

Megaparsec Scale Structure of the Universe

- **Large Scale Structure of the Universe:**
crucial information for our understanding of structure formation in the Universe
- **Dynamic Timescale ~ Hubble Time (age Universe):**
Megaparsec structures have evolved only mildly, so that one may infer their formation & evolution, and link to conditions primordial Universe
- **Compare timescales:**

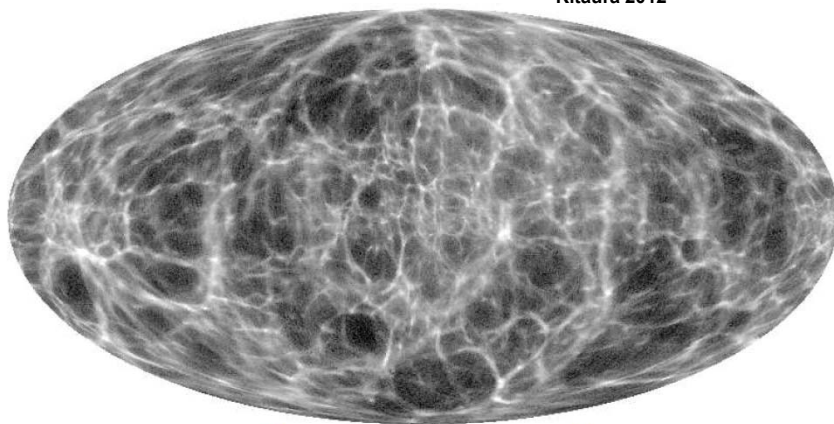
solar system	~ 1 yr
galaxy	~ 10^8 yr
clusters	~ 10^9 yr
Megaparsec structures	~ 10^{10} yr

Cosmic Fossil

Cosmic Web: 2MASS

Most detailed reconstruction
Local Cosmic Web (2MRS):

Kitaura 2012







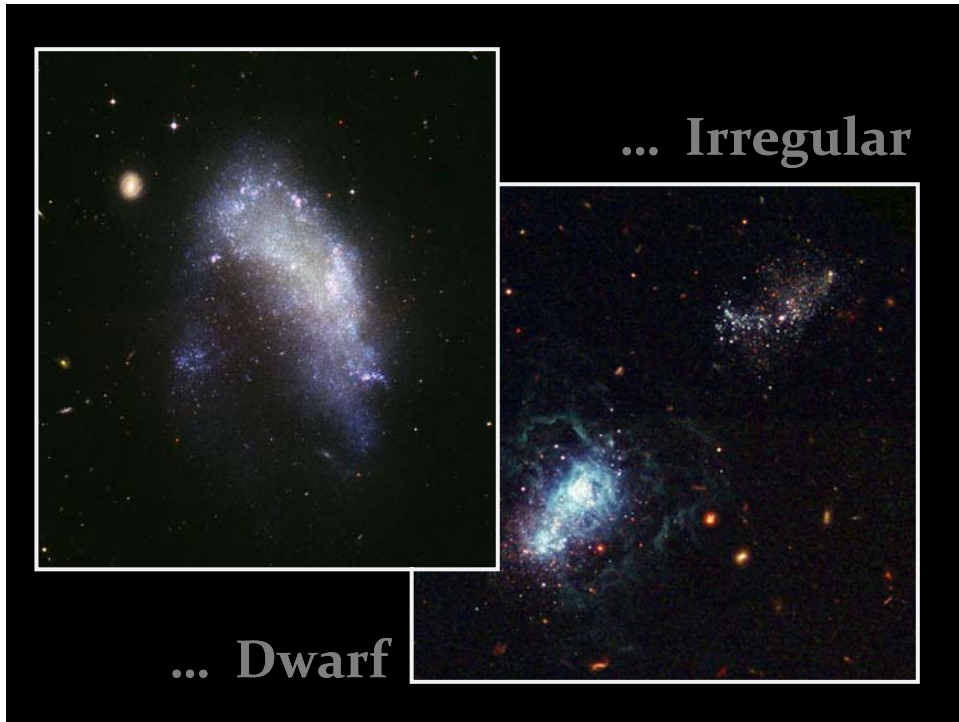
NGC 1300: a Milky Way look-alike ?



... Elliptical



... Lenticular



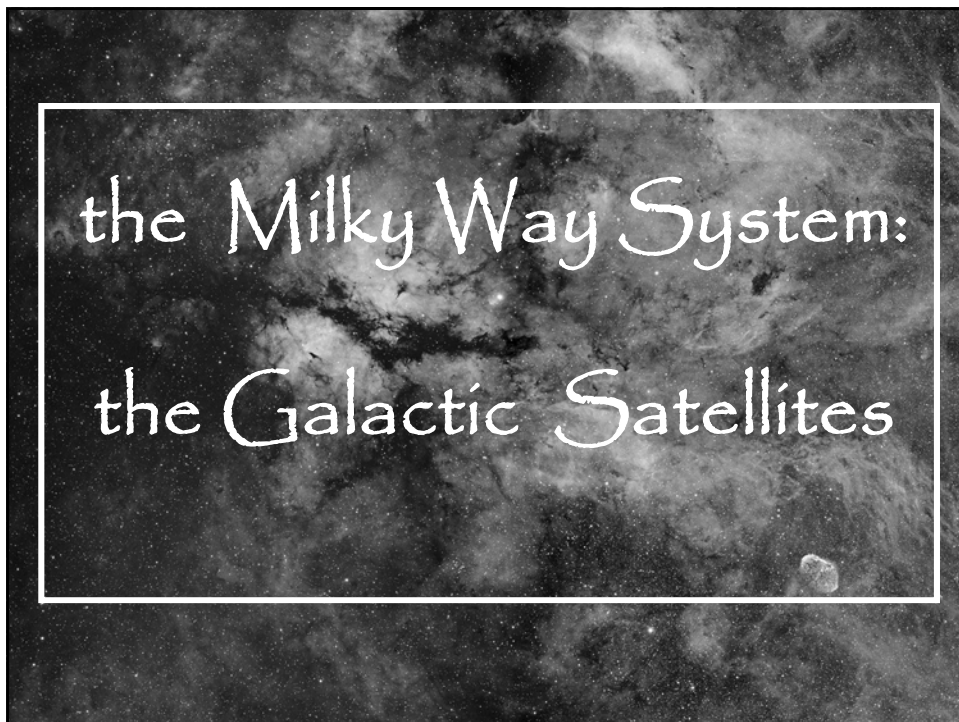
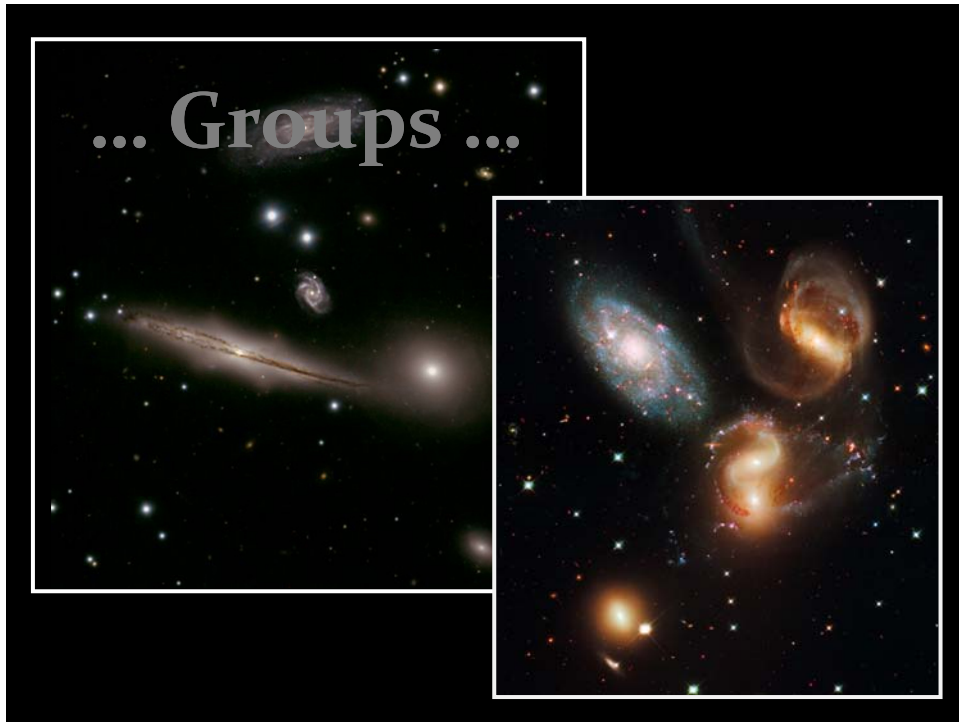
Sociology
of Galaxies

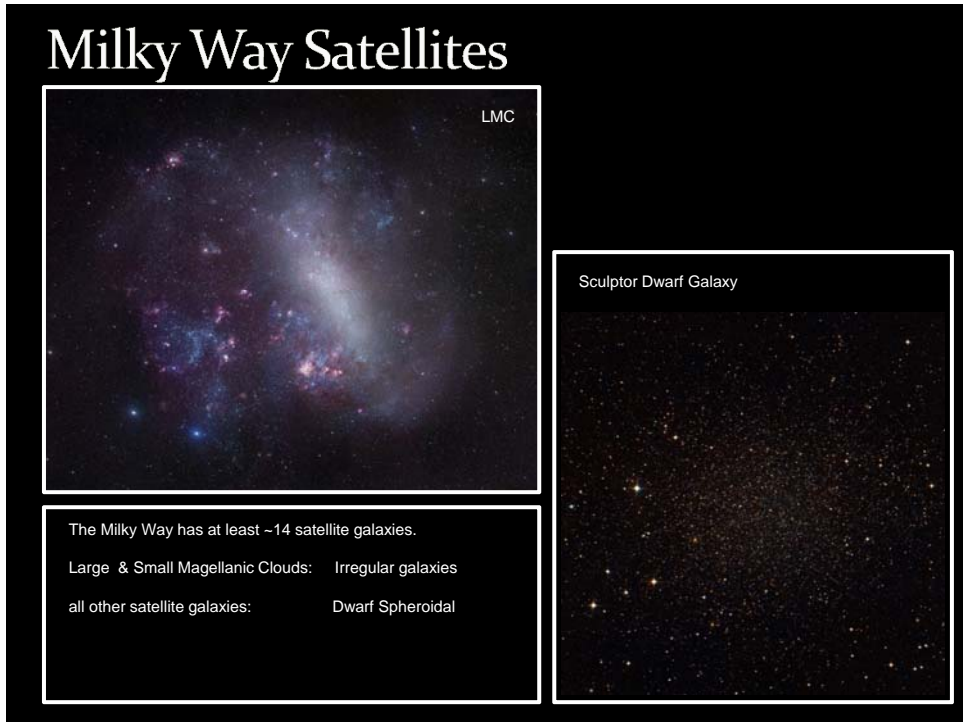
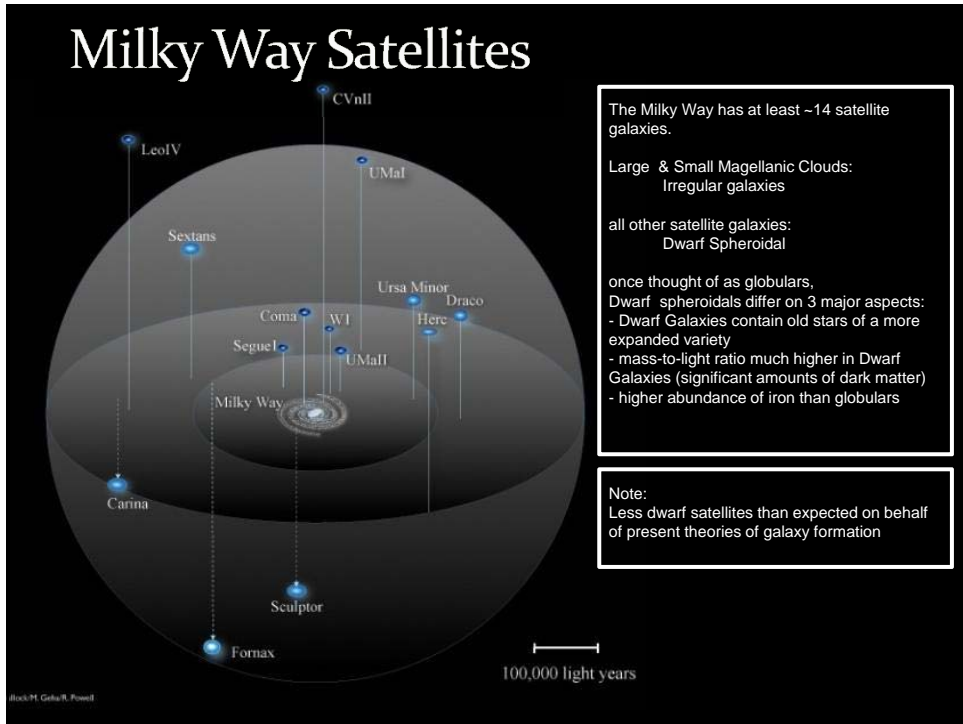
Sociology of Galaxies

- Galaxies are not singular objects:
- they group and cluster into a hierarchy of ever larger entities.
- direct manifestation of gravitational attraction between matter: clumping of matter
- Their sociology, ie. the characteristics and patterns in which they group together, is a key to unravelling the formation of structure in the Universe.

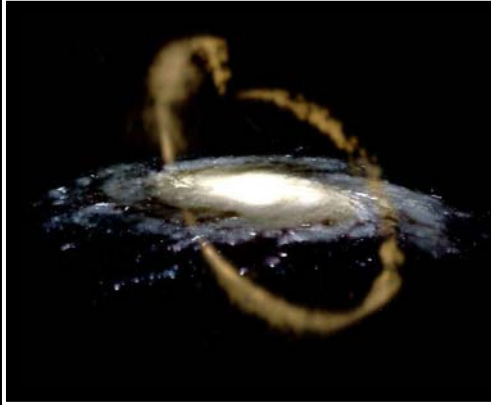
Interacting Galaxies



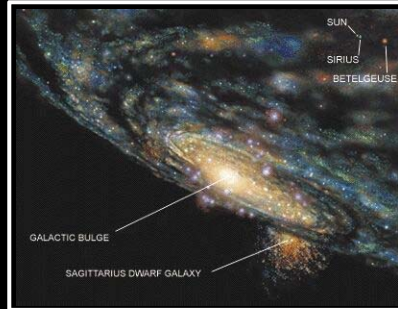




Sagittarius Dwarf Galaxy



Nearest known neighbour to Galaxy:
central cluster (old population II) +
loop-shaped structure wrapping around Galaxy



Based on current trajectory:

- Sag DEG main cluster is about to pass through the galactic disc of Milky Way within next 100 Myr
- extended loop-shaped ellipse already extended around and through our local space and on through the Milky Way galactic disc (will be slowly absorbed into Milky Way)

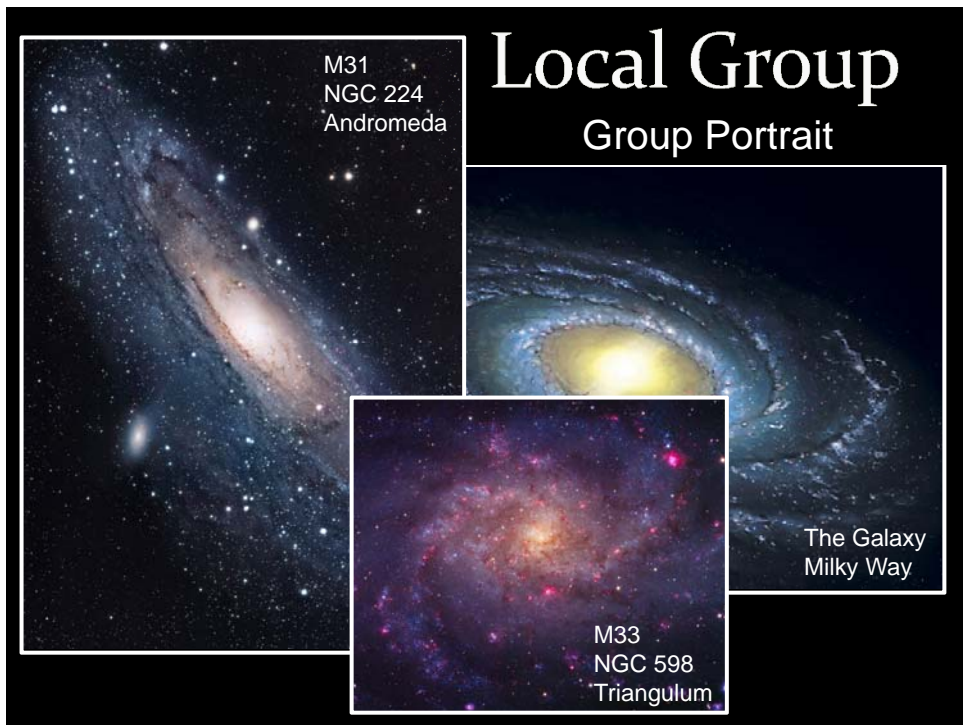
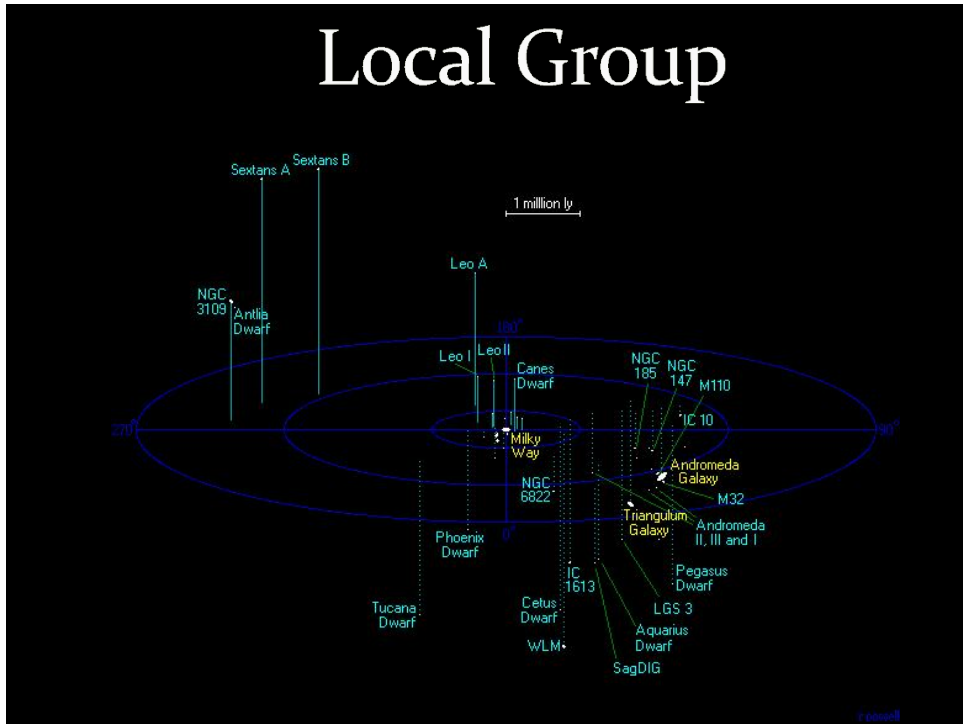
Globulars:

- 4 globular clusters (incl. M54)
- dynamically linked to 3 young globulars

Multiple stellar populations:

- very oldest globular cluster populations
- stars as young as ~ 100 Myr





Local Group

- Milky Way satellites:

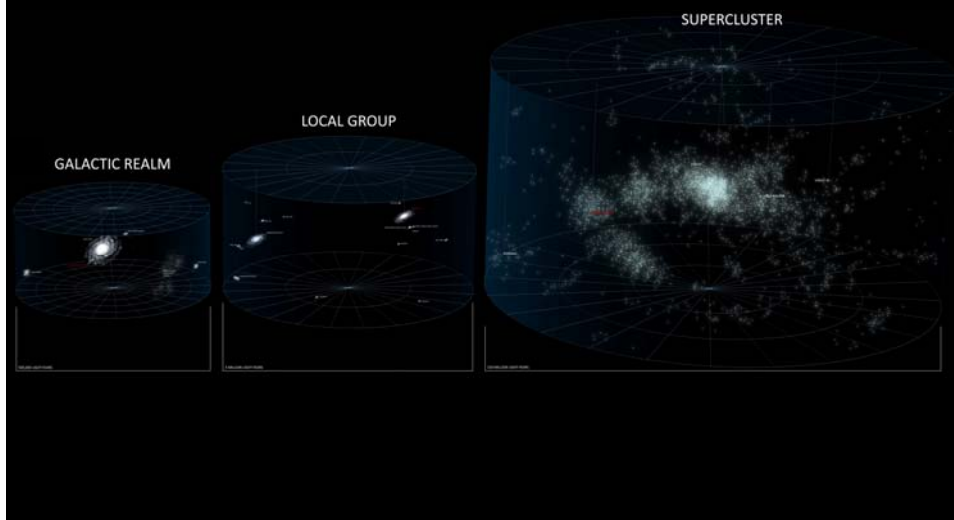
Sagittarius Dwarf Galaxy
 Large Magellanic Cloud (LMC)
 Small Magellanic Cloud (SMC)
 Canis Major Dwarf
 Ursa Minor Dwarf
 Draco Dwarf, Carina Dwarf,
 Sextans Dwarf, Sculptor Dwarf,
 Fornax Dwarf,
 Leo I, Leo II,
 Ursa Major Dwarf

- M₃₁ satellites:

M32,
 M110,
 NGC 147,
 NGC 185,
 And I, And II, And III,
 And IV, And V,
 Pegasus dSph,
 Cassiopeia Dwarf,
 And VIII, And IX, And X.

- Diameter Local Group: $D_{LG} \sim 3 \text{ Mpc}$
- Binary (dumbbell) shape
- Mass Local Group: $M_{LG} \sim 1.29 \pm 0.14 \times 10^{12} M_{\odot}$.
- The group itself is one of many density clumps within the Local Supercluster

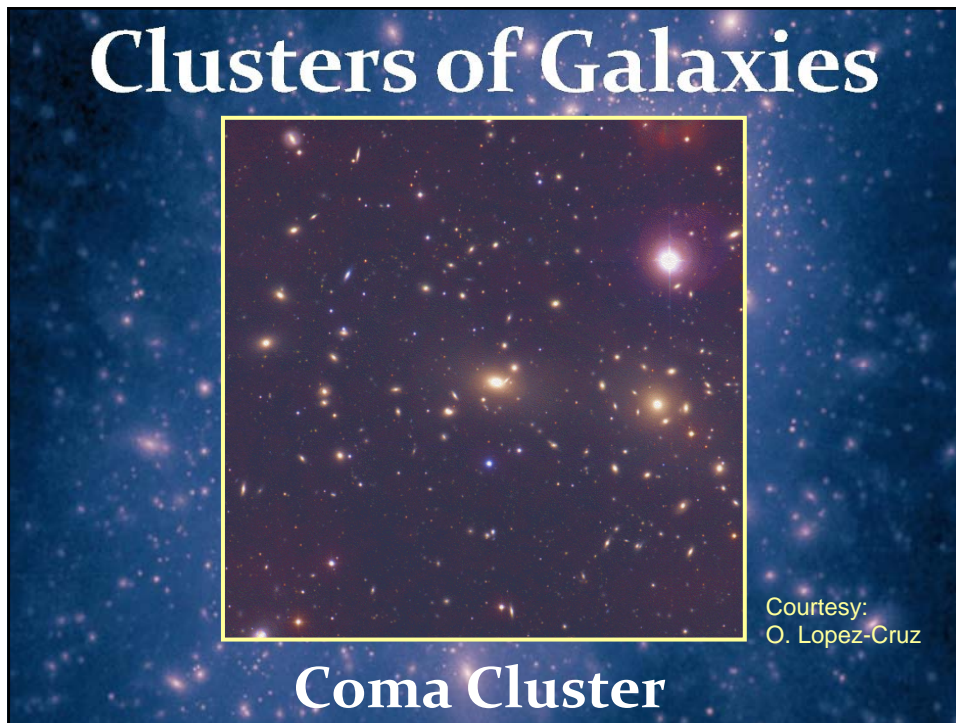
Local Universe: step by step





Clusters of Galaxies

- Assemblies of up to 1000's of galaxies within a radius of only
$$R \sim 1.5-2h^{-1} \text{ Mpc},$$
- Total masses:
$$M \sim 10^{14} M_{\odot}$$
- Representing overdensities of $\Delta \sim 1000$
- Galaxy move around with velocities
$$v \sim 1000 \text{ km/s}$$
- They are the most massive, and most recently, fully collapsed structures in our Universe.



Studying Clusters

Includes many different aspects of these versatile astrophysical laboratories:

- **Optical/Infrared/Ultraviolet**
 - Galaxy Population:
 - spatial distribution, kinematics, galaxy morphology
- **X-ray observations**
 - (hot, ionized) intracluster gas
 - distribution (density, temperature): cluster mass
 - abundances heavy elements (enrichment)
- **Sunyaev-Zel'dovich effect:**
 - "cluster shadows" in cosmic microwave background radiation
 - CMB microwave wavelength region
 - intracluster gas (pressure)
 - peculiar motion cluster (kinematic SZ)
- **Gravitational Lensing**
 - mainly optical, also radio, submm, ...
 - strong lensing (arcs, rings), weak lensing (sheared images)
 - dark matter mass
 - dark matter distribution
- **Radio wavelengths**
 - radio halos, radio relics
 - synchrotron radiation in shocked, hot, ionized intracluster plasma



Clusters of Galaxies

- Clusters not only contain galaxies:
- in fact, galaxies & stars are a minor component:

I. Clusters are Halos of Dark Matter:

$$M_{\text{DM}}/M_{\text{total}} \sim 82\%$$

II. Clusters are Hot Balls of (highly ionized) Gas

$$M_{\text{ICM}}/M_{\text{total}} \sim 16-17\%$$

III. Galaxies are mainly raisins in a sea of dark matter & hot gas

$$M_{\text{stars}}/M_{\text{total}} \sim 2\%$$

Clusters of Galaxies: X-ray intracluster gas

Baryonic matter in clusters is not only confined to galaxies:

~ 2 to 5 times more baryonic mass in the form of a **diffuse hot X-ray emitting**

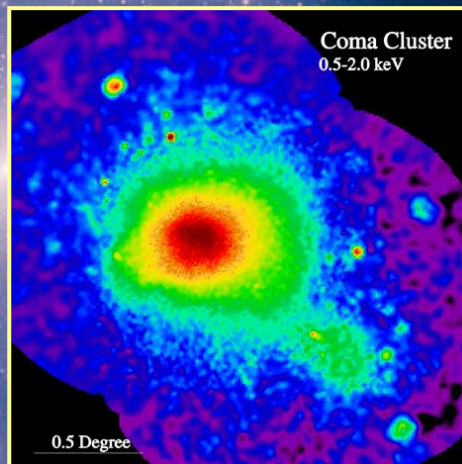
Intracluster Gas,

trapped and heated to a temperature of the order of

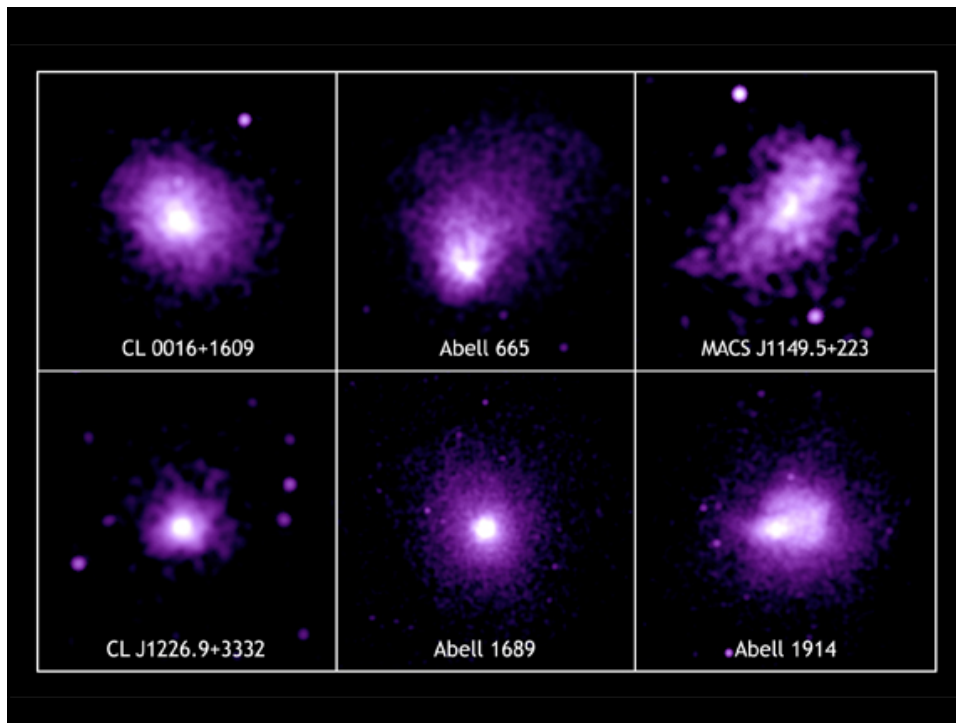
$$T \sim 10^8 \text{ K}$$

by the gravitational potential of the cluster.

