

Gravitational Instability

$$\frac{\partial \delta}{\partial t} + \frac{1}{a} \nabla \cdot \mathbf{v} = 0$$

$$\frac{\partial \mathbf{v}}{\partial t} + \frac{\dot{a}}{a} \mathbf{v} = -\frac{1}{a} \nabla \phi$$

$$\nabla^2 \phi = \frac{3}{2} \Omega H^2 a^2 \delta(\mathbf{x}, t)$$

Gravitational Instability

The linear system of structure growth equations can be written in terms of a second order differential equation,

$$\frac{\partial^2 \delta}{\partial t^2} + 2 \frac{\dot{a}}{a} \frac{\partial \delta}{\partial t} = \frac{3}{2} \Omega_0 H_0^2 \frac{1}{a^3} \delta$$

Gravitational Instability

... whose two solutions are separable in time and space,
leading to a universal "density growth factor" $D(t)$,

$$\delta(\mathbf{x}, t) = D_1(t) \Delta_1(\mathbf{x}) + D_2(t) \Delta_2(\mathbf{x})$$

"Growing Mode"

"Decaying Mode"

Linear Density Growth

... whose two solutions are separable in time and space,
leading to a universal "density growth factor" $D(t)$,

$$\delta(\mathbf{x}, t) = D_1(t) \Delta_1(\mathbf{x}) + D_2(t) \Delta_2(\mathbf{x})$$

"Growing Mode"

"Decaying Mode"

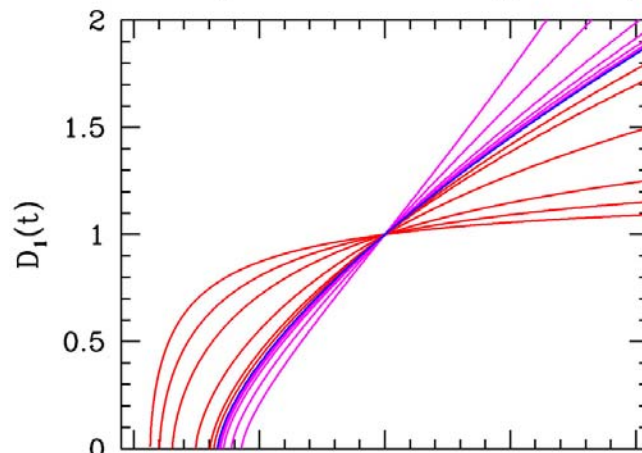
Linear Density Growth

... The universal "density growth factor" $D(t)$ can be computed for any cosmology through the integral

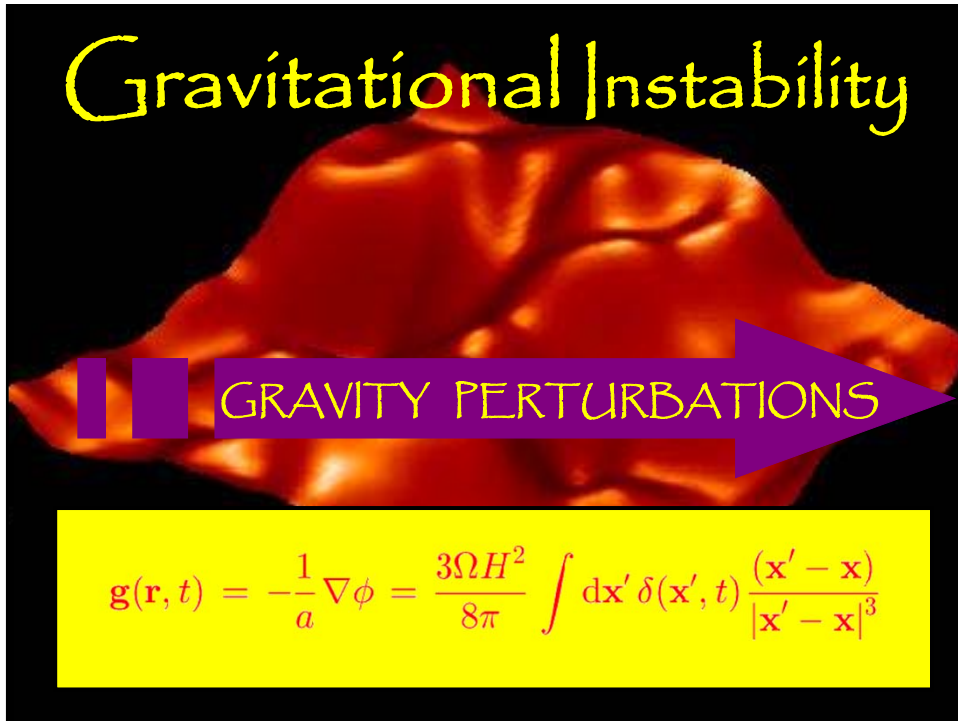
$$D(t) \approx H(t) \int \frac{dt}{a^2 H^2(t)}$$

Linear Density Growth

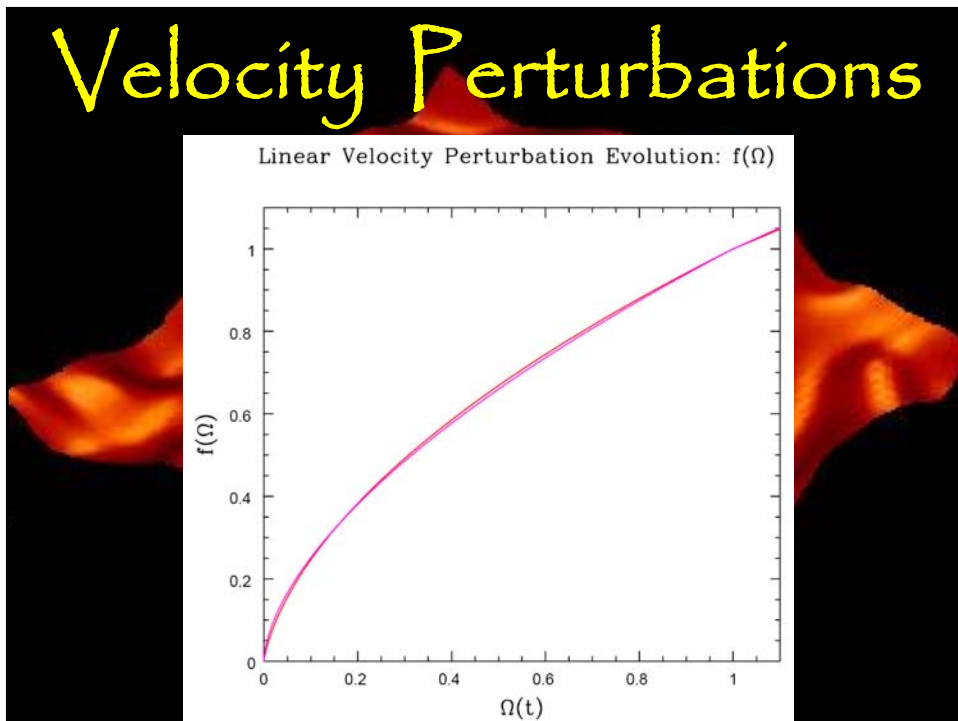
Linear Perturbation Evolution:
Density evolution: Growing Mode D_1



Gravitational Instability



Velocity Perturbations



Measuring Distances

Distance & Velocity Measurements

To measure peculiar velocities of galaxies, one needs to know their real distance r :

- ie. the distance independent of redshift, ie. of the use of the Hubble relation:

$$\vec{v}_{tot}(\vec{r}) = H\vec{r} + \vec{v}_{pec}$$

$$cz = \vec{v}_{tot} \cdot \vec{e}_r = Hr + \vec{v}_{pec} \cdot \vec{e}_r$$

$$\vec{v}_{pec} \cdot \vec{e}_r = cz - Hr$$

- to determine the (radial component) of the peculiar velocity, one would need to measure independently the distance r .
- Determining reliable distances directly is still one of the main challenges of observational cosmology.

Distance & Velocity Measurements

$$\vec{v}_{pec} \cdot \vec{e}_r = cz - Hr$$

- Determining reliable distances directly is still one of the main challenges of observational cosmology.
- In practice, one makes use of *galaxy scaling relations*, which relates an observable *intrinsic characteristic* of a galaxy – such as velocity dispersion or rotation velocity – with an observable *distance dependent characteristic* whose intrinsic value is physically related to the intrinsic characteristic.
- The 2 main examples are the Tully-Fisher (TF) relation – for late-type galaxies – and the Faber-Jackson (FJ) relation – for early-type galaxies. Both are relations based on the dynamics of galaxies, relating the mass M of the galaxy to their rotation velocity (TF) or velocity dispersion (FJ) of galaxies.
- Main obstacle: accuracy/measurement errors of peculiar velocities still only 20%, at best 10%

Tully-Fisher

- Spiral galaxies:
relation between rotation velocity v (measured by HI velocity width) and absolute luminosity L of galaxy

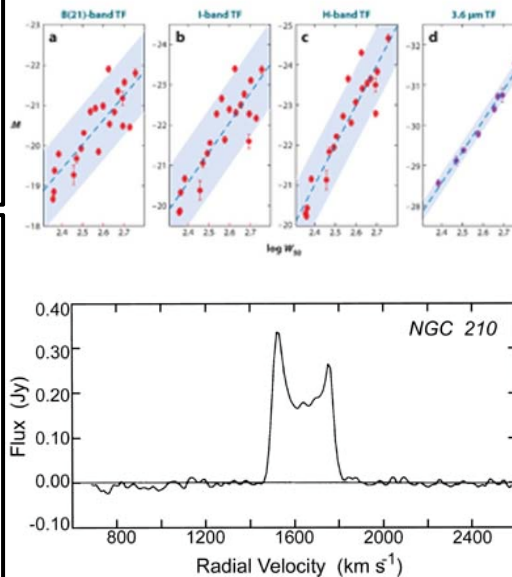
- $L \propto v^4$

- Measure rotation velocity v from linewidth 21cm line of galaxy:

$$TF \rightarrow L$$

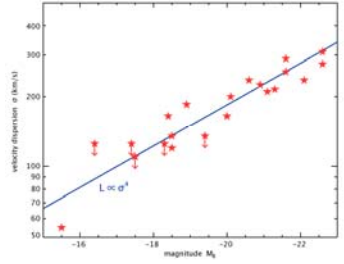
- Measure apparent magnitude, ie. apparent luminosity l :

- Distance r :
$$r = \sqrt{\frac{L}{l}}$$



Faber-Jackson

- Early-type galaxies:
relation between velocity dispersion σ_v
Luminosity L of galaxy
- $L \propto \sigma_v^4$



- Measure velocity dispersion σ_v of galaxy:
FJ \rightarrow L
- Measure apparent magnitude, ie. apparent luminosity l:
$$r = \sqrt{\frac{L}{l}}$$
- Distance r:

