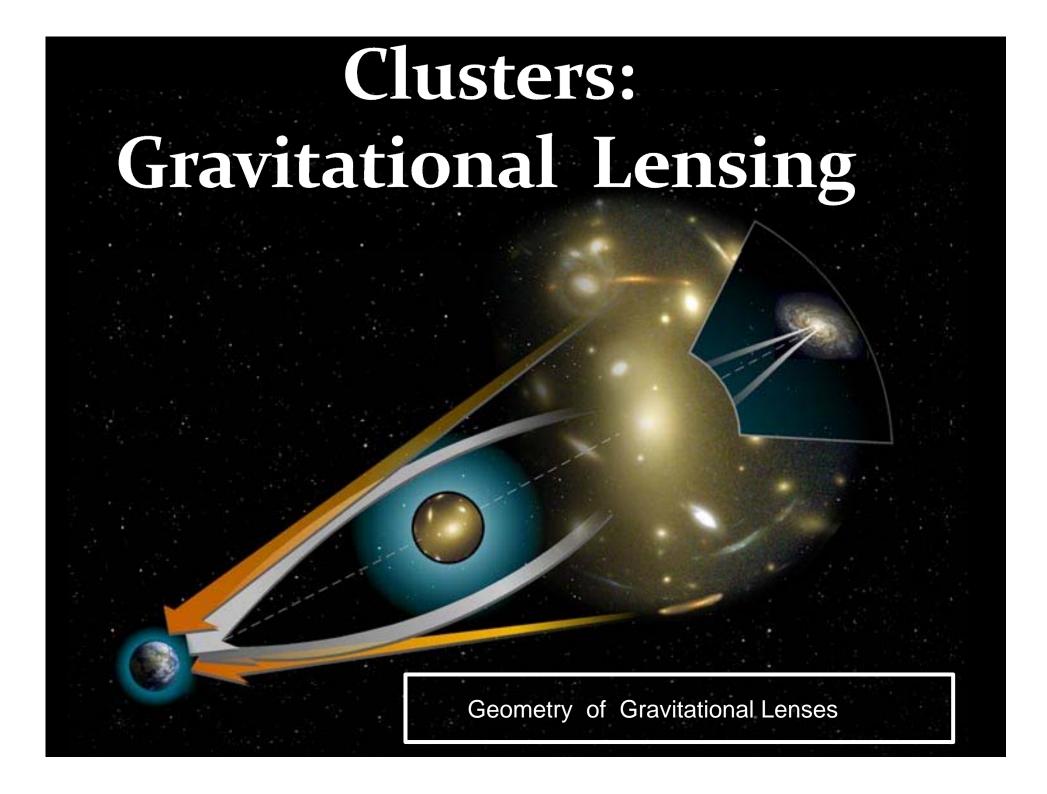
Einstein's theory of

General Relativity,

gravitational potential wells will bend and focus light. Dark matter concentrations act as a

Gravitational Lens





Clusters of Galaxies: Dark Matter Map

A highly promising method to determine the amount and distribution of

matter in the Universe

looks at the way it affects

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According to

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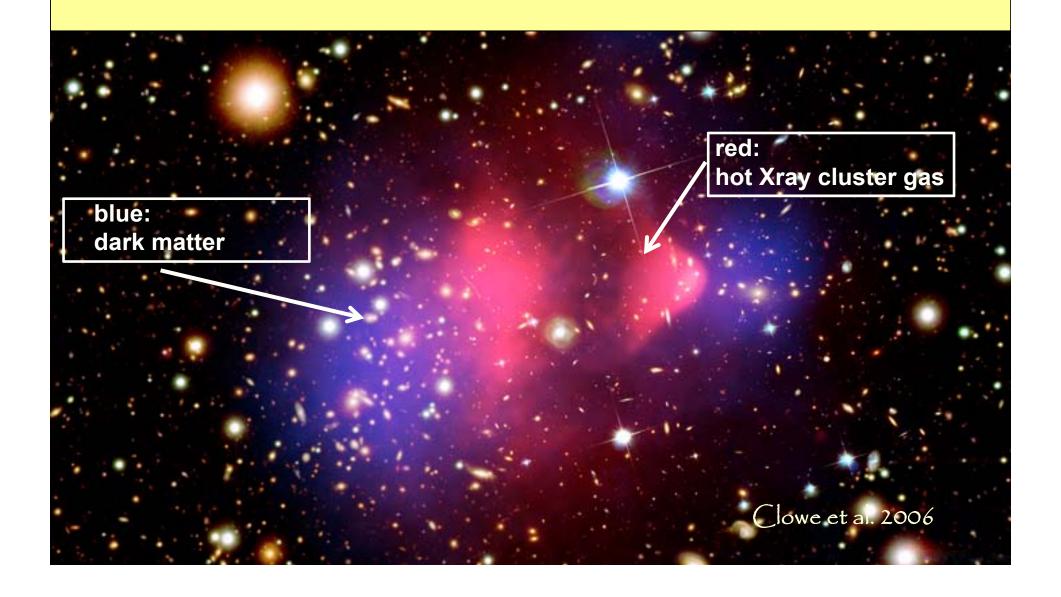
General Relativity,

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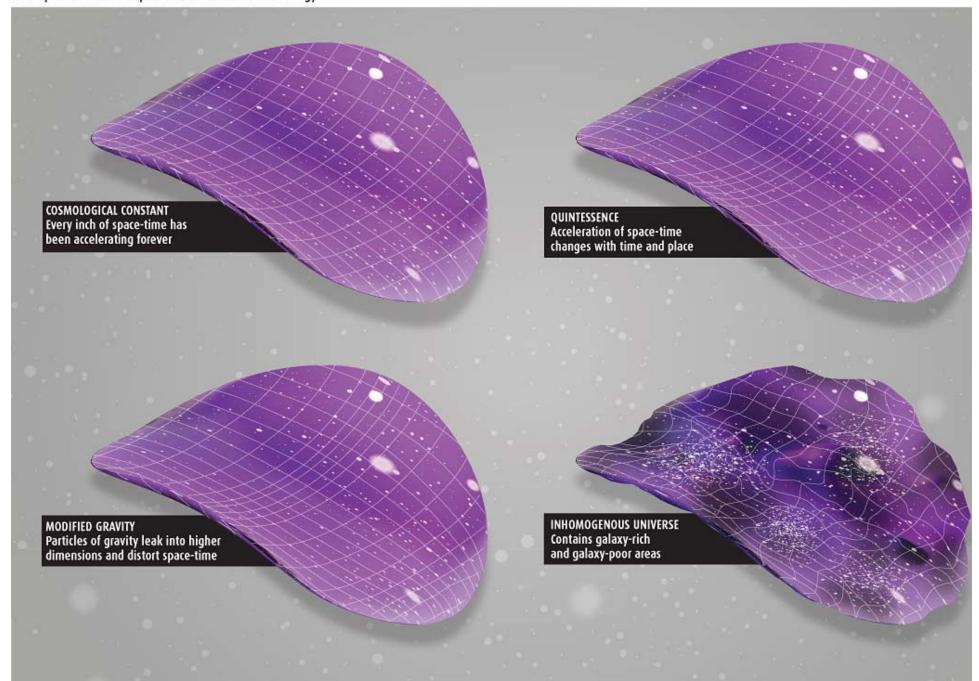
Bullet Cluster colliding ...



Dark Energy

FOUR WAYS TO EXPAND THE UNIVERSE

How space-time looks depends on the nature of dark energy



Dark Energy: Identity & Nature

Huge and ever growing list of suggestions on

identity & nature of Dark Energy:

- Cosmological Constant
- Cosmic Backreaction (inhomogeneities)
- Modified Gravity
- Quintessence, in a variety of flavours
- Phantom Energy
- Chameleon Energy
- Chaplygin gas
- Agegraphic DE
- •

Dark Energy = Vacuum Energy

Ya. Zel'dovich - 1960s S. Weinberg - 1989

Cosmological Constant to be identified with zero-point vacuum energy?

minor problem:

1st order estimate off by 120 orders magnitude:

~ 10¹²⁰

Phantom Energy:

De Big Rip?

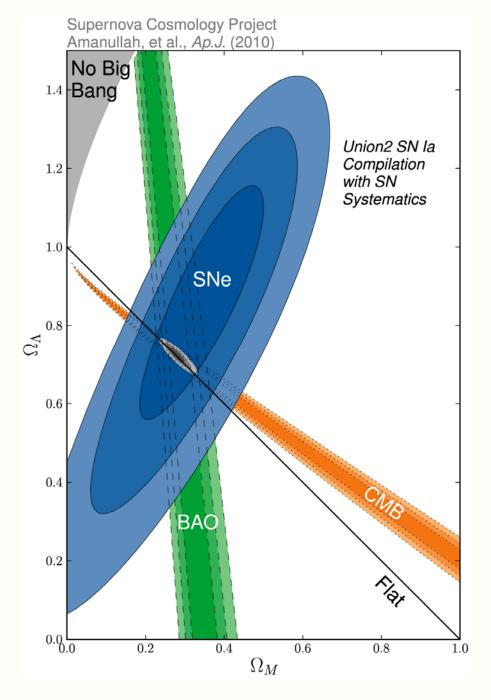
Ω_{m} vs. Ω_{Λ}

$$q \approx \frac{\Omega_m}{2} - \Omega_{\Lambda}$$

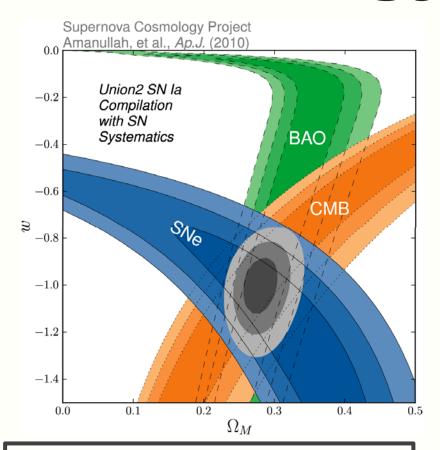
$$k = \frac{H^2 R^2}{c^2} (\Omega_m + \Omega_{\Lambda} - 1)$$