At such high temperatures, this gas is a fully ionized plasma, producing powerful X-ray emission, bremsstrahlung radiation induced by the electron-ion interactions.



ROSAT X-ray image Coma Cluster



Cluster Mass: X-ray intracluster gas

Hydrostatic Equilibrium:

$$\frac{GM(r)}{r^2} = -\frac{k_B T}{\mu m_H} \left[\frac{d \log \rho}{dr} + \frac{d \log T}{dr} \right]$$

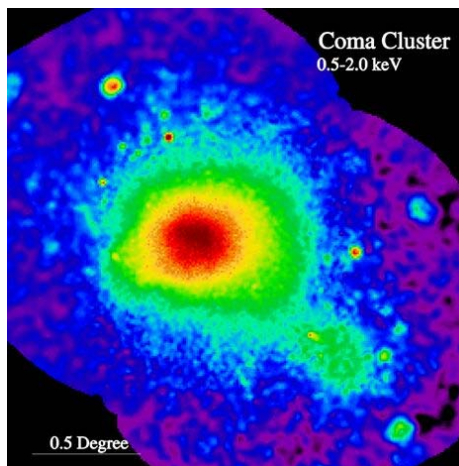
Determination Mass from X-ray observations:

-assumption:

 Isothermal: $T(r) = T_0$

-density profile:

 X-ray emission Bremsstrahlung: $L(r) \sim \rho(r)^2$



ROSAT X-ray image Coma Cluster

Clusters of Galaxies: Gravitational Lenses

A highly promising method to determine the amount and distribution of

matter in the Universe

looks at the way it affects

the trajectories of photons

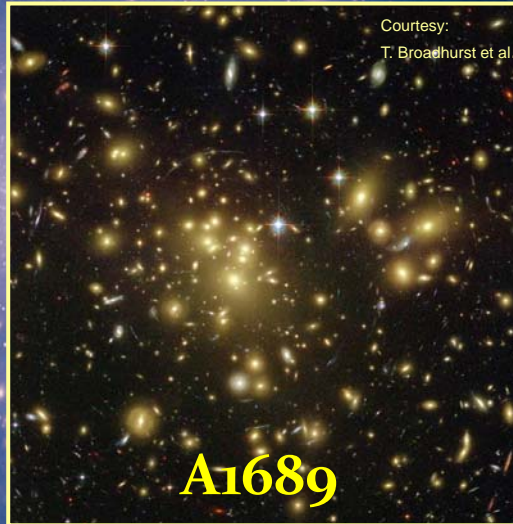
According to

Einstein's theory of

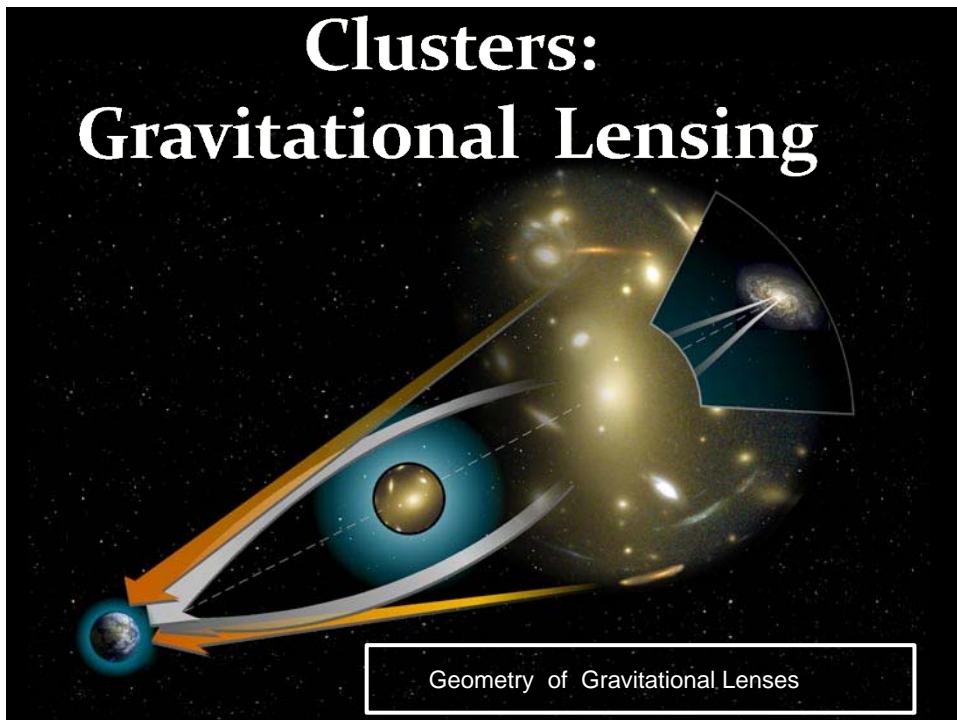
General Relativity,

gravitational potential wells will bend and focus light. Dark matter concentrations act as a

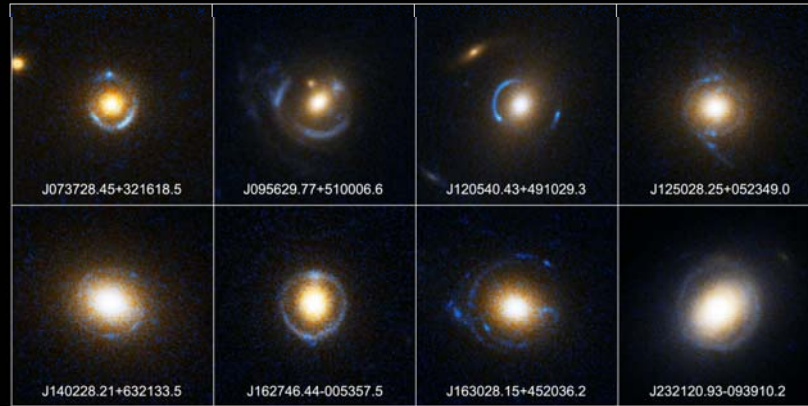
Gravitational Lens



Clusters: Gravitational Lensing



Gravitational Lensing: Einstein Ring



Einstein Ring Gravitational Lenses
Hubble Space Telescope • Advanced Camera for Surveys

NASA, ESA, A. Bolton (Harvard-Smithsonian CfA), and the SLACS Team

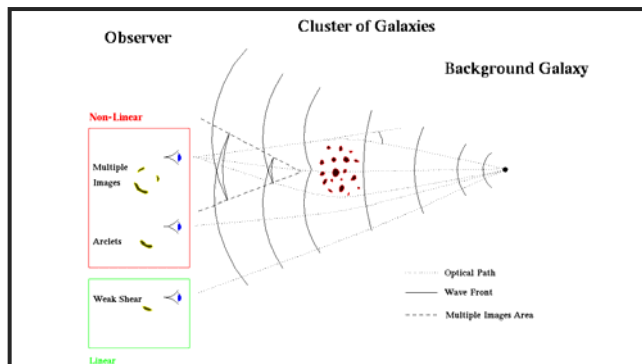
STScI-PRC05-32

Gravitational Telescopes: Weak vs. Strong Lensing

$$\theta_E = \sqrt{\frac{4GM}{c^2} \frac{d_{LS}}{d_L d_S}}$$

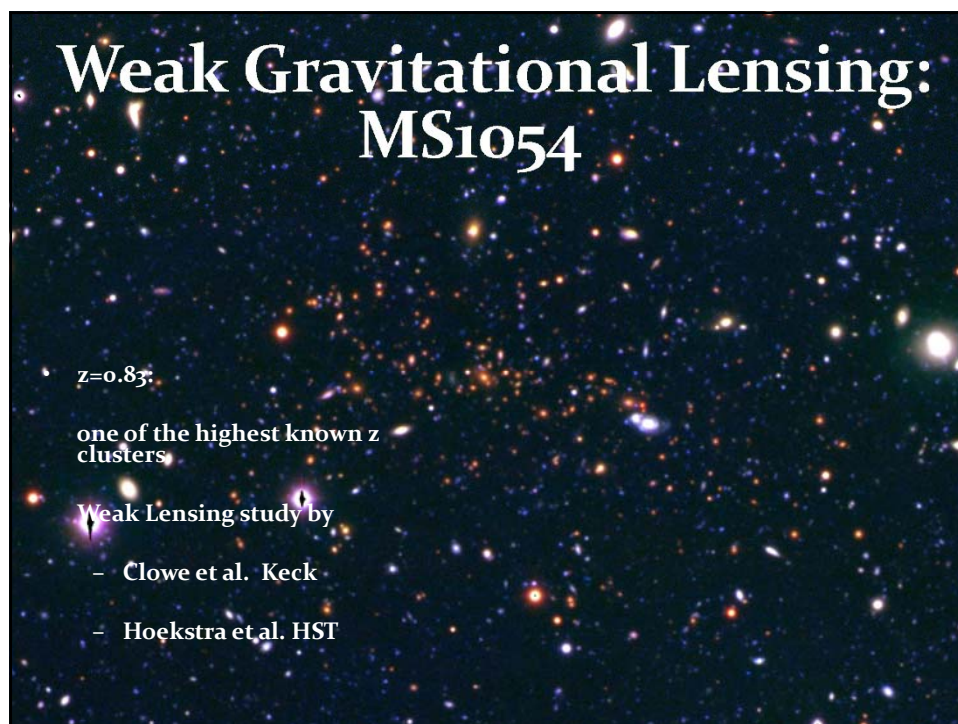
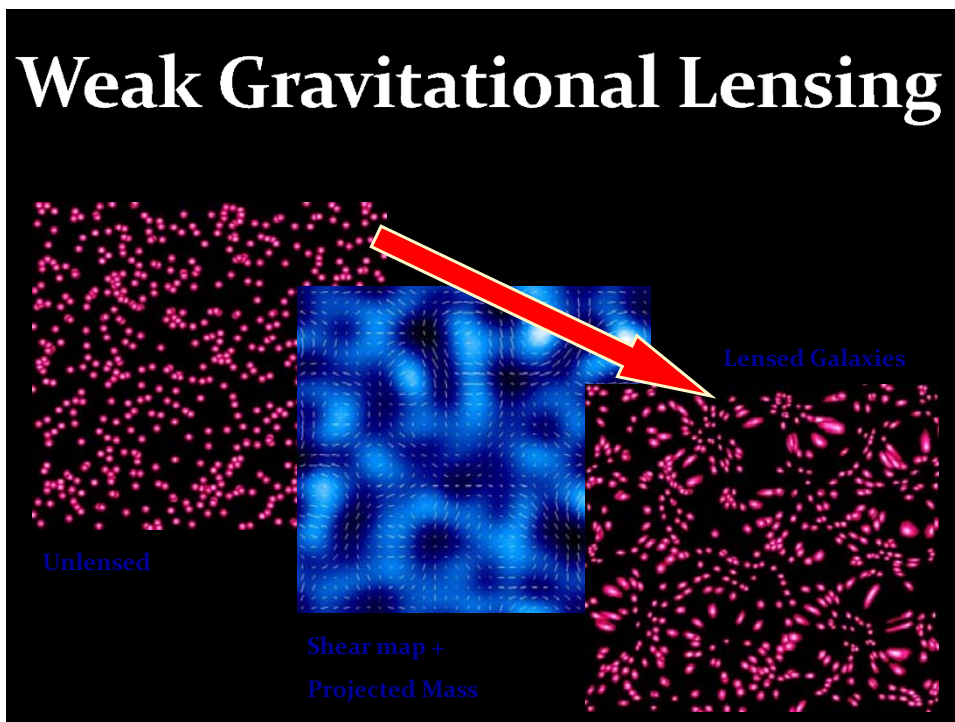
Two kinds of lensing:

- **Strong Lensing:**
 $\theta < \theta_E$
 - nonlinear distortions
 - multiple image
- **Weak Lensing:**
 $\theta > \theta_E$
 - linear distortions
 - sheared images



Cluster Mass determination:

- | | |
|-----------------|---|
| Weak Lensing: | Linear Inversion Distortion Field |
| Strong Lensing: | Complex Modeling density distribution.
non-trivial |



Clusters of Galaxies: Dark Matter Map

A highly promising method to determine the amount and distribution of

matter in the Universe

looks at the way it affects

the trajectories of photons.

According to

Einstein's theory of

General Relativity,

gravitational potential wells will bend and focus light. Dark matter concentrations act as a

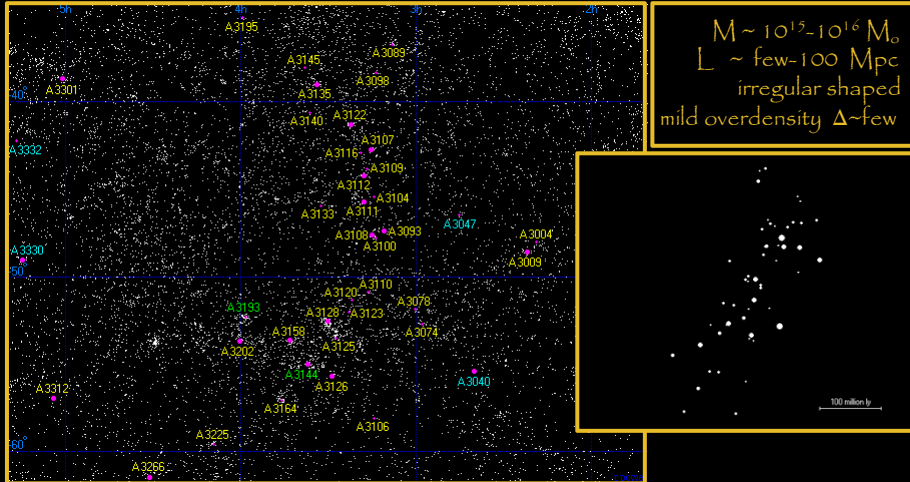
Gravitational Lens.



Superclusters

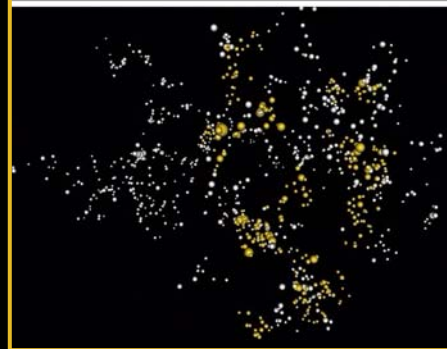
Superclusters

Large groups of clusters & galaxies (1-dozens)

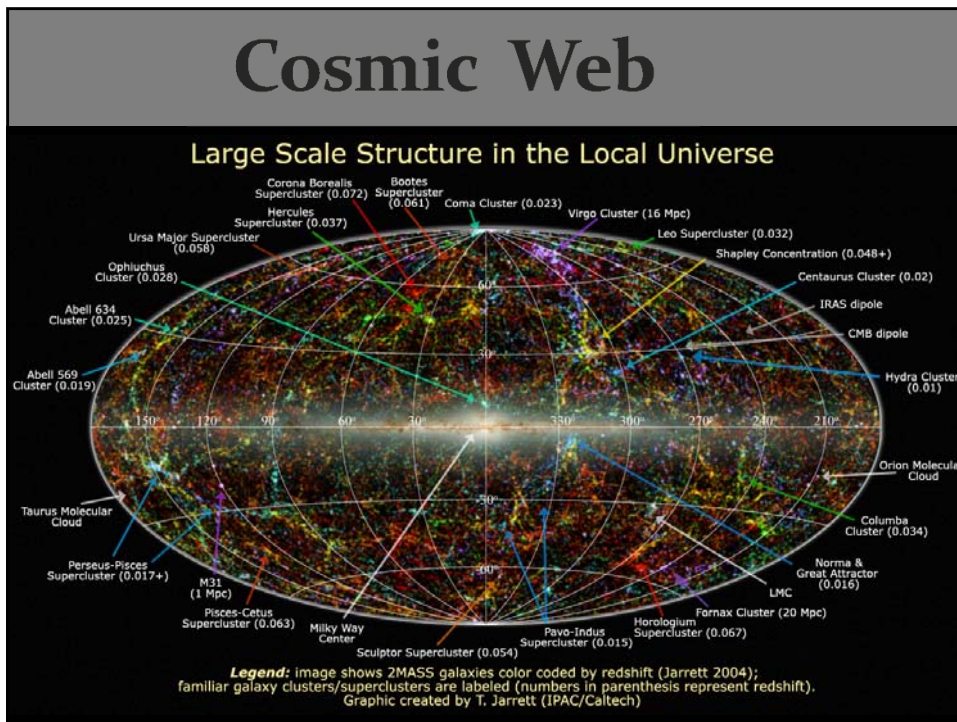


Superclusters:

Einasto et al. sample
X-ray clusters (yellow) and
Abell clusters (white)



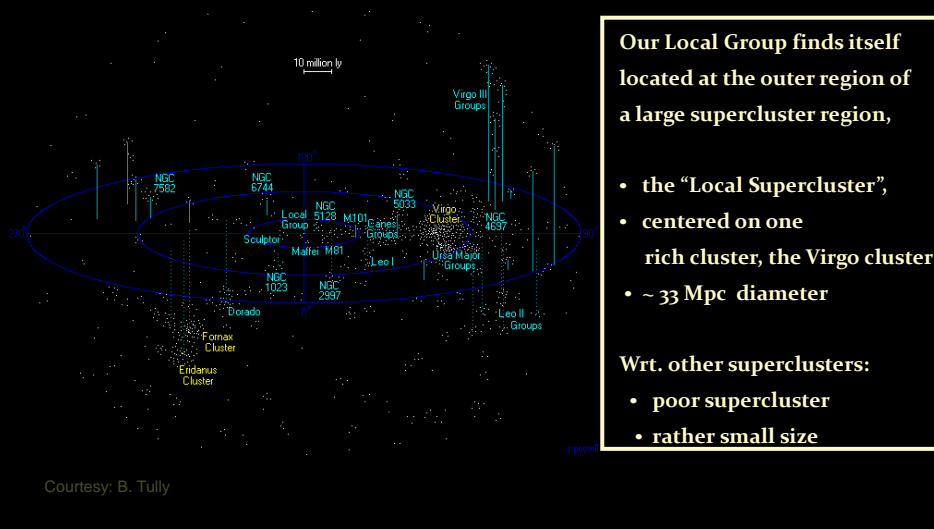
superclusters are not isolated single objects,
but integral components in the pervasive
Cosmic Web



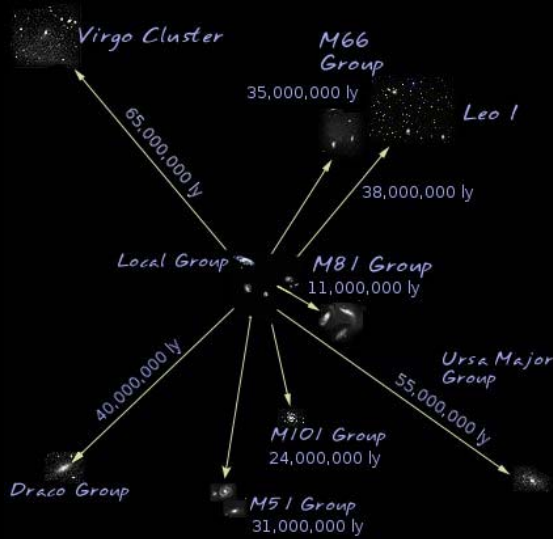
Local Supercluster

our cosmic province

Local Supercluster



Local Supercluster



Local Supercluster:

contains:

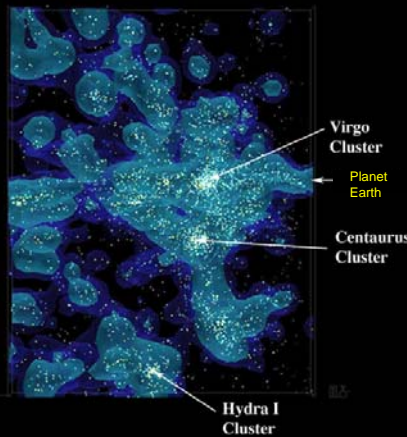
- ~ 100 galaxy groups
- 1 rich cluster - Virgo cluster

structure:

- Central Virgo cluster
- groups & galaxies connected via filamentary extensions
- Local Group:
 - outskirts Local Supercluster, on filament extending from Fornax cluster - Virgo cluster

Local Supercluster

End-on View of the Local Supercluster:



150 million light years wide x 190 million light years tall

Courtesy: B. Tully

Structure Local Supercluster:

2 components:

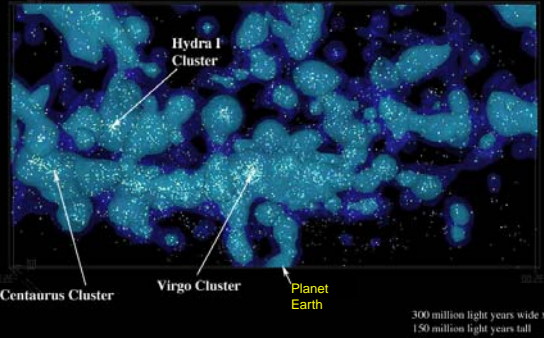
- flattened disk $\frac{2}{3}^{\text{rd}}$ galaxies
- spherical "halo" $\frac{1}{3}^{\text{rd}}$ galaxies

Disk:

- thin (~ 1 Mpc) disk,
- 1:6 - 1:9 flattened

Local Supercluster

Polar View of Local Supercluster:



Local Supercluster:

Mass (DM): $M \sim 1 \times 10^{15} M_{\odot}$

Luminosity: $L \sim 3 \times 10^{12} L_{\odot}$

M/L ~ 300

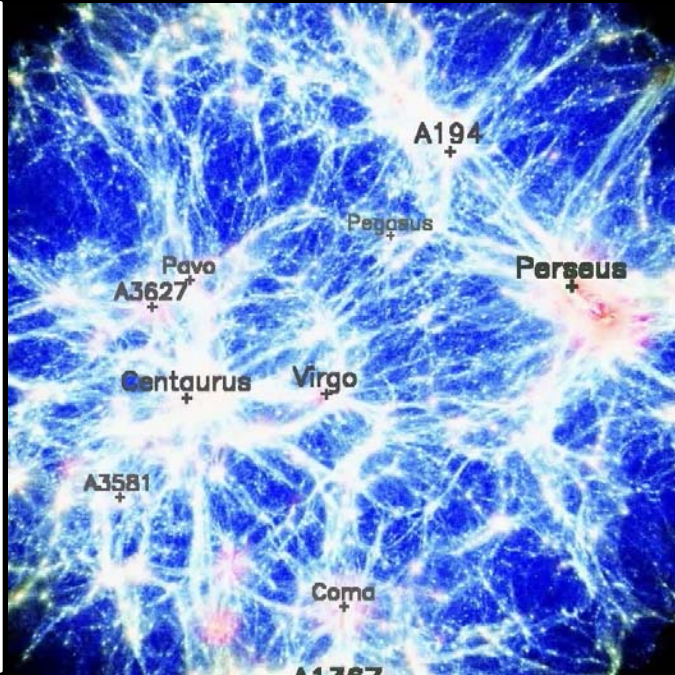
Courtesy: B. Tully

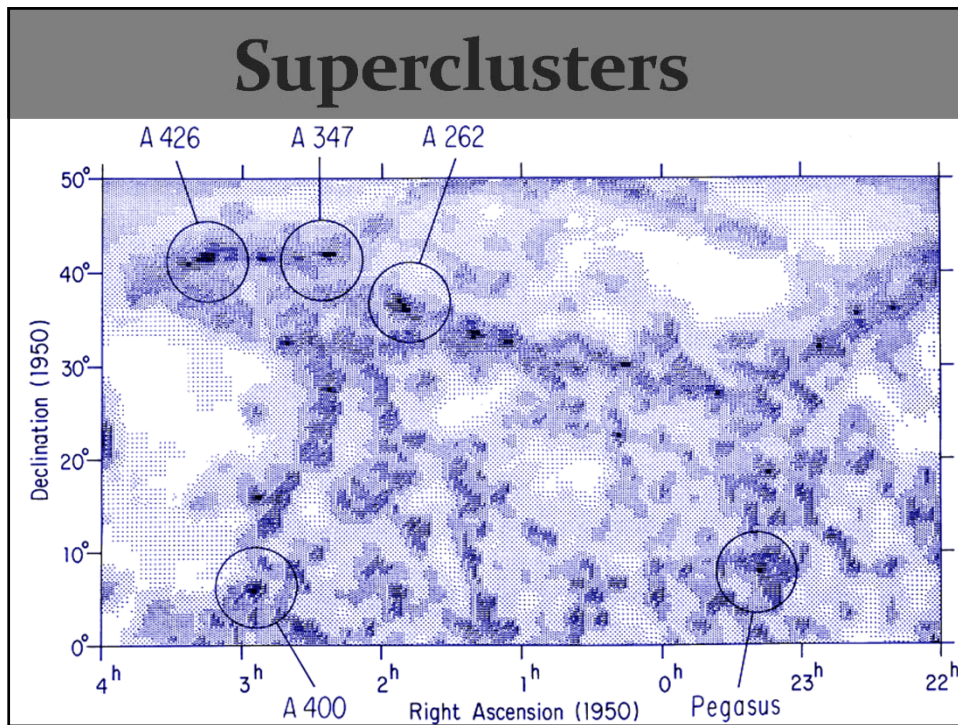
Local Universe:

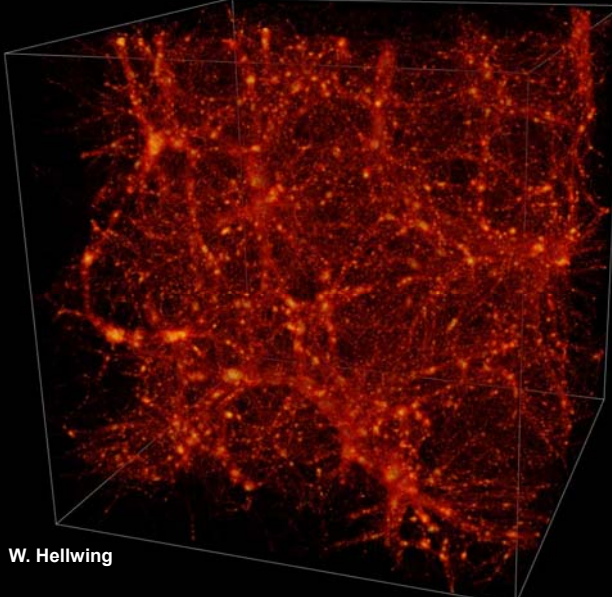
Constrained Simulation

Gas Distribution

courtesy:
Klaus Dolag







Stochastic Spatial Pattern of

- Clusters,
- Filaments &
- Walls

around

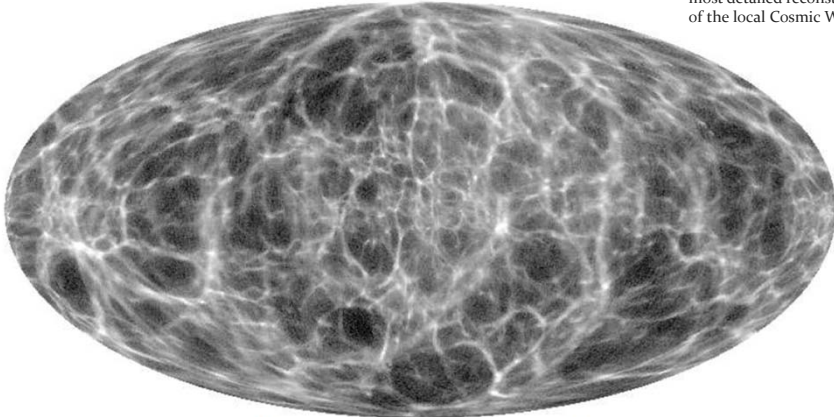
- Voids

in which matter & galaxies have agglomerated through gravity

W. Hellwing

The Cosmic Web

local Cosmic Web: 2MRS



most detailed reconstruction of the local Cosmic Web

1.0 ————— 6.0

Courtesy: Francisco Kitaura

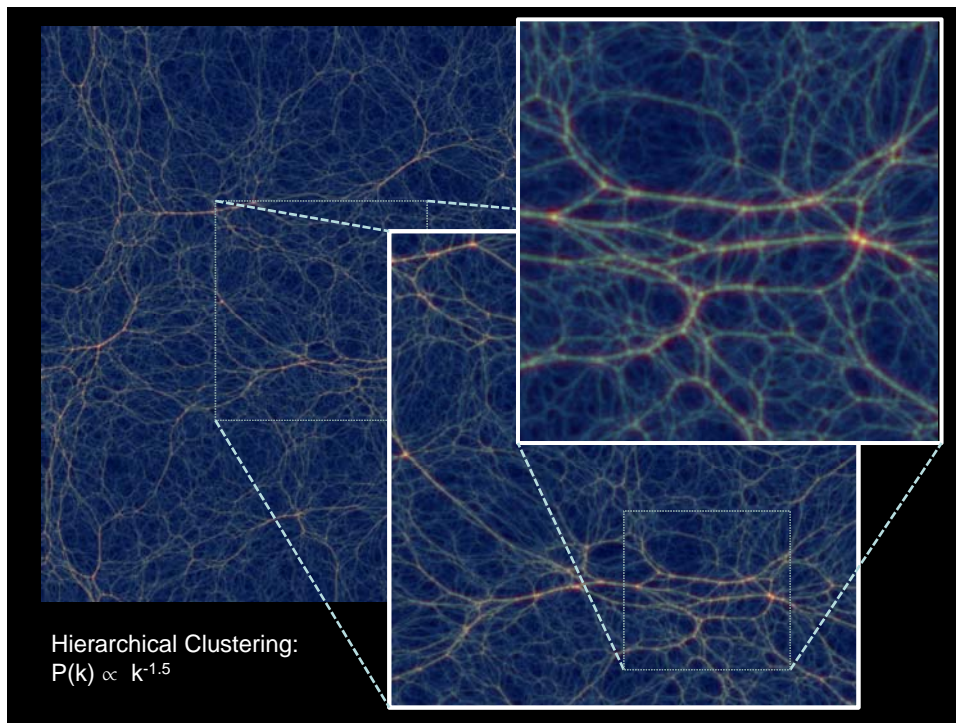
The Cosmic Web

Physical Significance:

- **Manifestation mildly nonlinear clustering:**
Transition stage between linear phase
and fully collapsed/virialized objects
- **Weblike configurations contain cosmological information:**
eg. Void shapes & Alignments
- **Cosmic environment within which to understand the formation of galaxies.**

Cosmic Web Characteristics

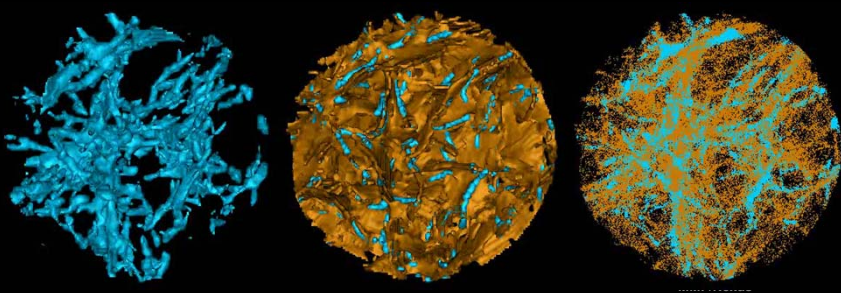
- **anisotropic structure:**
 - filaments dominant structural feature - elongated
 - sheets/walls - flattened
- **multiscale nature**
 - structure on wide range of scales
 - structures have wide range of densities
- **overdense-underdense asymmetry**
 - voids: underdense, large & roundish
 - filaments & walls: overdense, flattened/elongated
 - clusters: dense, massive & compact nodes
- **complex spatial connectivity**
 - all structural features connected in a complex, multiscale weblike network



the Cosmic Network:

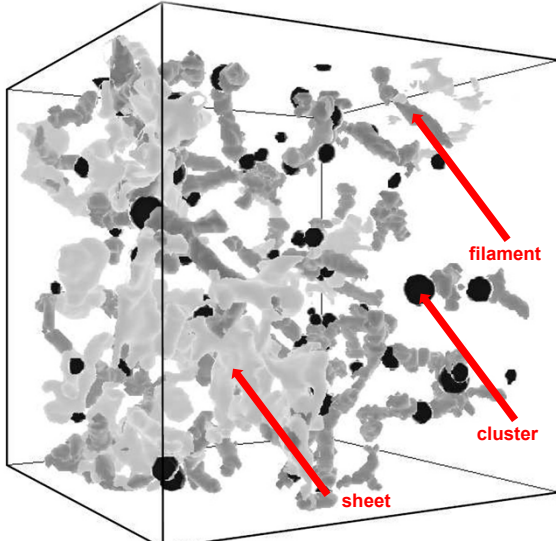
weaving the cosmic tapestry

Nexus/MMF



Cautun et al. 2013, 2014

<p style="text-align: center;">Stochastic Spatial Pattern</p> <ul style="list-style-type: none">• Clusters,• Filaments &• Walls <p style="text-align: center;">around</p> <ul style="list-style-type: none">• Voids	<p style="text-align: center;">in which matter & galaxies</p> <p style="text-align: center;">have agglomerated</p> <p style="text-align: center;">through gravity</p>
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Nexus/MMF Cosmic Web Analysis

Nexus/MMF dissection
into
sheets, filaments, clusters
...