The FJ relation is a projection of a higher dimensional relation, the Fundamental Plane (FP)

The FP relates, for E and SO galaxies, the surface brightness I_e , effective radius R_e & velocity dispersion σ_v of a galaxy

$$\log R_e = -0.82 \log I_e + 1.24 \log \sigma_v + C_{FP}$$

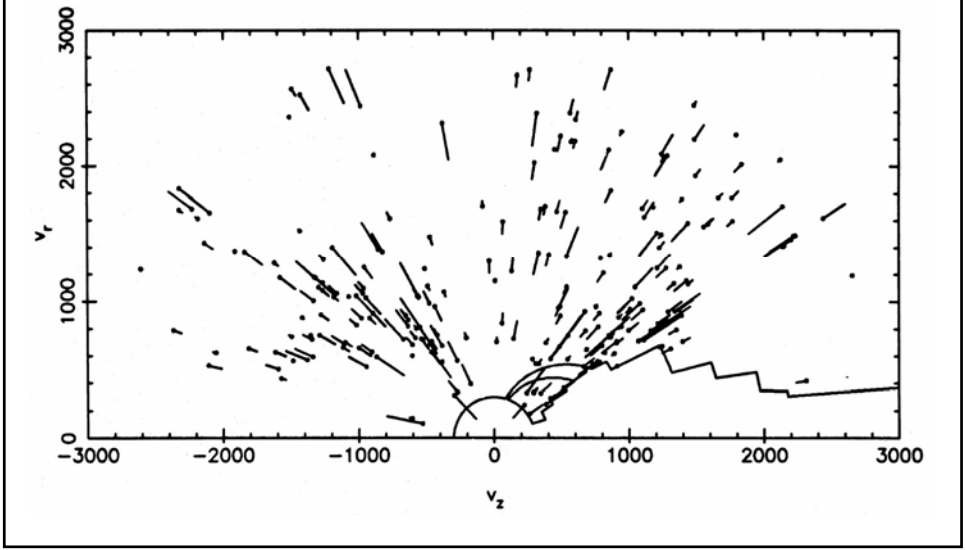
The FP is a reflection of the virial equilibrium of such a galaxy

Peculiar Velocities

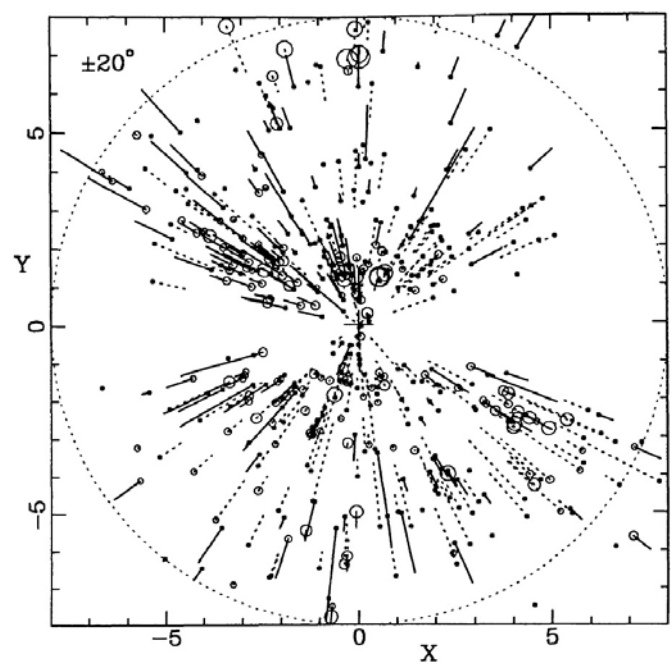
Local Universe

Local Supercluster flow

Lilje, Yahil & Jones 1986



Mark III
Peculiar velocities
Local Universe
Willick, Strauss et al.
First flow maps:
7 Samurai



POTENT

velocity reconstruction mass density distribution

- Surveys of galaxy peculiar velocities only give a sample of RADIAL velocities of galaxies,
- irregularly sample – at discrete galaxy locations – in sample volume
- Bertschinger & Dekel (1989++) proposed a beautiful idea to convert this into a map of the mass distribution in this volume.
- Their method, POTENT, is based on the realization that the flow on large scales is a potential flow, so that once can compute the velocity potential Φ_v :

$$v_{pec,r} = \vec{v}_{pec} \cdot \vec{e}_r = cz - Hr$$

$$\Phi_v(r) = \int_0^r v_{pec,r}(x) dx$$

- From this one can then simply get the FULL 3-D velocity flow:

$$\vec{v}(r) = \vec{\nabla} \Phi_v(r)$$

POTENT

velocity reconstruction mass density distribution

- Surveys of galaxy peculiar velocities only give a sample of RADIAL velocities of galaxies,
- irregularly sample – at discrete galaxy locations – in sample volume
- Bertschinger & Dekel (1989++) proposed a beautiful idea to convert this into a map of the mass distribution in this volume.
- Their method, POTENT, is based on the realization that the flow on large scales is a potential flow, so that once can compute the velocity potential Φ_v :

- From this one can then simply get the FULL 3-D velocity flow:

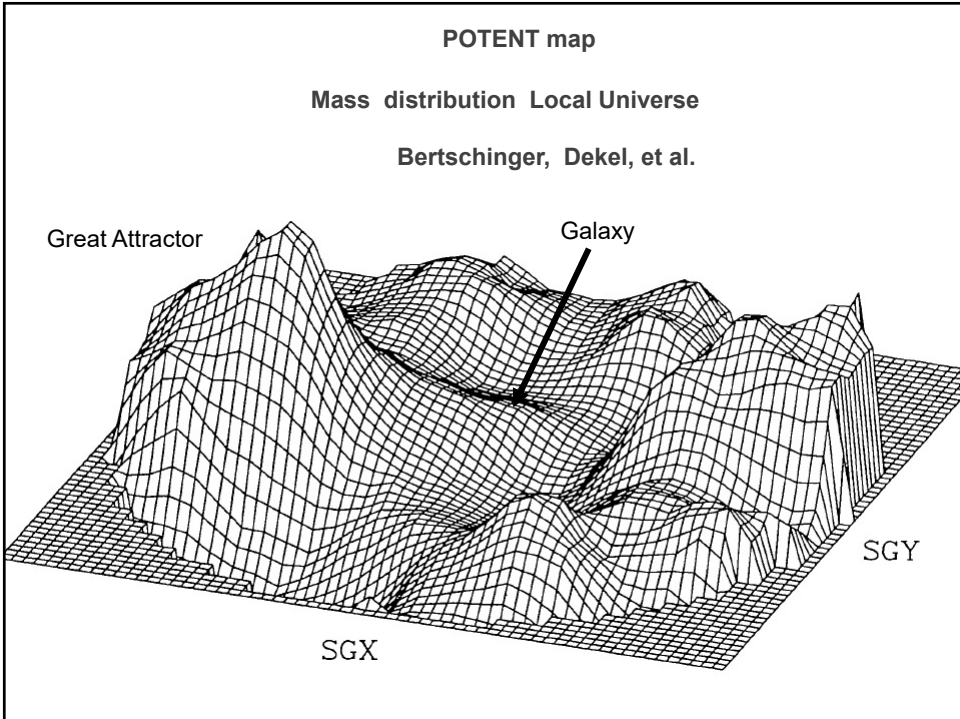
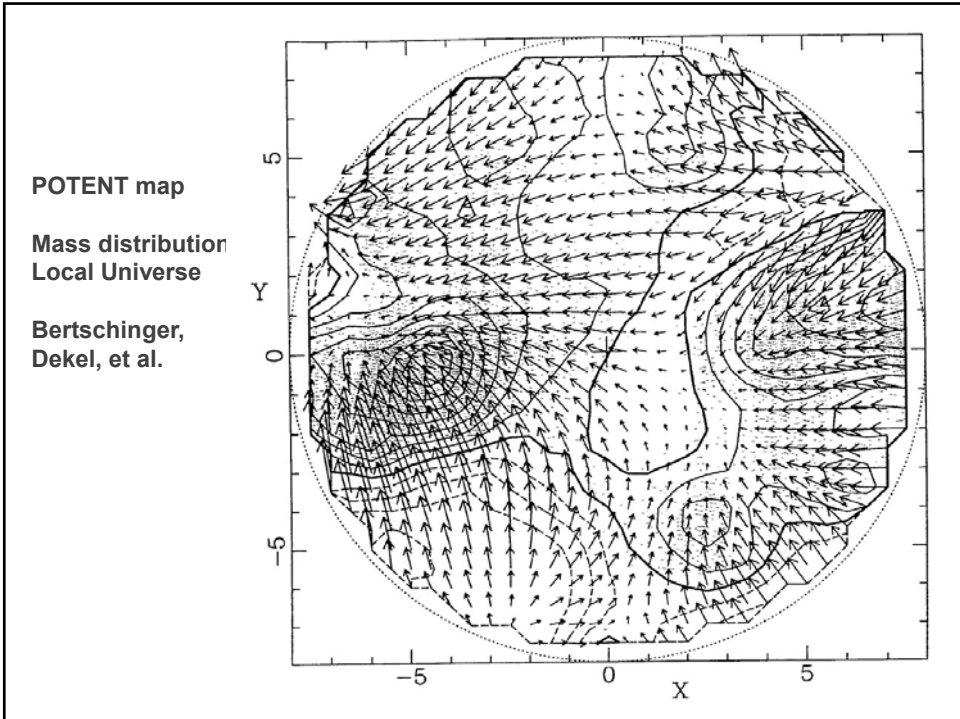
$$\vec{v}(r) = \vec{\nabla} \Phi_v(r)$$

- The density field $\delta(r)$ then simply follows from the linear continuity eqn.