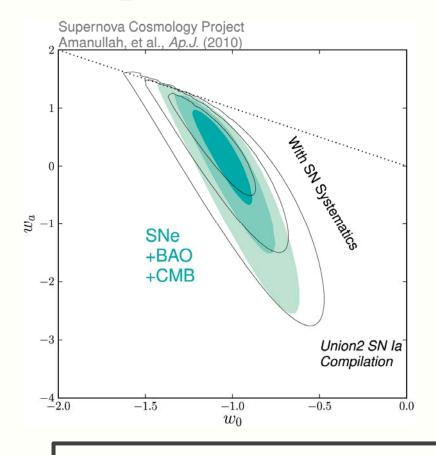
SCP Union2 constraints (2010)

on values of matter density $\Omega_{\rm m}$ dark energy density Ω_{Λ}



Dark Energy Eqn.State





SCP Union2 constraints (2010)

on values of matter density $\Omega_{\rm m}$ dark energy eqn. state w

on dynamical evolution dark energy:

eqn. state parameters

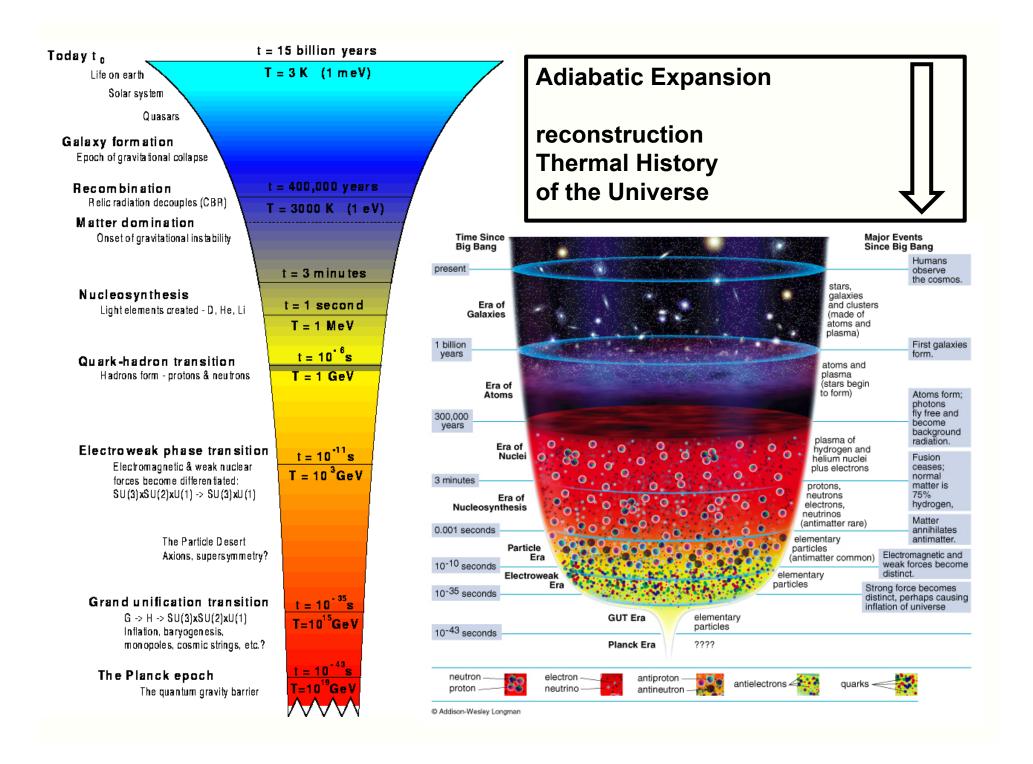
 W_0

Adiabatic Expansion

Adiabatic Expansion

- The Universe of Einstein, Friedmann & Lemaitre expands *adiabatically*
- Energy of the expansion of the Universe corresponds to the decrease in the energy of its constituents
- The Universe COOLS as a result of its expansion!

$$T(t) \propto 1/a(t)$$



Cosmic Epochs

Planck Epoch

Phase Transition Era

Hadron Era

Lepton Era

Radiation Era

Post-Recombination Era

GUT transition

electroweak transition quark-hadron transition

muon annihilation neutrino decoupling electron-positron annihilation primordial nucleosynthesis

radiation-matter equivalence recombination & decoupling

Structure & Galaxy formation
Dark Ages
Reionization
Matter-Dark Energy transition

 $t < 10^{-43} sec$

 $10^{-43} \sec < t < 10^{5} \sec$

t~10-5 sec

 $10^{-5} \sec < t < 1 \min$

 $1 \min < t < 379,000 \text{ yrs}$

t > 379,000 yrs

History of the Universe in Four Episodes: I

On the basis of the

- 1) complexity of the involved physics
- 2) our knowledge of the physical processes we may broadly distinguish four cosmic episodes:



 $t \le 10^{-43} \, \text{sec}$

fundamental physics:

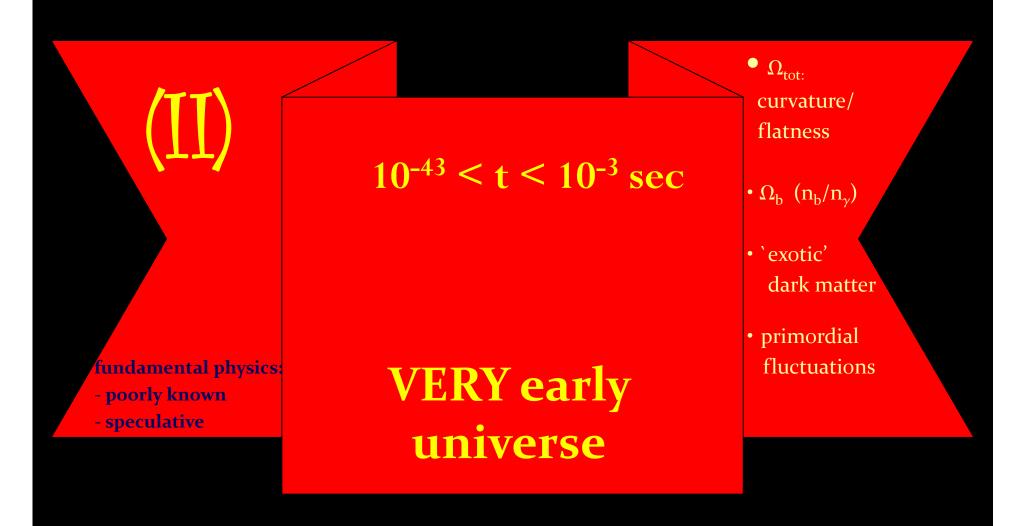
- totally unknown

Planck Era

Origin universe

???

History of the Universe in Four Episodes: II



History of the Universe in Four Episodes: III



 $10^{-3} < t < 10^{13} sec$

Standard

Hot Big Bang

Fireball

- primordial nucleosynthesis
- blackbody radiation:CMB

<u>fundamental</u> <u>microphysics</u>:

known very well

History of the Universe in Four Episodes: IV



complex macrophysics:

-Fundamentals known

- complex interplay

 $t > 10^{13} sec$

Post

(Re)Combination

universe

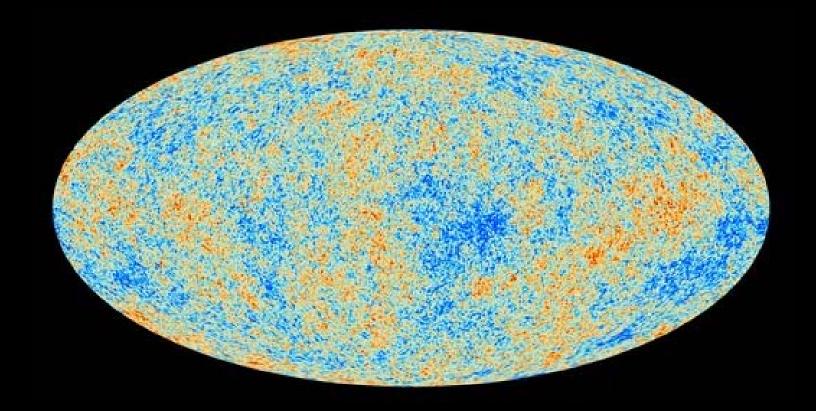
• structure formation:

stars, galaxies clusters

•••

Cosmic Curvature

Cosmic Microwave Background



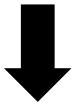
Map of the Universe at Recombination Epoch (Planck, 2013):

- 379,000 years after Big Bang
- Subhorizon perturbations: primordial sound waves
- $\Delta T/T$ < 10-5

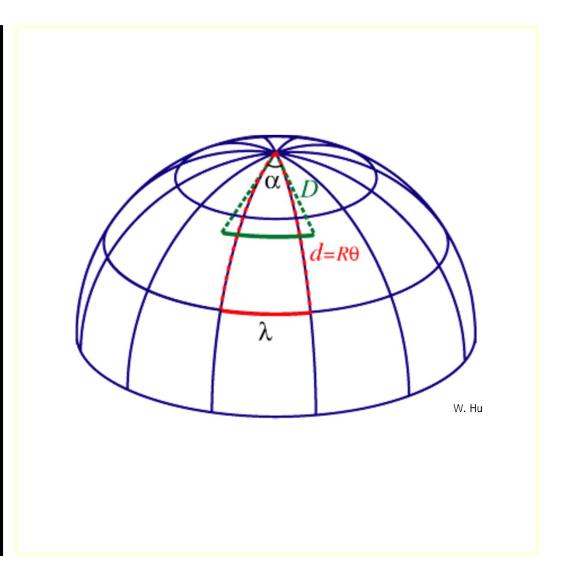
Measuring Curvature

Measuring the Geometry of the Universe:

- Object with known physical size, at large cosmological distance
- Measure angular extent on sky
- Comparison yields light path, and from this the curvature of space