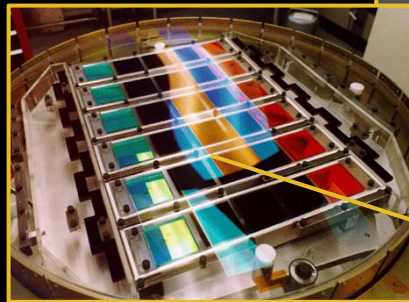
Aragon-Calvo et al. 2007

Mapping the Cosmic Web

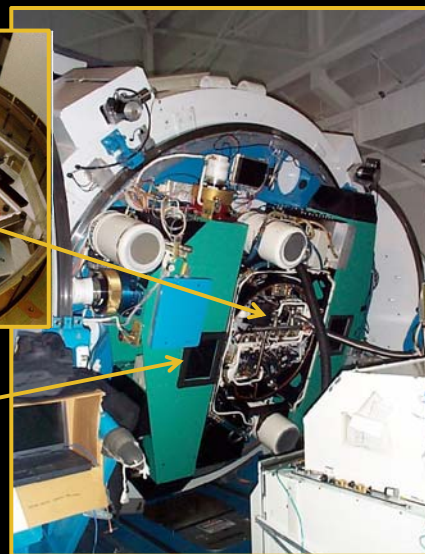
galaxy surveys

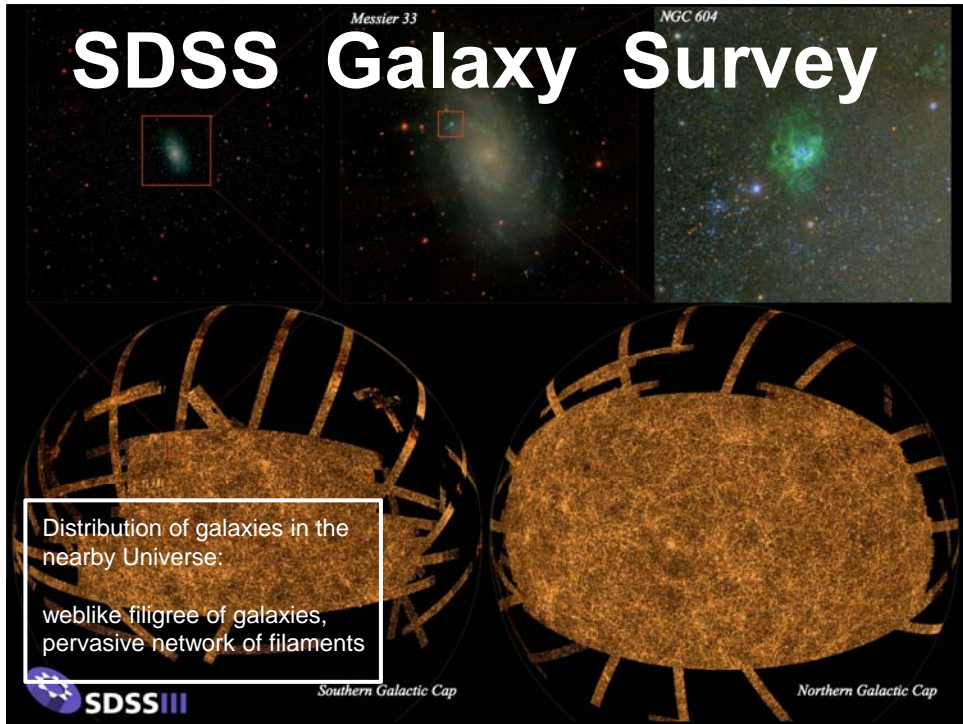
SDSS survey

5-color
Camera
30 CCD
chips

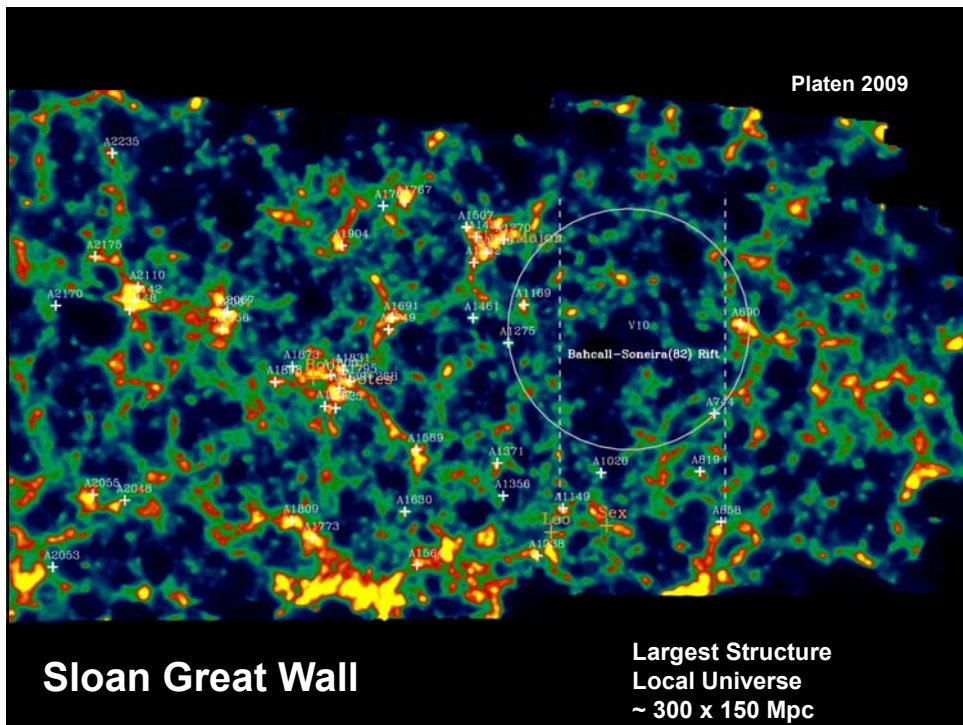
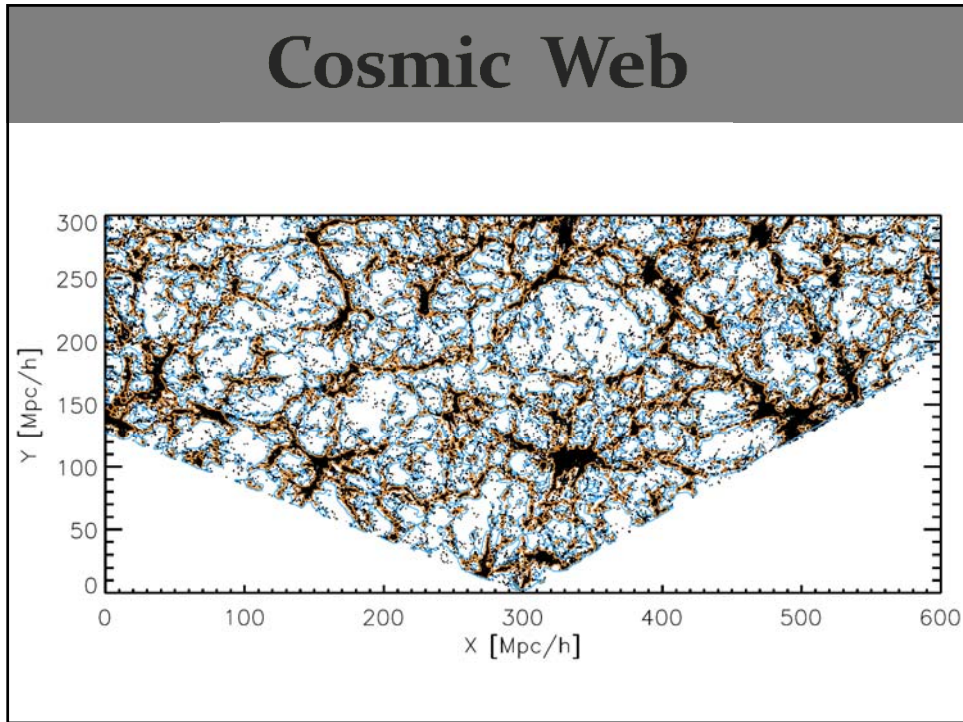


Fiber
Spectrograph

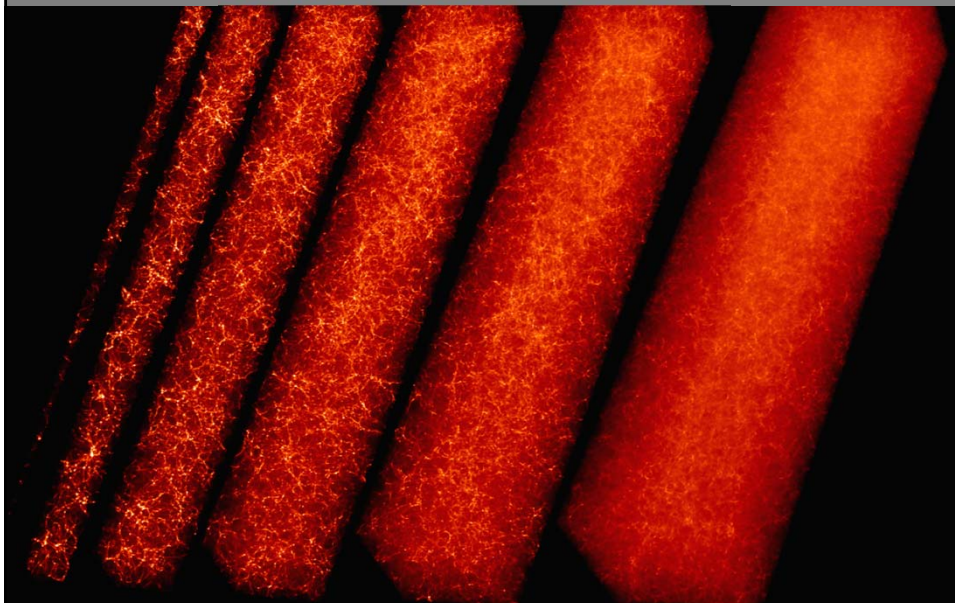




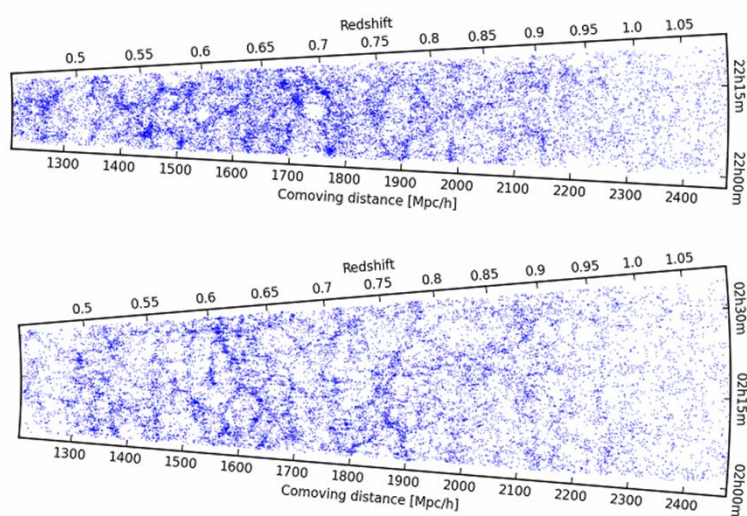




Cosmic Web

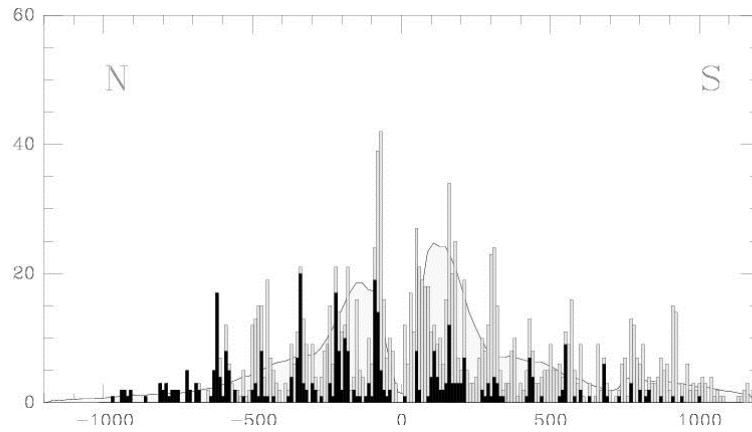


Cosmic Web at High z



VIPERS deep redshift survey, $z=0.4-1.2$ (Guzzo et al.)

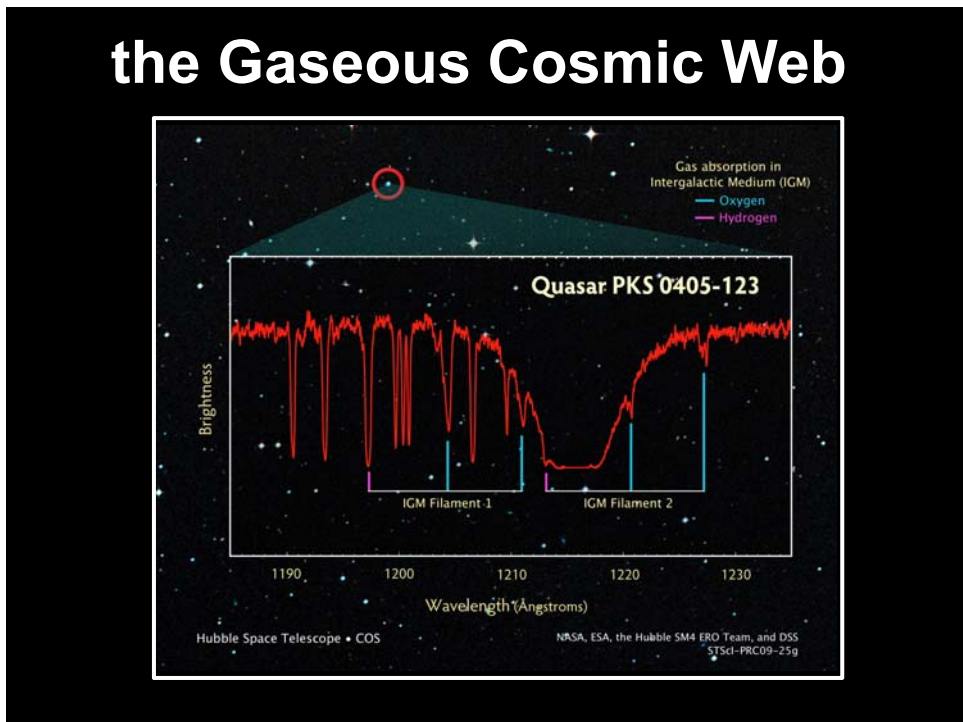
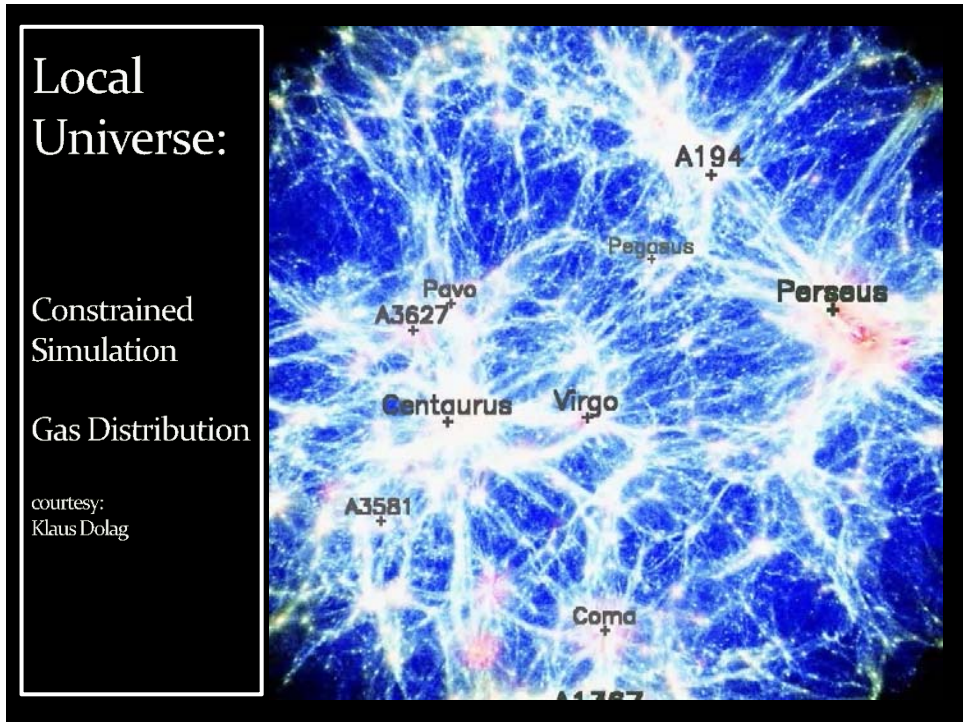
Cosmic Web at High z



Deep pencil beam survey (Broadhurst et al):

A semi-regular pattern of redshift spikes along line of sight, indicating the passage of l.o.s. through sheets, filaments and clusters. Suggestions for a characteristic scale of $\sim 120h^{-1} \text{Mpc}$ should be ascribed to the 1-D character of the redshift skewer through 3-D structure.

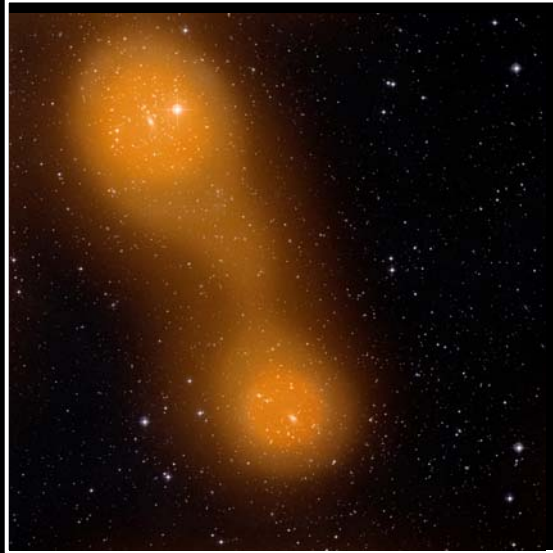
Cosmic Web: Gas & Dark Matter



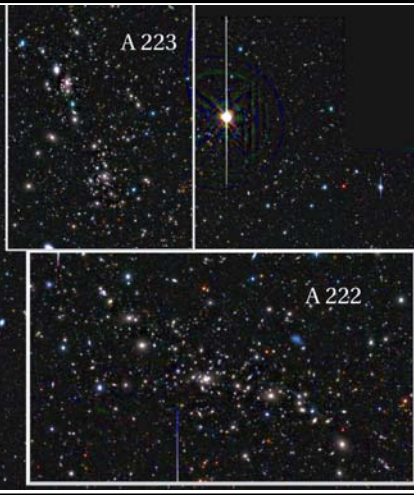
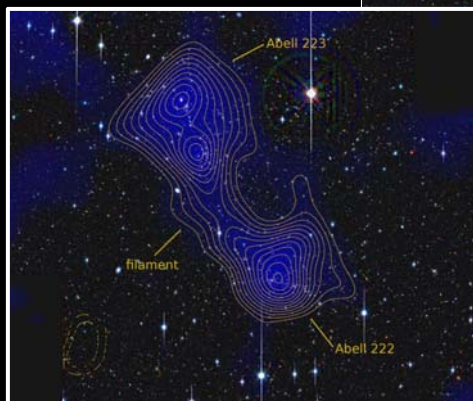
the Gaseous Cosmic Web

SZ detection of
Inter-cluster bridge/filament
in between clusters
A401 and A399

ESA/Planck collaboration



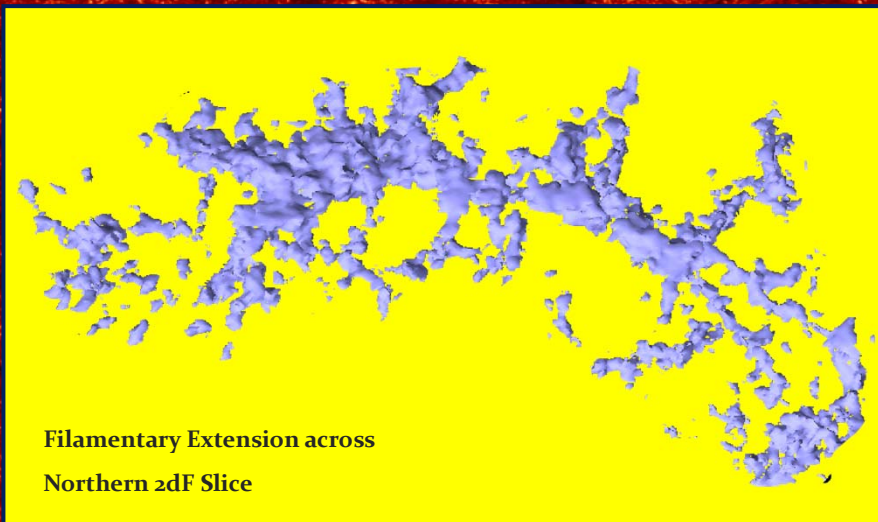
Dark Matter Cosmic Web



A222-A223
Dietrich et al. 2013

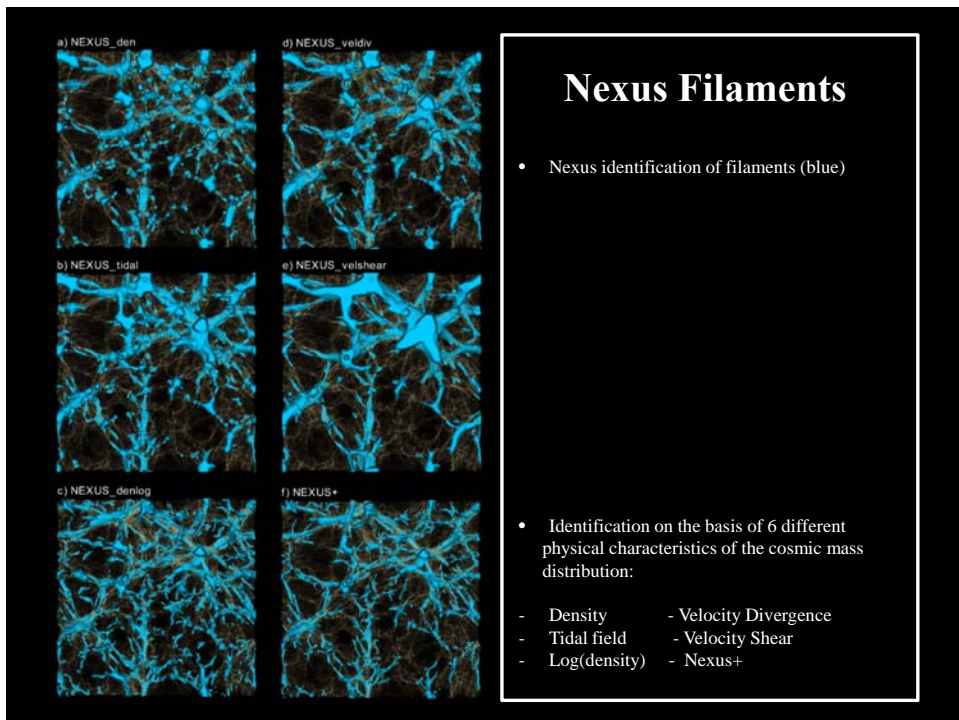
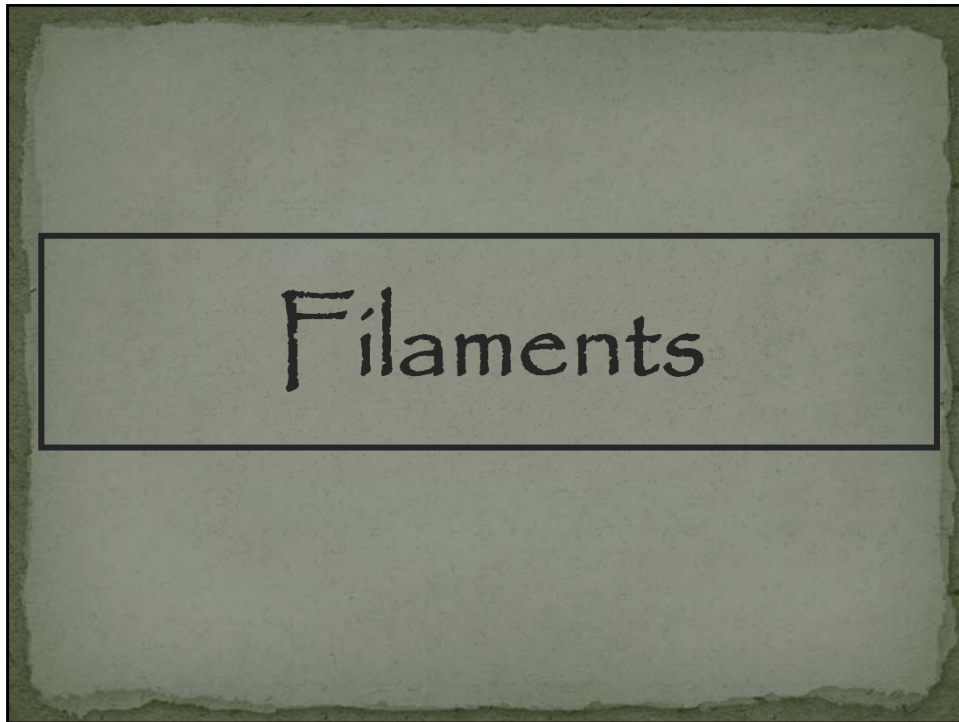
Cosmic Web: The Elements

