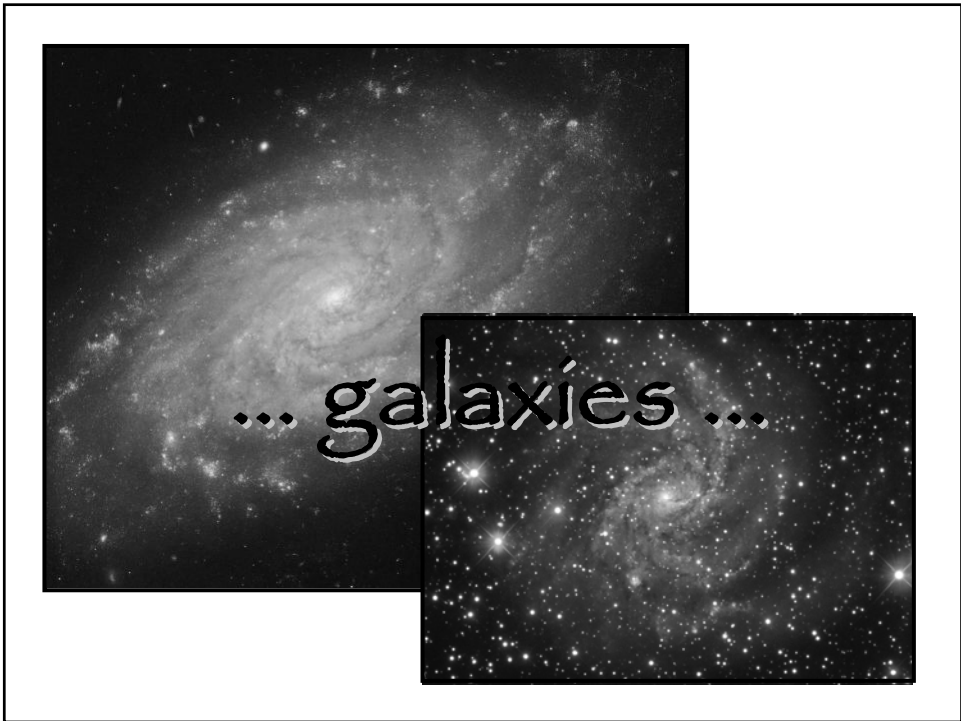
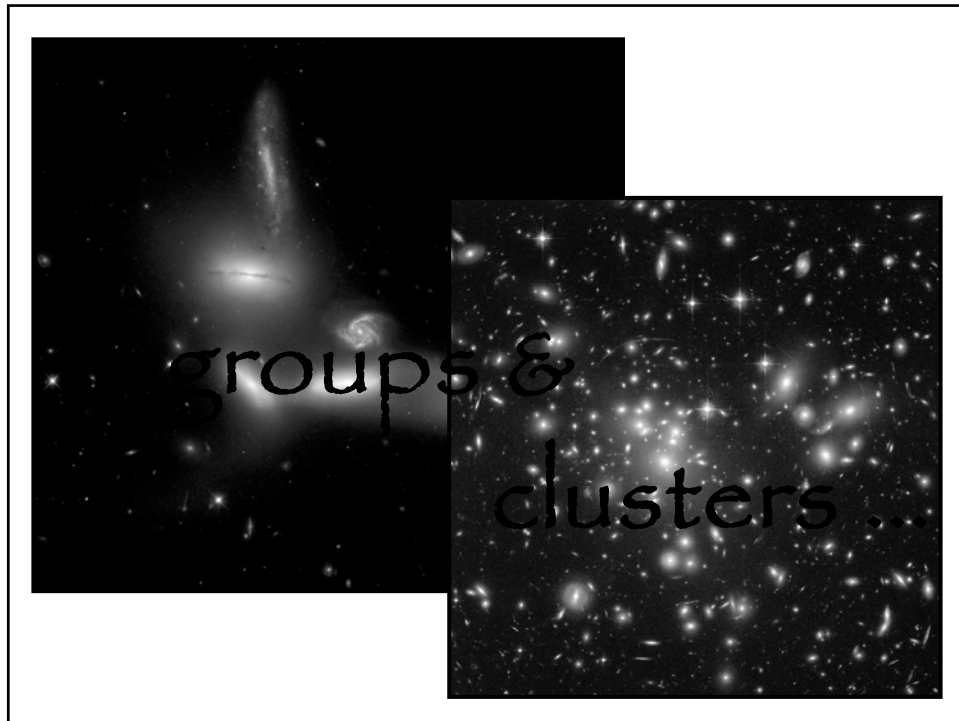