Geometry of Space

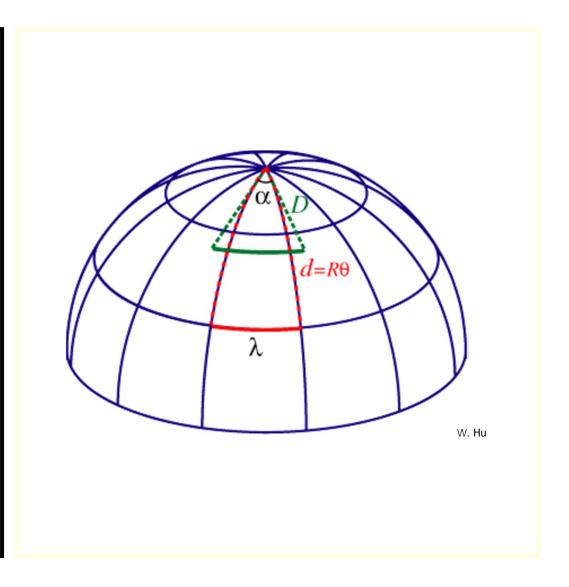


Measuring Curvature

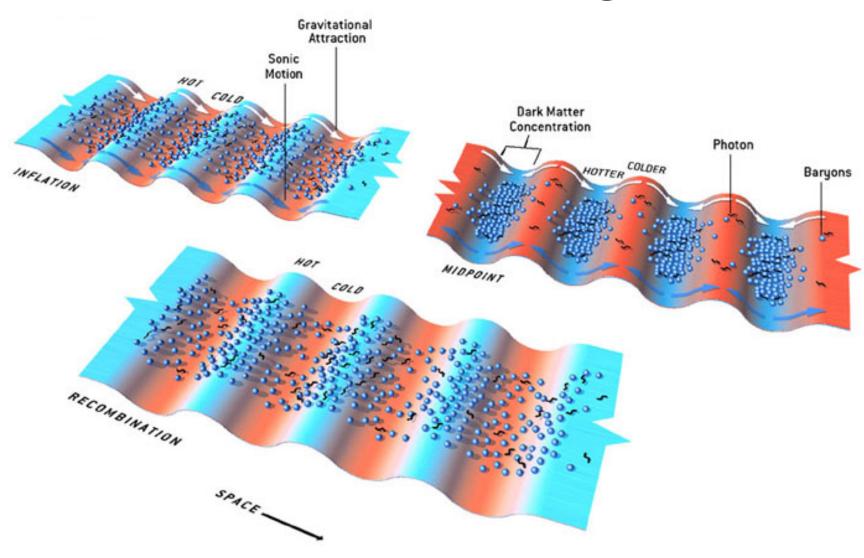
- Object with known physical size, at large cosmological distance:
- Sound Waves in the Early Universe !!!!



Temperature Fluctuations CMB

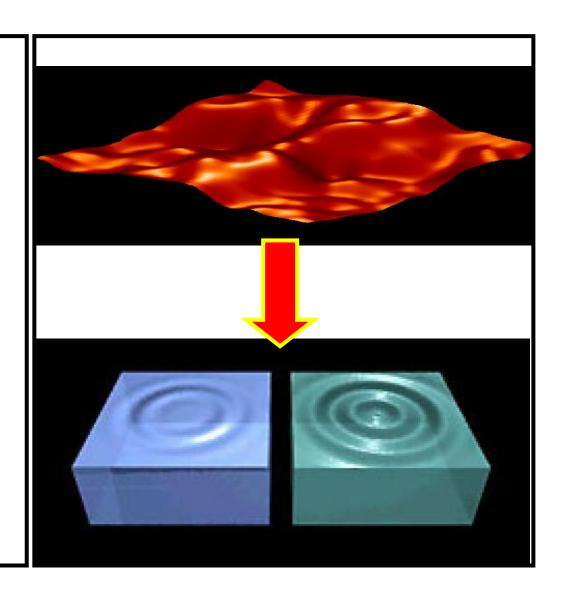


Fluctuations-Origin

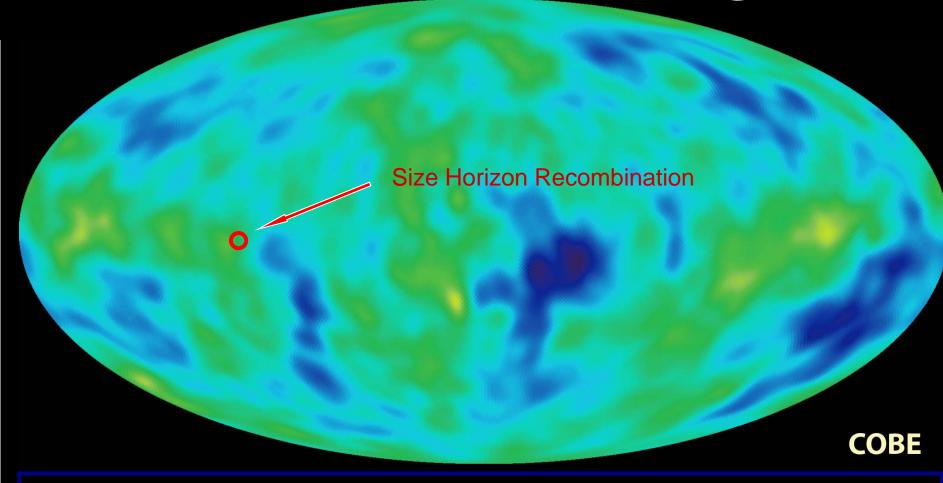


Music of the Spheres

- small ripples in primordial matter & photon distribution
- gravity:
 - compression primordial photon gas
 - photon pressure resists
- compressions and rarefactions in photon gas: sound waves
- sound waves not heard, but seen:
 - compressions: (photon) T higher
 - rarefactions: lower
- fundamental mode sound spectrum
 - size of "instrument":
 - (sound) horizon size last scattering
- Observed, angular size: θ~1°
 - exact scale maximum compression, the "cosmic fundamental mode of music"



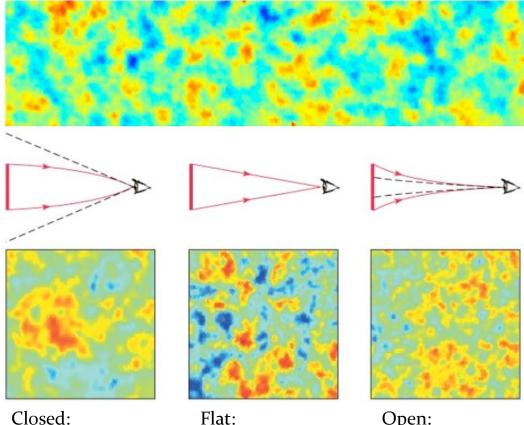
Cosmic Microwave Background



COBE measured fluctuations: $> 7^{\circ}$ Size Horizon at Recombination spans angle $\sim 1^{\circ}$

Flat universe from CMB

• First peak: flat universe



Closed: hot spots appear larger

Flat: appear as big as they are

Open: spots appear smaller

We know the redshift and the time it took for the light to reach us:

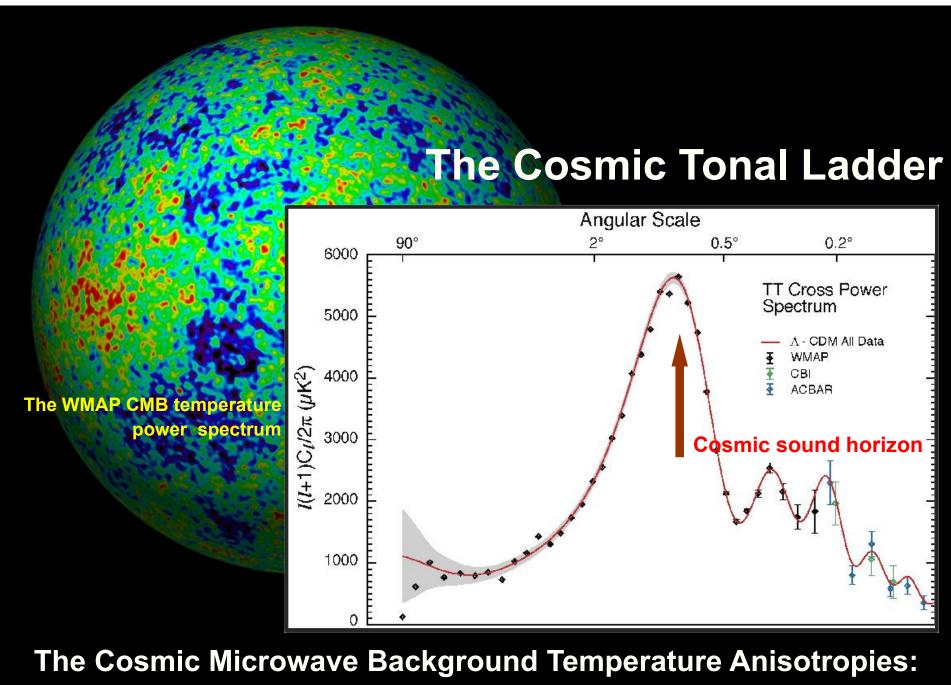
from this we know the

- length of the legs of the triangle
- the angle at which we are measuring the sound horizon.

$$v \approx \frac{c}{\sqrt{3}}$$

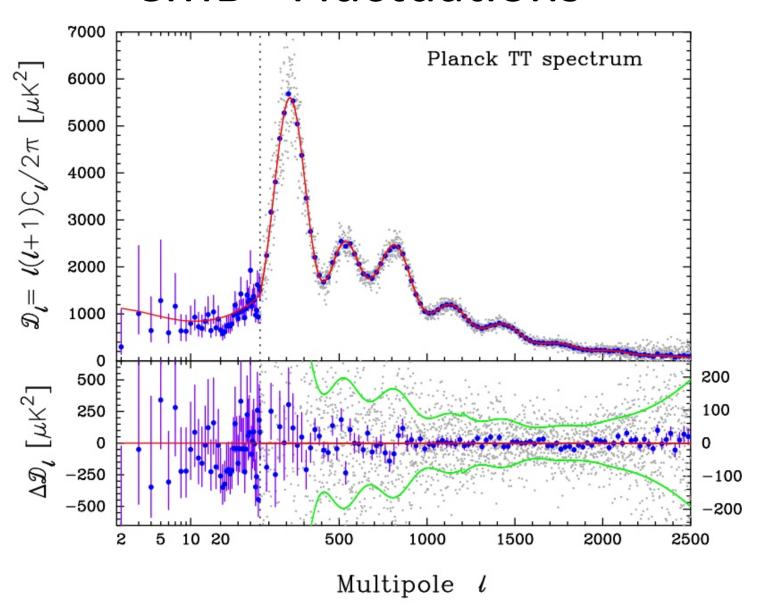
$$\ell \approx 200/\sqrt{1-\Omega_k}$$

Angular Scale Standard Ruler: 90° 0.5° 0.2° 1° arc measurement of dominant energy spike 8000 **OPEN** 7000 6000 Anisotropy Power 5000 4000 3000 **FLAT** 2000 1000 10 100 500 1000 Multipole moment 1



The Cosmic Microwave Background Temperature Anisotropies:
Universe is almost perfectly FLAT !!!!