$$\vec{\nabla} \cdot \vec{v} = -Haf(\Omega) \delta(\vec{r})$$

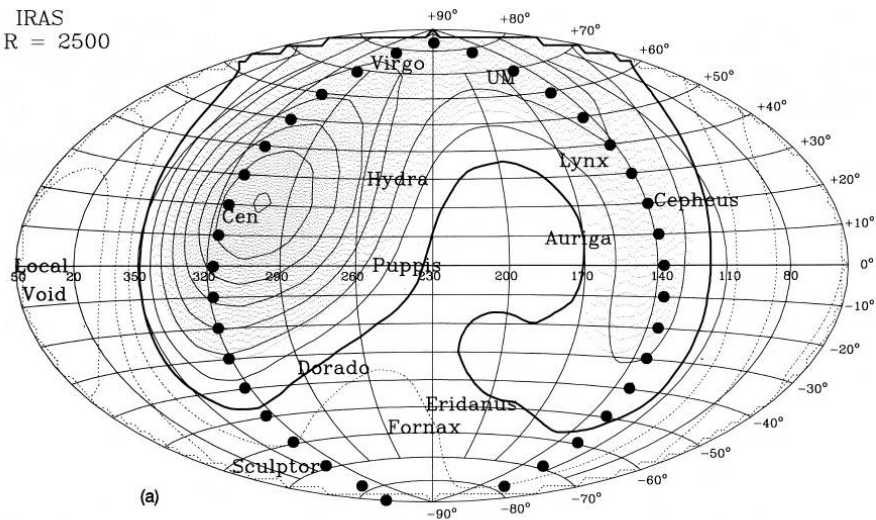
$$\Downarrow$$

$$\delta(\vec{r}) = -\frac{\vec{\nabla} \cdot \vec{v}}{Haf(\Omega)}$$

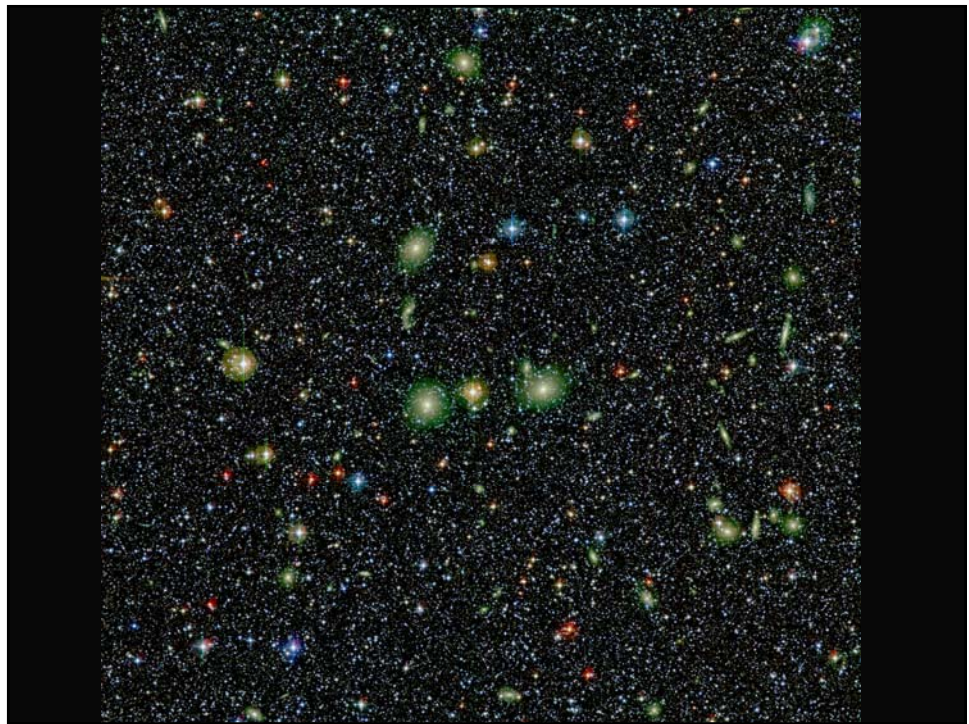
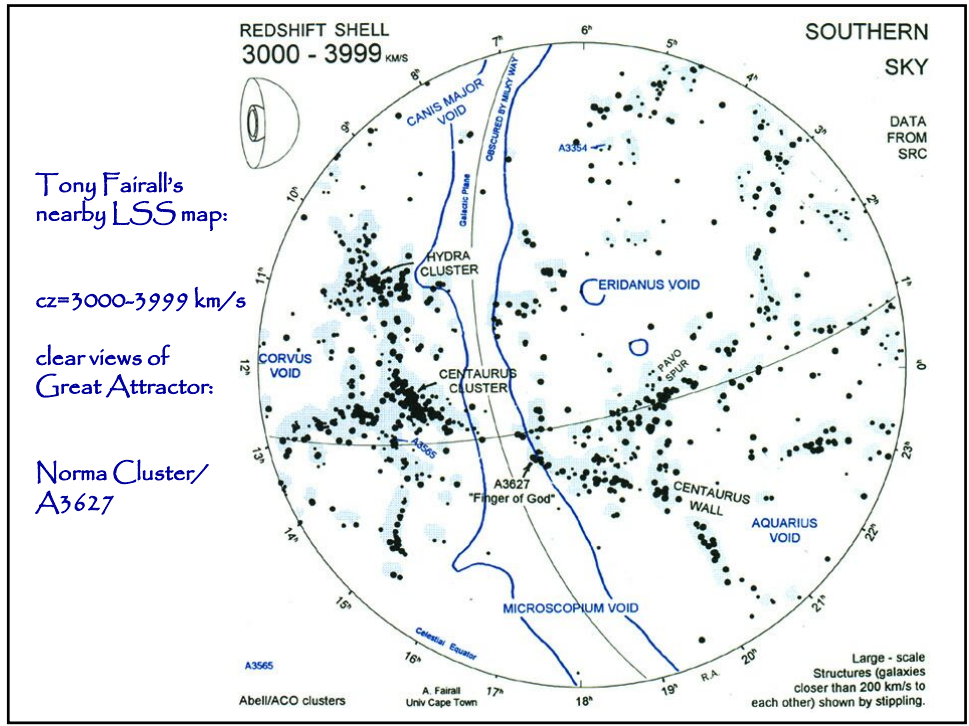


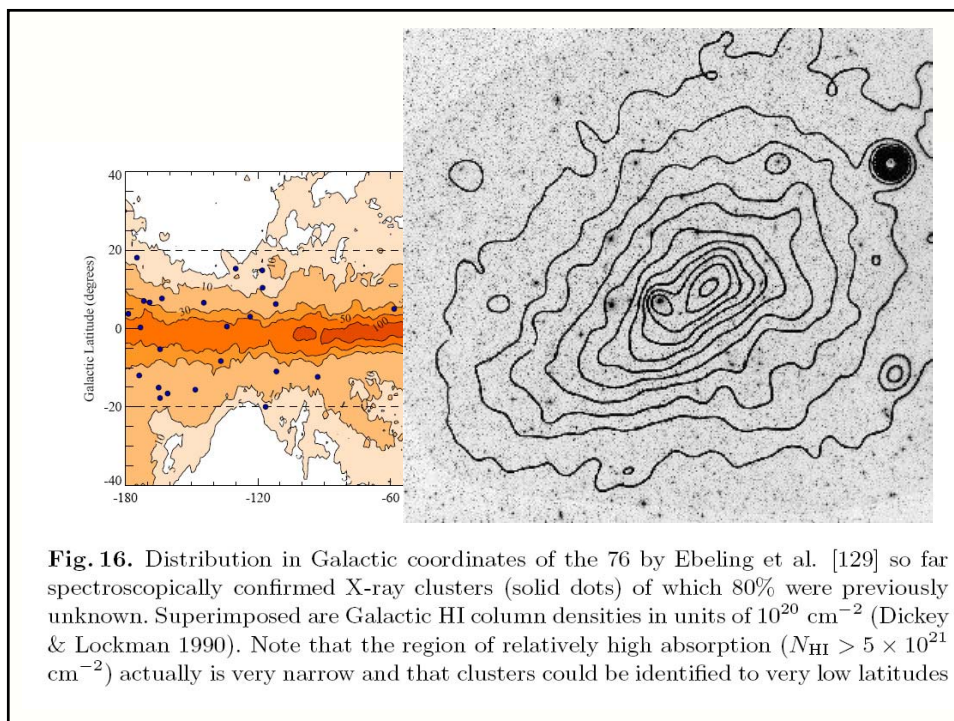
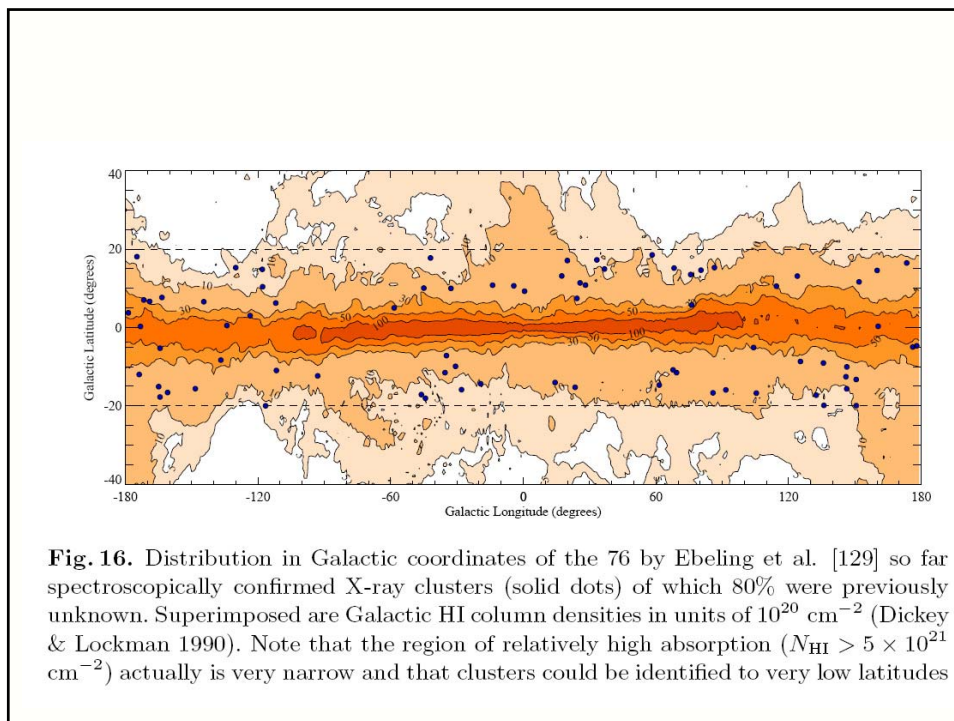
the Great Attractor