Walls, Filaments & Nodes

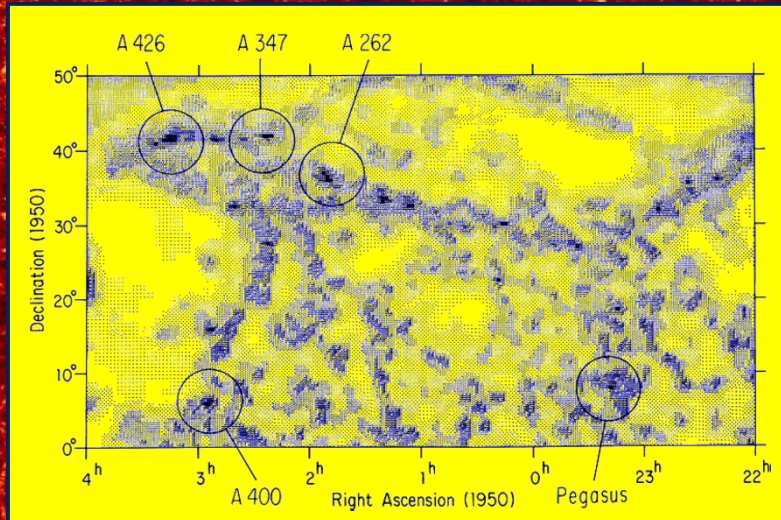


Filamentary Extension across
Northern 2dF Slice

DTFE rendering: W. Schaap



Pisces-Perseus Chain



21 cm line redshift survey,
Giovanelli & Haynes

Pisces-Perseus Chain

Canonic example of a strongly flattened supercluster consisting of

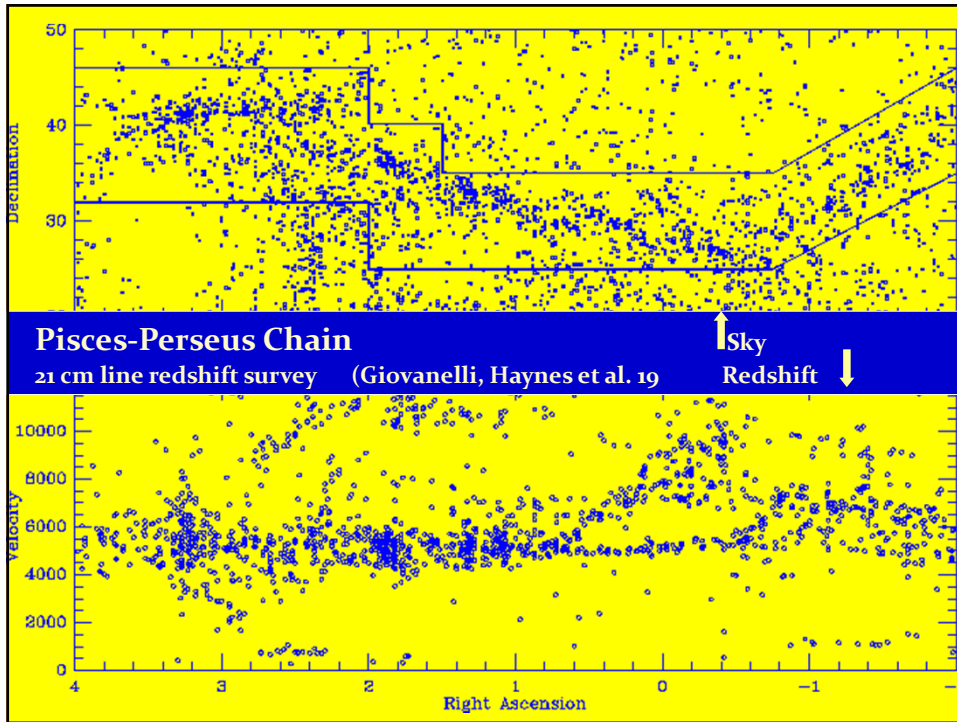
- sheet-like central region, dense filamentary boundary ridge
- Relative proximity ($d \sim 55h^{-1}$ Mpc),
- Characteristic & salient filamentary morphology,
- Favourable orientation.

Northern boundary: ridge south-westward of Perseus cluster (A426)

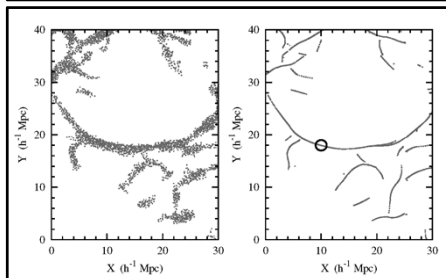
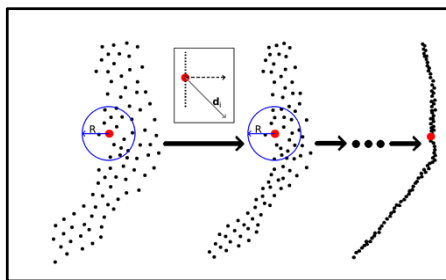
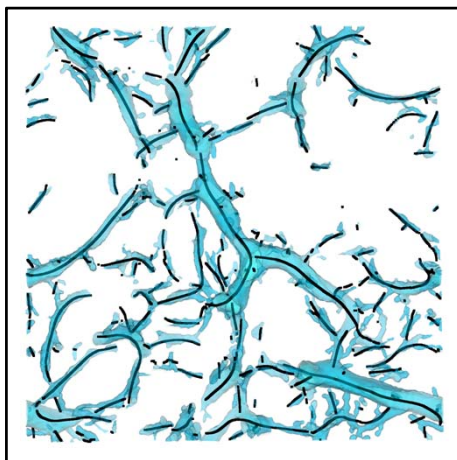
Dimensions Ridge: $5h^{-1}$ Mpc wide

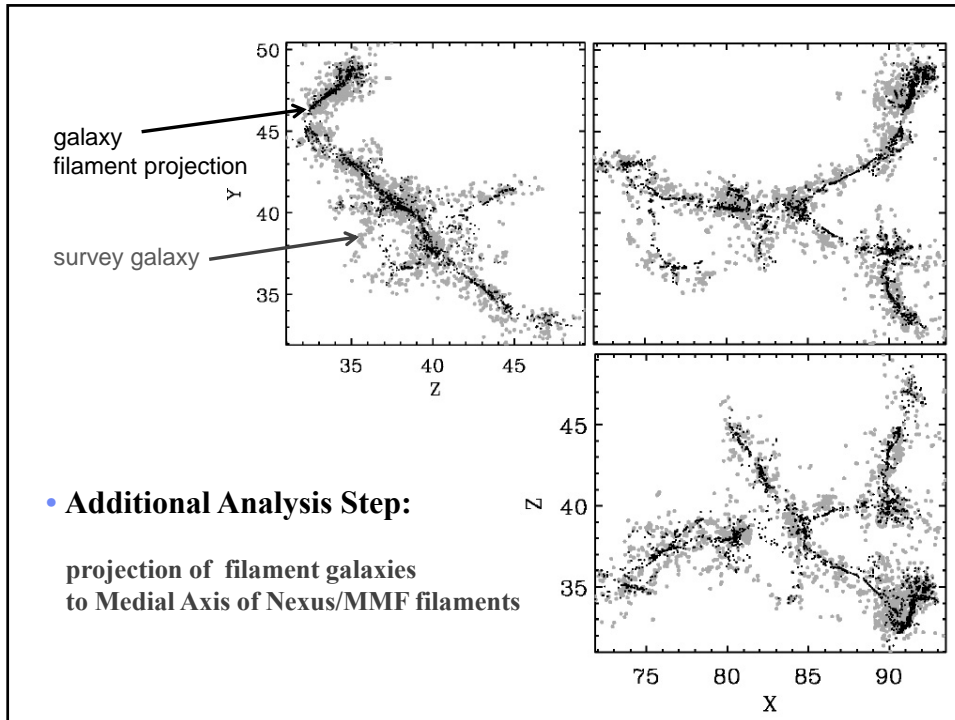
$50h^{-1}$ Mpc length; possible $140h^{-1}$ Mpc extension

Along Ridge: high density clusters, incl. A462, A347, A262

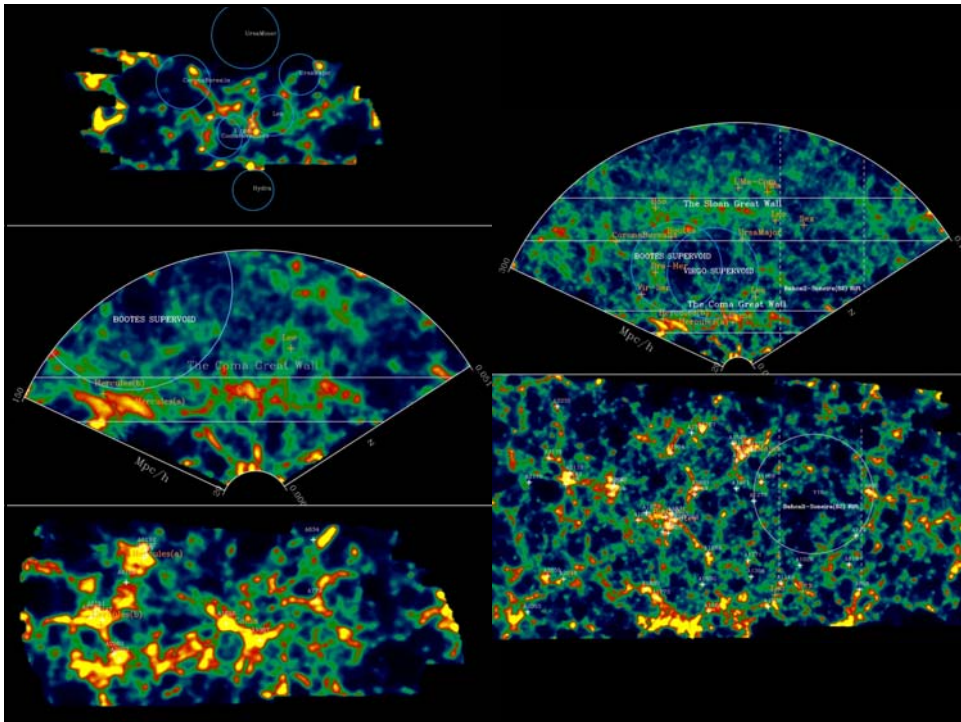
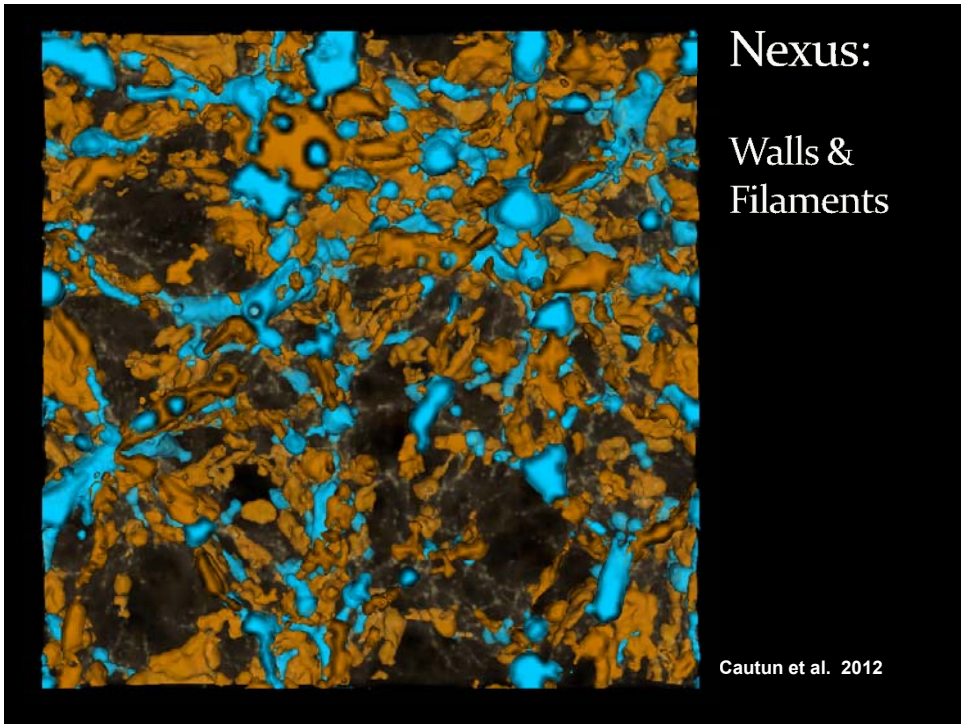


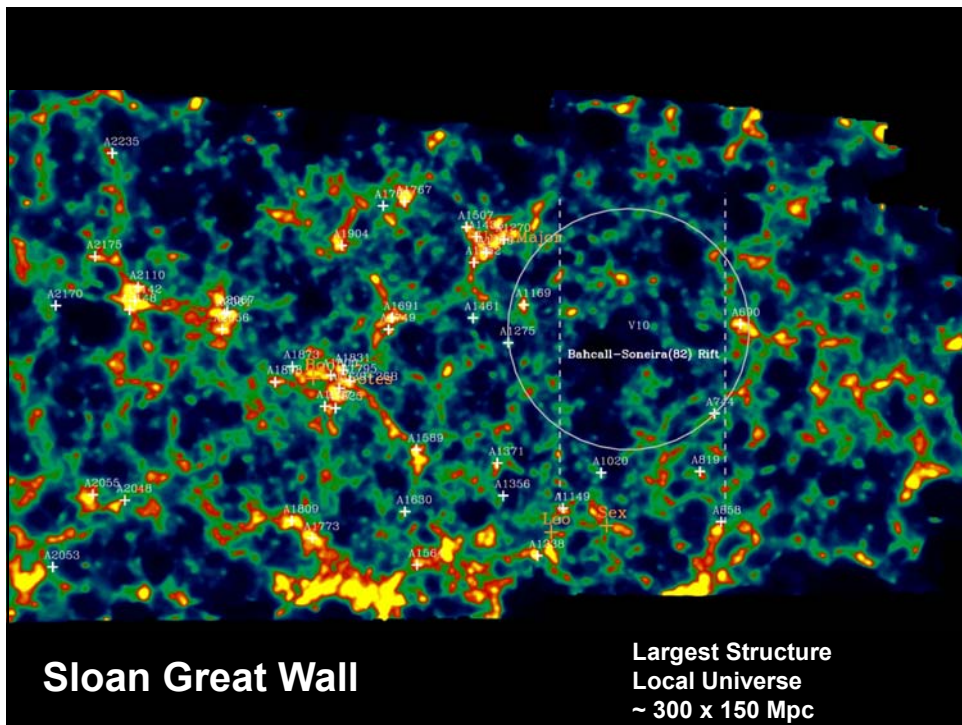
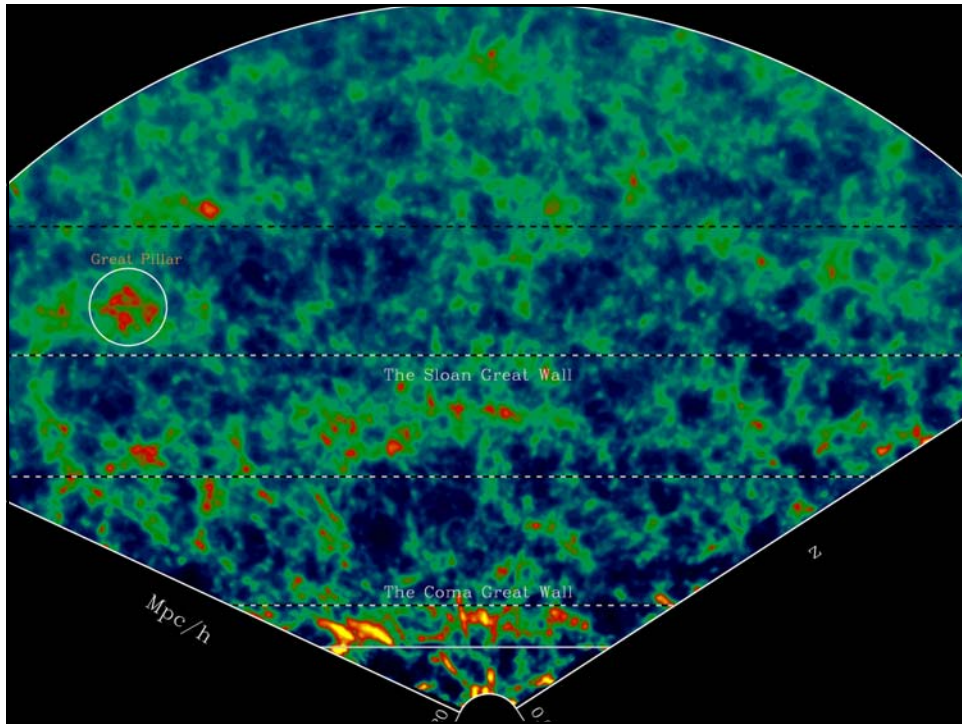
Spine of the Cosmic Web

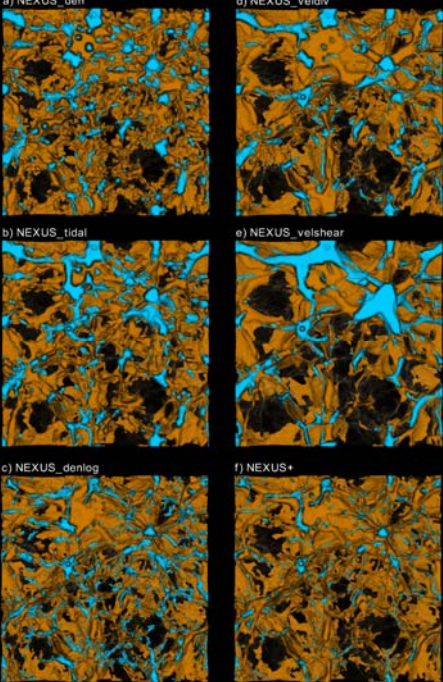




Walls - Sheets







a) NEXUS_den

d) NEXUS_veldiv

b) NEXUS_tidal

e) NEXUS_velshear

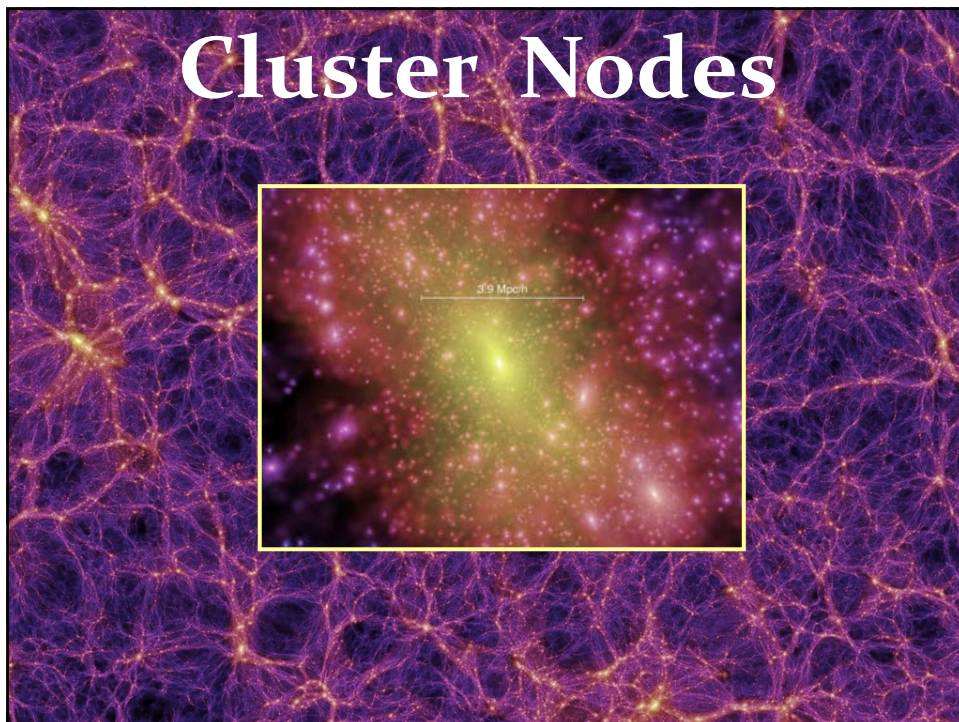
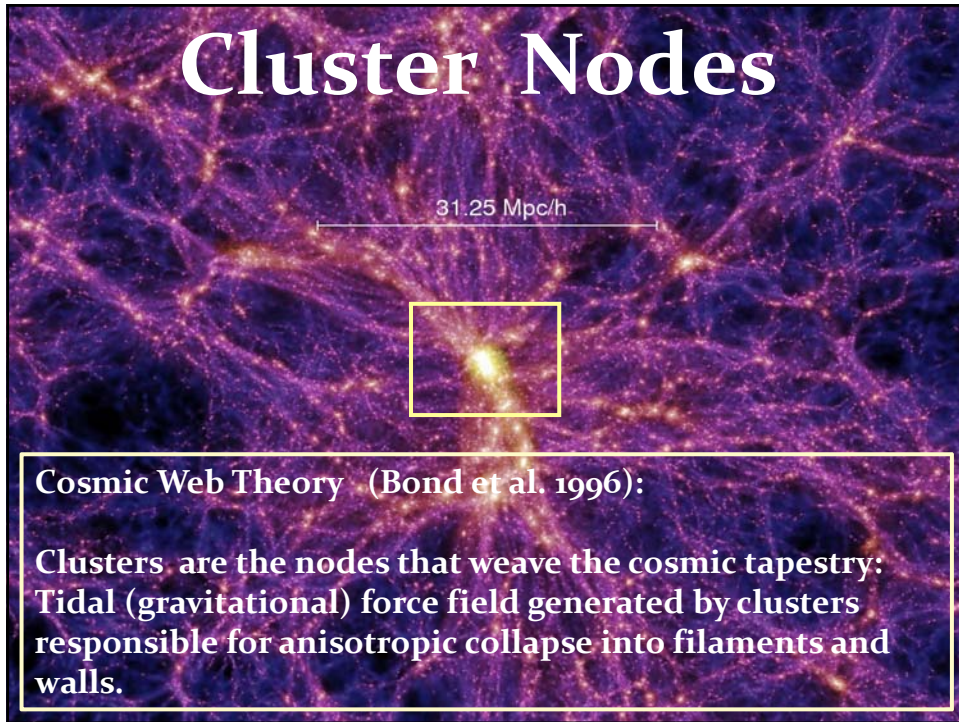
c) NEXUS_denlog

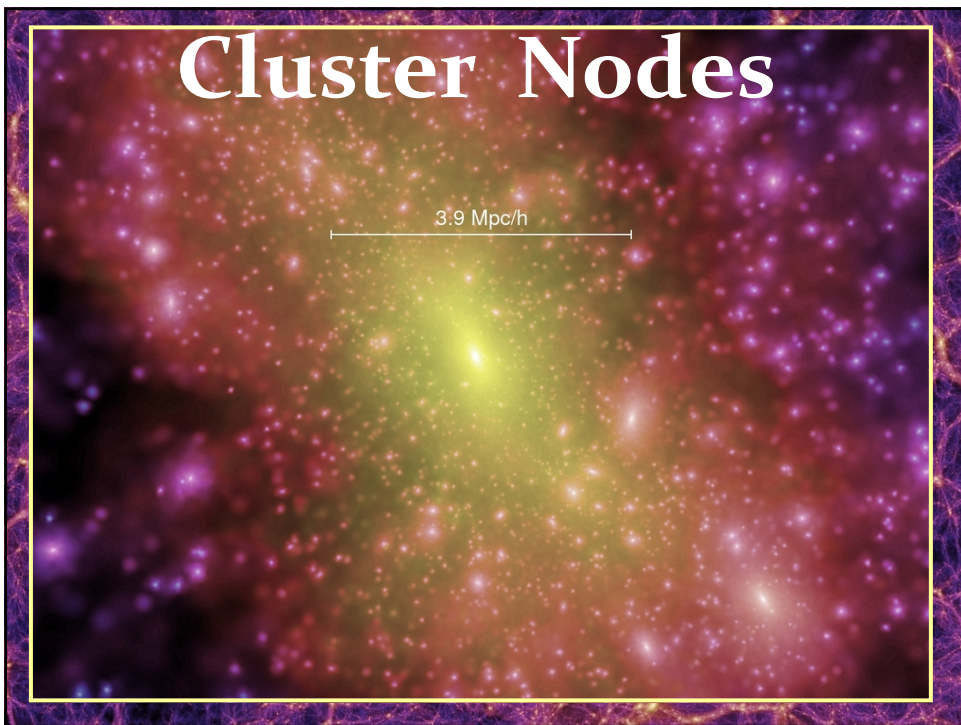
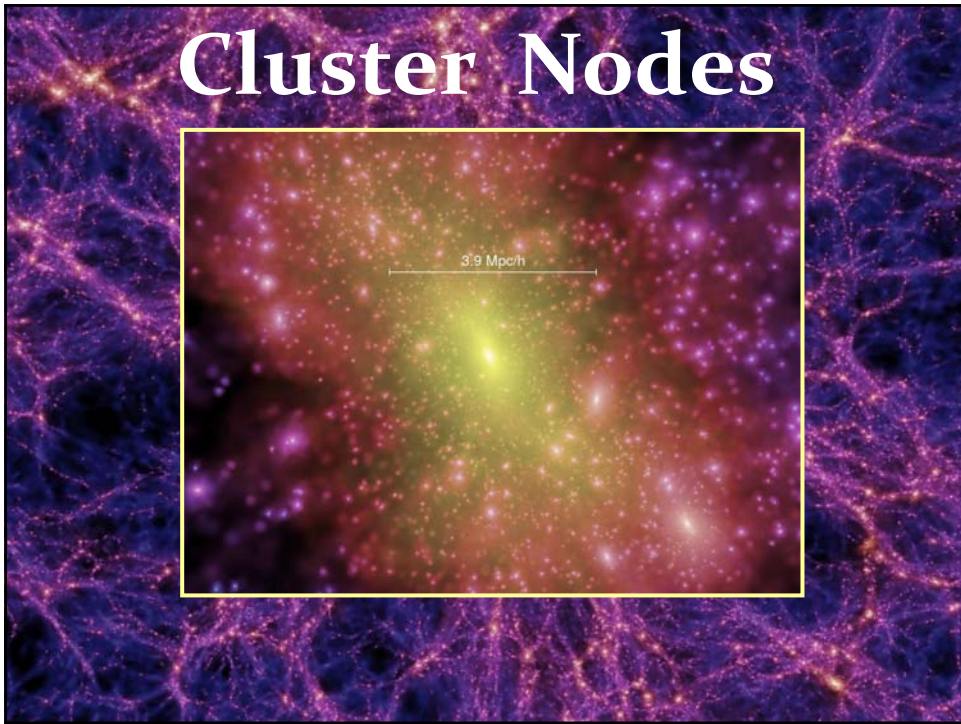
f) NEXUS+