CMB - Fluctuations



Standard Big Bang:

what it cannot explain ...

Flatness Problem

the Universe is remarkably flat, and was even (much) flatter in the past

· Horizon Problem

the Universe is nearly perfectly isotropic and homogeneous, much more so in the past

Monopole Problem:

There are hardly any magnetic monopoles in our Universe

Fluctuations, seeds of structure

Structure in the Universe: origin

Flatness Problem

Flatness Problem

FRW Dynamical Evolution:

Going back in time, we find that the Universe was much flatter than it is at the present.

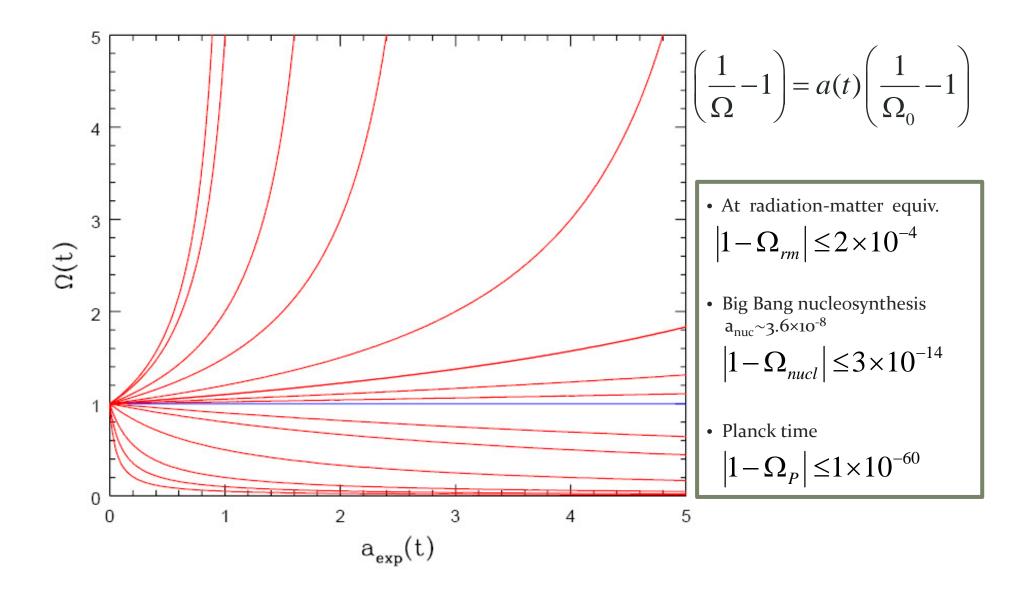
Reversely, that means that any small deviation from flatness in the early Universe would have been strongly amplified nowadays ...

We would therefore expect to live in a Universe that would either be almost Ω =0 or Ω ~ ∞ ;

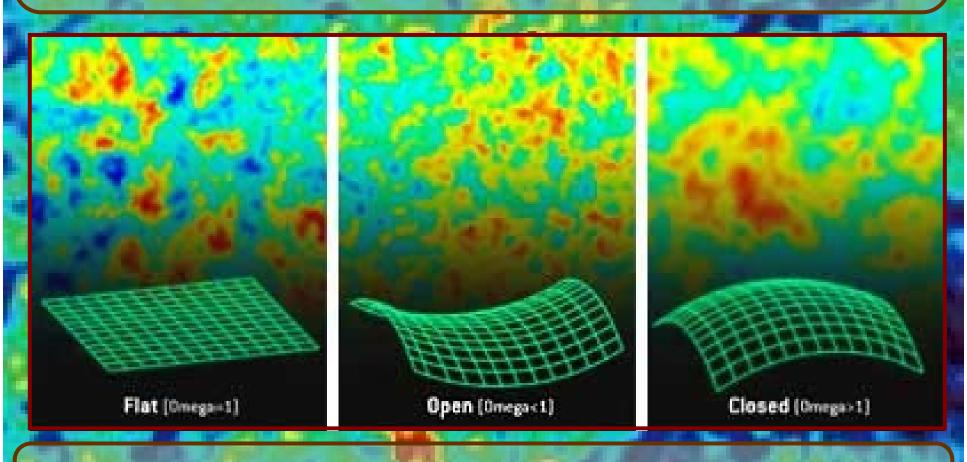
Yet, we find ourselves to live in a Universe that is almost perfectly flat ... $\Omega_{\rm tot} \sim 1$

How can this be?

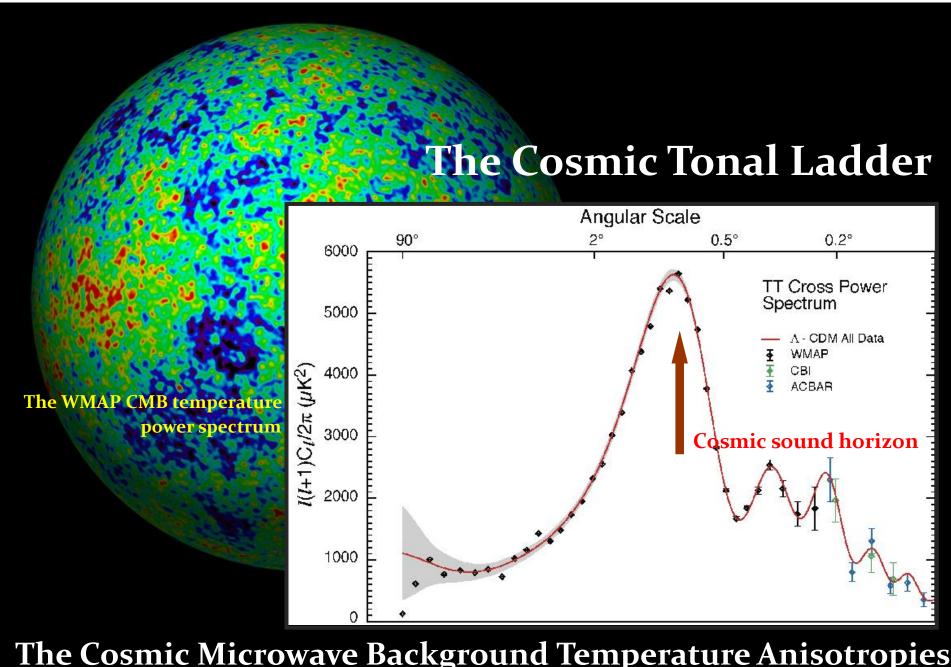
Flatness Evolution



Angular CMB temperature fluctuations



CMB: Universe almost perfectly Flat



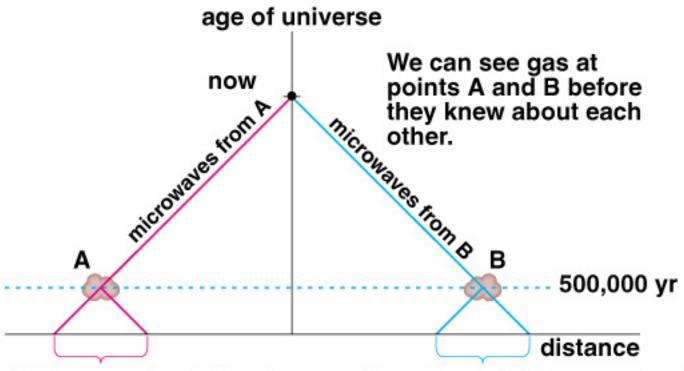
The Cosmic Microwave Background Temperature Anisotropies:
Universe is almost perfectly flat

Horizon Problem

Fundamental Concept for our understanding of the physics of the Universe:

- Physical processes are limited to the region of space with which we are or have ever been in physical contact.
- What is the region of space with which we are in contact ?
 Region with whom we have been able to exchange photons
 (photons: fastest moving particles)
- From which distance have we received light.
- Complication: light is moving in an expanding and curved space
 fighting its way against an expanding background
- This is called the

Horizon of the Universe



Gas at point A has received signals from this part of the universe.

Gas at point B has received signals from this part of the universe.

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Horizon of the Universe: distance that light travelled since the Big Bang

In an Einstein-de Sitter Universe

$$R_{Hor} = 3ct$$

Horizon distance in physical space

Horizon of the Universe: distance that light travelled since the Big Bang

The horizon distance at recombination/decoupling (ie. time at which Cosmic Microwave Background is coming from)

angular size on the sky:

$$R_{Hor} = 3ct$$

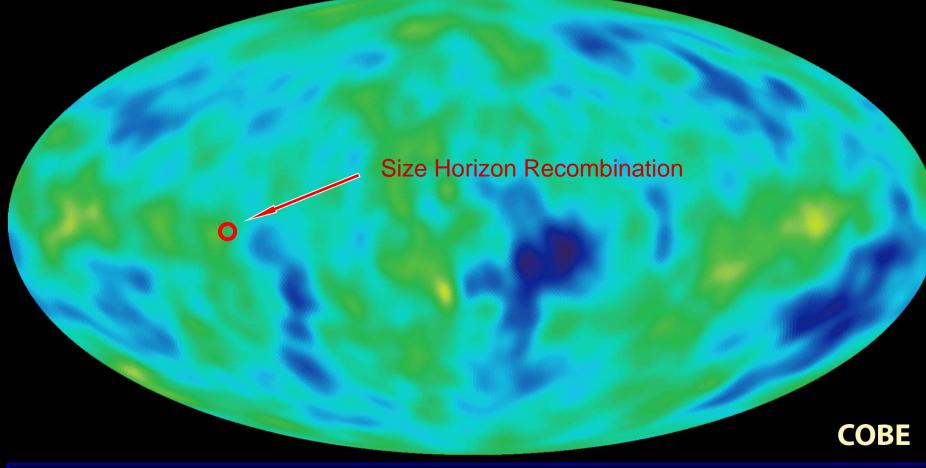


$$heta > 1^{\circ}$$
 Large angular scales: NOT in physical contact

$$heta \ll 1^\circ$$
 Small angular scales: In physical (thus, also thermal) contact

Horizon of the Universe: distance that light travelled since the Big Bang

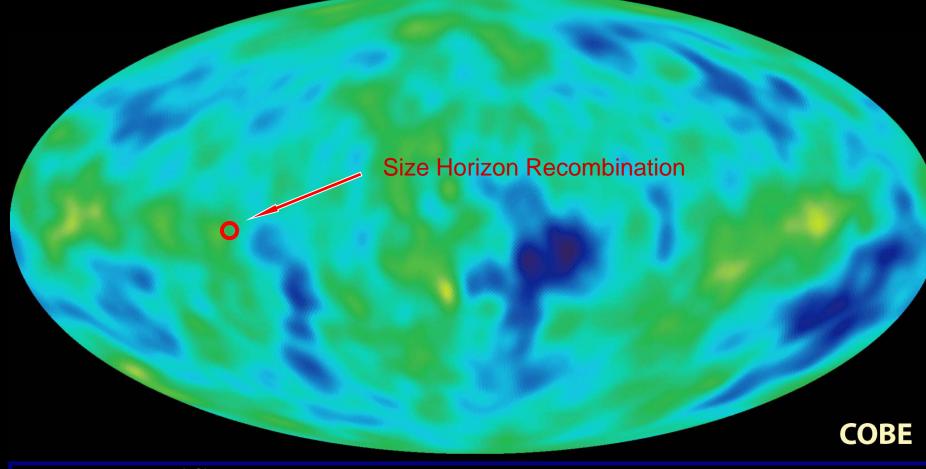
Cosmic Microwave Background



COBE measured fluctuations: > 7° Size Horizon at Recombination spans angle ~ 1°

How can it be that regions totally out of thermal contact have the same temperature?