IRAS
R = 2500

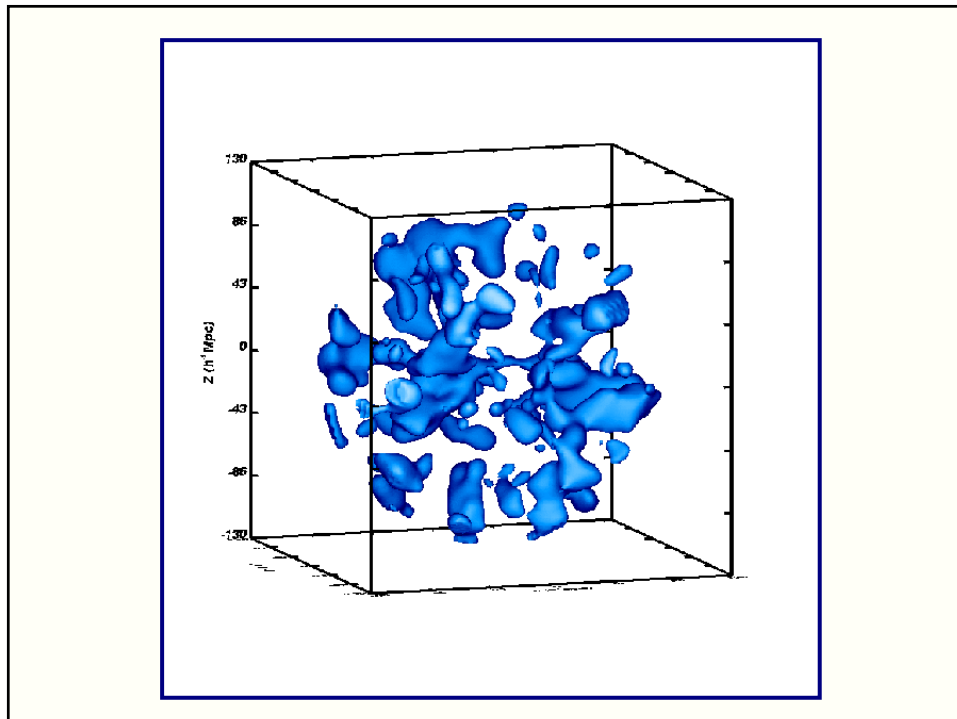


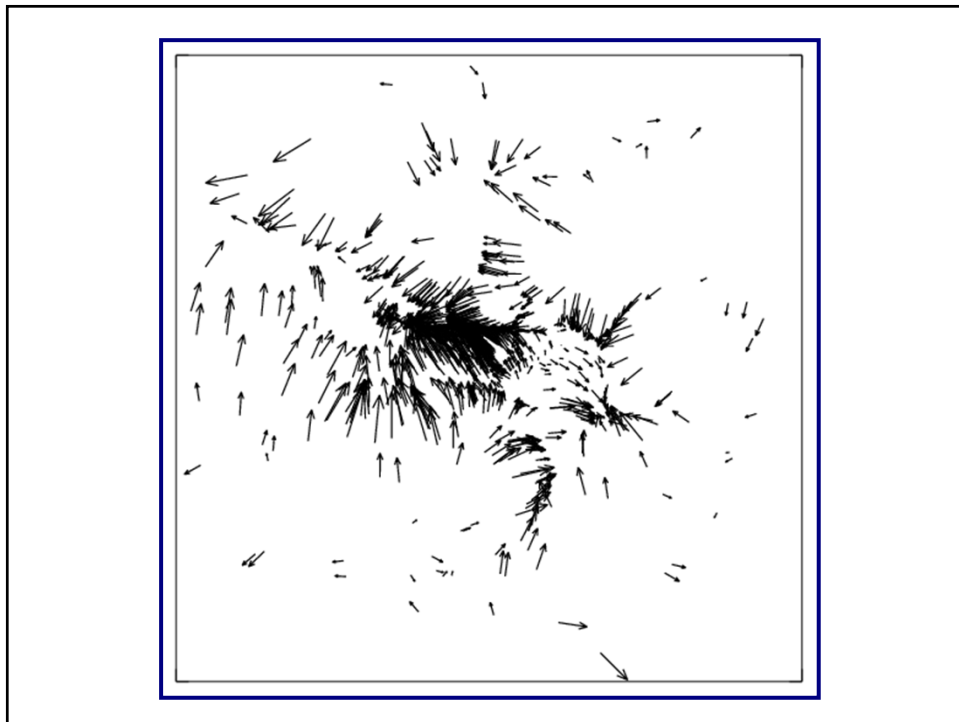
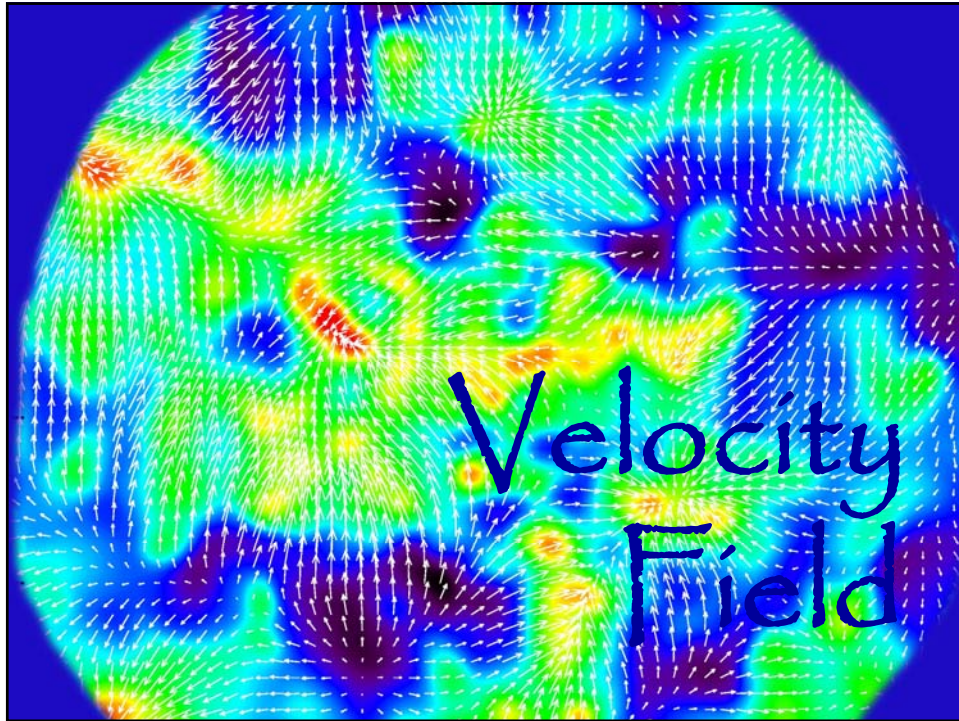
(a)
Figure 4. The galaxy density fluctuation field from the IRAS 1.9-Jy survey (by Yahil et al. 1991). Coordinates, smoothing, contours and shell distances are as in Fig. 3.

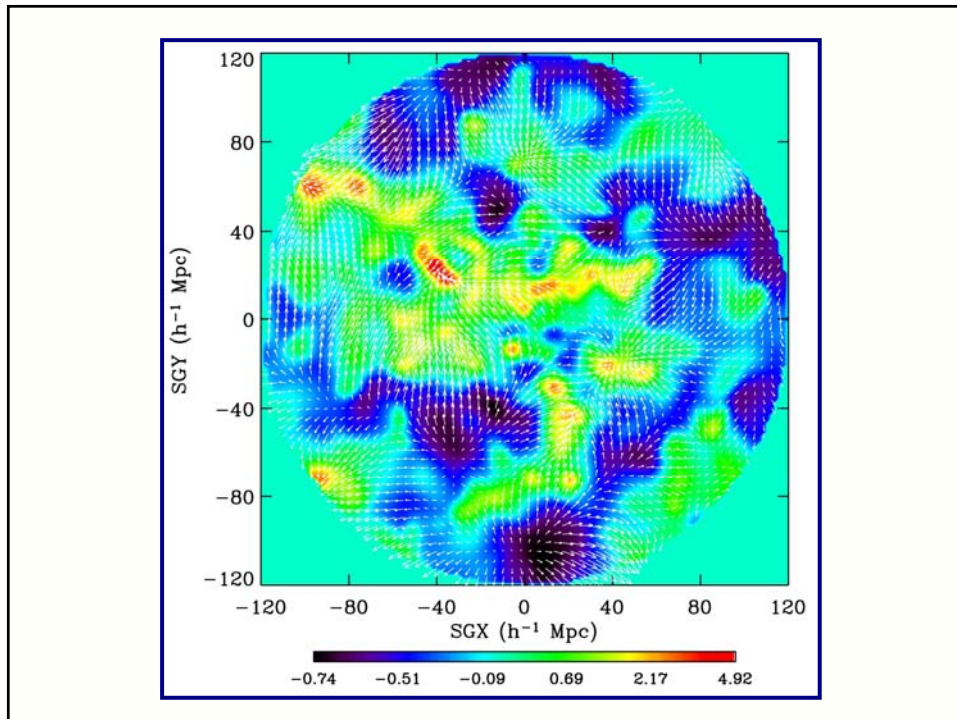
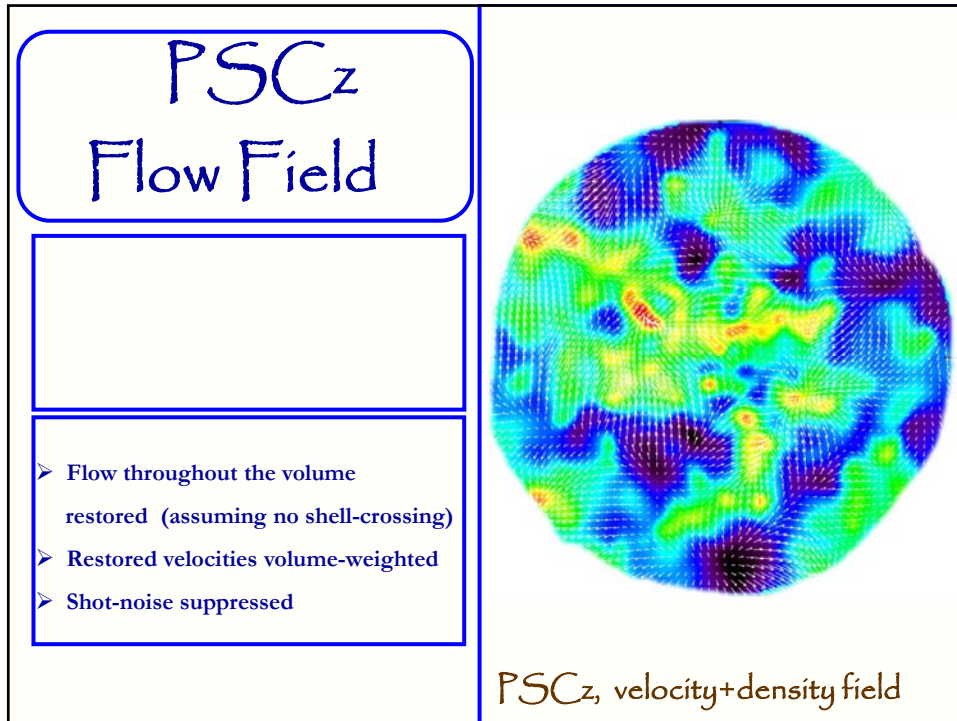