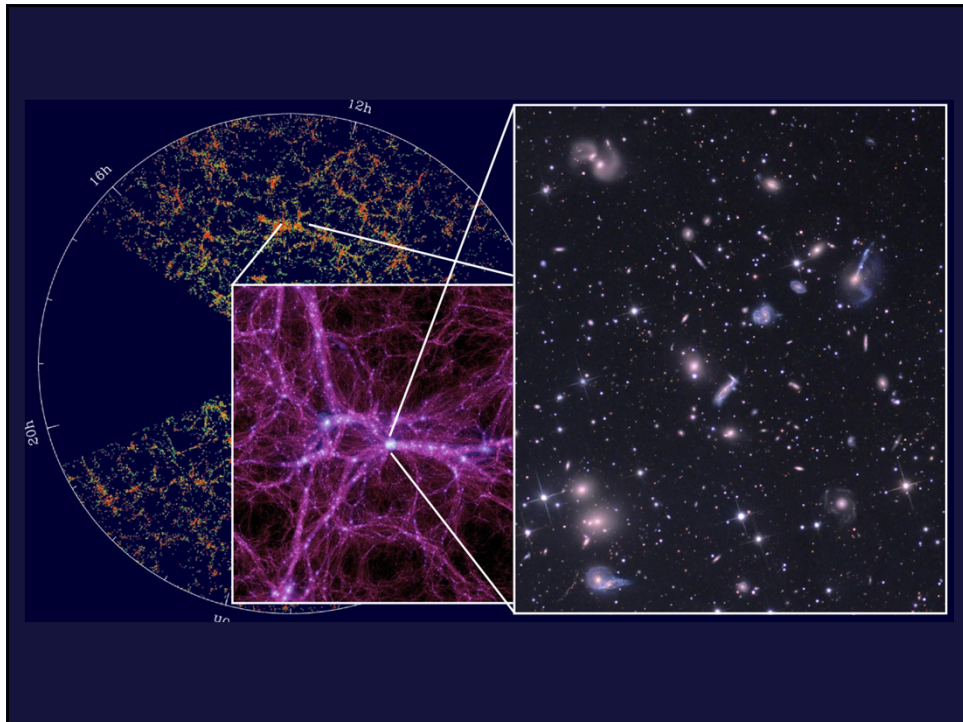
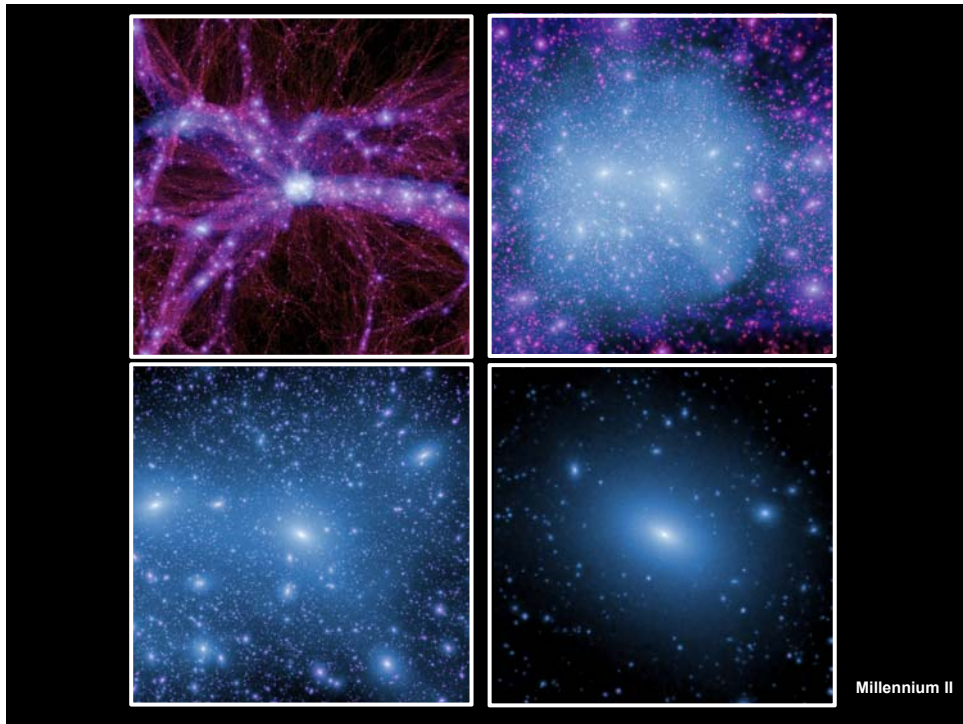
Nexus:
Multiscale Morphology
Identification
Cosmic Web Elements
Walls

Cautun et al. 2012

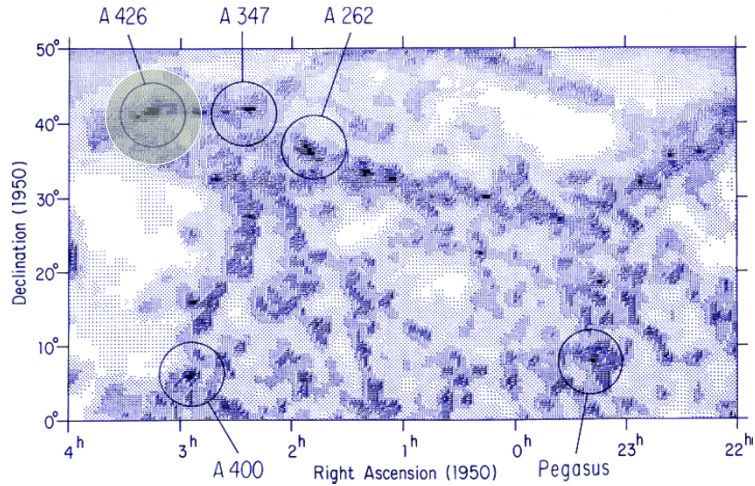
Cluster Nodes





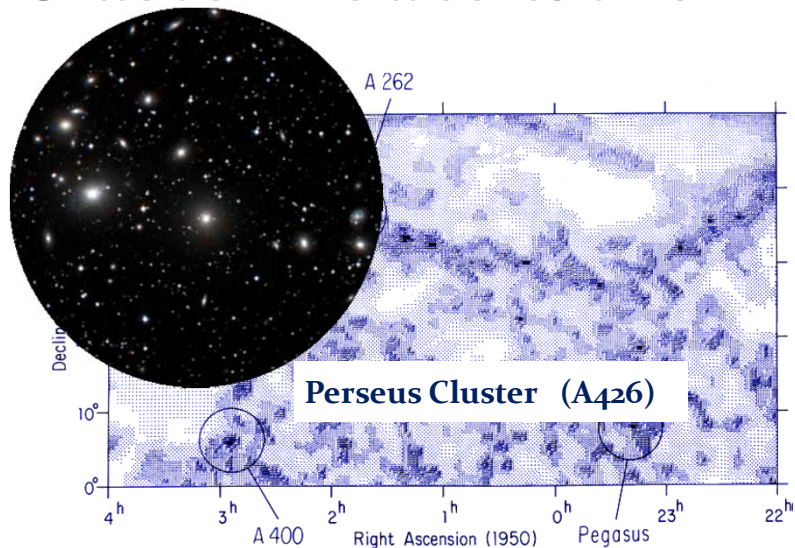


Cluster Nodes & the Web



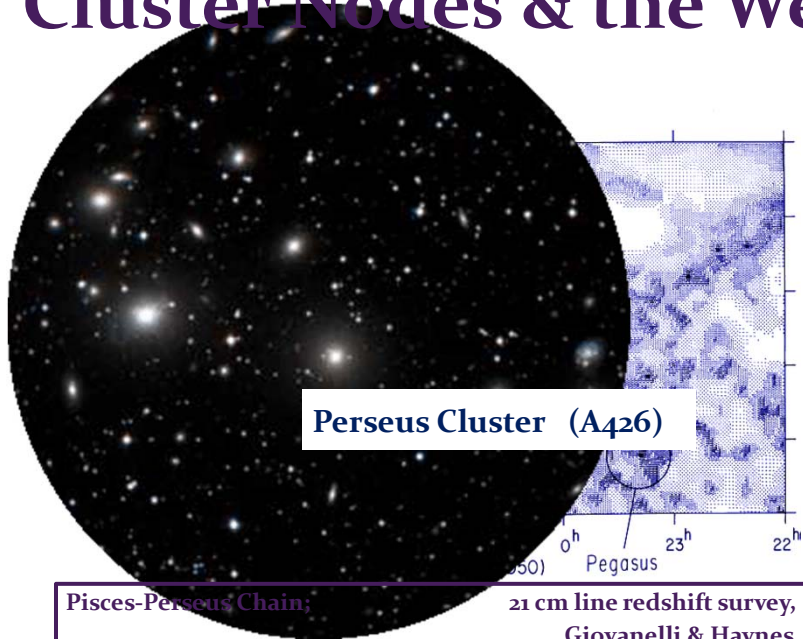
Pisces-Perseus Chain; 21 cm line redshift survey, Giovanelli & Haynes

Cluster Nodes & the Web



Pisces-Perseus Chain; 21 cm line redshift survey, Giovanelli & Haynes

Cluster Nodes & the Web



Voids

REVIEW ARTICLE

Giant voids in the Universe

Ya. B. Zeldovich*, J. Einasto^{†‡} & S. F. Shandarin*

* Institute of Applied Mathematics, Moscow A-47, 125047, USSR

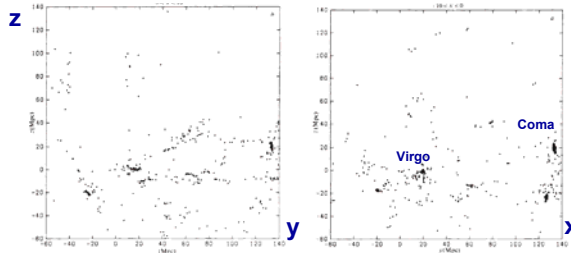
† Tartu Astrophysical Observatory, 202444 Estonia, USSR

‡ European Southern Observatory, 8046 Garching, FRG

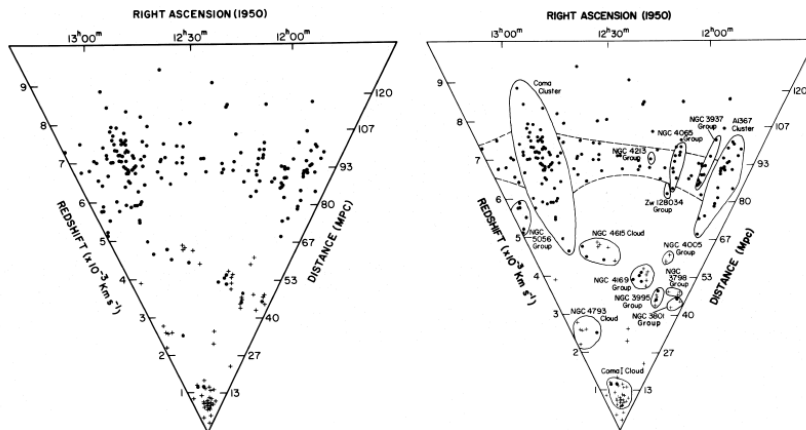
Recent observations indicate that most galaxies are concentrated in superclusters consisting of galaxies, and clusters of galaxies, aligned along strings. Giant volumes exist between superclusters which are almost empty of visible objects. Theories of galaxy formation predict the formation of non-spherical superclusters and giant voids. Large-scale structure changes very slowly, so the currently observed structure reflects the whole history of galaxy formation and structural evolution.

Zeldovich, Einasto & Shandarin 1982:

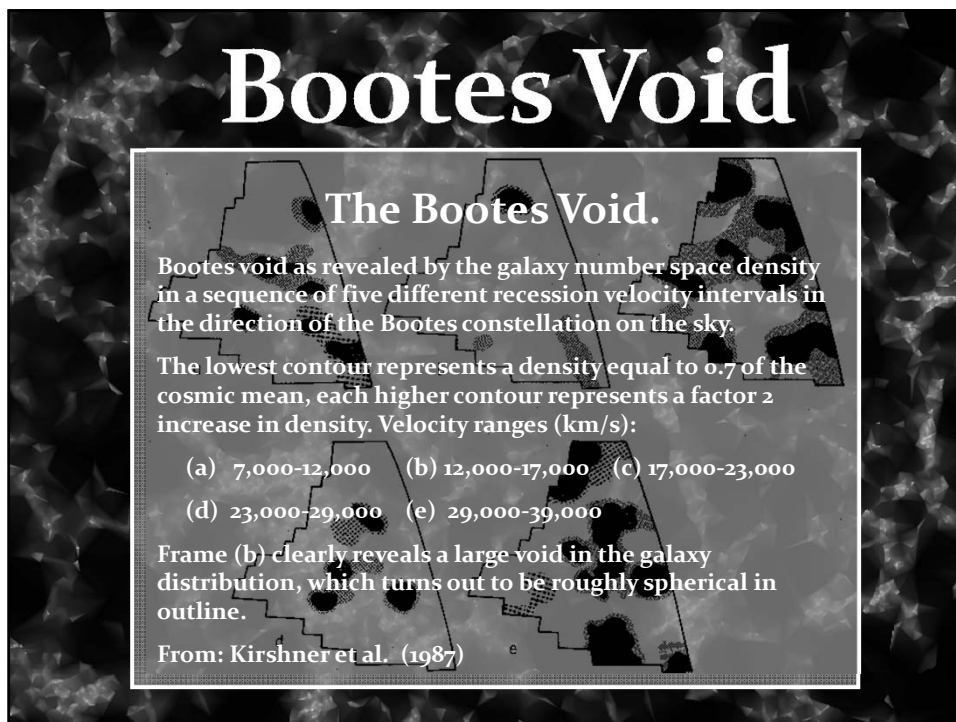
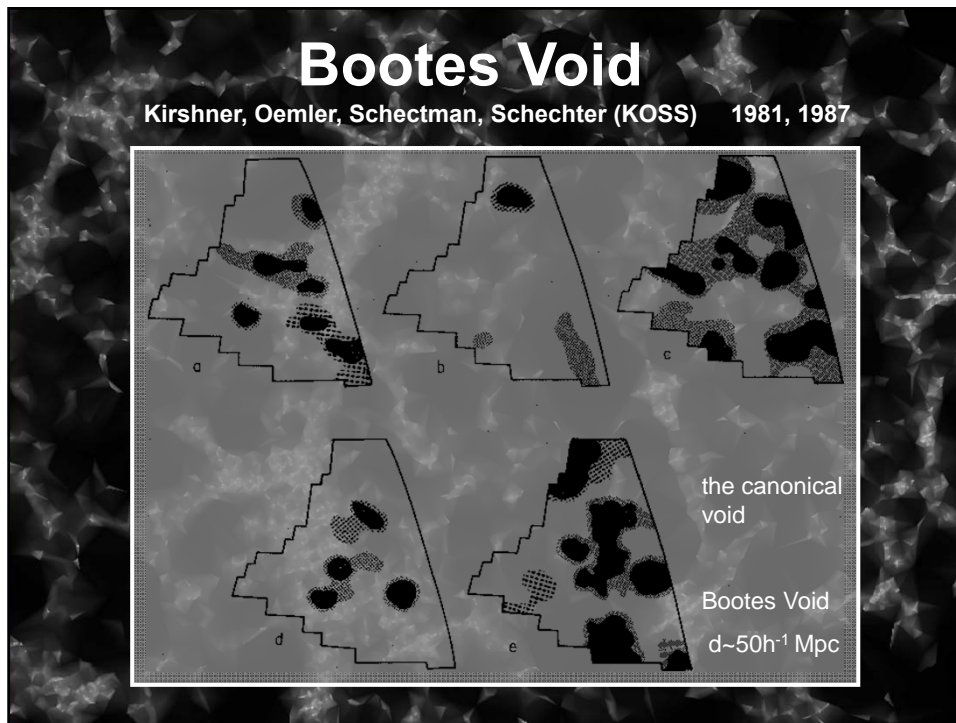
First linking of observationally visible void regions and the theory of cosmic structure formation.



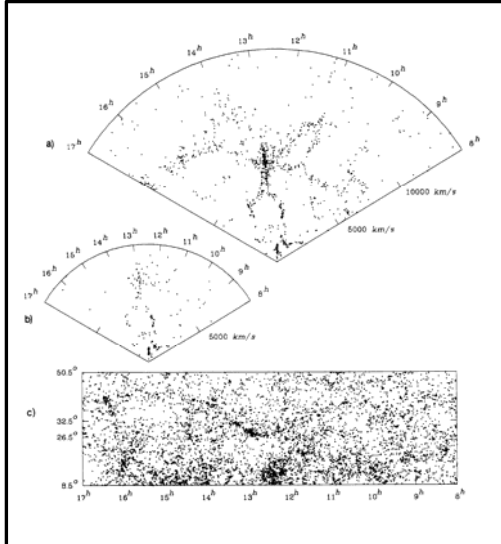
First Voids



Gregory & Thompson 1978:
redshift survey of Coma/A1367 supercluster region revealed existence of large near-empty regions of space.



Voids & the Cosmic Web

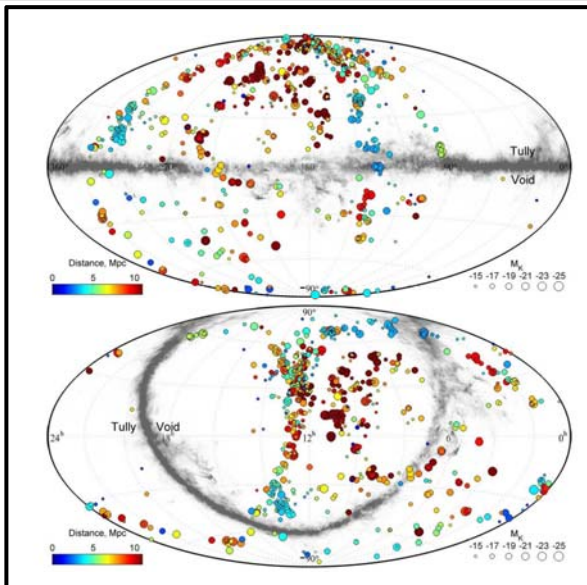


deLapparent, Geller & Huchra, 1986:

“a slice of the Universe”

Voids appear to be an integral part of a complex weblike arrangement of galaxies

local Cosmic Web: Local Void



Karachentsev et al.

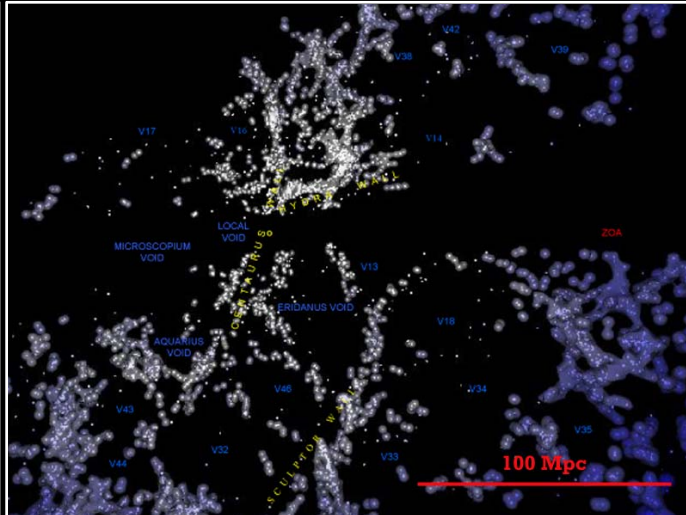
LV catalog:
galaxies within 10 Mpc reveal
beautifully the magnificent

Local Void – Tully Void

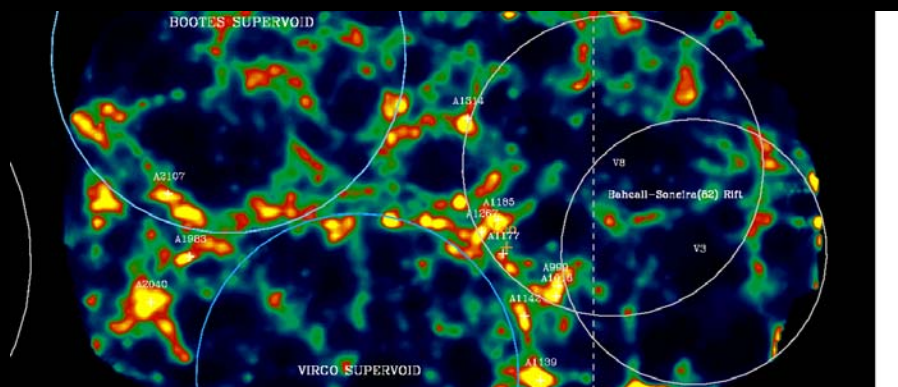
Fairall Void Catalogue

6dF based catalogue

of 526 visually identified voids.

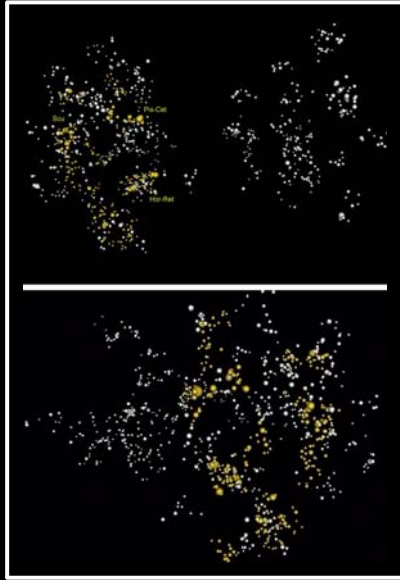


Bootes Void: Substructure



Platen et al. 2009

Voids & Clusters

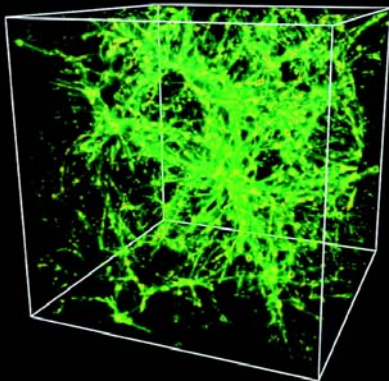


Einasto, Saar et al. (1990s)

- Superclustering in Abell/APM clusters catalog
- Finding of characteristic scale ~ 140 Mpc, corresponding to large voids in the cluster distribution

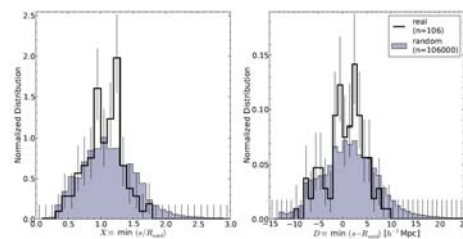
Reflex II cluster catalog (Bohringer et al.) reveals same population of voids in cluster distribution (see talk by Collins).

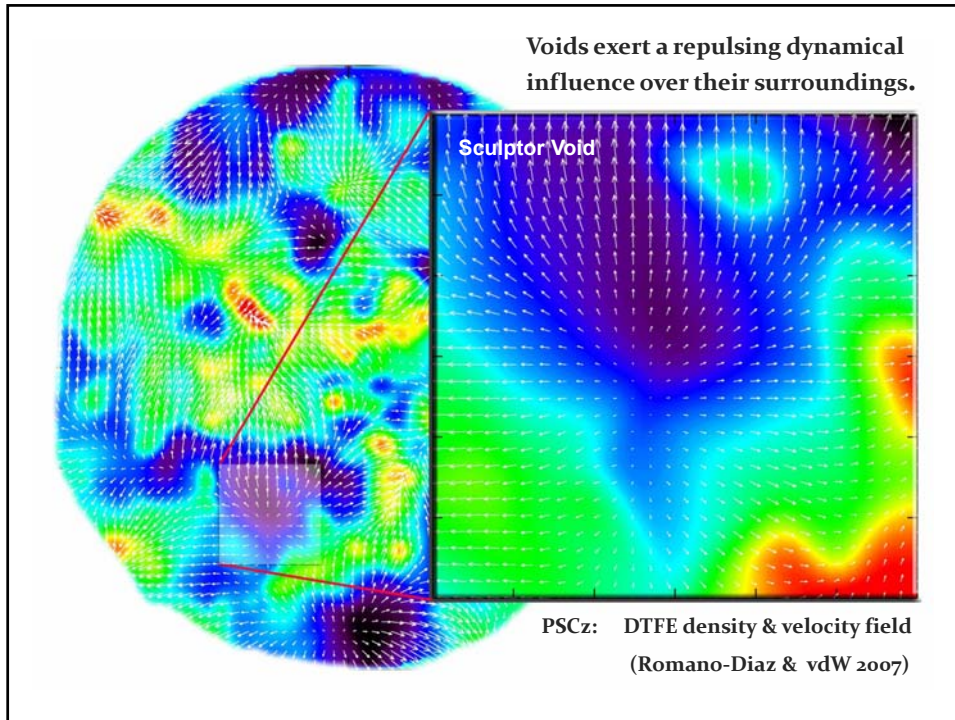
Voids & the Gaseous Web



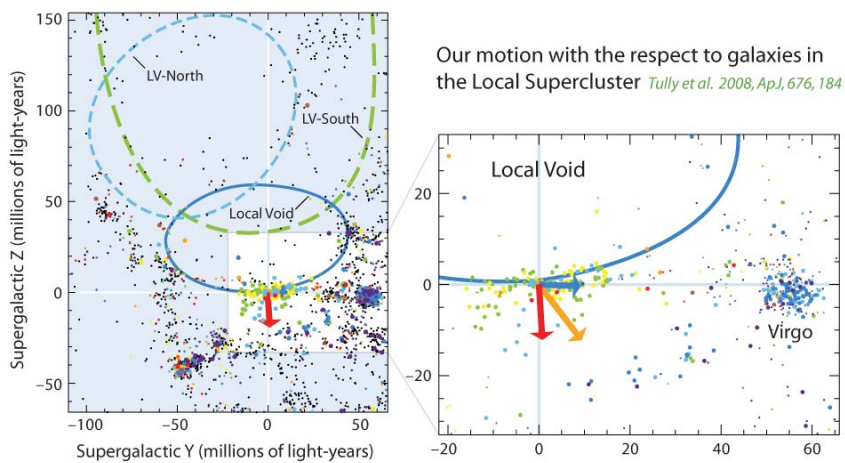
Tejos et al. 2012:

HI Ly α absorption systems clearly delineate voids



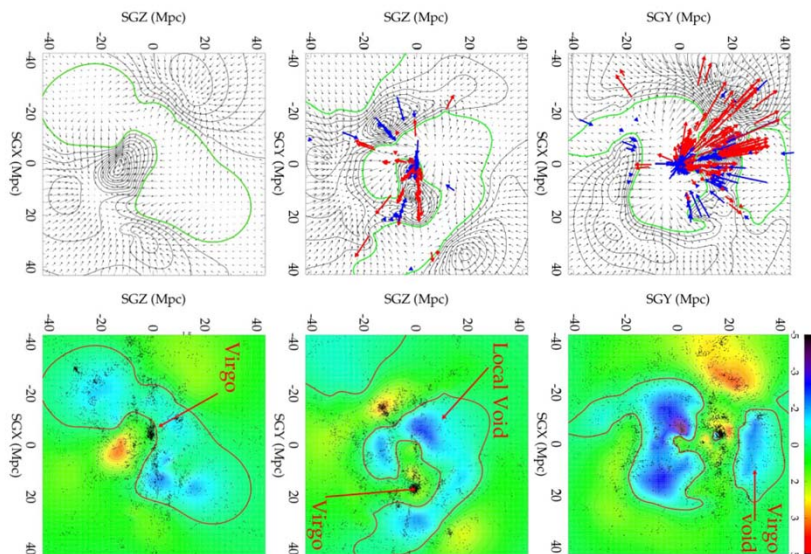


Push of the Local Void



Tully et al. 2008:
Local Void pushes with ~260 km/s against our local neighbourhood

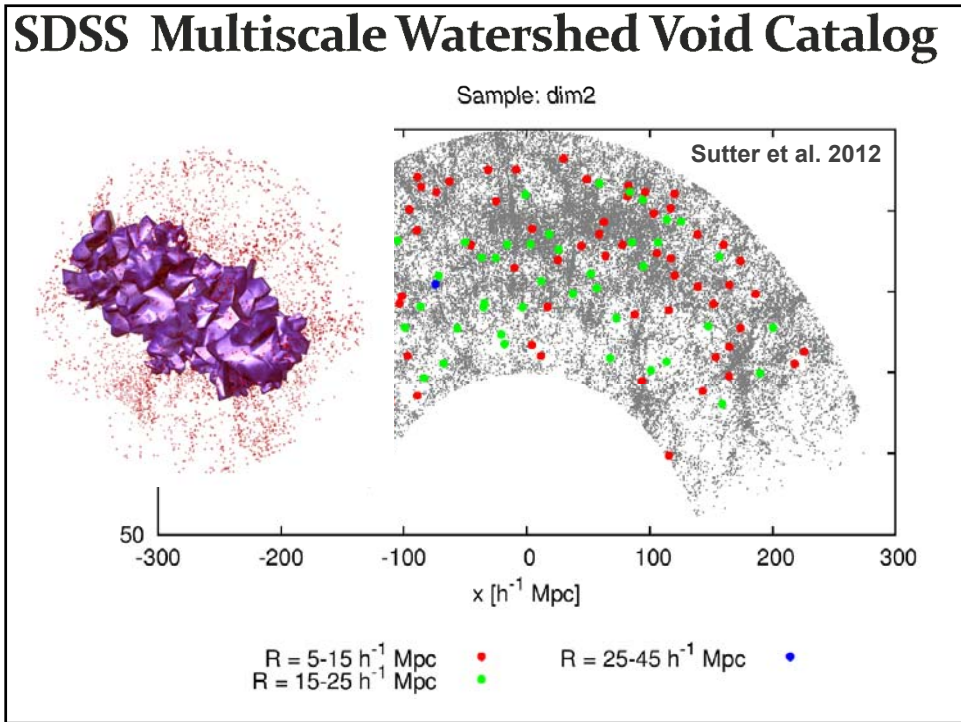
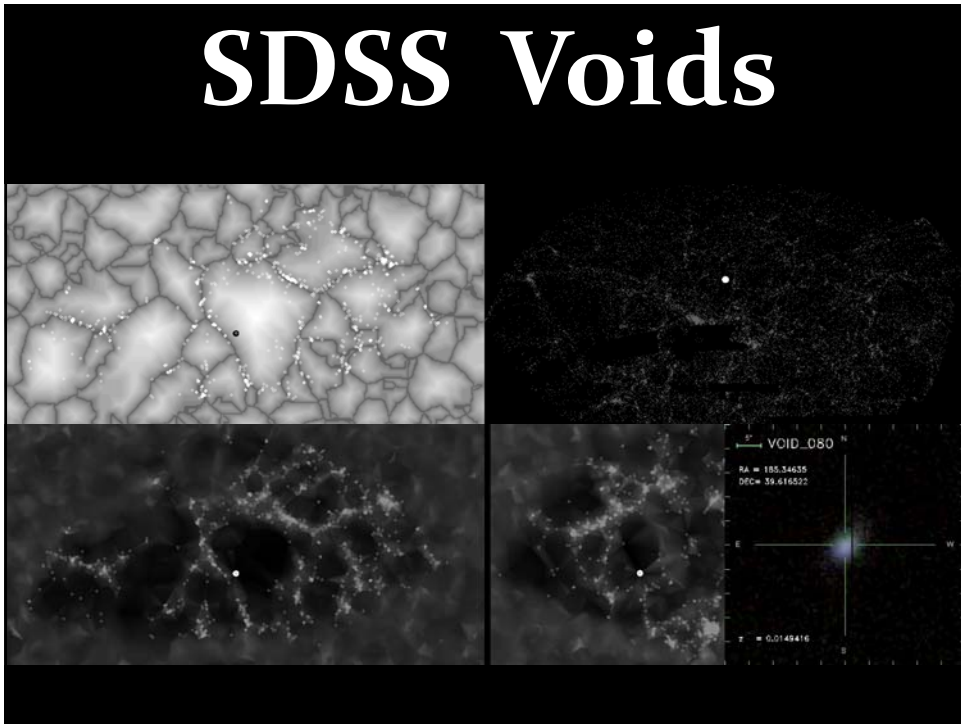
Void Dynamics: Local Void