Cosmic Microwave Background



COBE measured fluctuations: > 7° Size Horizon at Recombination spans angle ~ 1°

COBE proved that superhorizon fluctuations do exist:

prediction Inflation !!!!!

Structure Problem

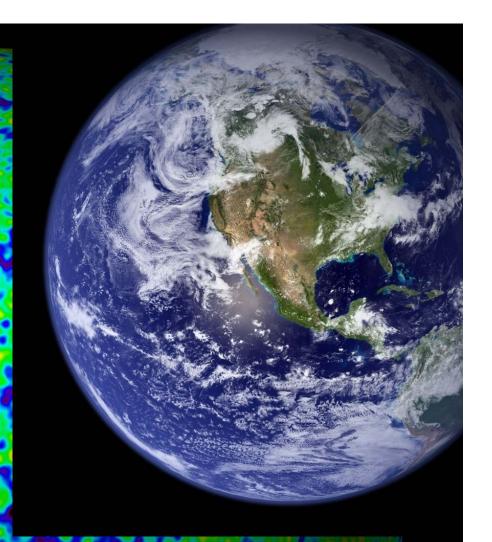
Primordial Noise:

Seeds of Cosmic Structure

Universe at 379000 years:

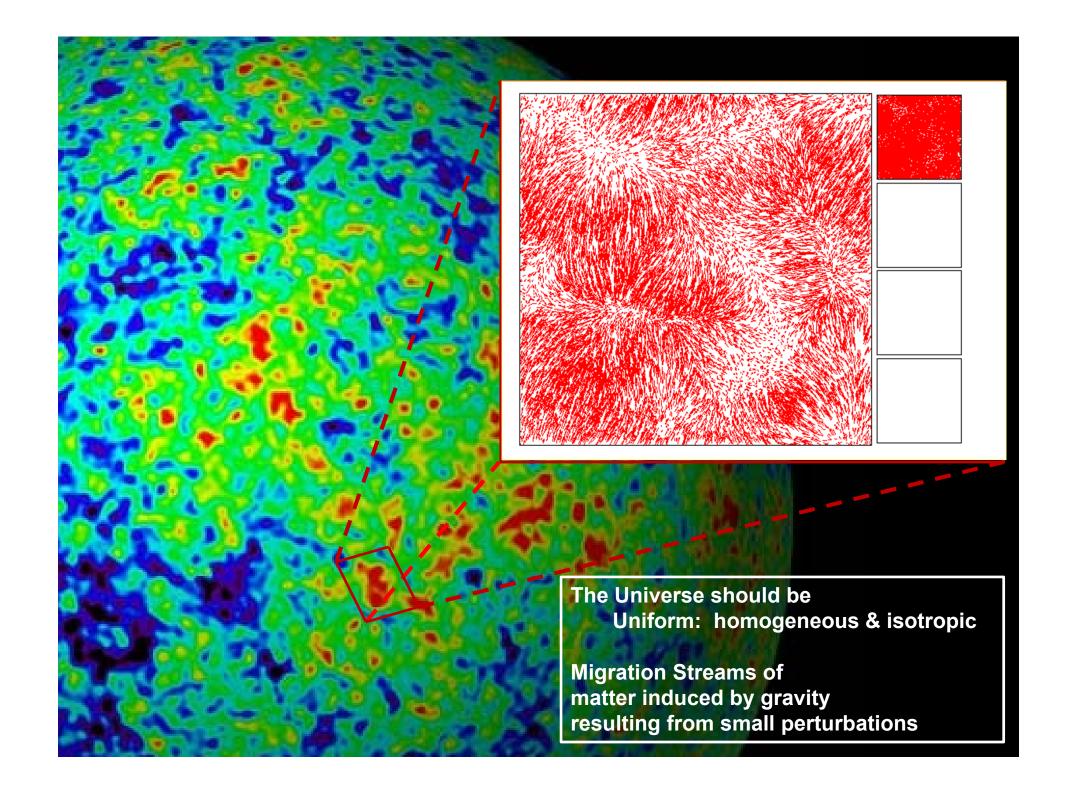
almost featureless

$$\frac{\Delta T}{T} < 10^{-5}$$



$$\frac{\Delta r}{r} \le 1.4 \times 10^{-3}$$

$$\frac{\Delta r}{r} \sim 10^{-5}$$
: $r \sim 60.4 \, m$



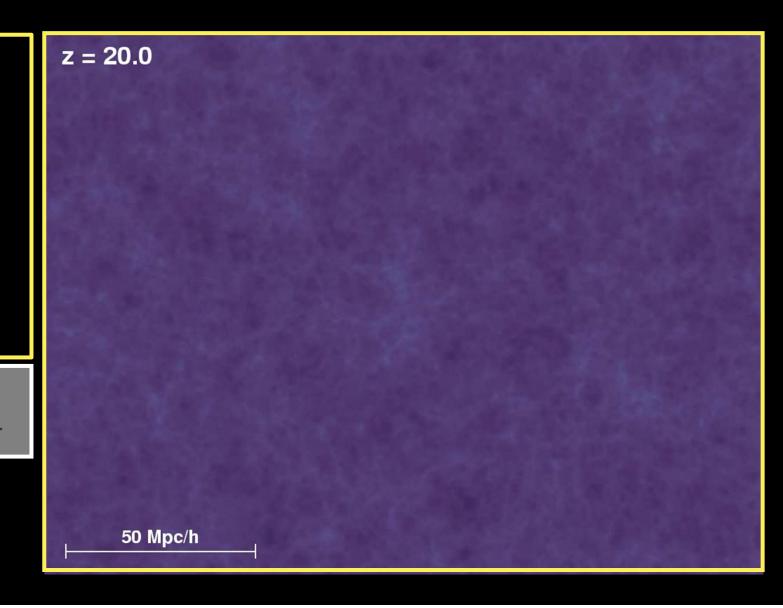
Cosmic Structure Formation

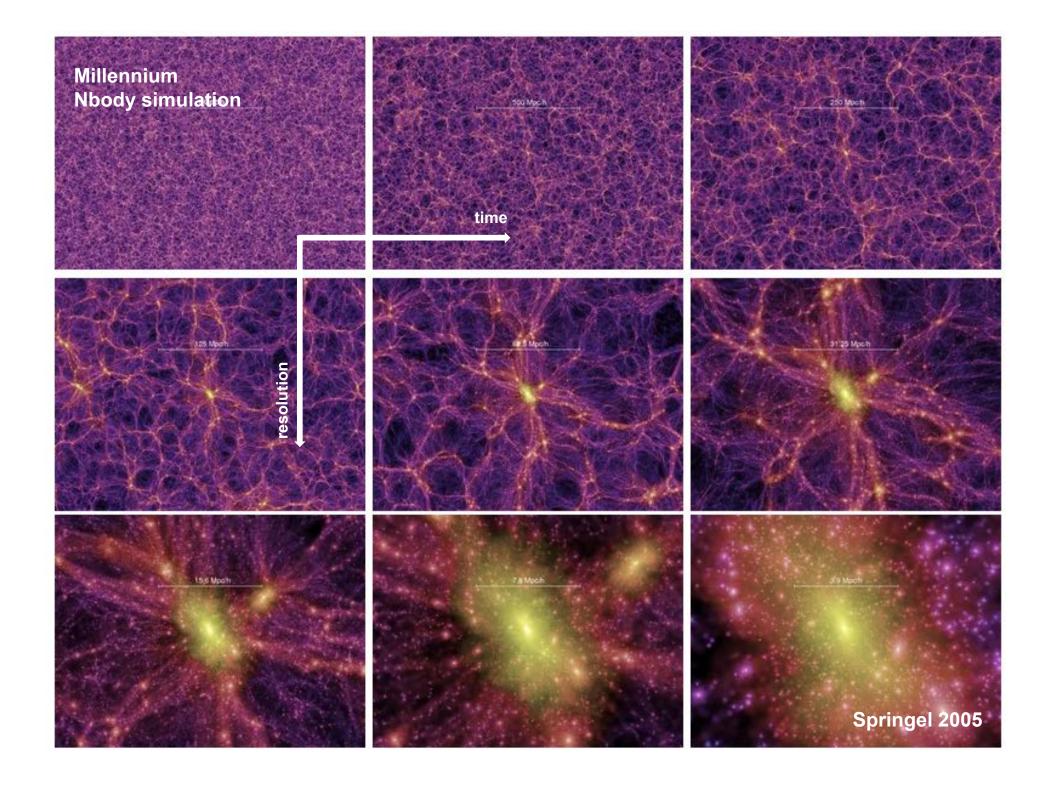
Formation Cosmic Web:

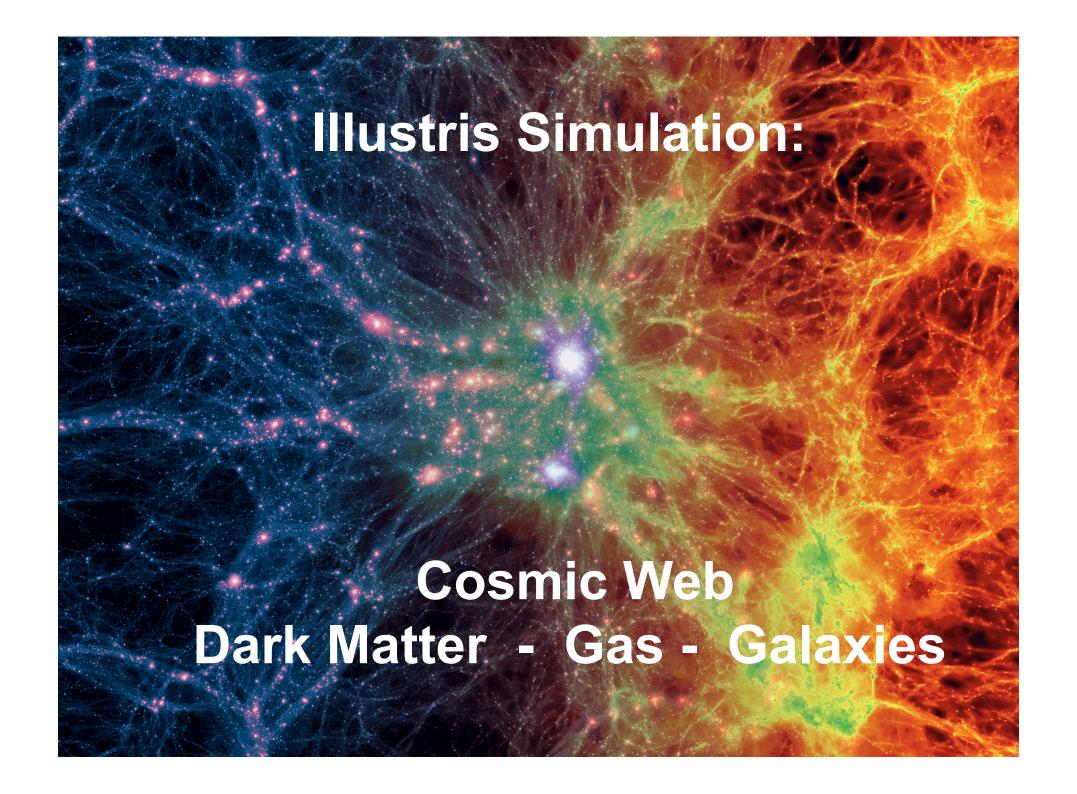
simulation sequence

(cold) dark matter

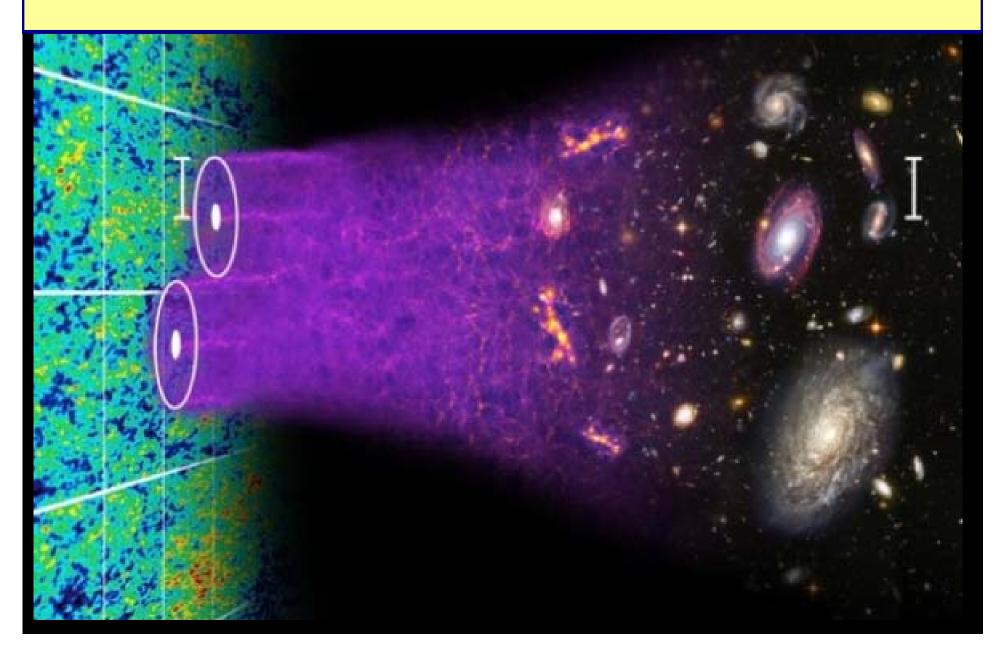
(courtesy: Virgo/V. Springel).



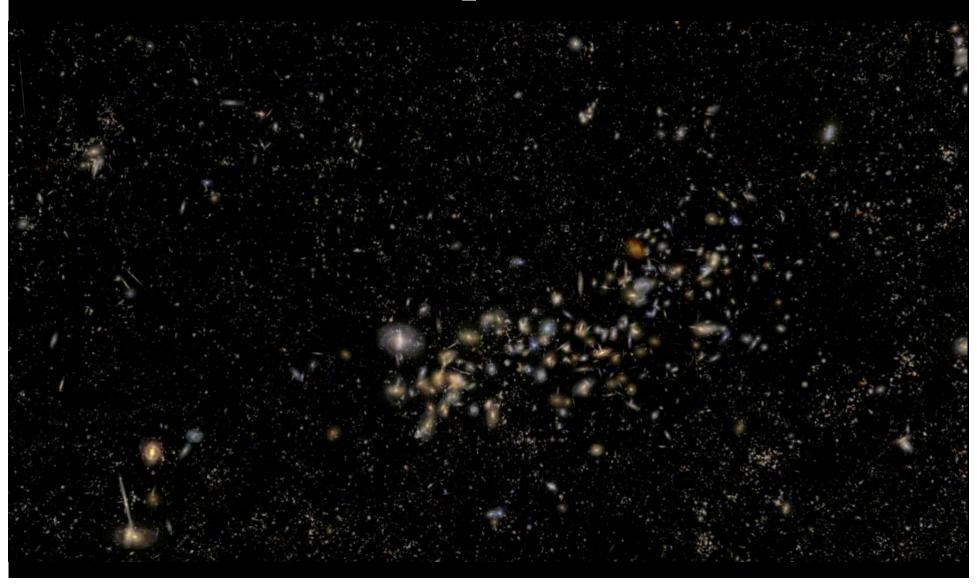




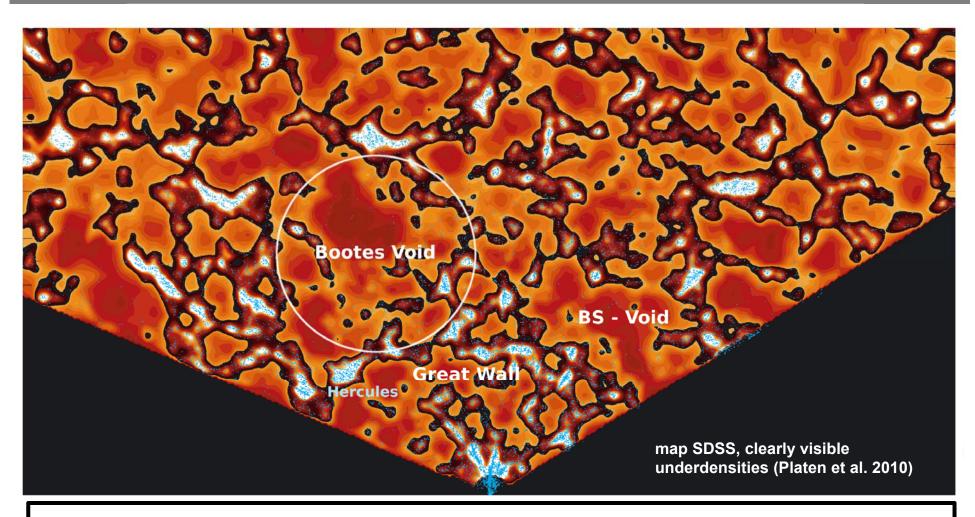
Formation Cosmic Structures



Universe at 13.8 Gyrs: rich & complex structure



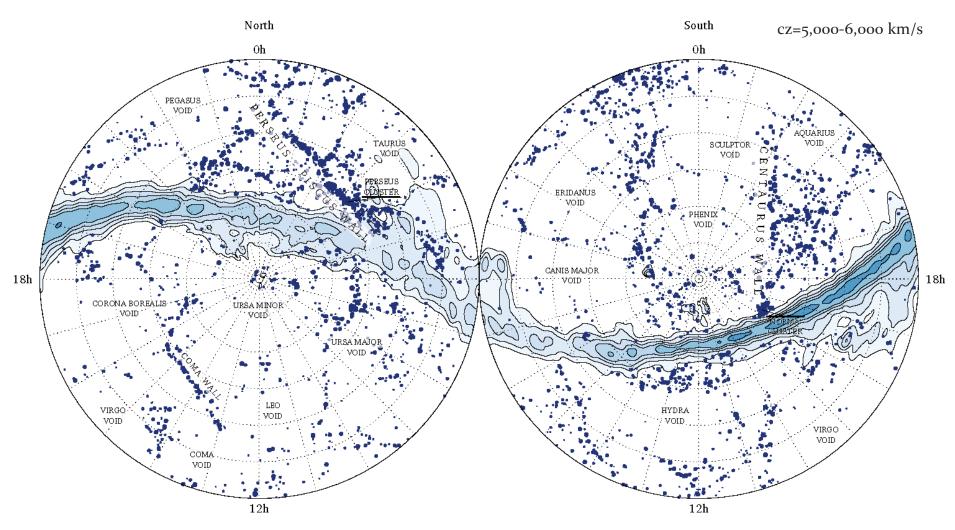
SDSS Galaxy Survey



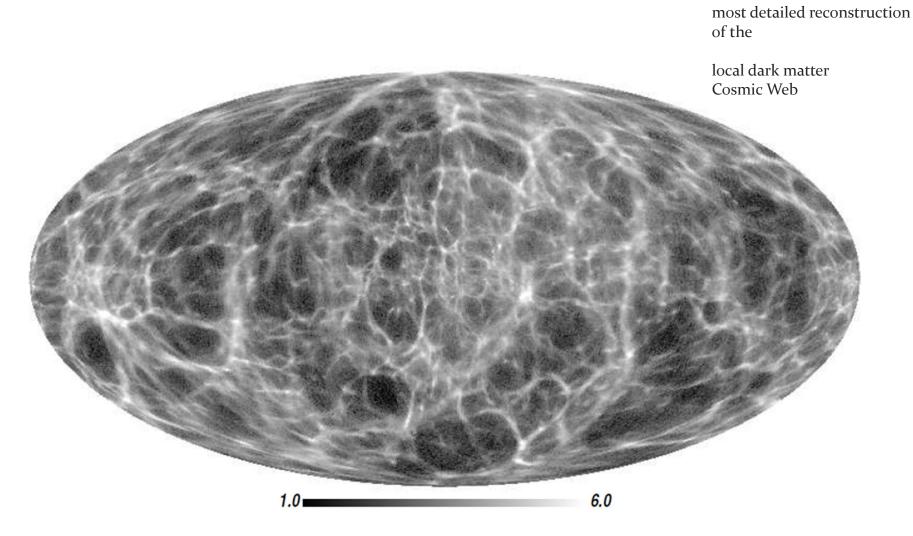
with the advent of large galaxy redshift surveys