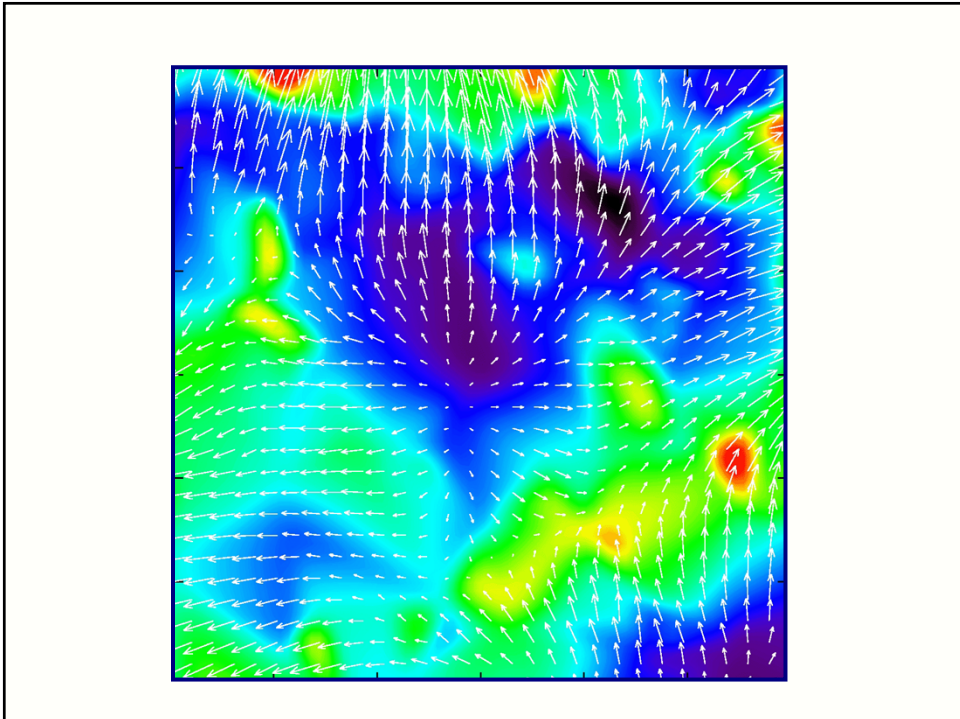
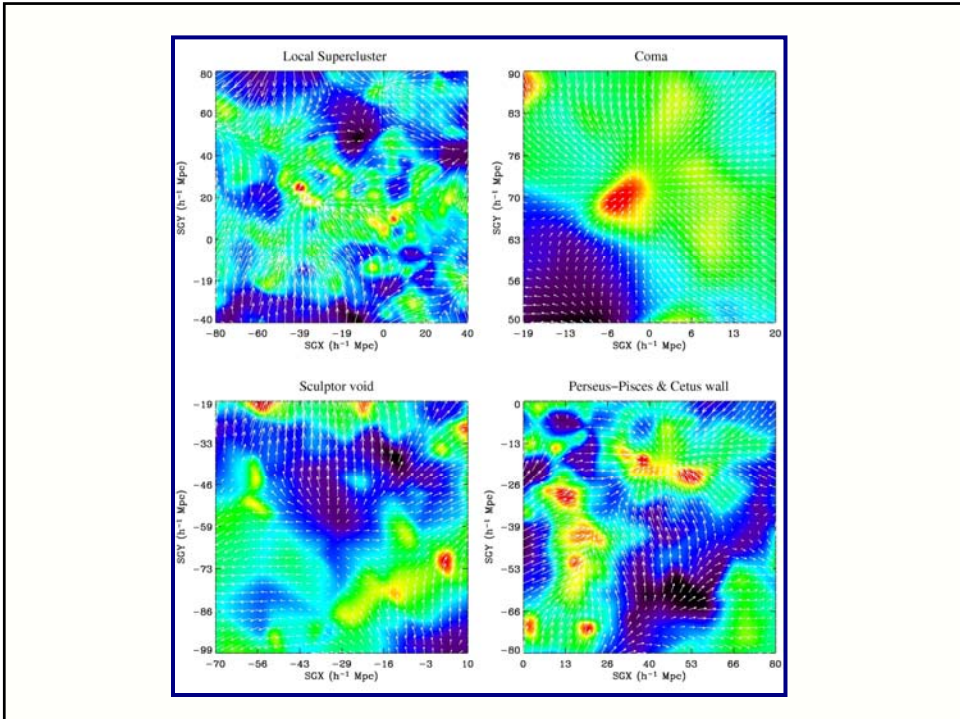


PSCz: Cosmic Migration Flows Local Universe









Cosmic Web: Cosmic Migration Flows

Large Scale Flows

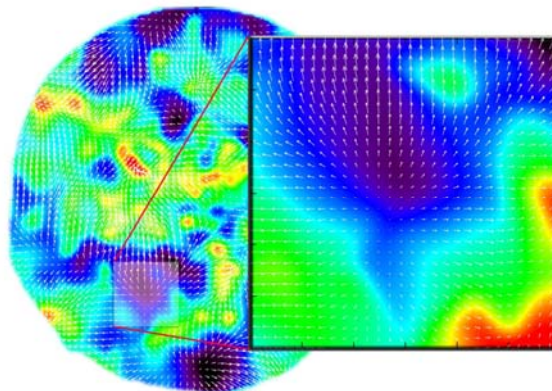
Large-Scale Flows:

- Structure buildup accompanied by displacement of matter:
- Cosmic flows
- On large (Mpc) scales, structure formation still in linear regime
- Directly related to cosmic matter distribution
- Note:
redshift space distortion

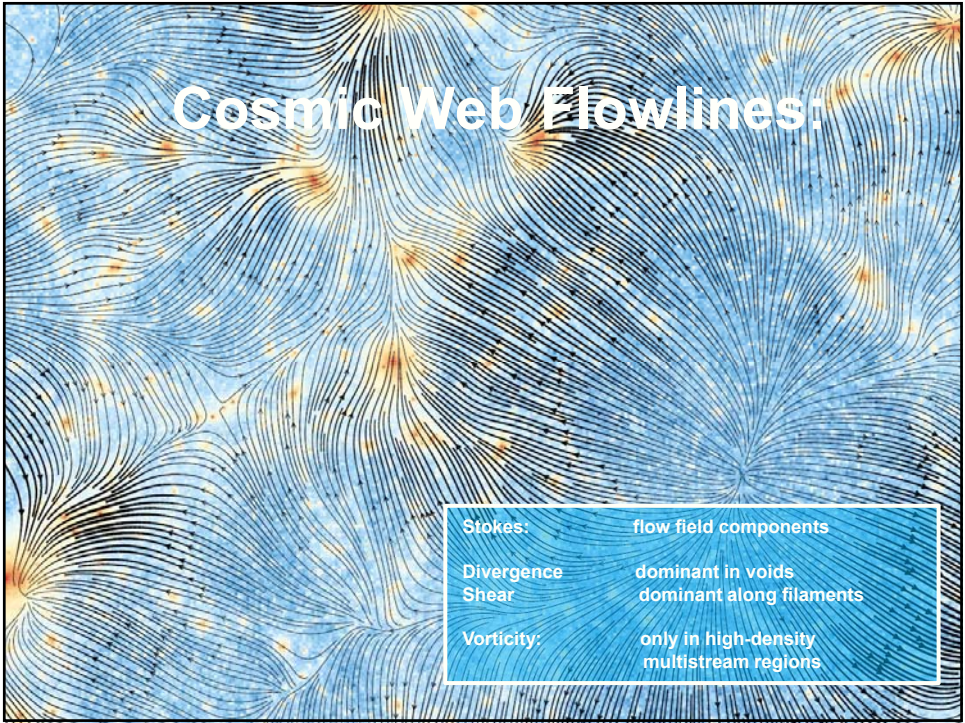
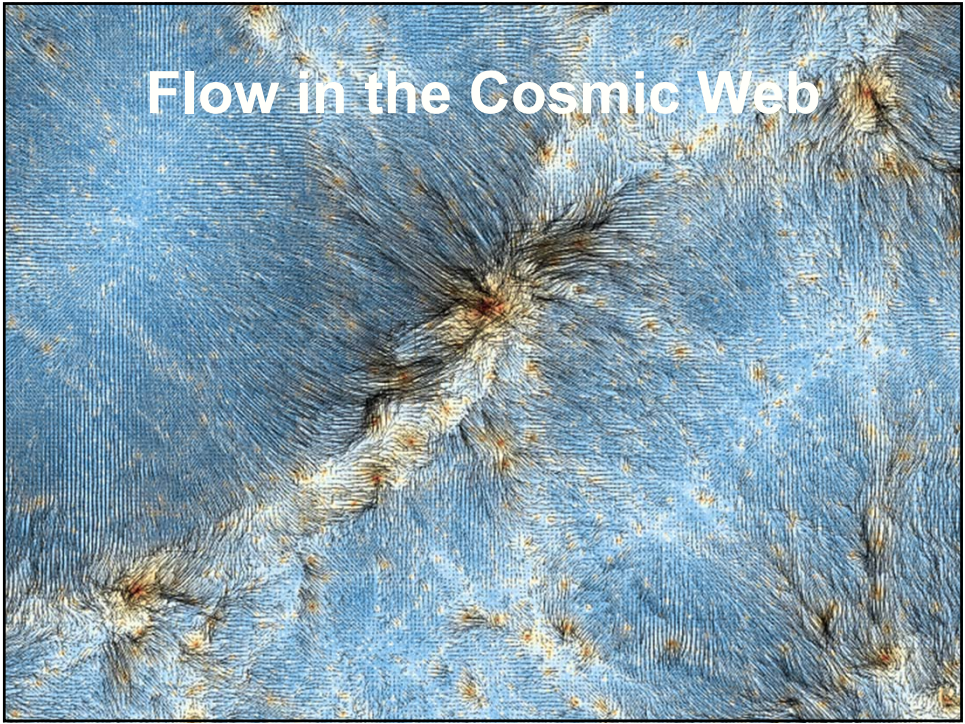
$$cz = Hr + v_{pec}$$

In principle possible to correct for this distortion, ie. to invert the mapping from real to redshift space

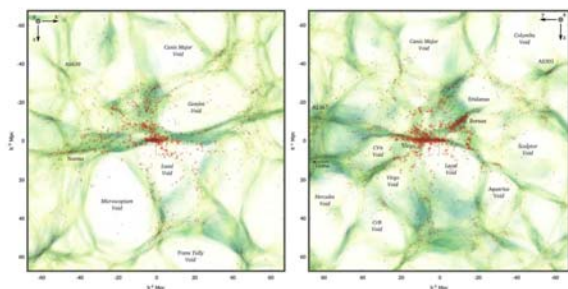
- Condition:
entire mass distribution within volume should be mapped



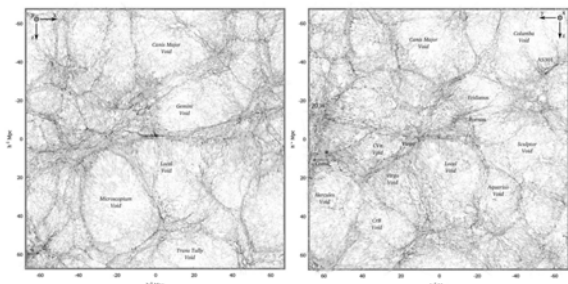
$$\mathbf{v}(\mathbf{x}, t) = \frac{H}{4\pi} \frac{f(\Omega_m)}{b} a \int d\mathbf{x}' \delta_{gal}(\mathbf{x}', t) \frac{(\mathbf{x}' - \mathbf{x})}{|\mathbf{x}' - \mathbf{x}|^3}$$