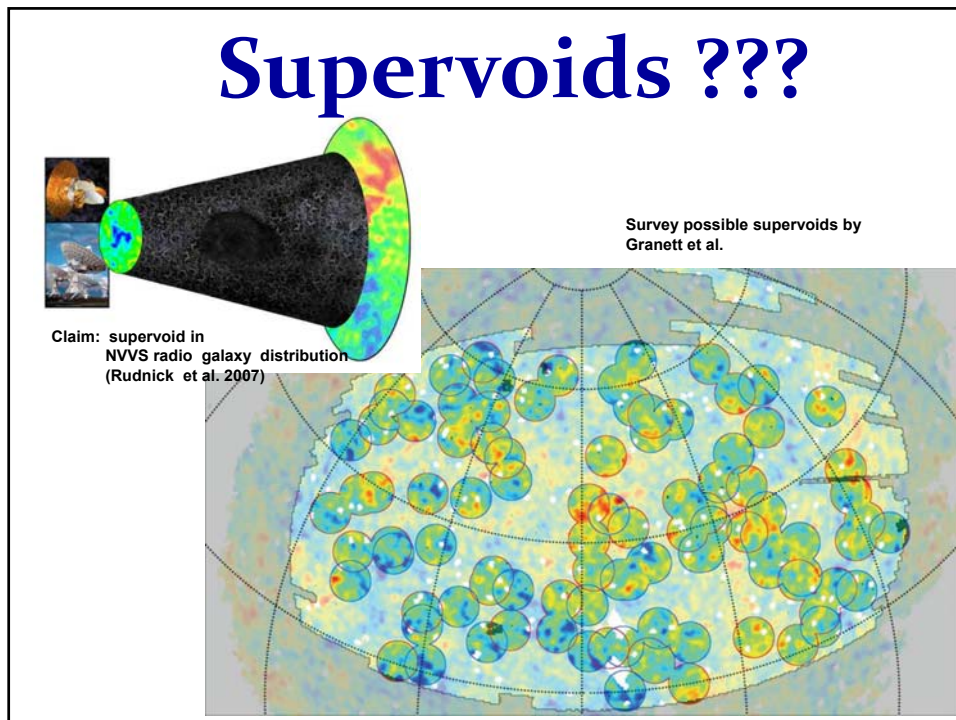


Voids: Identification & Catalogues

- Voids are not easily defined
not as cleanly & objectively identifiable objects as clusters
- range of criteria & identifiers,
often conflicting see Colberg et al. 2008
- increased interest due to cosmological/dark energy
information contained in voids

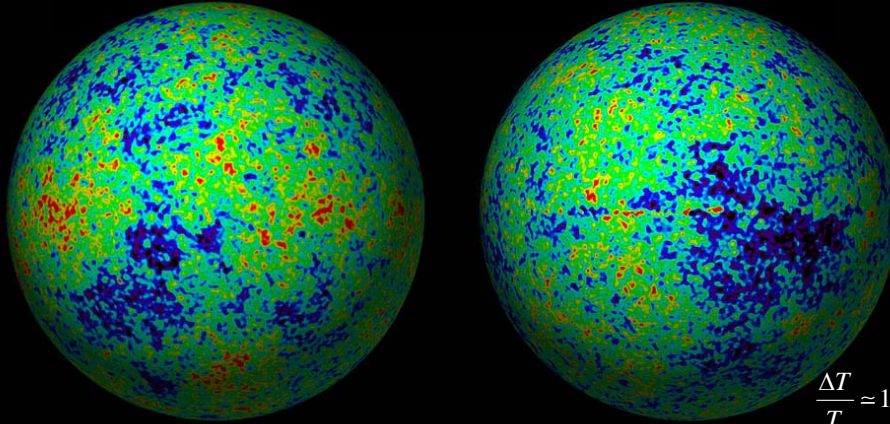
- Catalogues:
 - Fairall 2006 by eye
 - Pan et al. 2012 Hoyle-Vogeley algorithm
 - Sutter et al. 2012 Watershed/ZOBOV multiscale





**Cosmic
Structure Formation:
Gravitational
Instability**

Primordial Universe

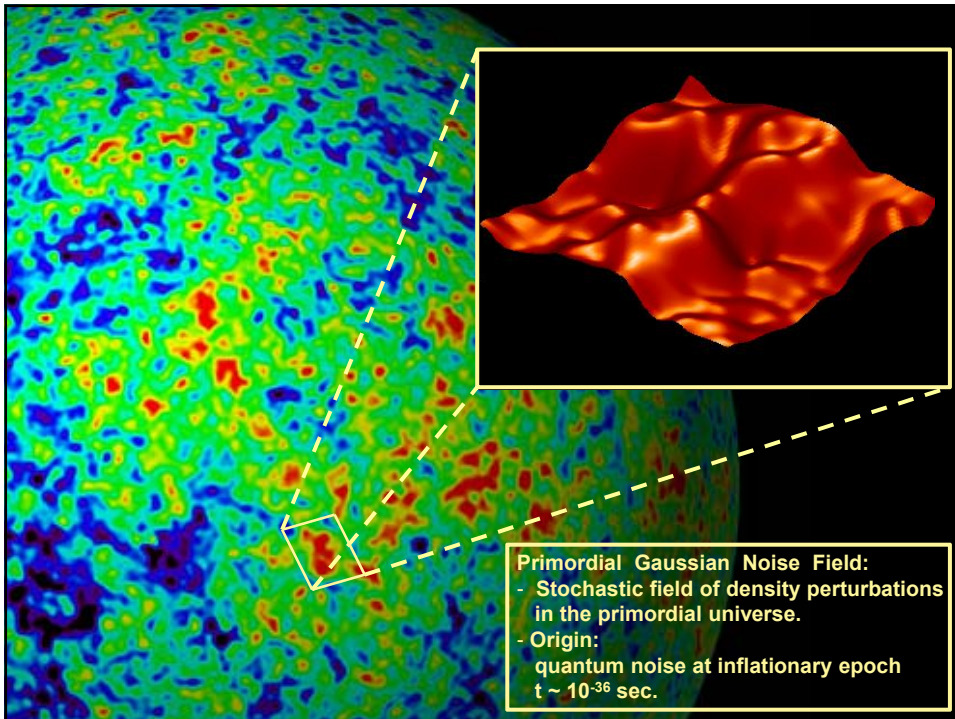


$$\frac{\Delta T}{T} \approx 10^{-5}$$

global representation cosmic surface last scattering: the world inside out

Temperature Map CMB radiation:

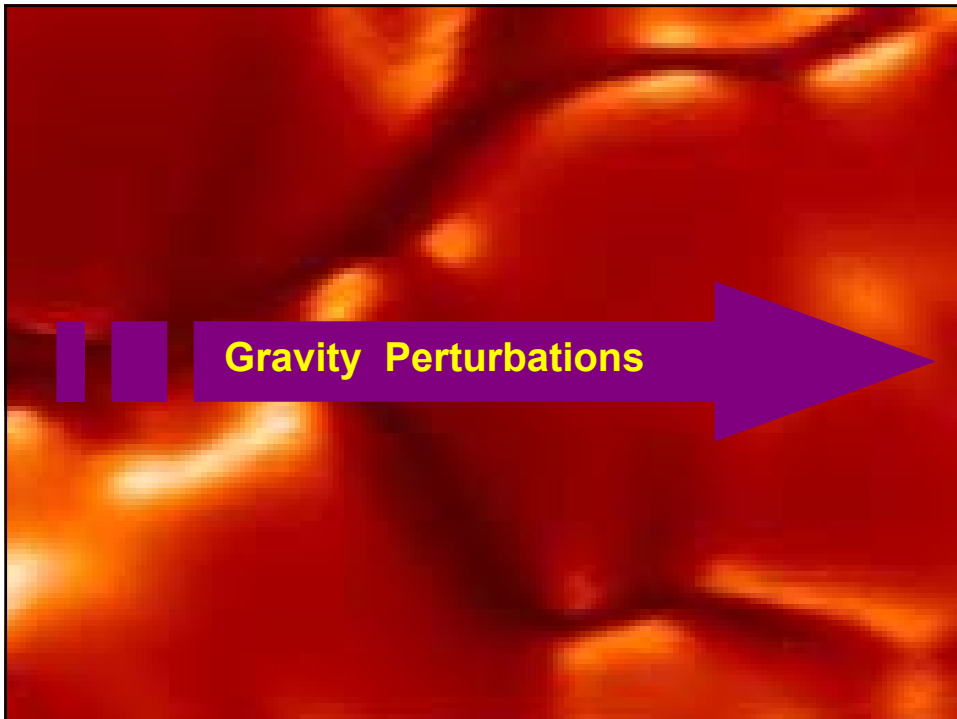
Tiny variations in primordial temperature, reflecting tiny inhomogeneities in energy density of $\Delta \sim 10^{-5}$ K at recombination epoch, 379,000 yrs after Big Bang

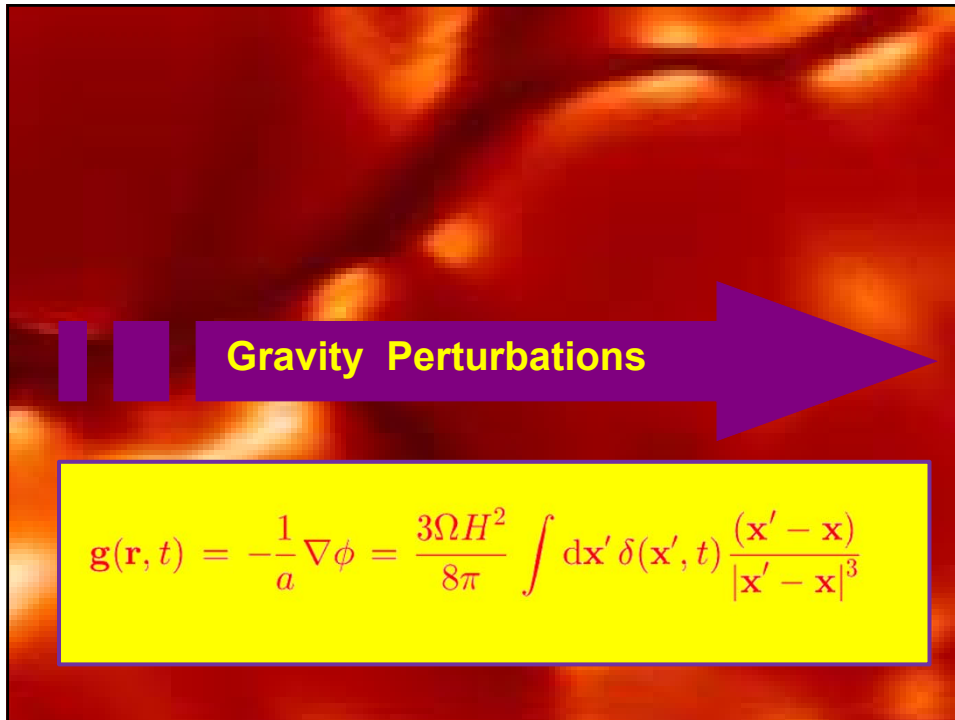


Primordial Gaussian Noise Field:
 - Stochastic field of density perturbations in the primordial universe.
 - Origin: quantum noise at inflationary epoch $t \sim 10^{-36}$ sec.

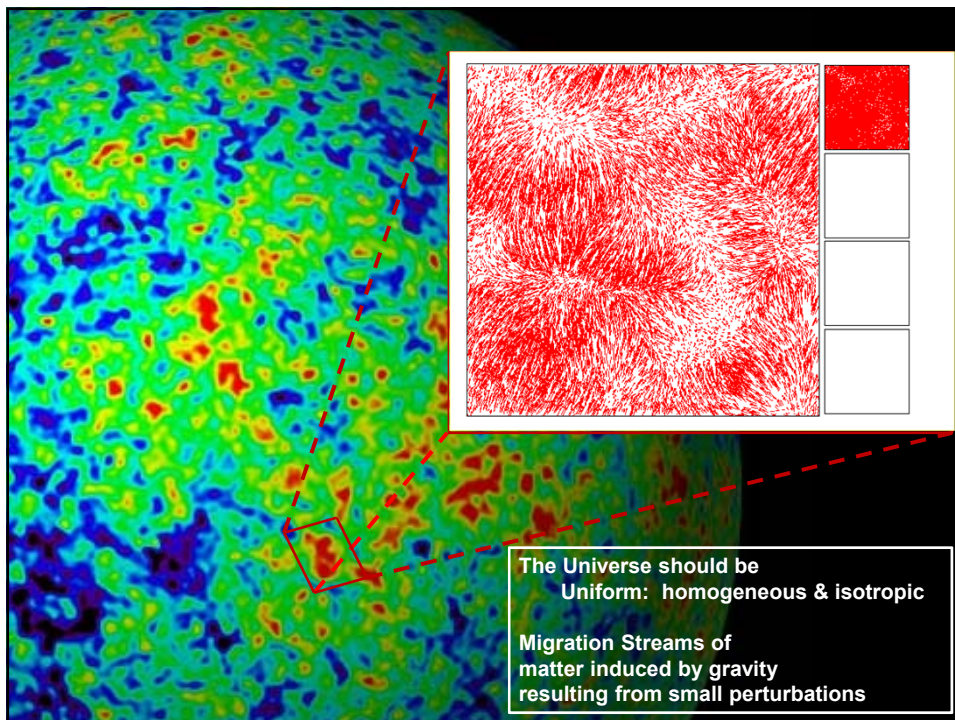
Density Perturbation Field:

$$\delta(\vec{x}, t) = \frac{\rho(x, t) - \rho_u(t)}{\rho_u(t)}$$





Gravity Perturbations

$$\mathbf{g}(\mathbf{r}, t) = -\frac{1}{a} \nabla \phi = \frac{3\Omega H^2}{8\pi} \int d\mathbf{x}' \delta(\mathbf{x}', t) \frac{(\mathbf{x}' - \mathbf{x})}{|\mathbf{x}' - \mathbf{x}|^3}$$


Cosmic Structure Formation

(Energy) Density Perturbations



Gravity Perturbations



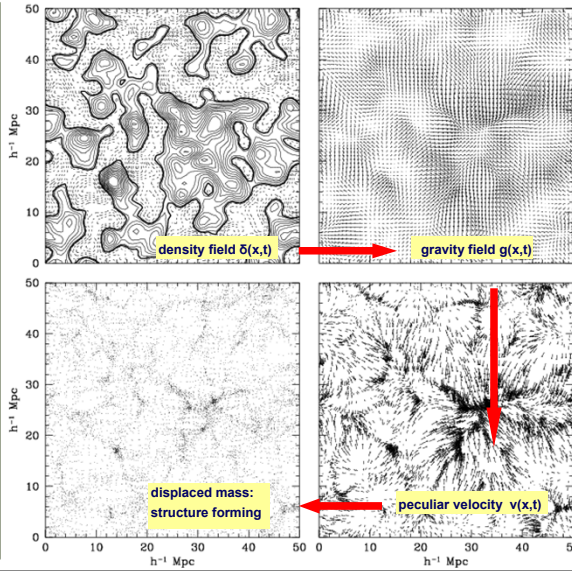
(Cosmic) Flows of (Energy) & Matter:

- towards high density regions:
 - assemble more and more matter
 - their expansion comes to a halt
 - turn around and collapse
- evacuating void regions
 - low-density regions expand
 - matter moves out of region
 - turn into prominent empty voids



Emergence of cosmic structures

- Computer Simulations
 - succesfull confrontation with observational reality



Cosmic Structure Formation

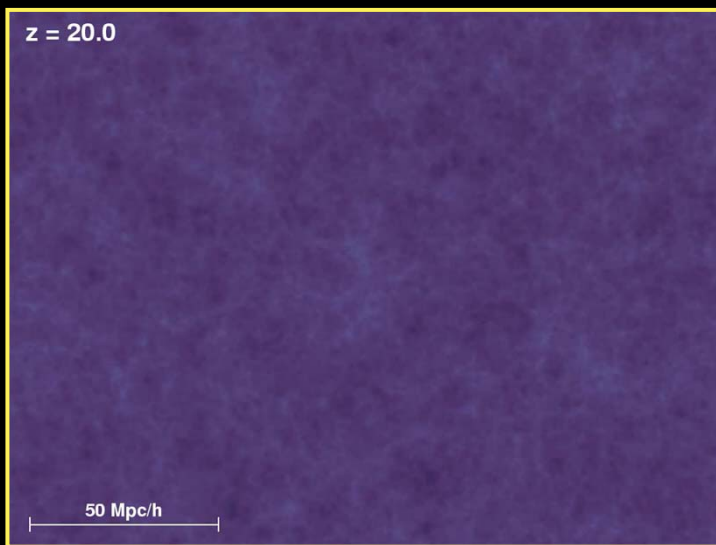
Formation
Cosmic Web:

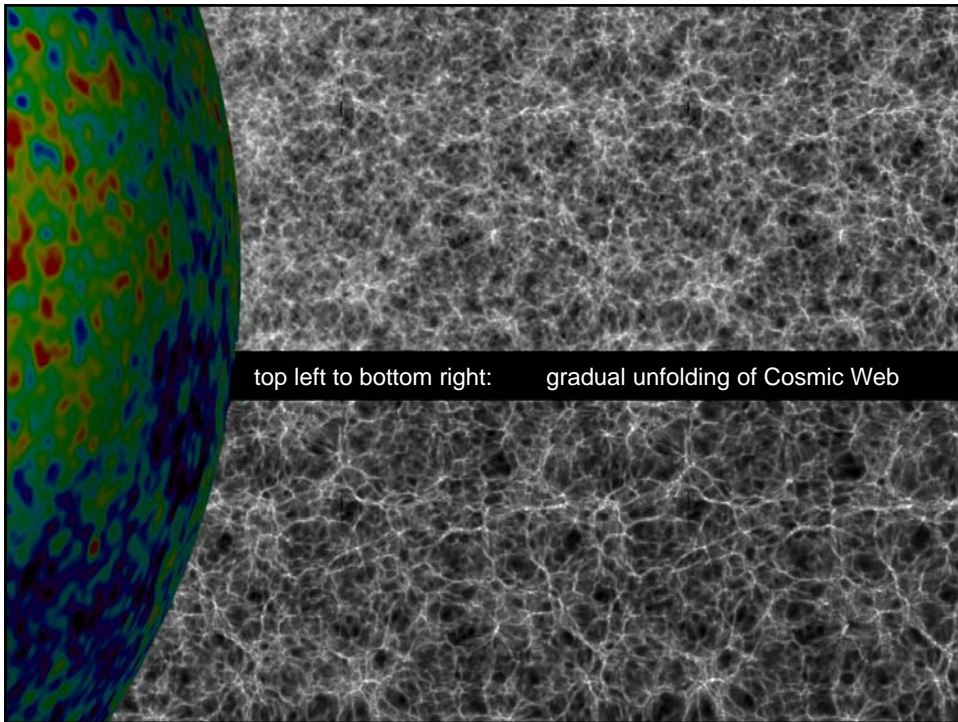
simulation
sequence

(cold)
dark matter

(courtesy:
Virgo/V. Springel).

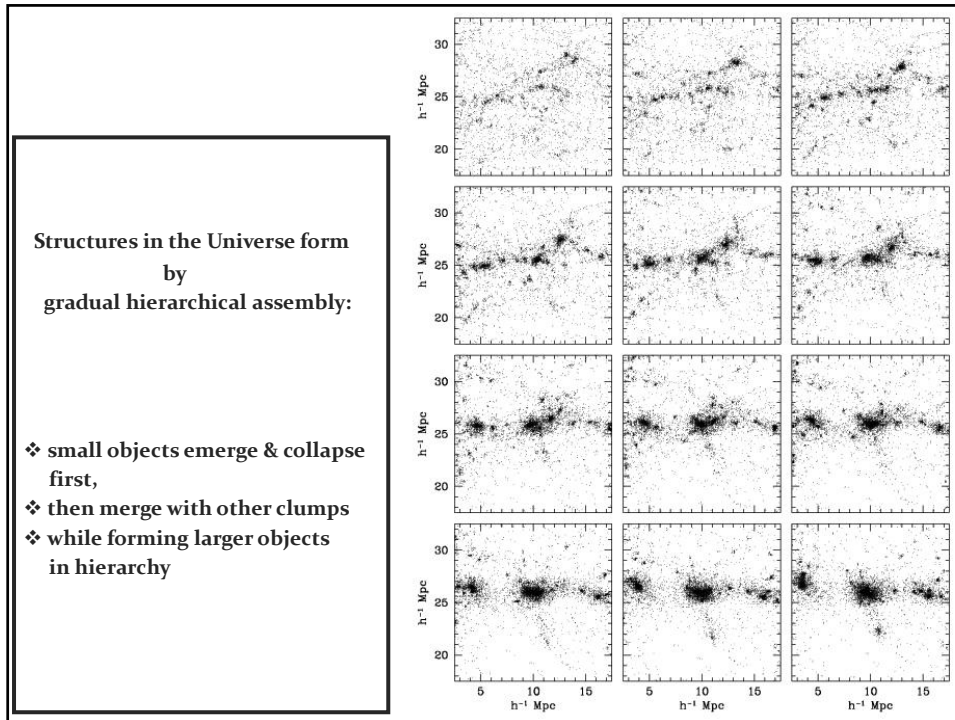
$z = 20.0$





Dynamical Evolution Cosmic Web

- hierarchical structure formation
- anisotropic collapse
- void formation:
asymmetry
overdense vs. underdense



Voids:

Formation & Structure

Void Formation

Void Evolution

an illustration

cosmology:

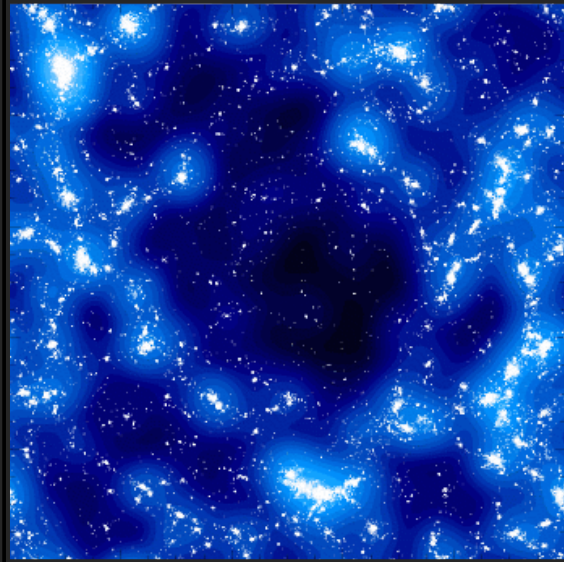
$$\Omega_m = 1.0; \quad H_0 = 70 \text{ km/s/Mpc}$$

initial conditions:

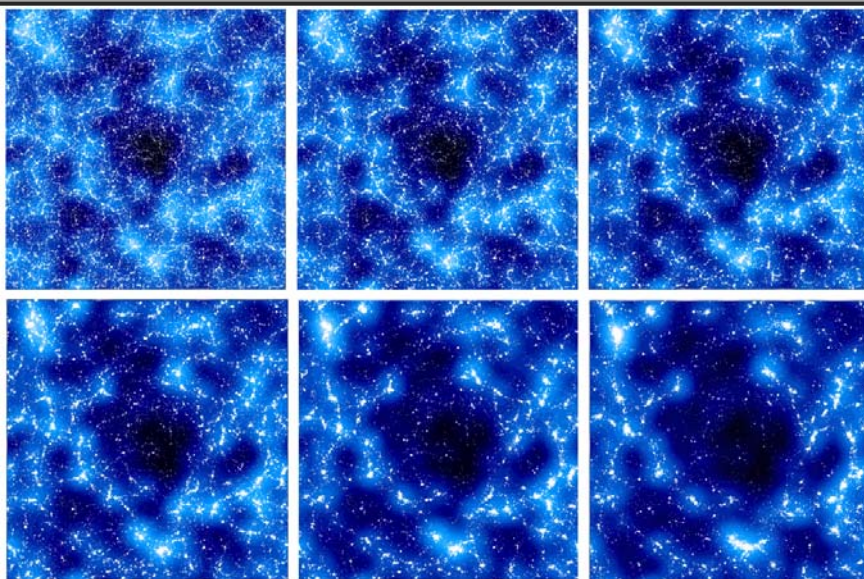
underdensity, Gaussian field

$$R_G \sim 4h^{-1} \text{ Mpc}$$

$$P(k) \propto k^{-0.5}$$



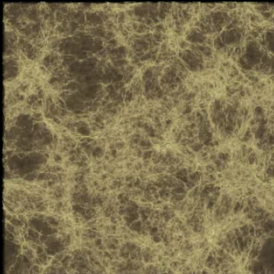
Void Formation



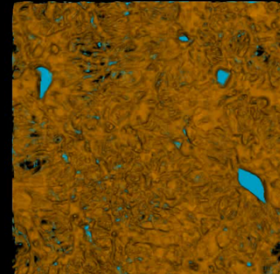
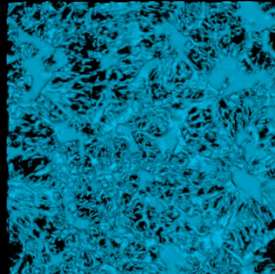
Multiscale Cosmic Web: hierarchical evolution