# Structure in the Universe





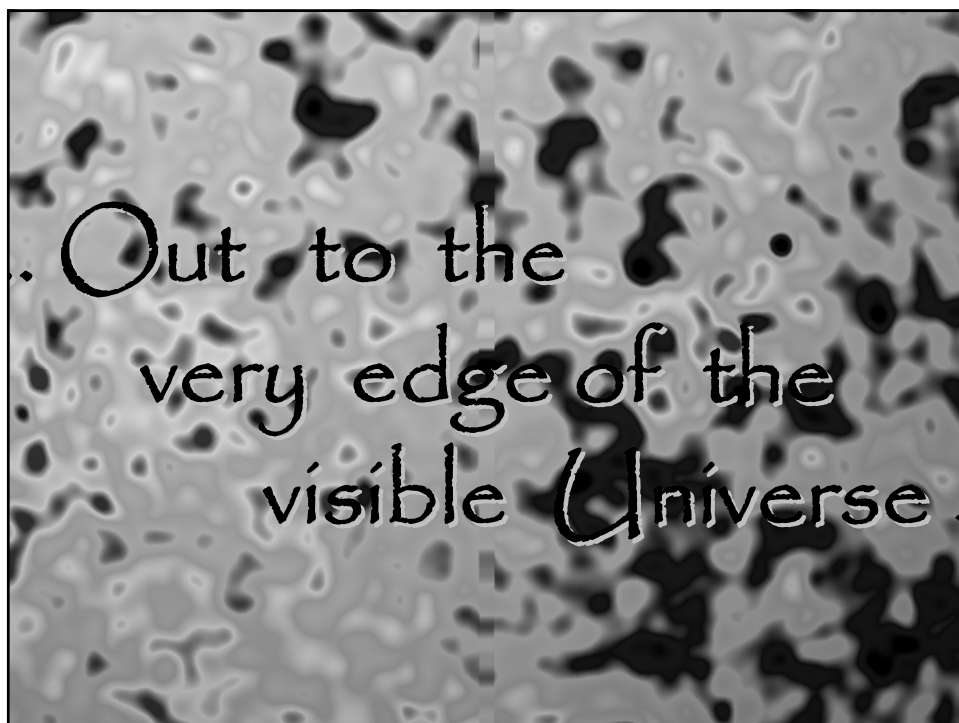




... Out to the  
furthest realms  
galaxies roaming...

A black and white image of a star field, showing numerous bright stars of varying sizes and colors, set against a dark background. The text is overlaid in a white, serif font.

... into the regions  
with the First Stars  
setting ablaze  
the skies ...

A black and white image of a star field, showing numerous bright stars of varying sizes and colors, set against a dark background. The text is overlaid in a white, serif font.

. Out to the  
very edge of the  
visible Universe .

Central Theme:

Cosmic Enigma

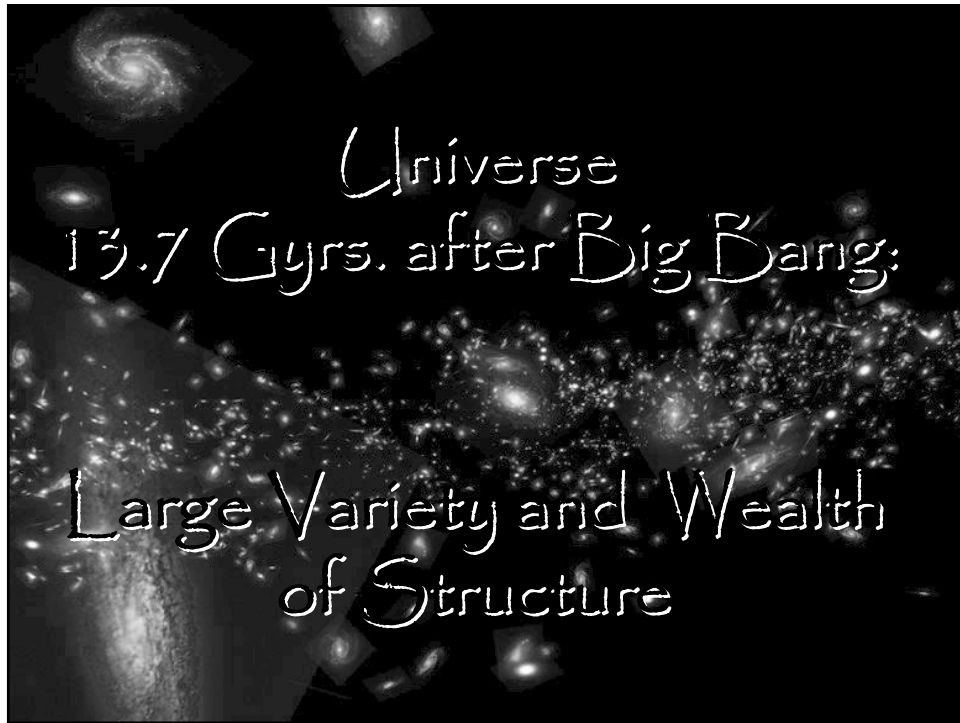
Universe

379,000 years after Big Bang

almost perfectly smooth

Microwave Background Radiation, surface of last scattering of cosmic photons is almost perfectly isotropic, all around the same temperature:

$T=2.725 \text{ K}$



### The Early Universe:

Almost perfectly homogeneous and isotropic,  
without any discernable structure ...

How did the present wealth and variety of  
structure emerge out of  
an almost featureless, pristine early Universe  
?????

Cosmic Paradigm:

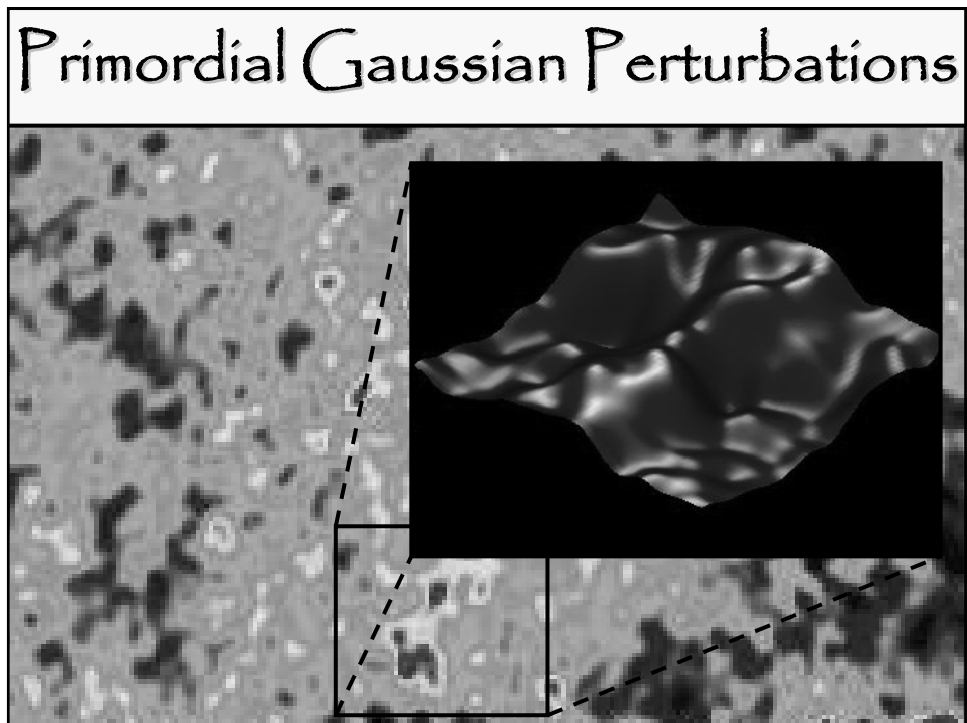
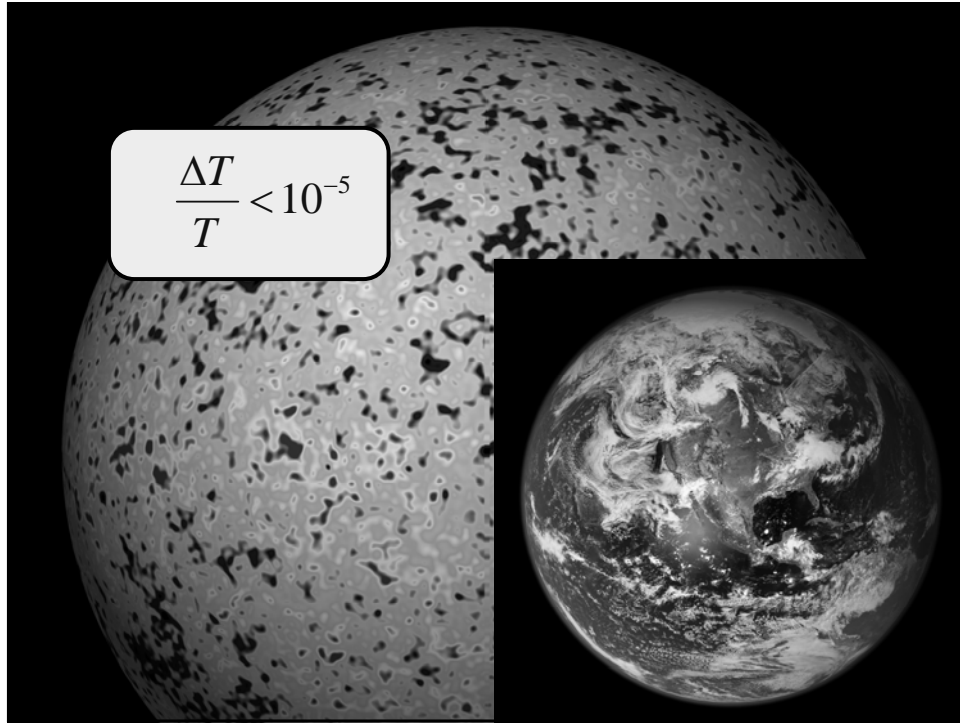
Gravitational  
Instability