2MRS Local Universe



KIGEN-adhesion reconstruction 2MRS

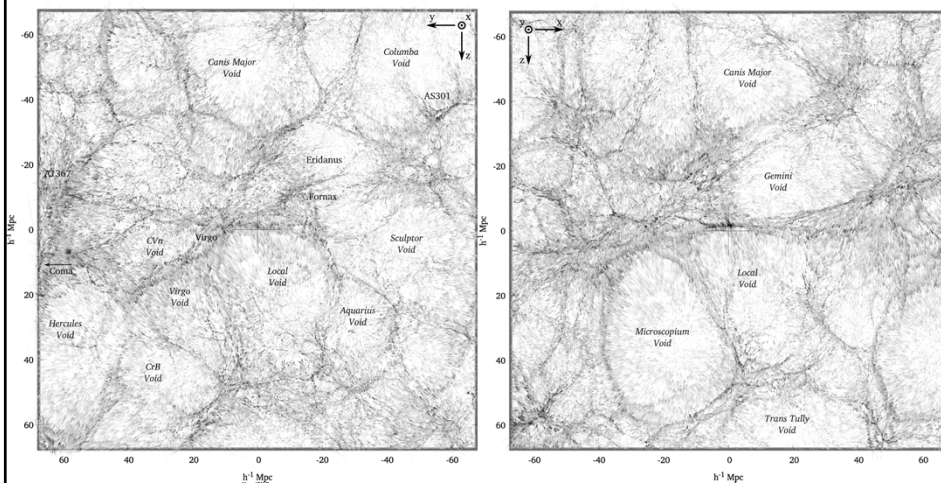


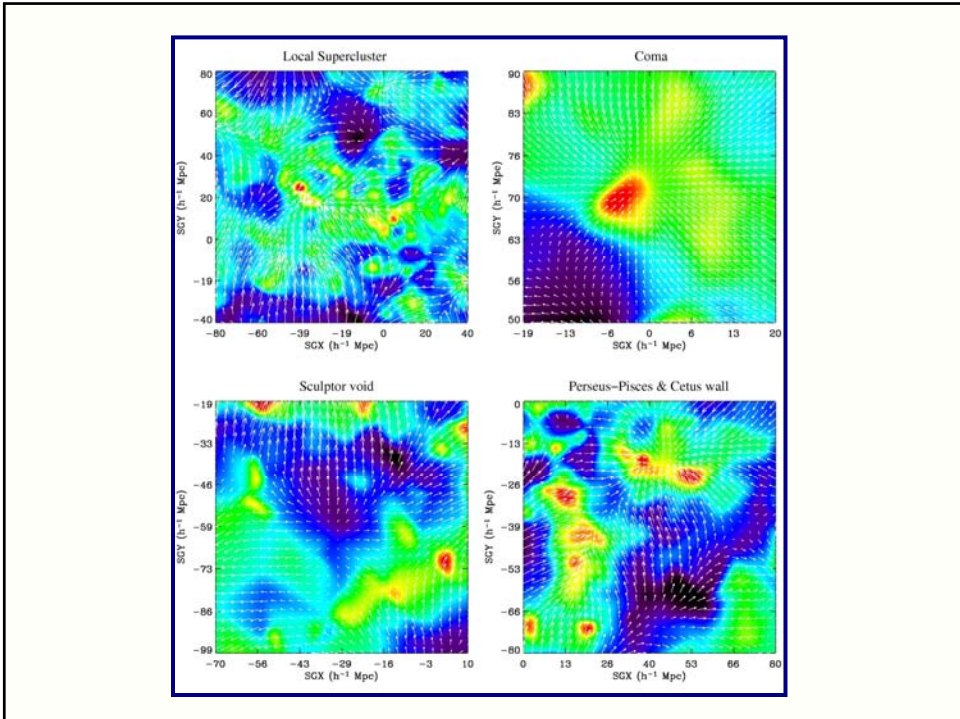
Hidding, vdW, Kitaura & Hess 2018

Supergalactic Plane

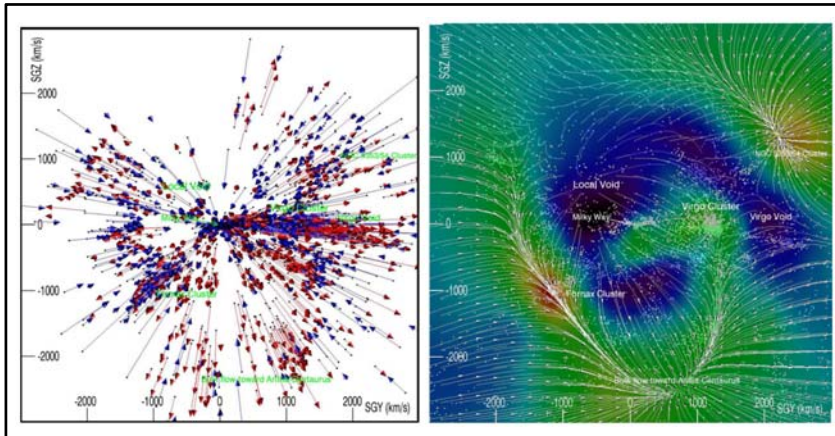
mean KIGEN - adhesion reconstruction

Hidding, Kitaura, vdW & Hess 2016/2017



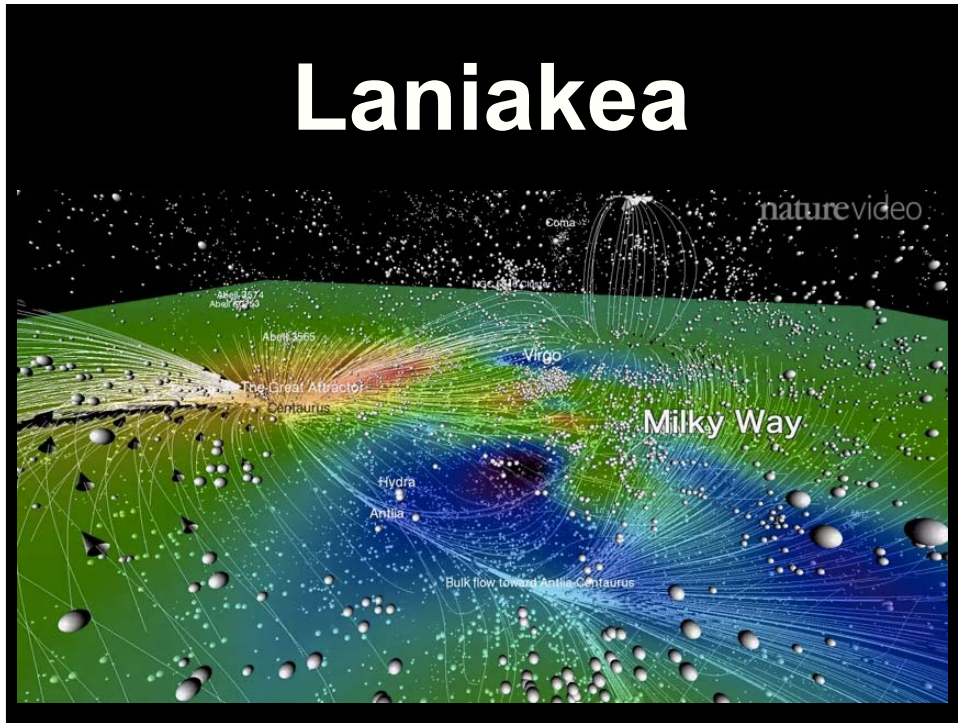


CosmicFlows-2

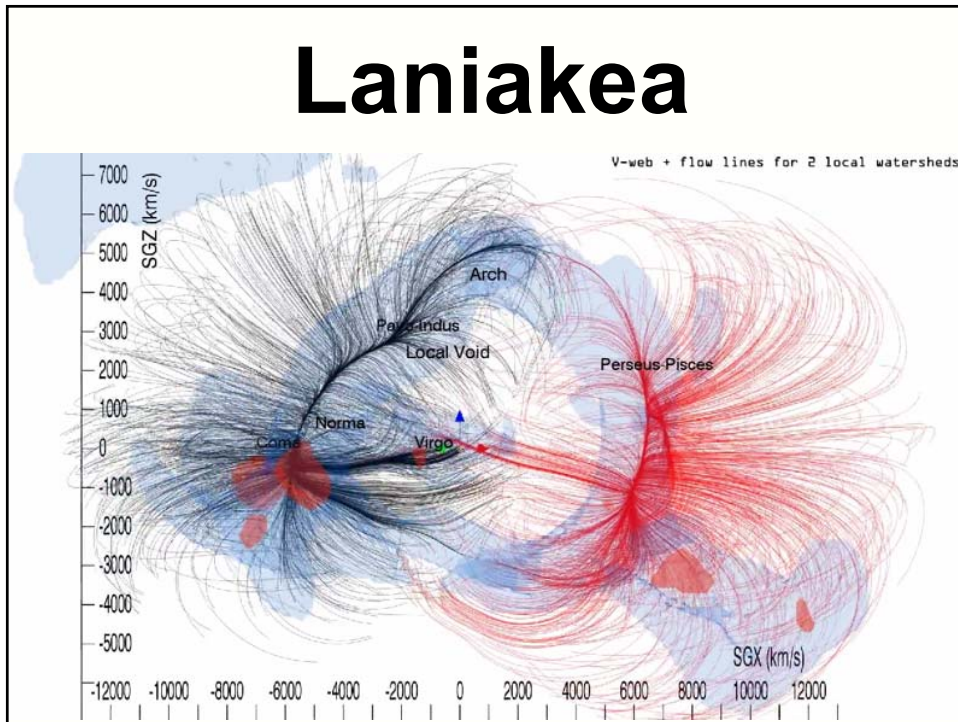


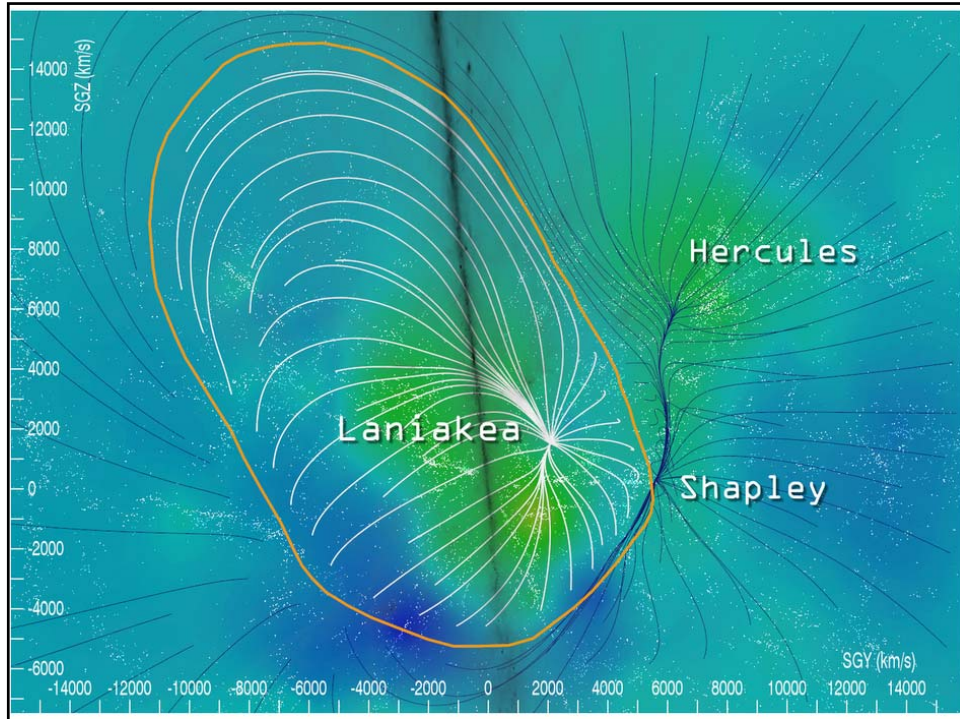
Courtois et al. 2013
Local void expansion in Cosmicflows-2