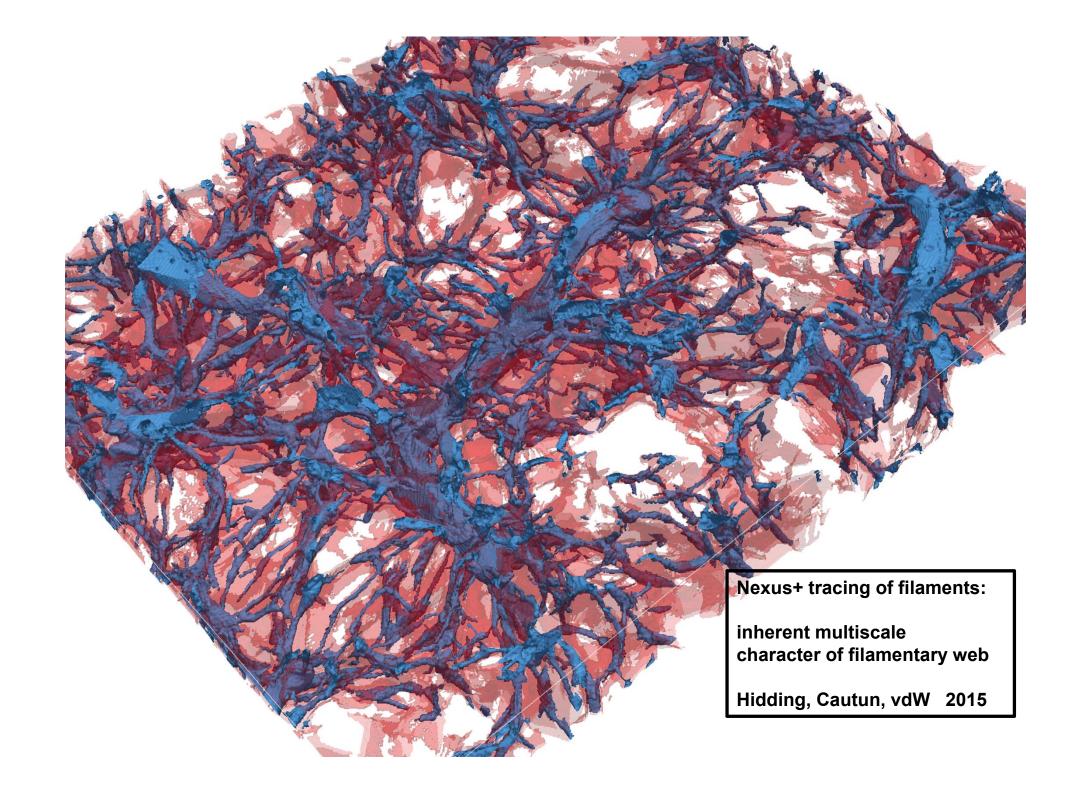
- LCRS, 2dFGRS, SDSS, 2MRS voids have been recognized as one of the quintessential components of the Cosmic Web

local Cosmic Web: 2MRS



local Cosmic Web: 2MRS





Horizon Problem

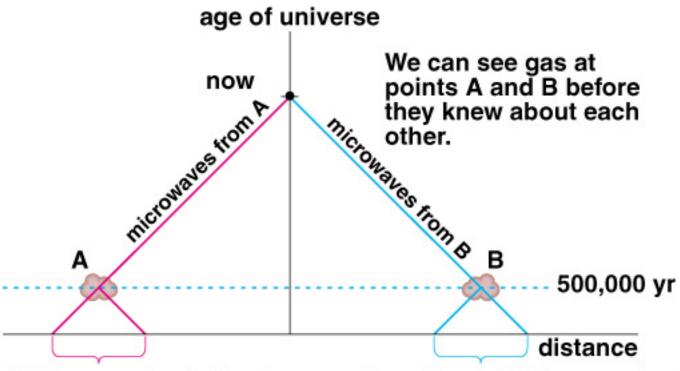
Cosmic Horizons

Fundamental Concept for our understanding of the physics of the Universe:

- Physical processes are limited to the region of space with which we are or have ever been in physical contact.
- What is the region of space with which we are in contact ?
 Region with whom we have been able to exchange photons
 (photons: fastest moving particles)
- From which distance have we received light.
- Complication: light is moving in an expanding and curved space
 fighting its way against an expanding background
- This is called the

Horizon of the Universe

Cosmic Horizon



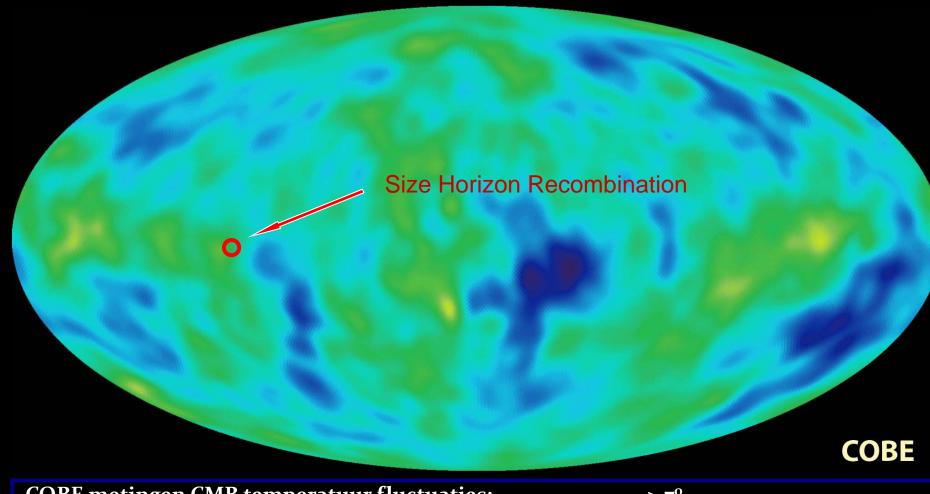
Gas at point A has received signals from this part of the universe.

Gas at point B has received signals from this part of the universe.

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(Particle) Horizon of the Universe: distance that light travelled since Big Bang

Probleem van Kosmische Horizon

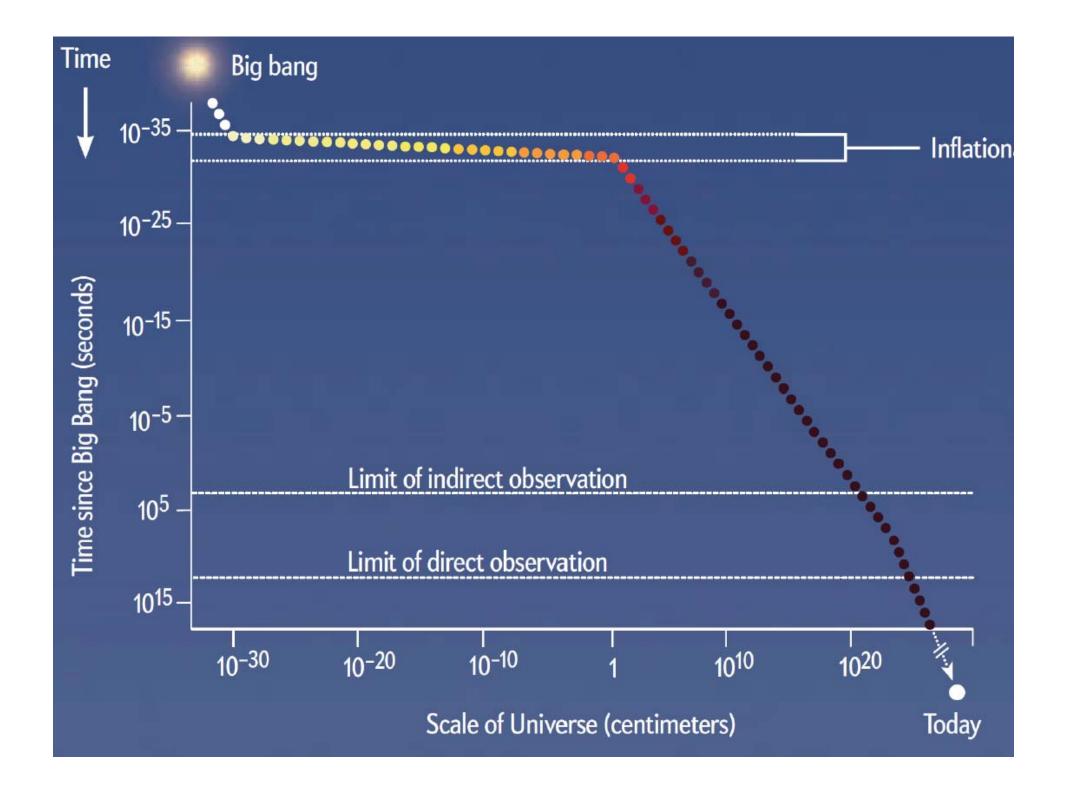


COBE metingen CMB temperatuur fluctuaties: > 7° Schaal Horizon Zichtbare Heelal 379000 jr. na Big Bang: ~ 1°