## Ripples in the Universe

Tiny density perturbations in  
Early Universe:

- Origin: Quantum Fluctuations expanded to superhorizon scale during Inflation
- Gaussian Noise !!!
- Primordial Gaussian Density & Velocity Perturbations visible as corresponding Radiation Temperature Perturbations in Cosmic Microwave Background Radiation (CMB) Radiation





# Cosmic Structure Formation

After decoupling, density perturbations in the matter distribution gradually develop into forming structures by means of the “gravitational instability” mechanism. The origin of these density perturbations is still an unsettled issue. Their presence, however, has been proven beyond doubt: their imprint in the CMB beautifully confirmed by COBE and WMAP.

Hidden in the depths of the very first instances of the early universe, at present the most viable suggestion is that it concerns quantum fluctuations blown up to macroscopic proportions in an inflationary phase of cosmic expansion.

In the later phases of more “quiescent” cosmic expansion, density fluctuations, frozen while they have the superhorizon scale assumed in inflation, gradually enter the horizon (i.e they are overtaken).

From that instant on they can start growing!

$$\delta(\mathbf{x}, t) \equiv \frac{\rho(\mathbf{x}, t) - \bar{\rho}(t)}{\bar{\rho}(t)}$$

$$\delta(\mathbf{x}) = \int \frac{d\mathbf{k}}{(2\pi)^3} \hat{\delta}(\mathbf{k}) e^{-i\mathbf{k}\cdot\mathbf{x}}$$

# Gravitational Instability

Density Perturbations  
correspond to

GRAVITY PERTURBATIONS

# Gravitational Instability



$$\mathbf{g}(\mathbf{r}, t) = -\frac{1}{a} \nabla \phi = \frac{3\Omega H^2}{8\pi} \int d\mathbf{x}' \delta(\mathbf{x}', t) \frac{(\mathbf{x}' - \mathbf{x})}{|\mathbf{x}' - \mathbf{x}|^3}$$

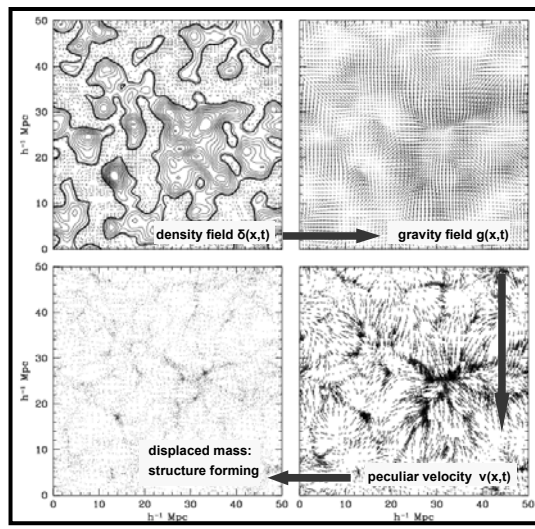
# Cosmic Structure Formation

The gravity perturbations induce cosmic flows of matter. High density regions start to contract and finally collapse, assembling more and more matter from their surroundings.