NEXUS/MMF Evolution Cosmic Web

t = 0.56 Gyrs

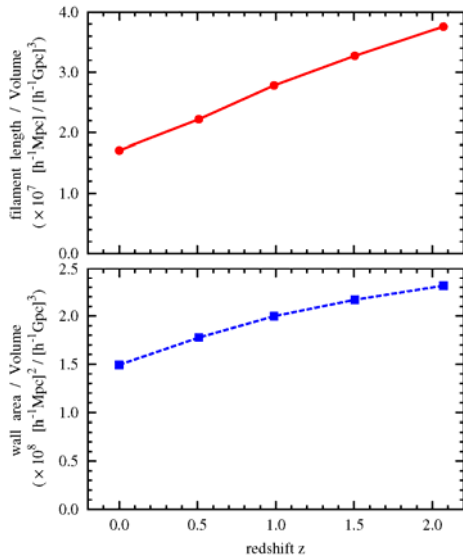


z = 8.70



Cautun et al. 2013

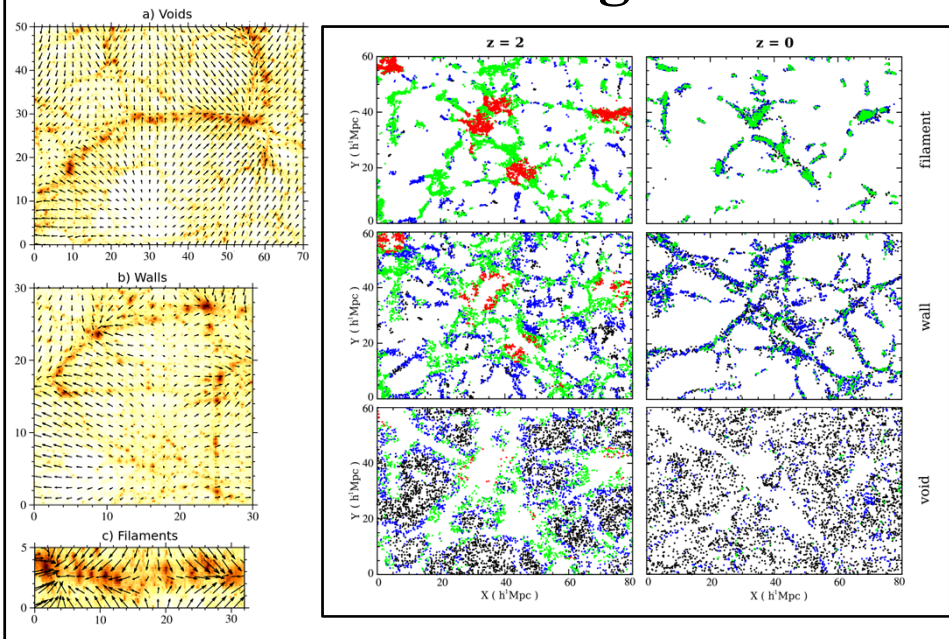
Evolving Filament & Wall Network



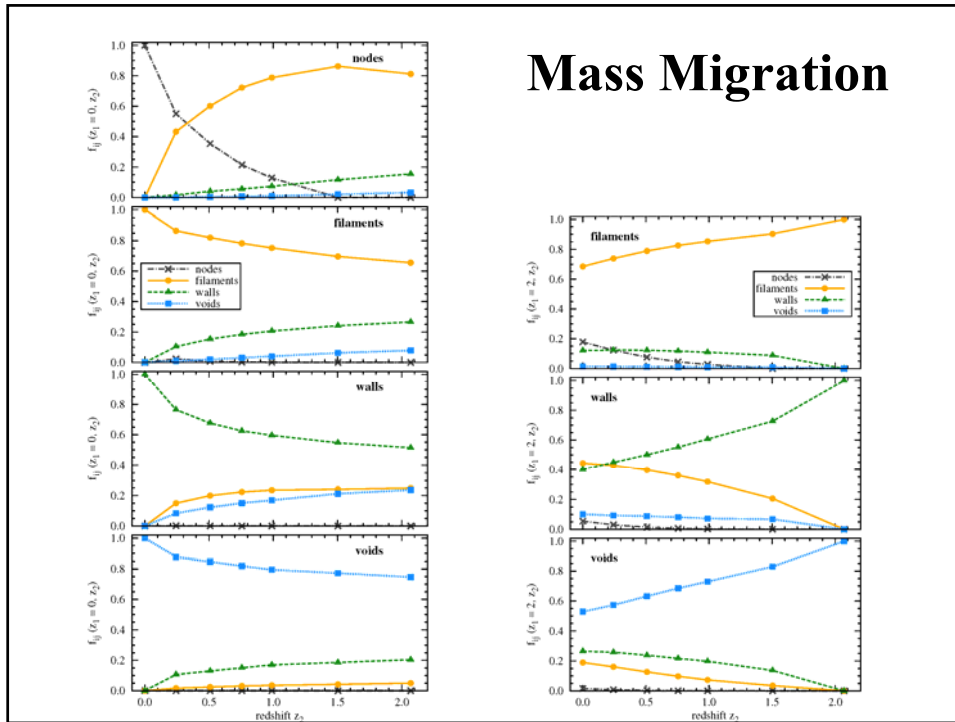
Total length of filament network :
decreasing as a function of time

Total surface area of wall network :
decreasing as a function of time

Web Mass Emigration



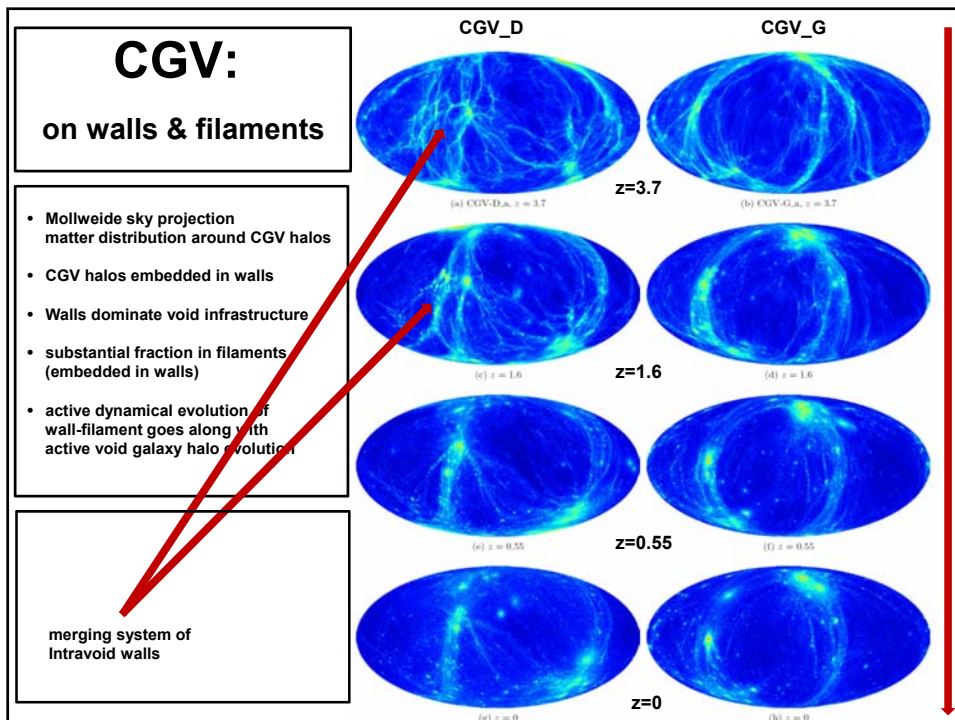
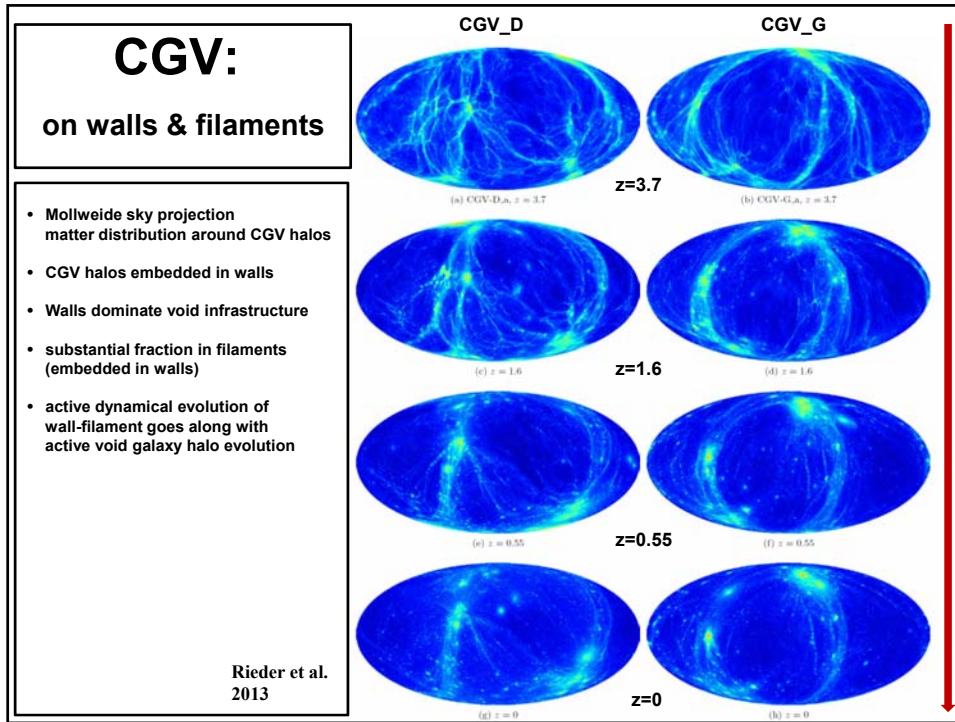
Mass Migration



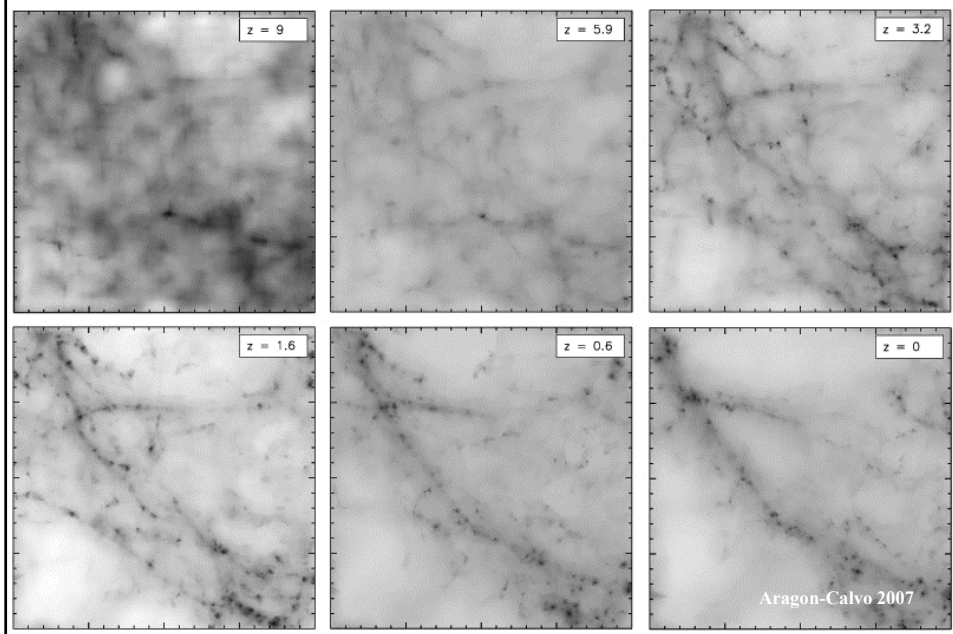
CGV halo & web evolution



Rieder et al. 2013



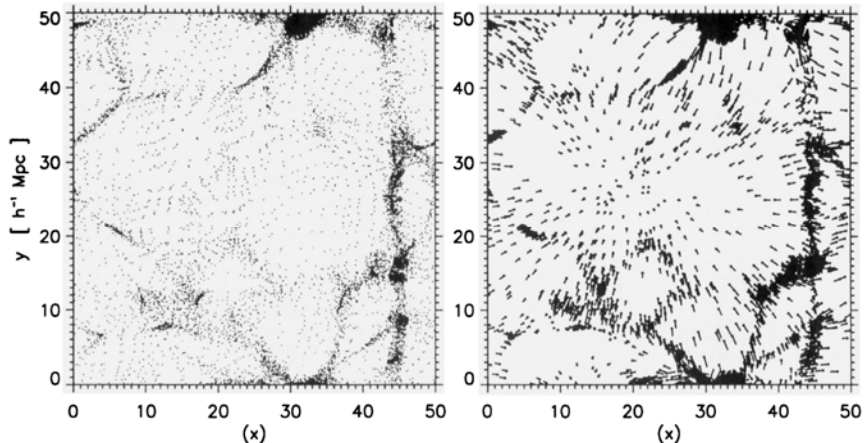
Hierarchical Filament Formation



Void Hierarchy

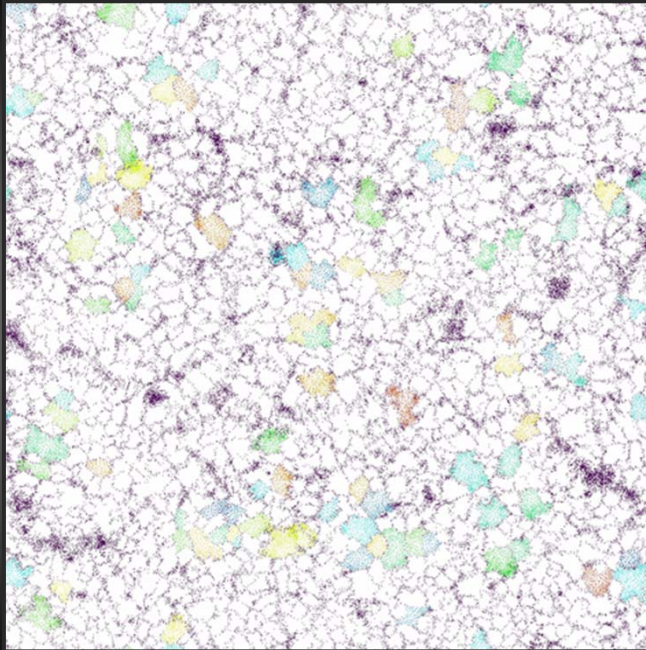
Void formation: - via gradual merging of voids
- demolition of small voids

Dubinski et al. 1993
Van de Weygaert & van Kampen 1993



Constrained Void Simulations:
Van de Weygaert 1991
vdW & van Kampen 1993

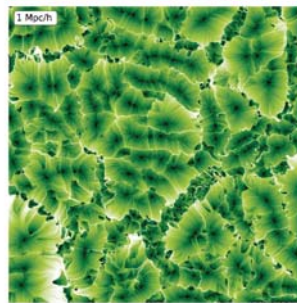
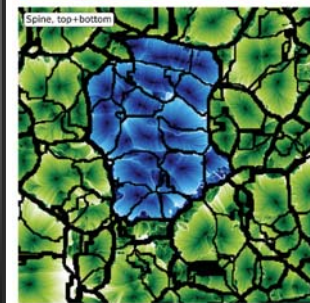
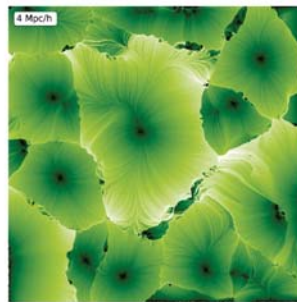
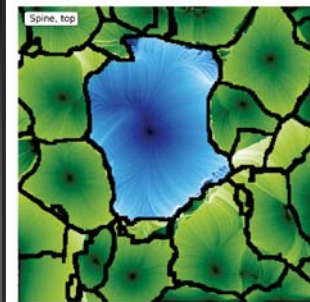
CRF formalism:
Bertschinger 1987
vdW & Bertschinger 1996



**Hierarchical
Web Evolution:**

“Lagrangian” view:
development and fate
patterns LSS

Platen & vdW 2004



**Hierarchical
Web Evolution:**

Void hierarchy
expressed in
multiscale structure
velocity outflow

Aragon-Calvo & Szalay 2012

Weaving the Cosmic Web:

dynamics & tessellations

Hidding et al. 2012, Hidding et al. 2014

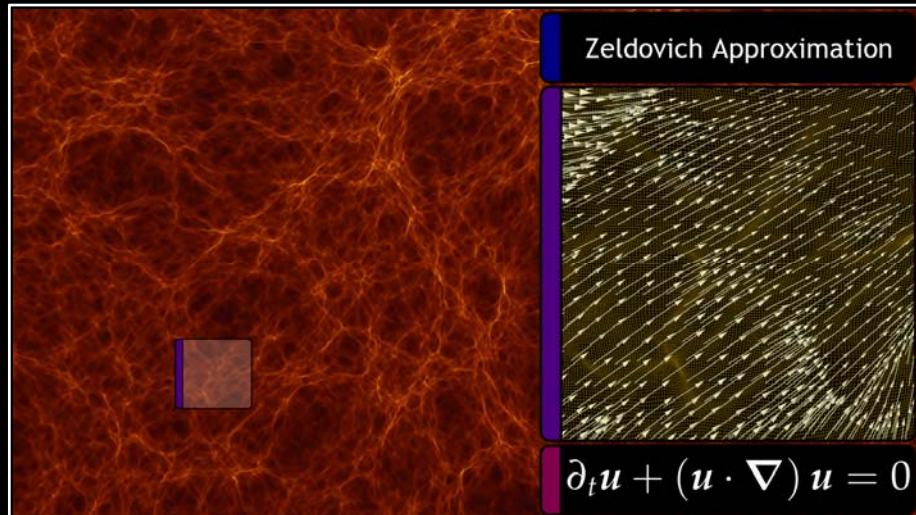
Zel'dovich Approximation

$$\vec{x} = \vec{q} + D(t)\vec{u}(\vec{q})$$

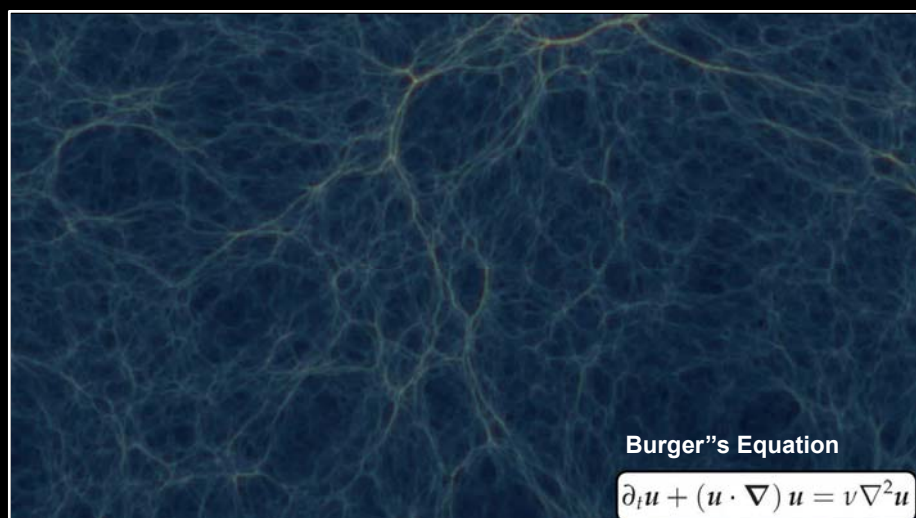
$$\vec{u}(\vec{q}) = -\vec{\nabla}\Phi(\vec{q})$$

$$\Phi(\vec{q}) = \frac{2}{3Da^2 H^2 \Omega} \phi_{in}(\vec{q})$$

Zel'dovich Approximation



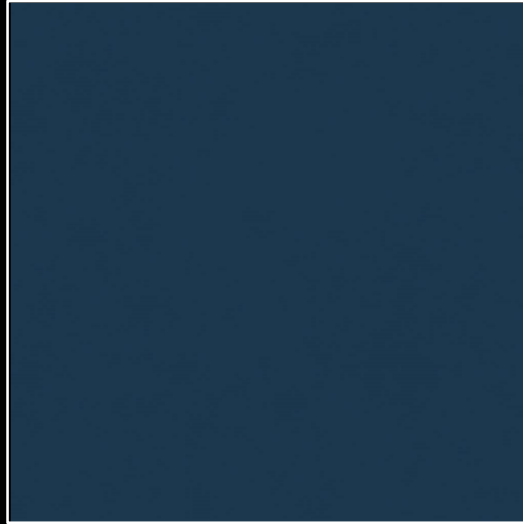
Adhesion Approximation



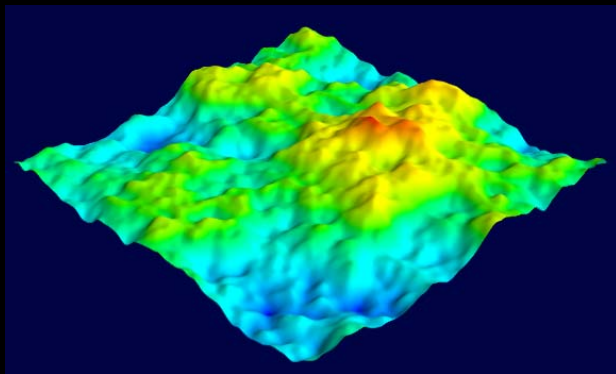
Adhesion Approximation

Gurbatov, Saichev & Shandarin 1987

Hidding 2012



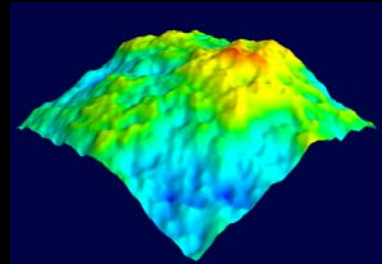
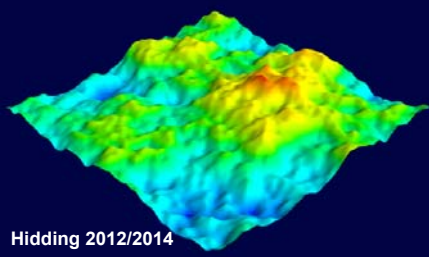
Velocity & Gravity Potential



$$\vec{u}(\vec{q}) = \vec{\nabla}\Phi(\vec{q})$$

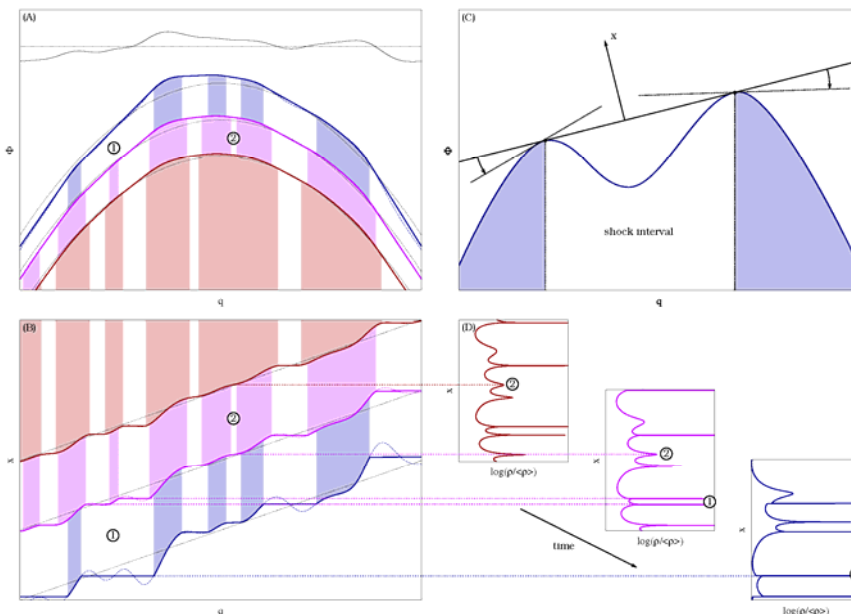
Burger's Equation: Hopf Solution

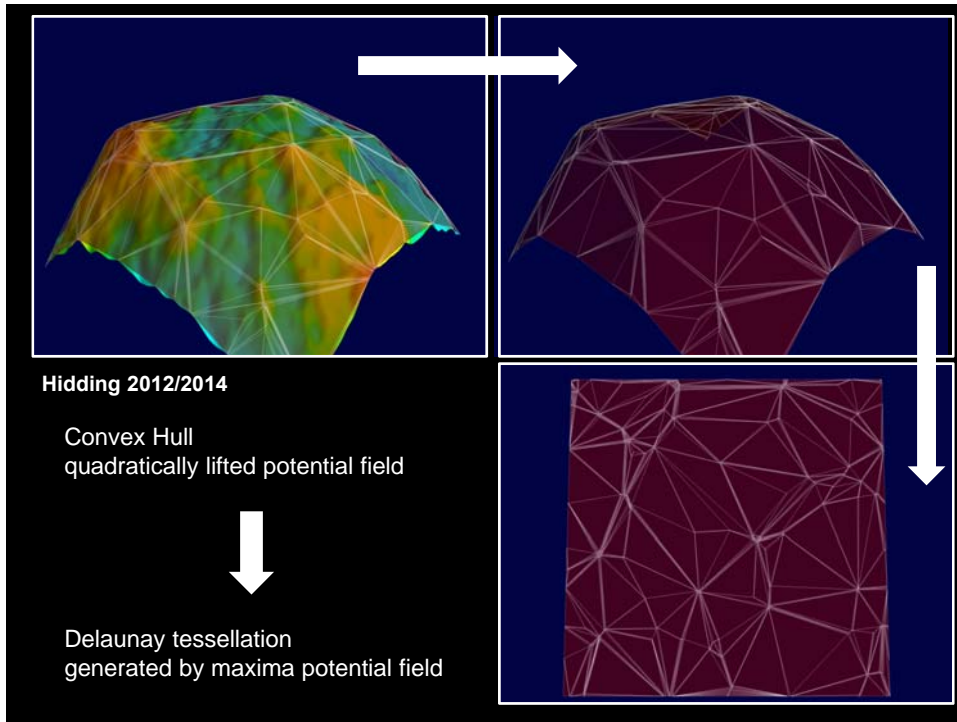
$$\frac{\partial \vec{u}}{\partial t} + (\vec{u} \cdot \vec{\nabla}) \vec{u} = \nu \nabla^2 \vec{u}$$



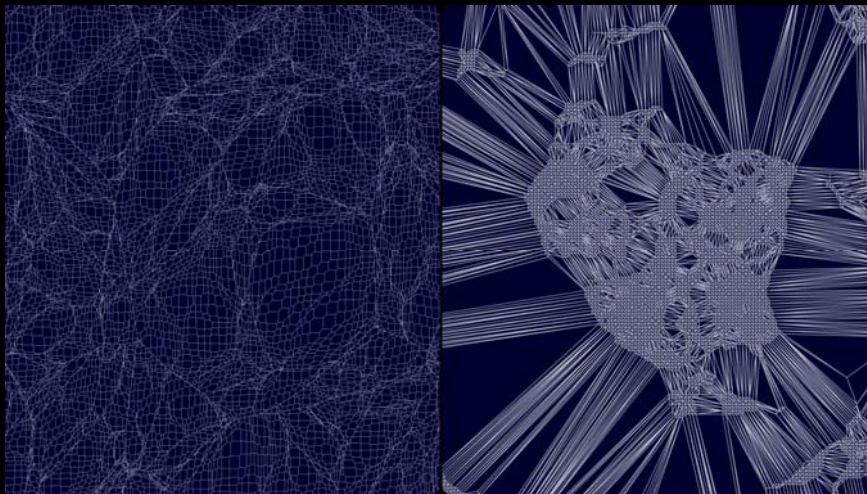
$$\Phi(\vec{x}, t) + \frac{x^2}{2} = \max_q \left[\left(t\Phi_0(q) - \frac{q^2}{2} \right) + \vec{x} \cdot \vec{q} \right]$$

Burger's Equation: Hopf Solution

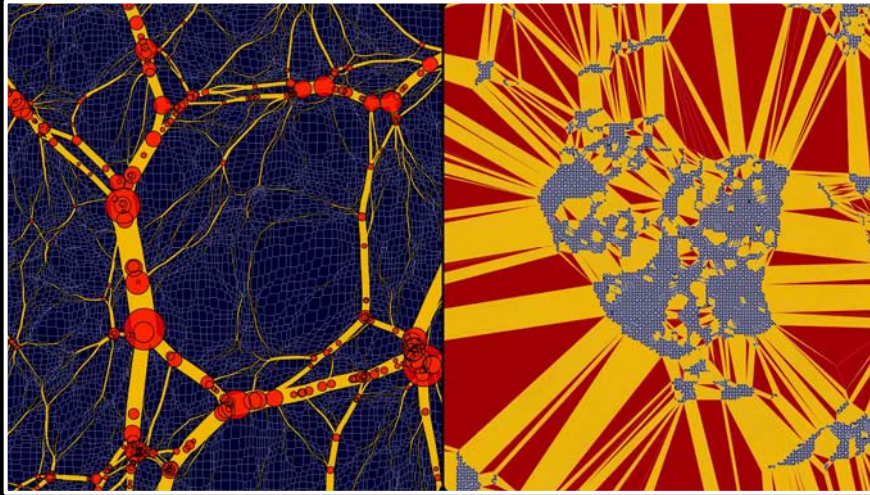




Eulerian – Lagrangian Voronoi - Delaunay



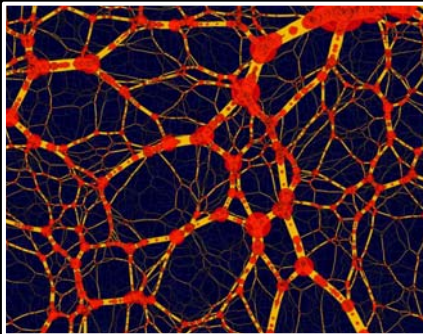
Eulerian – Lagrangian Voronoi - Delaunay



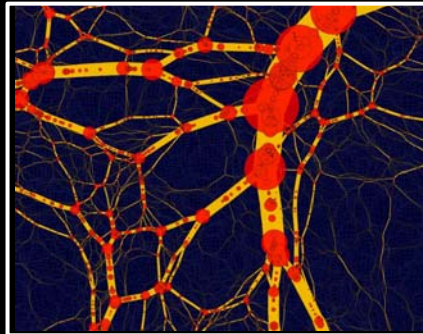
Cosmological Sensitivity

the morphology of the weblike network is highly sensitive to the underlying cosmology