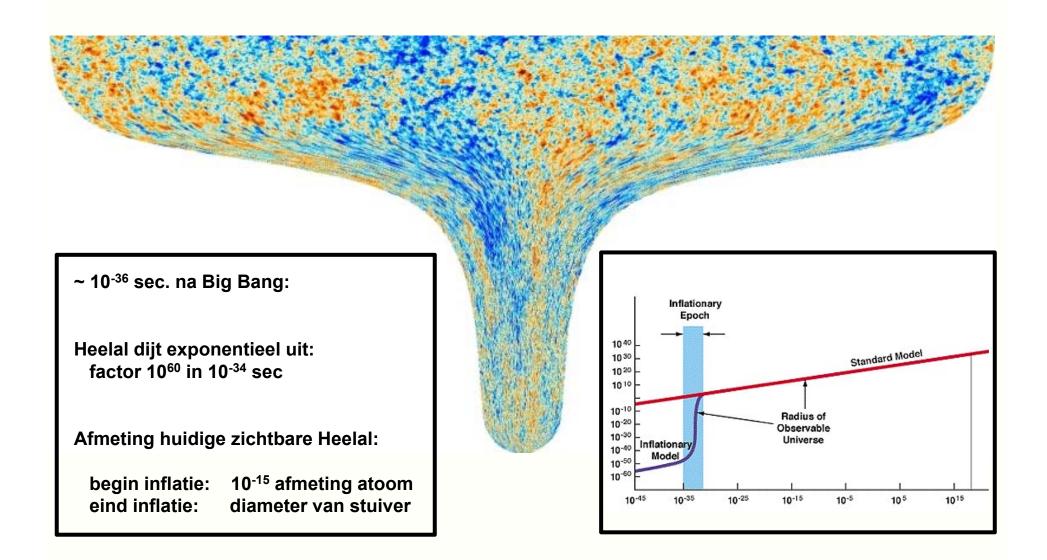
Temperatuur hetzelfde over gehele hemel, maar hoe kan dat zonder ooit in thermisch contact te zijn geweest?

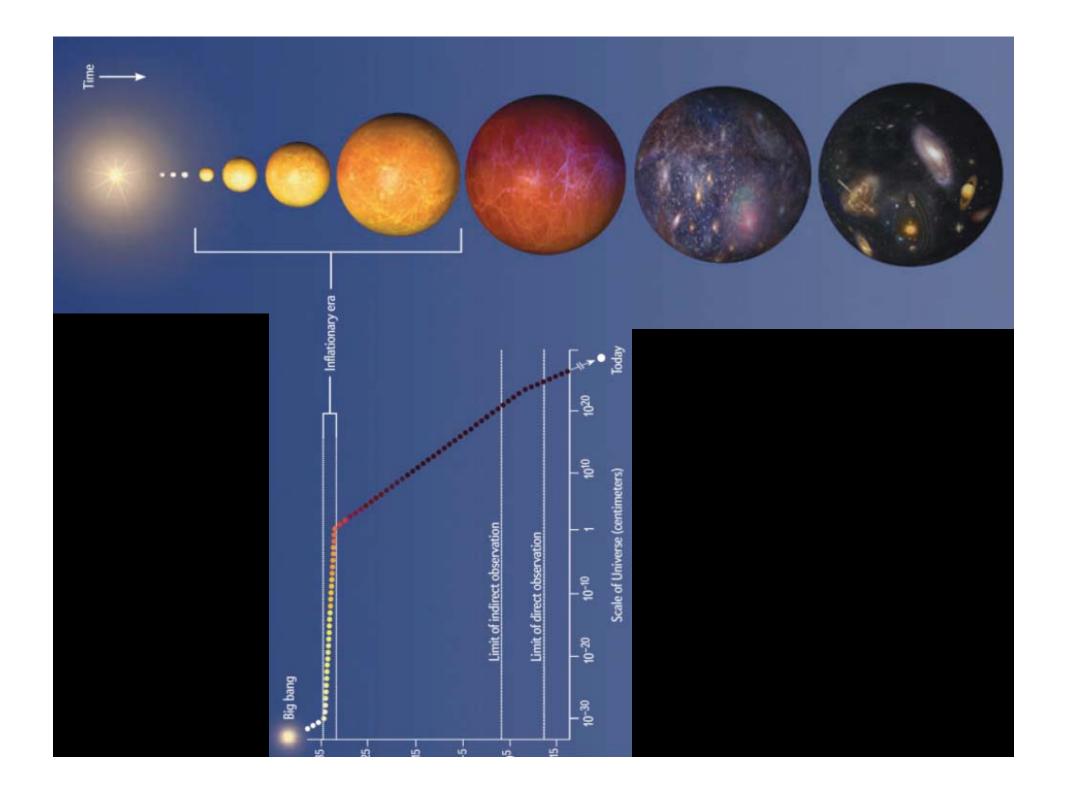
INFLATION



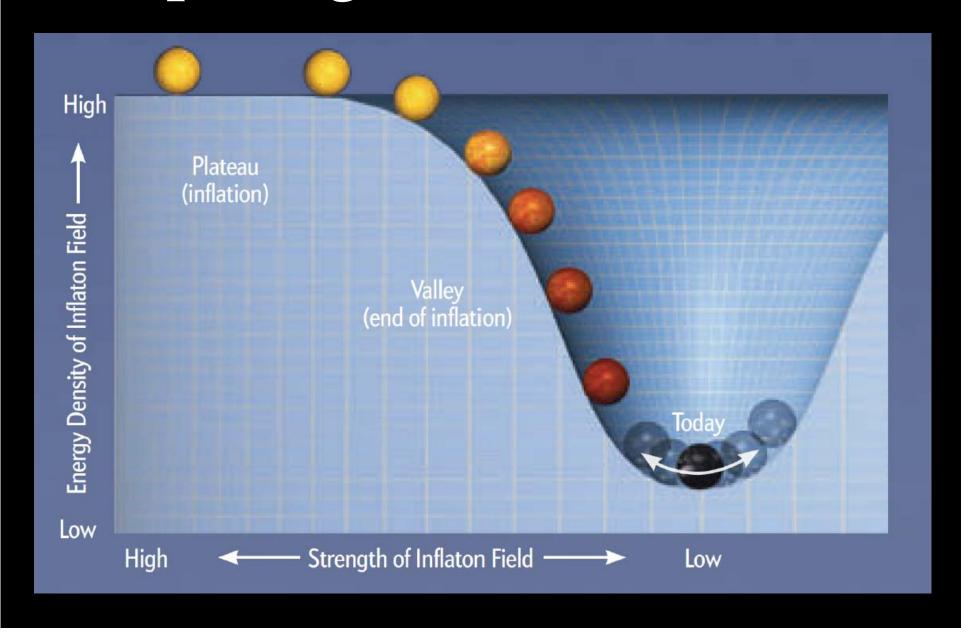


Kosmische Inflatie

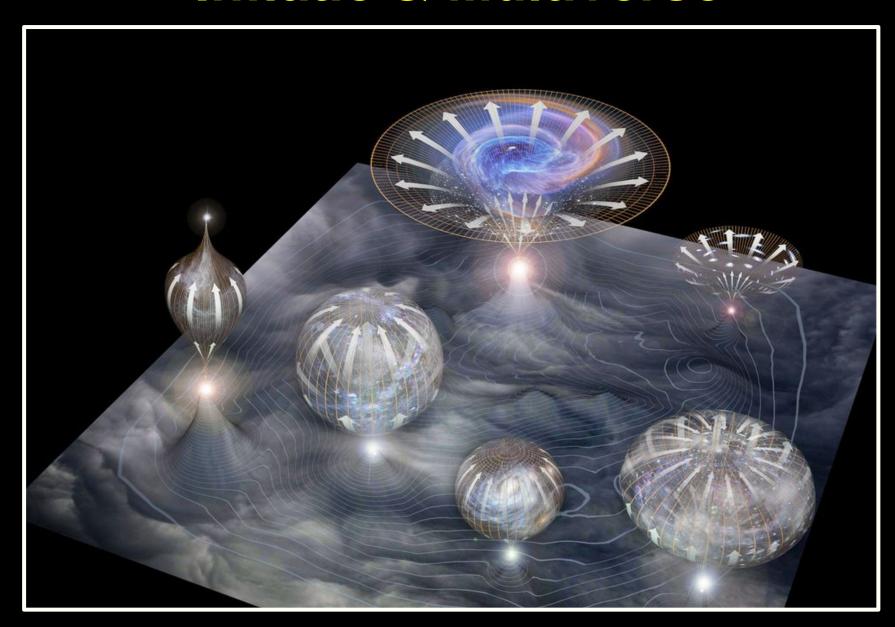




Propelling Inflation: Inflaton



Inflatie & Multiverse



Cosmic Future

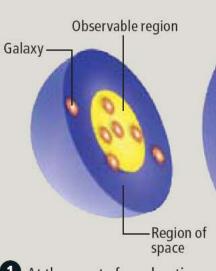
Cosmic Fate

100 Gigayears: the end of Cosmology



EXPANDING UNIVERSE, SHRINKING VIEW

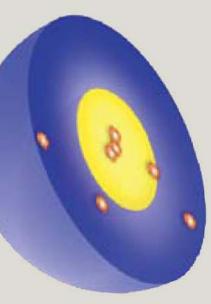
The universe may be infinite, but consider what happens to the patch of space around us (purple sphere), of which we see only a part (yellow inner sphere). As space expands, galaxies (orange spots) spread out. As light has time to propagate, we observers on Earth (or our predecessors or descendants) can see a steadily increasing volume of space. About six billion years ago, the expansion began to accelerate, carrying distant galaxies away from us faster than light.



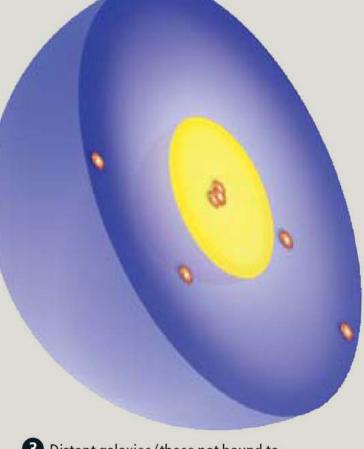
 At the onset of acceleration, we see the largest number of galaxies that we ever will.

NOTE:

Because space is expanding uniformly, alien beings in other galaxies see this same pattern.



2 The visible region grows, but the overall universe grows even faster, so we actually see a smaller fraction of what is out there.



3 Distant galaxies (those not bound to us by gravity) move out of our range of view. Meanwhile, gravity pulls nearby galaxies together.