By contrast, as matter is moving out of them, low density regions turn into empty void regions.

Gradually, dependent on scale, we see the emergence of cosmic structures.

These days we can simulate the characteristics of the process through large computer simulations. Successful confrontation with the observational reality has given confidence in our understanding.



# Millennium Simulation

Millennium  
Simulation:  
LCDM

500 Mpc/h

(courtesy:  
Virgo/V. Springel).

# Millennium Simulation

Millennium  
Simulation:  
LCDM

500 Mpc/h

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# Millennium Simulation

Millennium  
Simulation:  
LCDM

500 Mpc/h

(courtesy:  
Virgo/V. Springel).

# Millennium Simulation

Millennium  
Simulation:  
LCDM

125 Mpc/h

(courtesy:  
Virgo/V. Springel).

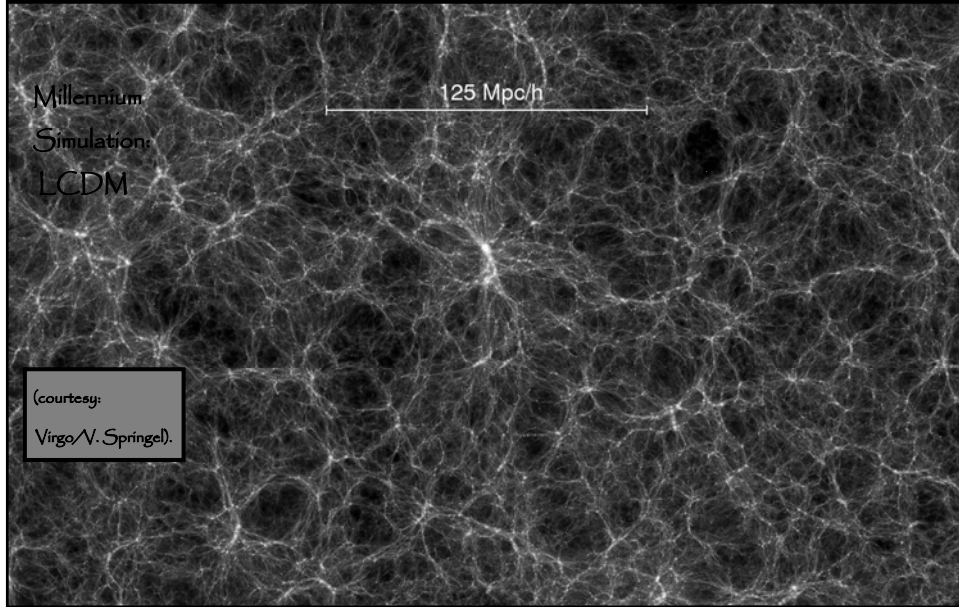
# Millennium Simulation

Millennium  
Simulation:  
LCDM

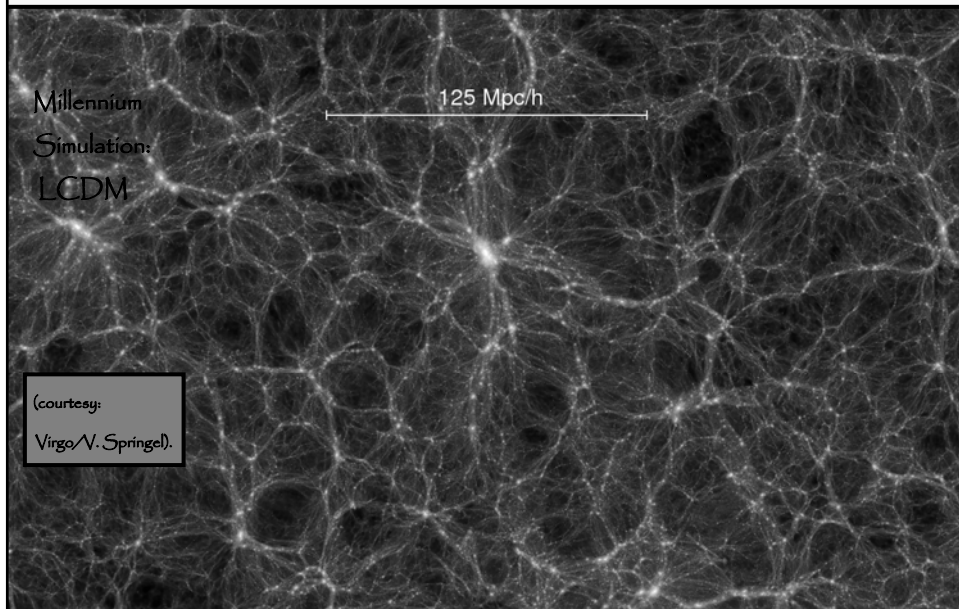
125 Mpc/h

(courtesy:  
Virgo/V. Springel).

# Millennium Simulation



# Millennium Simulation



# Millennium Simulation

Millennium  
Simulation:  
LCDM

31.25 Mpc/h

(courtesy:  
Virgo/V. Springel).

# Millennium Simulation

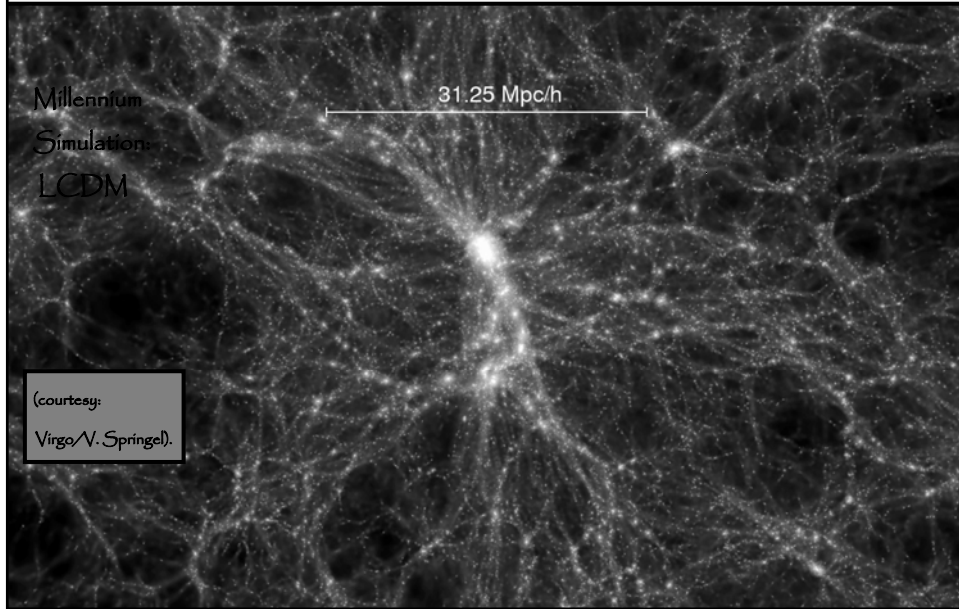
Millennium  
Simulation:  
LCDM

31.25 Mpc/h

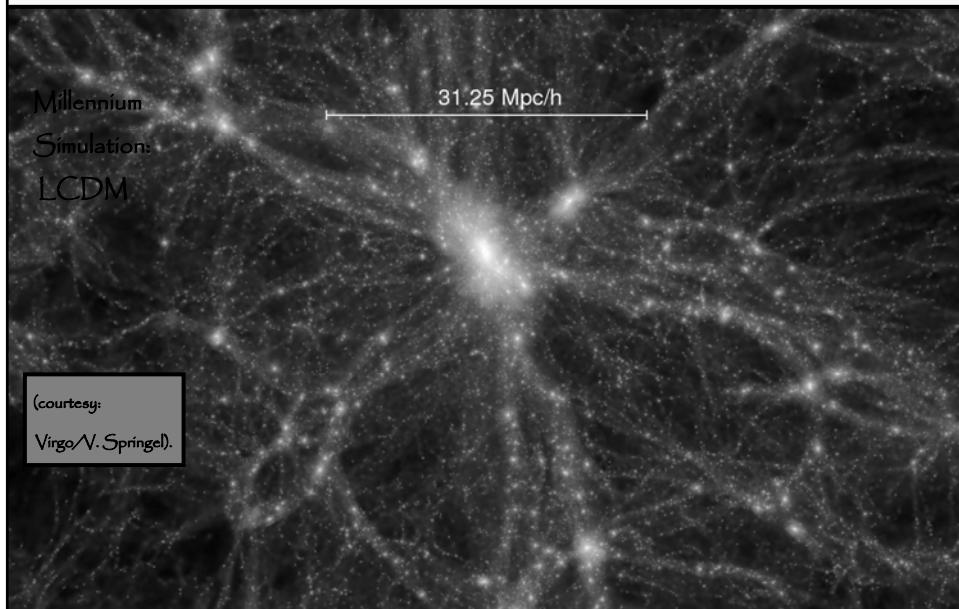
(courtesy:  
Virgo/V. Springel).