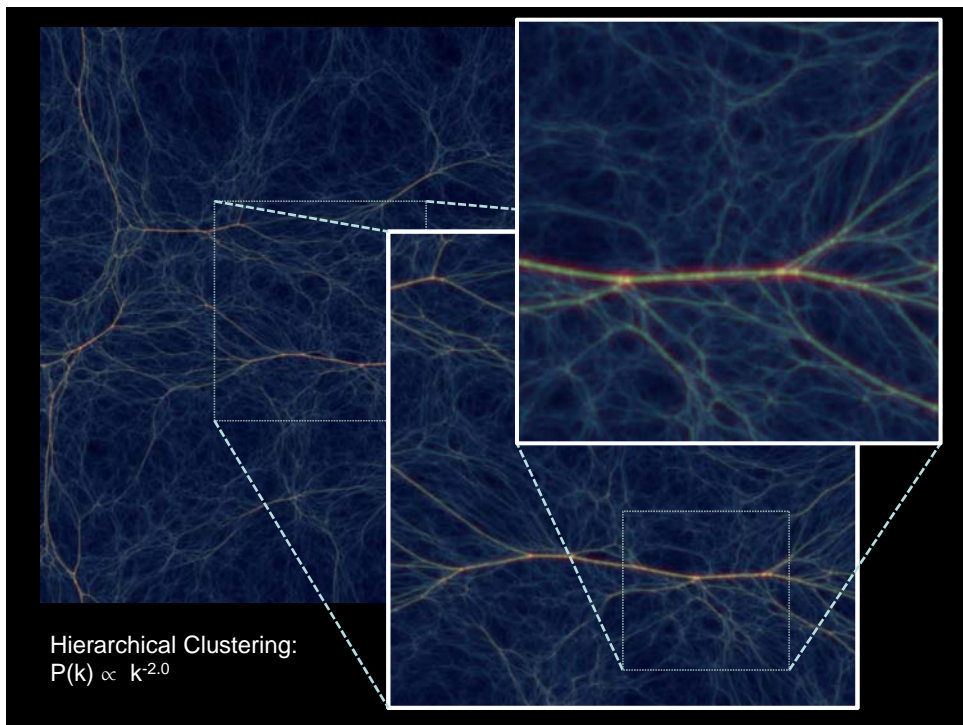
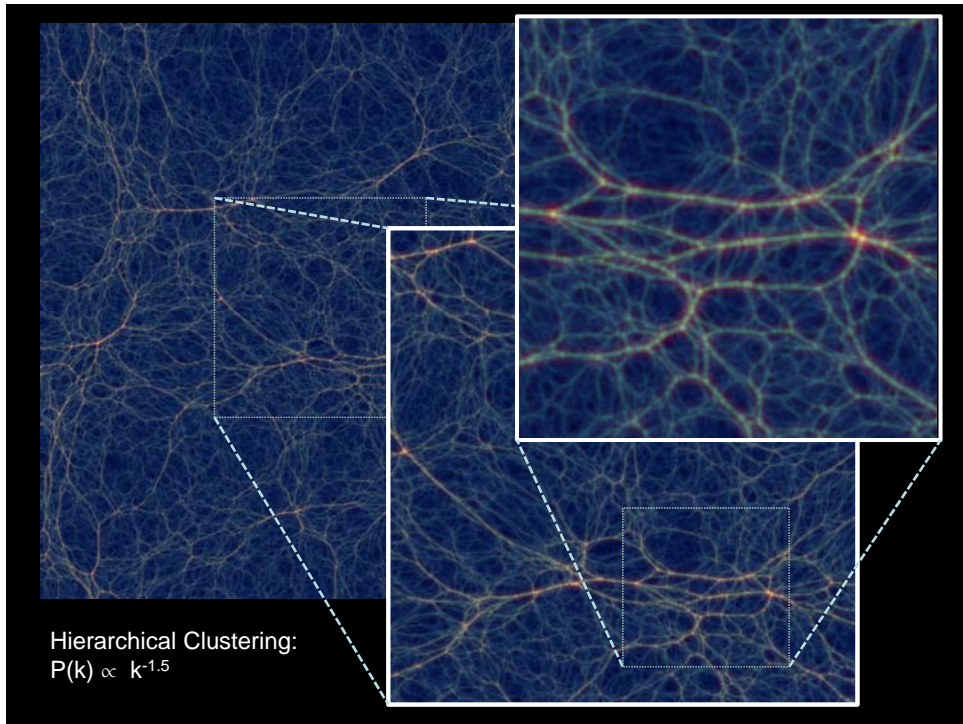
$P(k) \propto k^{-1.5}$



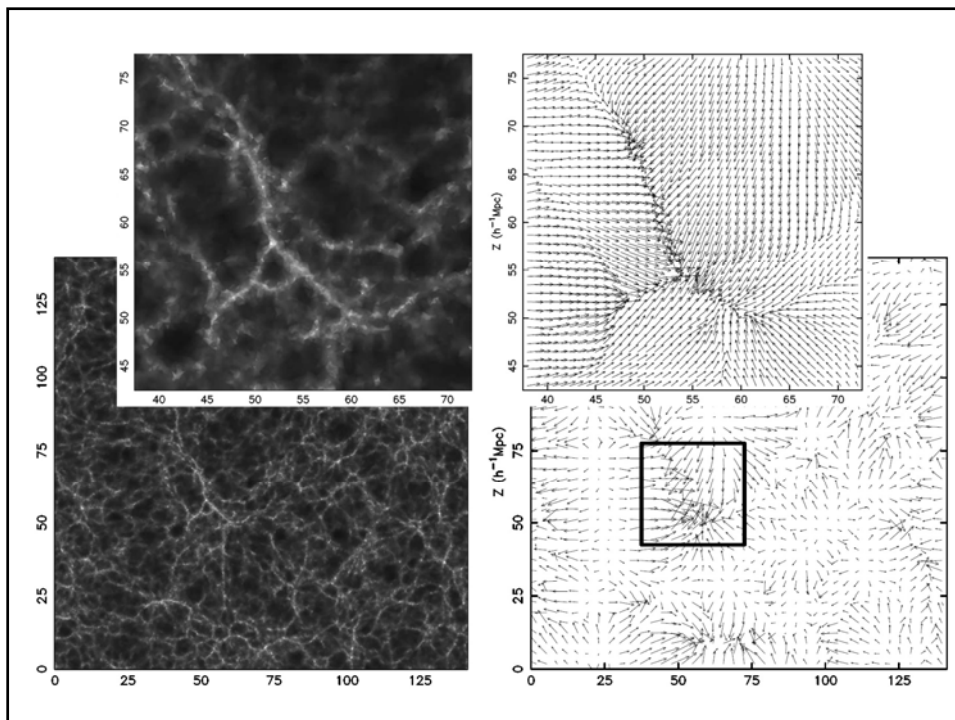
Hidding 2012/2014



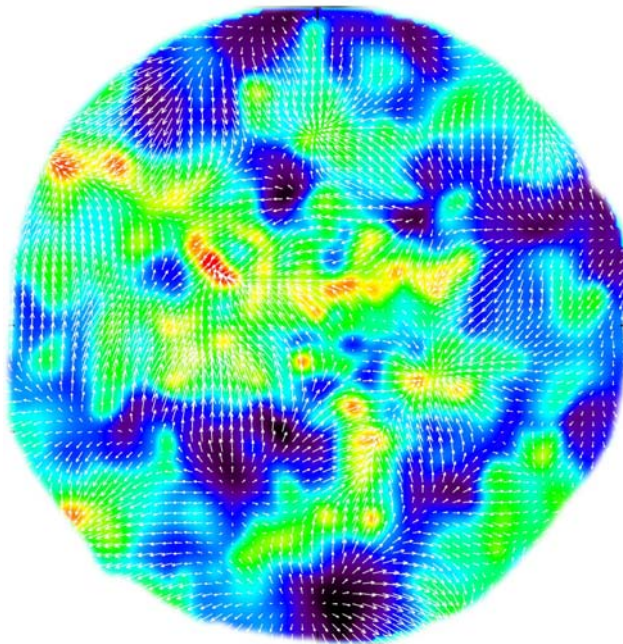
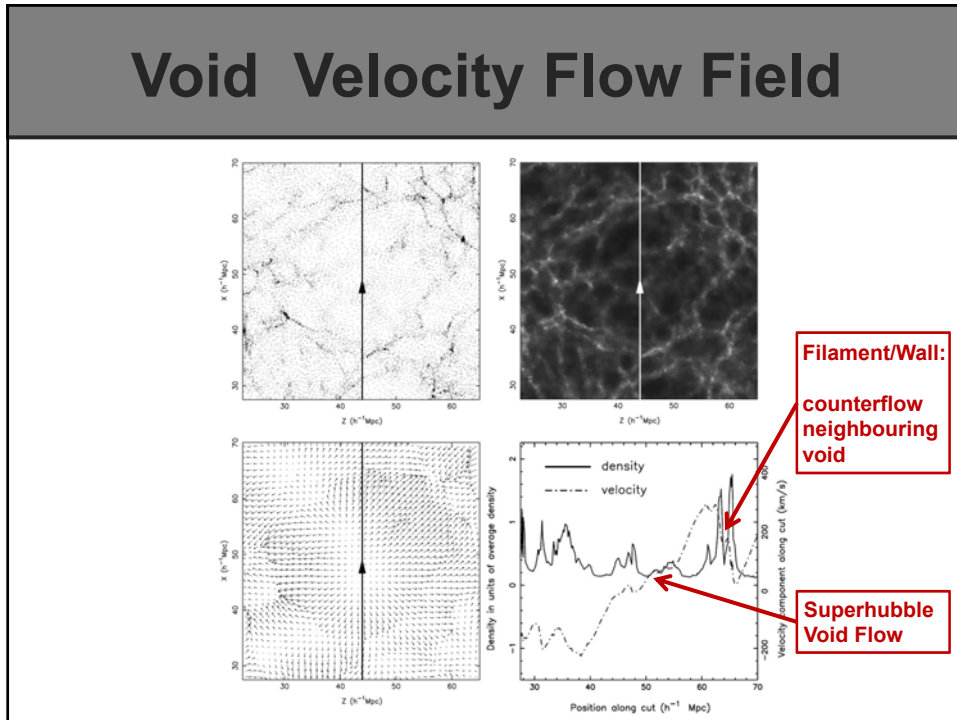
$P(k) \propto k^{-2.0}$



Cosmic Web: Dynamics

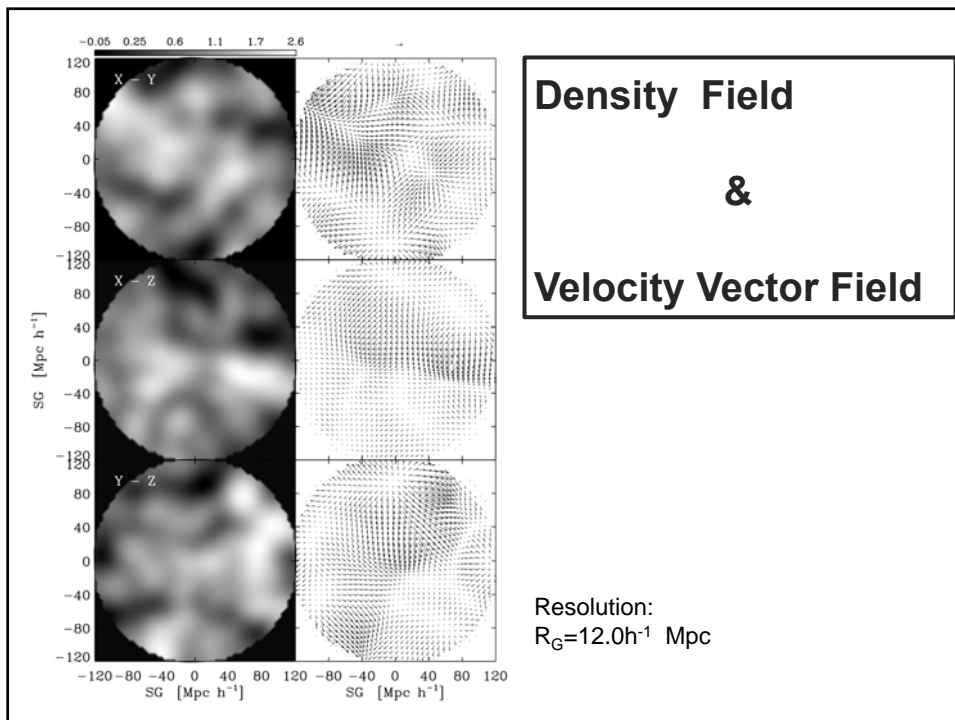
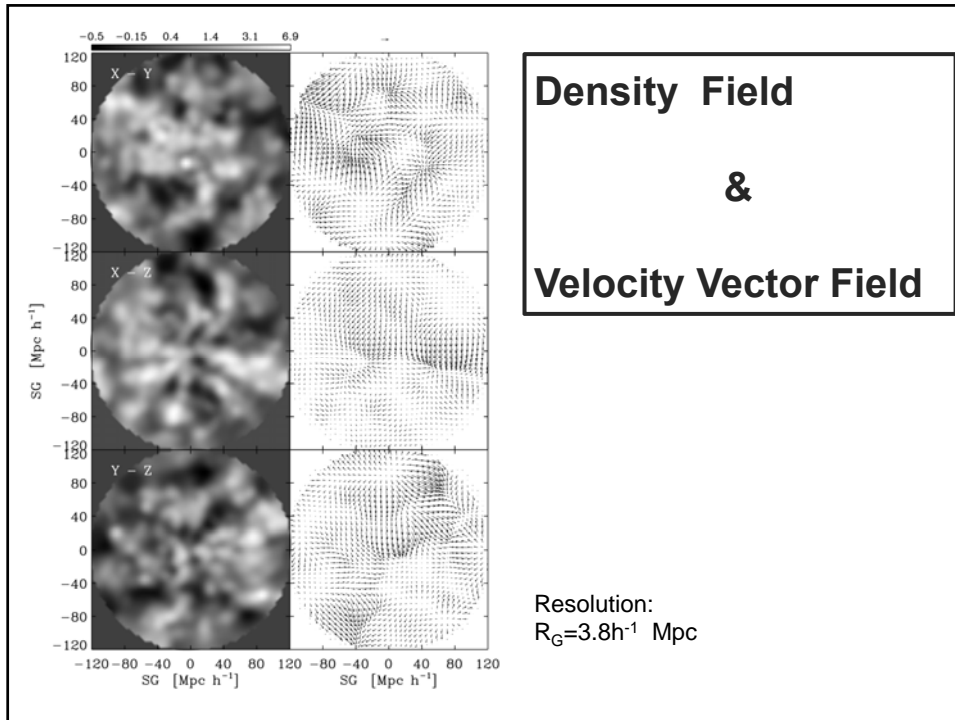


Void Velocity Flow Field



**Density Field
Velocity Field
superposition**

- Flow throughout the volume restored
- Restored velocities volume-weighted
- Shot-noise suppressed
- assumption: no shell-crossing



Phase-Space Dynamics Cosmic Web:

the Phase-Space Sheet

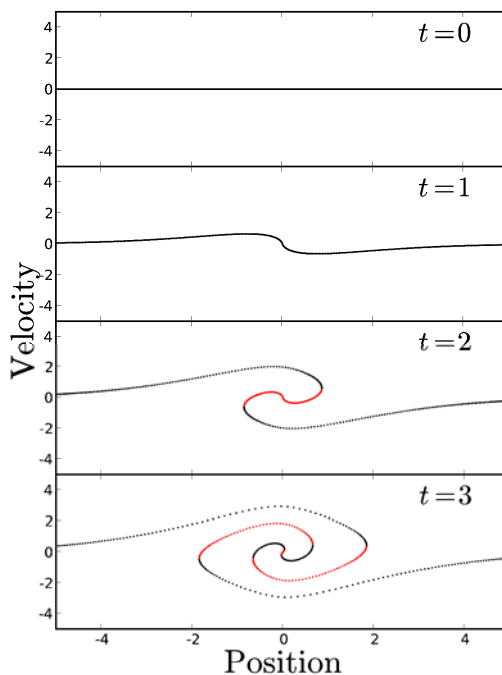
Phase Space Evolution

Dark Matter Phase Space sheet:

3-D structure projection of a
folding DM phase space sheet
In 6-D phase space

- Shandarin 2010, 2011
- Neyrinck et al. 2011, 2012
Origami
- Abel et al. 2011

Evolving matter distribution in
position-velocity space – 1D

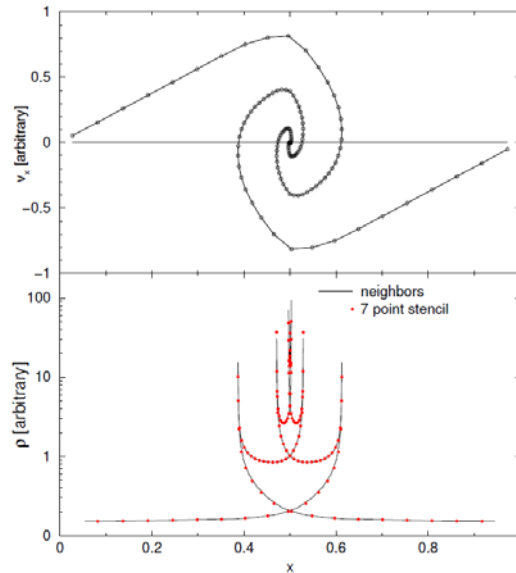


Phase Space Evolution

Phase space:
Velocity vs. Position



Density:
 $\rho(\vec{x}, t) = \int f(\vec{x}, \vec{v}, t) d\vec{v}$



Lagrangian-Eulerian Phase Space

To follow evolving phase-space of cosmic structure, it is sometimes insightful to consider a coordinate transformation of 6D phase-space:

Eulerian coordinates \vec{x} and Eulerian coordinates \vec{q} of a mass element:

$$f(\vec{x}, \vec{q})$$

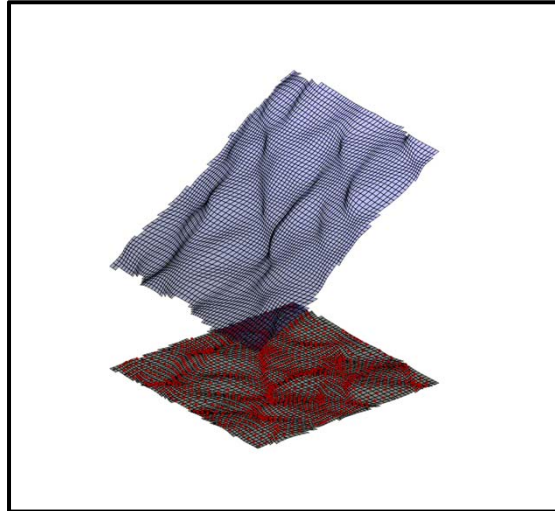
Note that in Zeldovich approximation, the velocity of a mass element is:

$$\vec{v}(\vec{q}, t) = -a(t)D(t)f(\Omega) \vec{\nabla}\Phi(\vec{q})$$

Tessellation Deformation & Phase Space Projection

Translation towards Multi-D space:

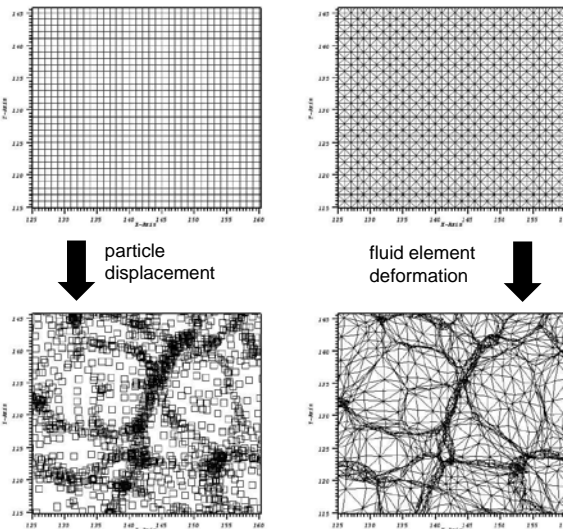
- Look at deformation of initial tessellation
- each tessellation cell represents matter cell
- evolution deforms cell
- once cells start to overlap, manifestation of different phase-space matter streams



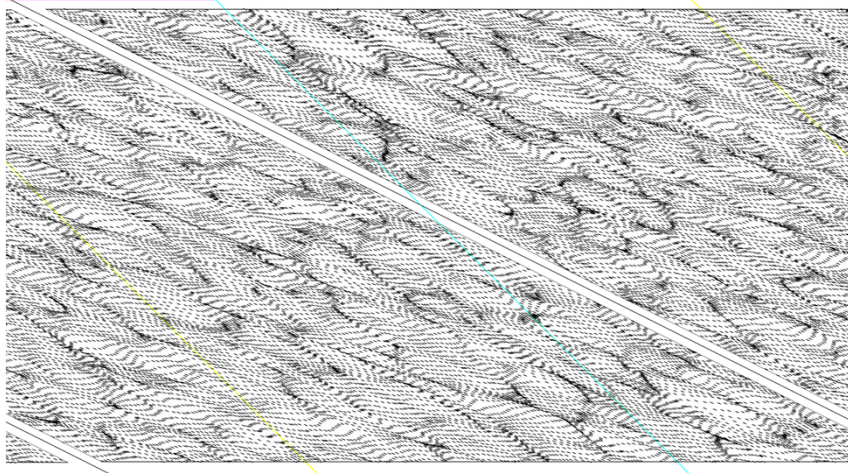
Tessellation Deformation & Phase Space Projection

Translation towards Multi-D space:

- Look at deformation of initial tessellation
- each tessellation cell represents matter cell
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- once cells start to overlap, manifestation of different phase-space matter streams



Particle Simulation



Mass Element Evolution

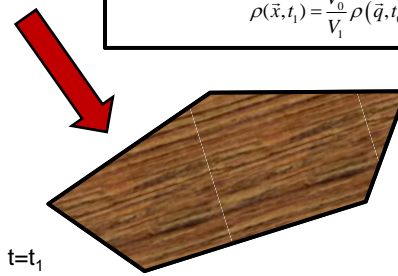
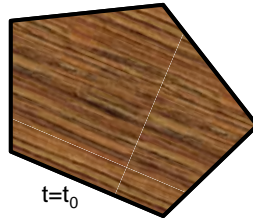


Tessellation Deformation & Phase Space Projection

Translation towards
Multi-D space:

- Look at deformation of initial tessellation
- each tessellation cell represents matter cell
- evolution deforms cell

Monostream
Density Evolution



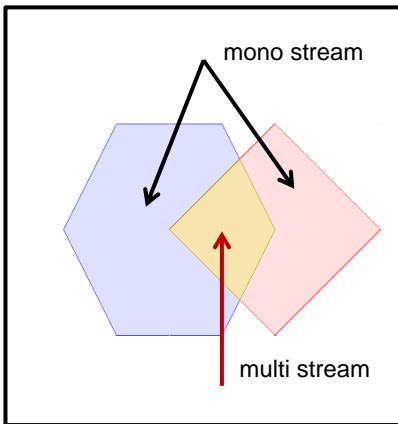
Conservation of mass
(continuity eqn.):

$$\rho(\vec{x}, t) = |J(\vec{x}, \vec{q})|^{-1} \rho(\vec{q}) = \left| \frac{\partial \vec{x}}{\partial \vec{q}} \right|^{-1} \rho(\vec{q})$$

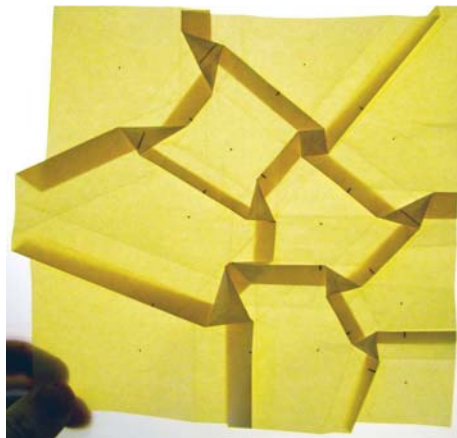


$$\rho(\vec{x}, t_1) = \frac{V_0}{V_1} \rho(\vec{q}, t_0)$$

(Cosmic) ORIGAMI

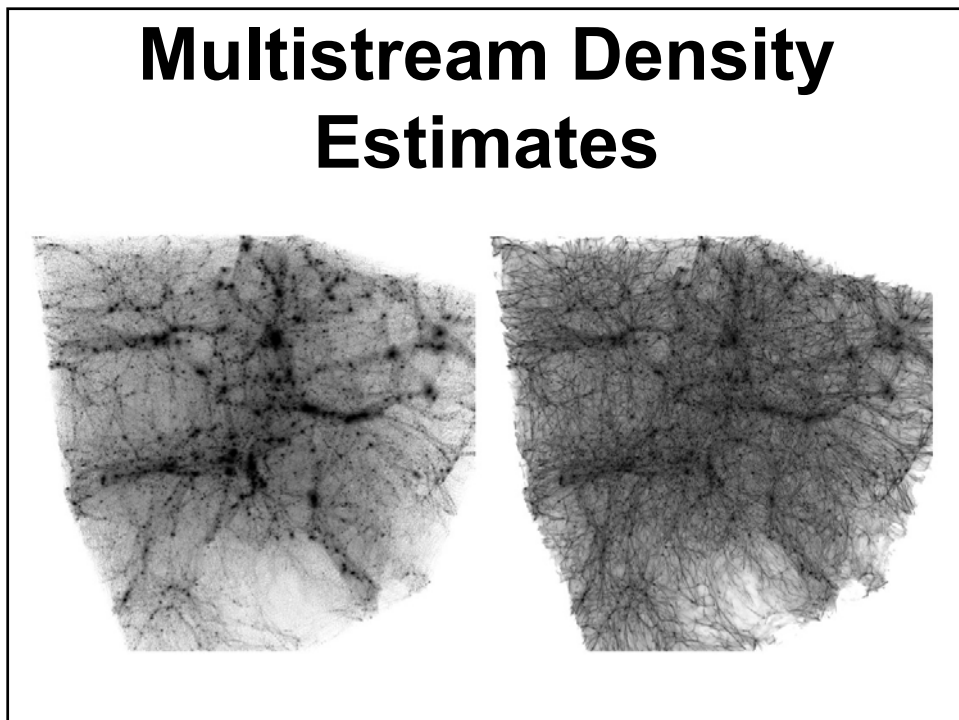
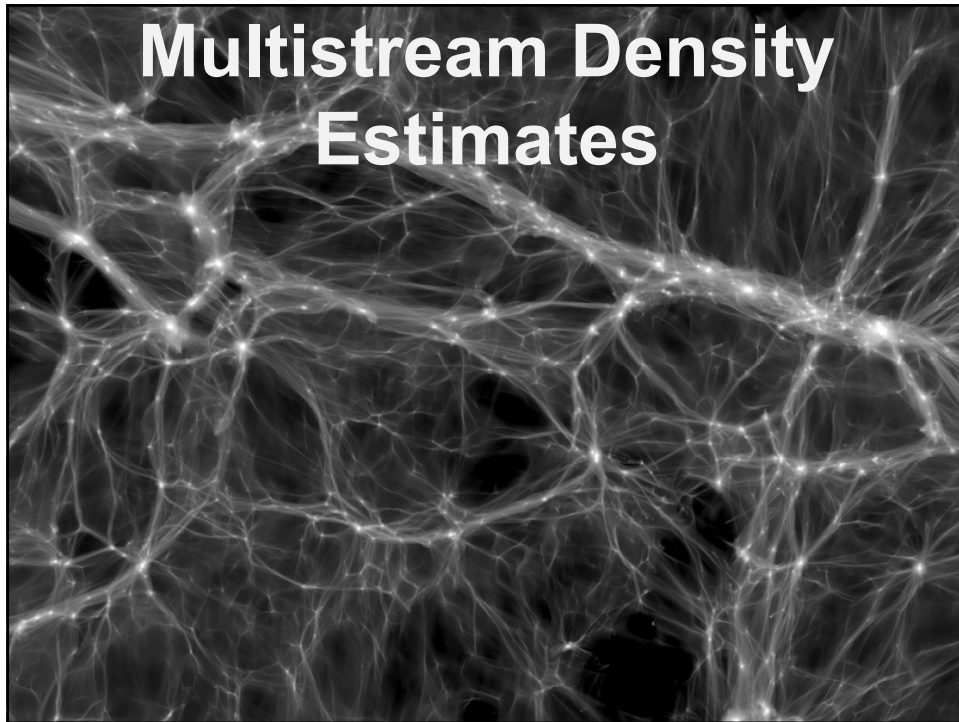


Evolution of dynamical system:
Phase-space folding – Cosmic Origami



Mark Neyrinck

$$\rho_{total}(\vec{x}, t_1) = \sum_i \frac{V_{0i}}{V_{1i}} \rho(\vec{q}_i, t_0)$$



Cosmic Web Stream Density

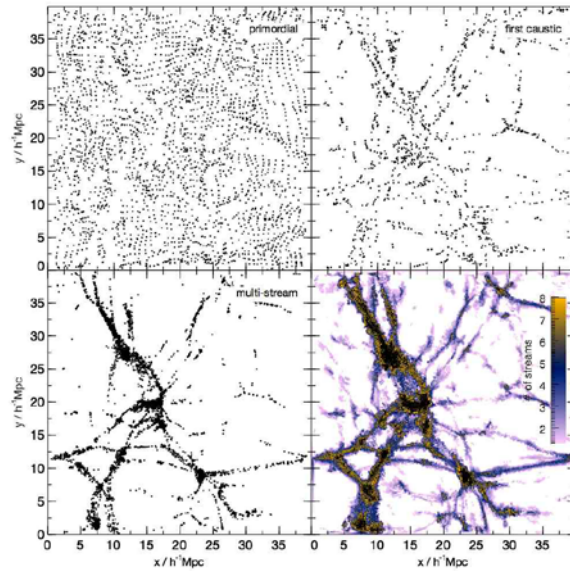
Translation towards
Multi-D space:

Density of
dark matter streams:

- # phase space folds

=

locally overlapping
tessellation cells



Origins:

anisotropies in CMB