Laniakea

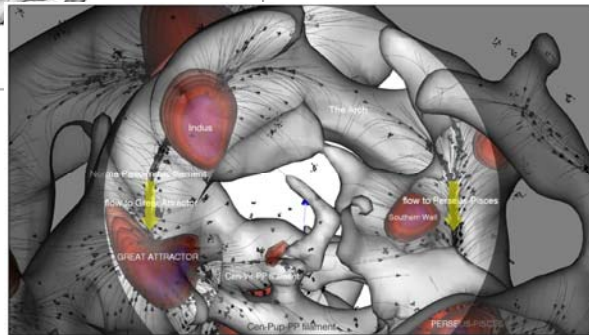
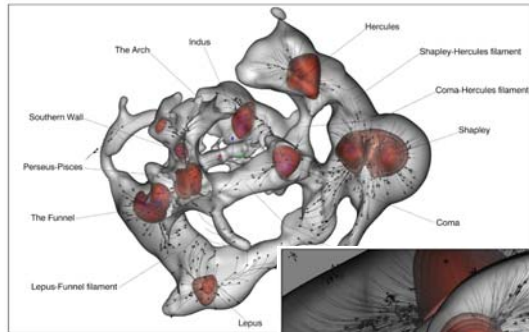


Laniakea





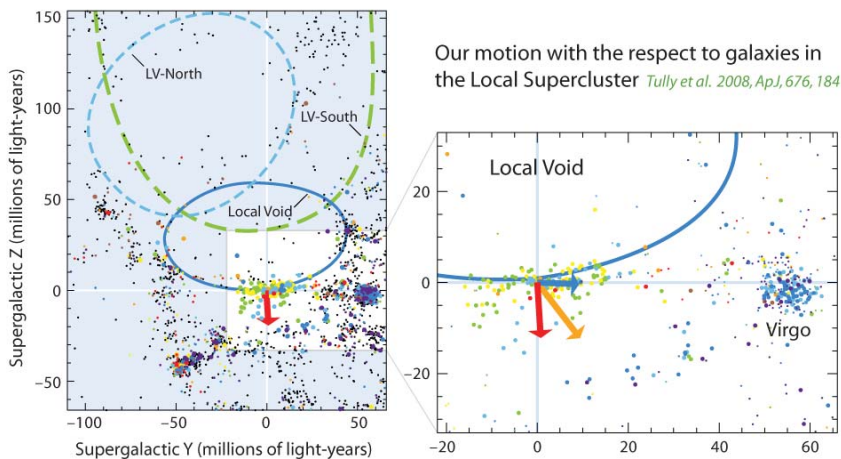
CosmicFlows-3



**Cosmic Web morphology:
velocity shear based
V-web identification
flow pattern in cosmic web**

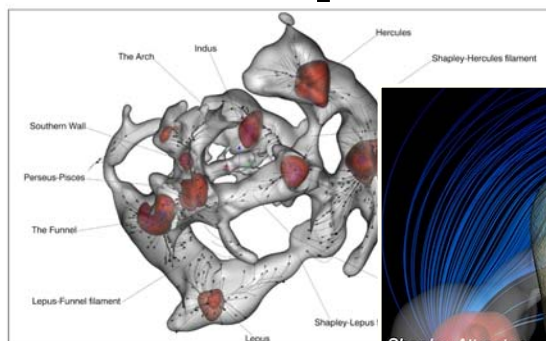
(Pomarede et al. 2017)

Push of the Local Void



Tully et al. 2008:
Local Void pushes with ~260 km/s against our local neighbourhood

Void Dipole Repeller

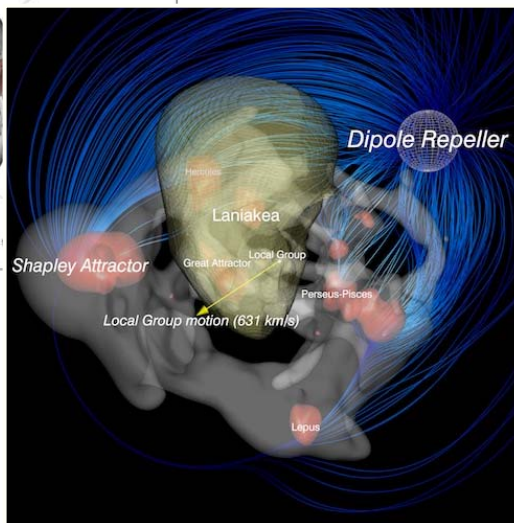


Cosmicflows-3 Cosmic Web
morphology Local Universe

(Pomarede et al. 2017)

Void Dipole Repeller
dominant dynamical
Presence Local Universe

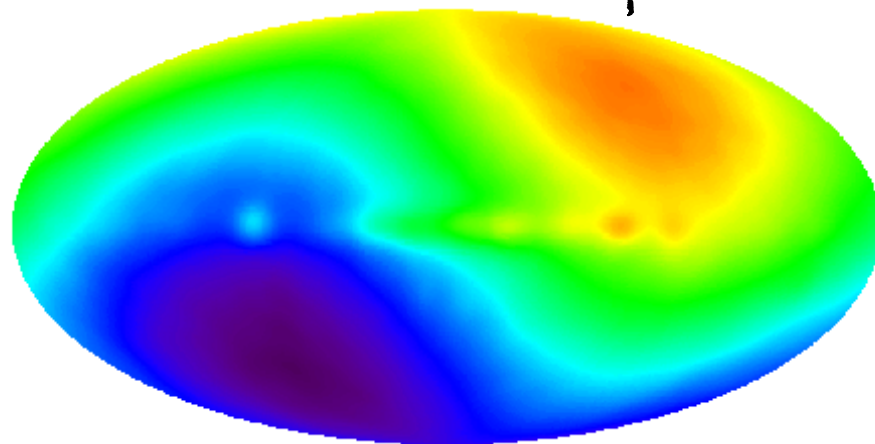
(Tully et al. 2017)



Cosmic Dipoles:

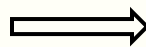
Motion of the Milky Way

The CMB Dipole



$$\Delta T = 3.36 \text{ mK}$$

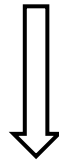
$$(l, b) = (264.3^\circ, 48.1^\circ)$$



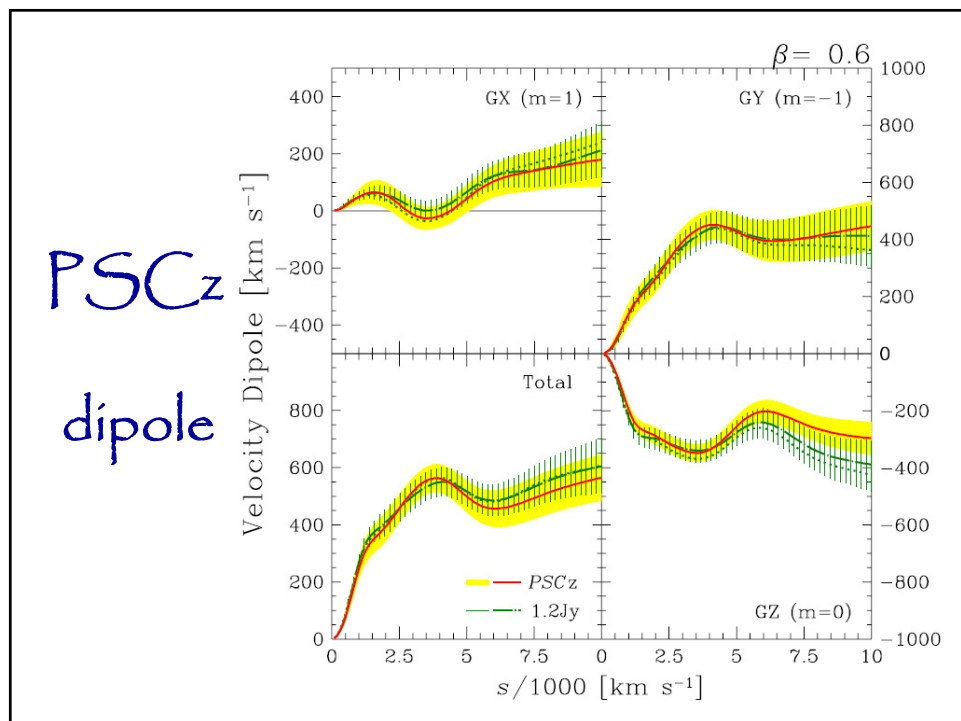
$$v_{LG} = 627 \pm 22 \text{ km/s}$$

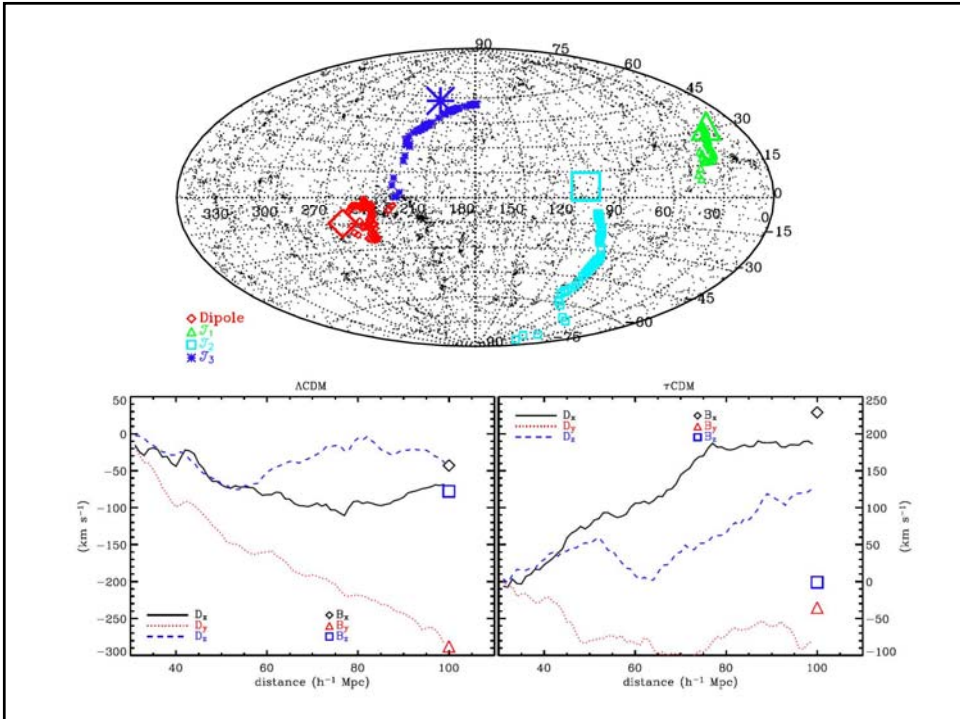
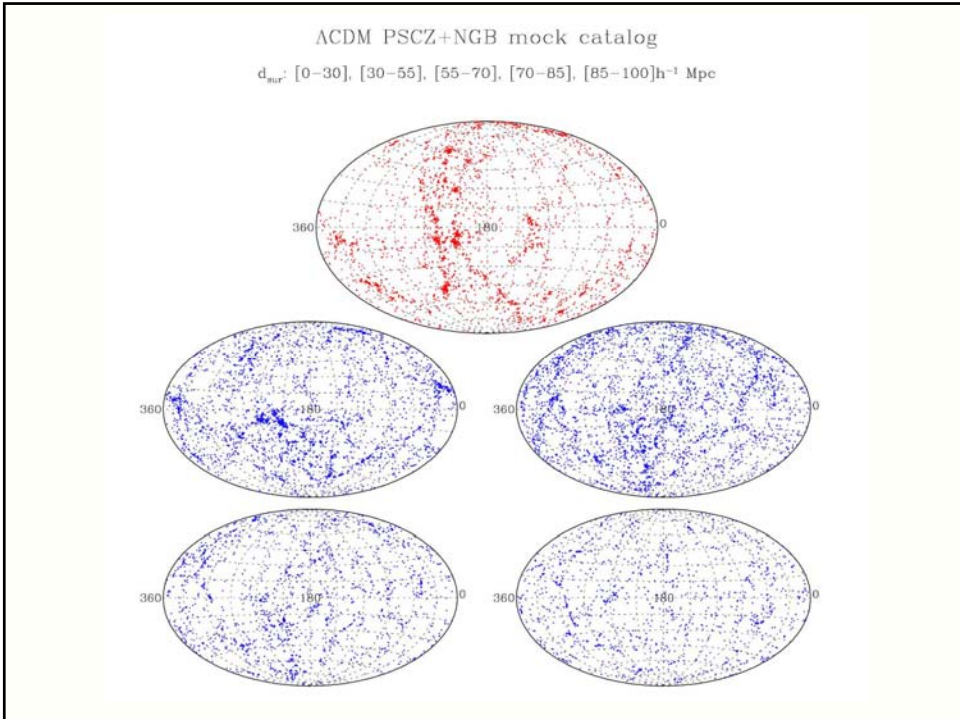
$$(l, b) = (276^\circ, 30^\circ)$$

$$\mathbf{v}_{\text{LG}} = \frac{H_0 \beta}{4\pi} \int_r^\infty d^3 \mathbf{r}' \delta_g(\mathbf{r}') \frac{\mathbf{r}' - \mathbf{r}}{|\mathbf{r}' - \mathbf{r}|^3}$$



$$\mathbf{v}(\mathbf{r}) = \frac{H_0 \beta}{4\pi \bar{n}} \sum_i^N \frac{w_i \hat{\mathbf{r}}_i}{r_i^2}$$





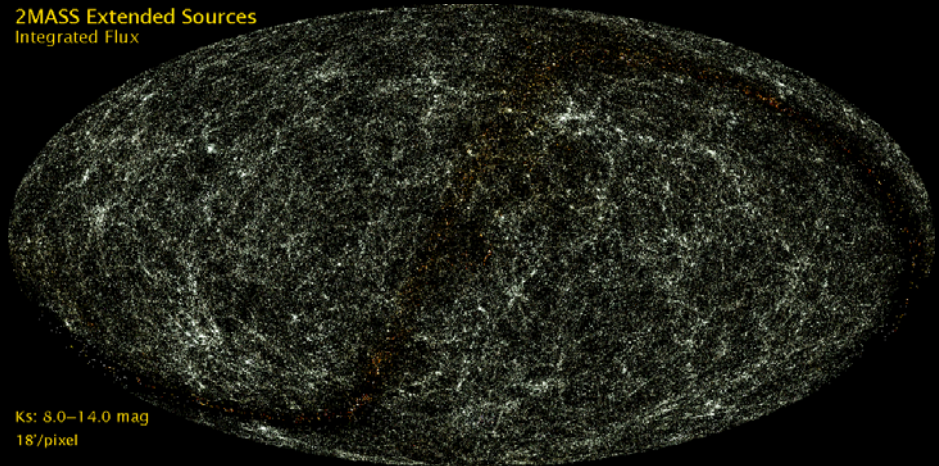
2MASS survey

- 2MASS all-sky survey:
ground-based near-infrared survey whole sky,
J(1.2 μ m), H(1.6 μ m), K(2.2 μ m)
- 2MASS extended source catalog (XSC):
1.5 million galaxies
- unbiased sample nearby galaxies
- photometric redshifts:
depth in 2MASS maps,
“cosmic web” of (nearby) superclusters spanning the entire sky.

courtesy: T. Jarrett

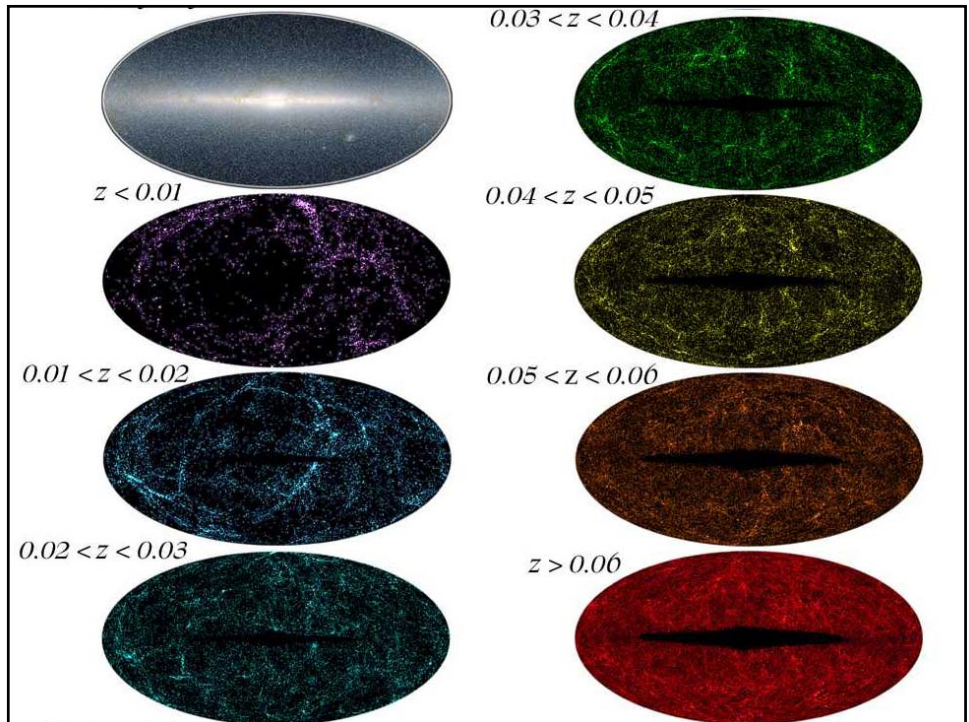
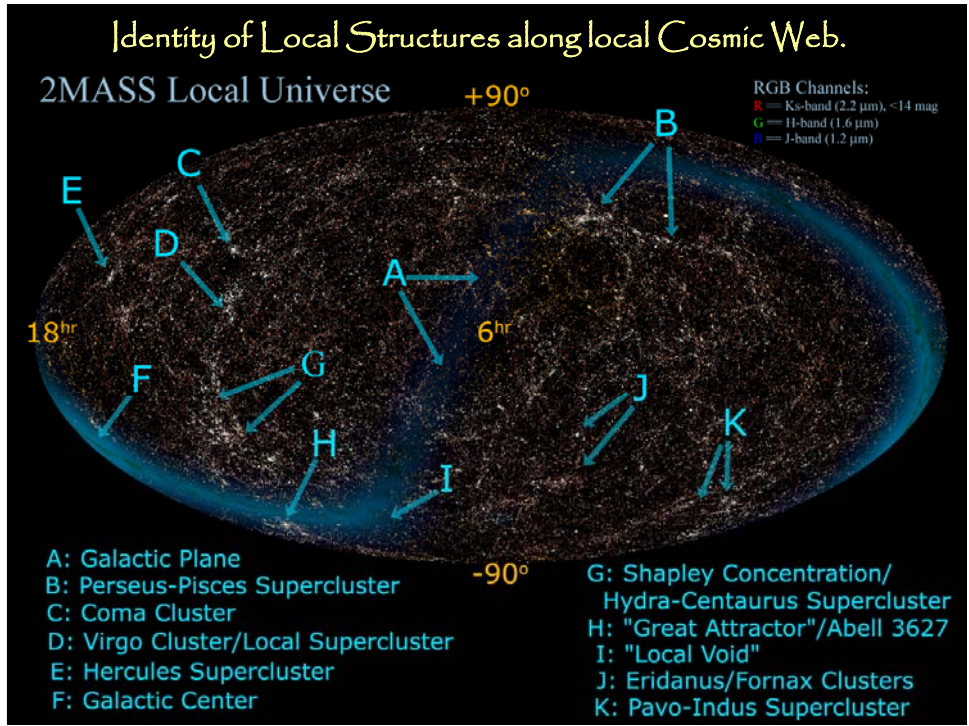
2MASS Cosmic Web

2MASS Extended Sources
Integrated Flux



Ks: 8.0–14.0 mag
18"/pixel

Looking around us we already see the unmistakable signatures of an intriguing foamlike matter distribution in our immediate Cosmic Vicinity.



2MASS dipole