# Millennium Simulation



# Millennium Simulation



# Gravitational Instability

## Perturbation Development:

- Generation: - .... Inflationary Phase?
  - Gaussian Quantum Noise inflated to Cosmic Scale
- Superhorizon: - As long as perturbations superhorizon, no evolution
- Linear Growth: - Density & Velocity perturbations tiny
  - Can be described analytically!
- Nonlinear Growth: - Interaction between fluctuations over range of scales
  - Emergence complex patterns & formation objects
  - Only analytical approximations,
    - Computer (N-body) simulations necessary

# Cosmic Structure Formation

Once the first linear phase of structure formation has passed, we start to recognize the emergence of genuine cosmic structures.

Three generic properties nonlinear structure formation:

- hierarchical structure formation
- anisotropic collapse
- void formation:
  - asymmetry
  - overdense vs. underdense

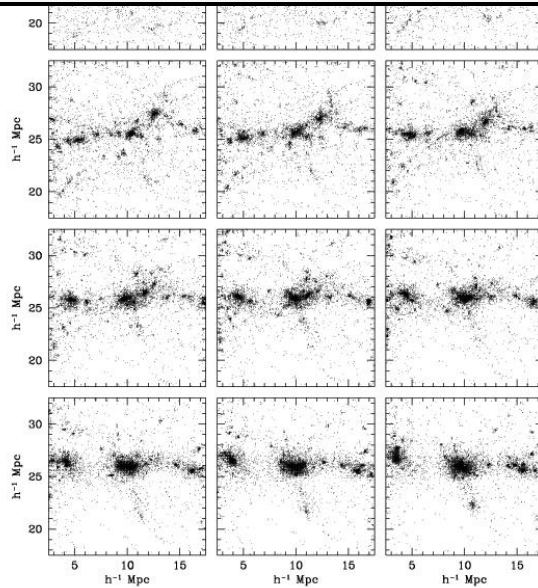
# Hierarchical Structure Formation

Small structures form first, then merge into larger and larger features.

## 1. Hierarchical Structure Formation

Structures in the Universe form  
by  
gradual hierarchical assembly:

- ❖ small objects emerge & collapse first
- ❖ merge with other clumps while forming larger object in hierarchy



# Anisotropic Structure Formation

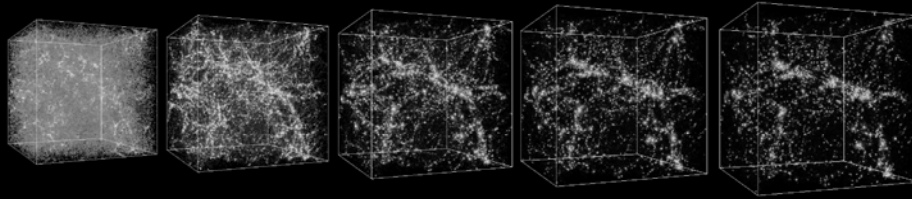
Structures tend to collapse into anisotropic filamentary and planar structures

## II. Anisotropic Collapse

- Gravitational Instability:
  - any small initial deviation from sphericity of a collapsing cloud gets magnified
  - gravitational collapse proceeds along sequence:

• collapse along smallest axis	→	planar geometry	←	wall
• collapse medium axis	→	elongated	←	filament
• full 3-D collapse	→	clump	←	clump/halo

- After having collapsed into a clump, virialization and emergence cosmic object



# Asymmetric Structure Formation: Void Dominance

While matter aggregates into ever denser and compacter structures, underdense void regions assume dominance in terms of occupied space.

## III. Void Formation

### Origin of Voids:

- Voids natural product gravitational instability
- Voids evolve out of primordial underdensities:
  - Underdensity       $\Rightarrow$
  - Gravity Deficit       $\Rightarrow$
  - Matter Emigration
- Primordial Density Troughs  $\Rightarrow$  Present-Day voids

# Structure Formation:

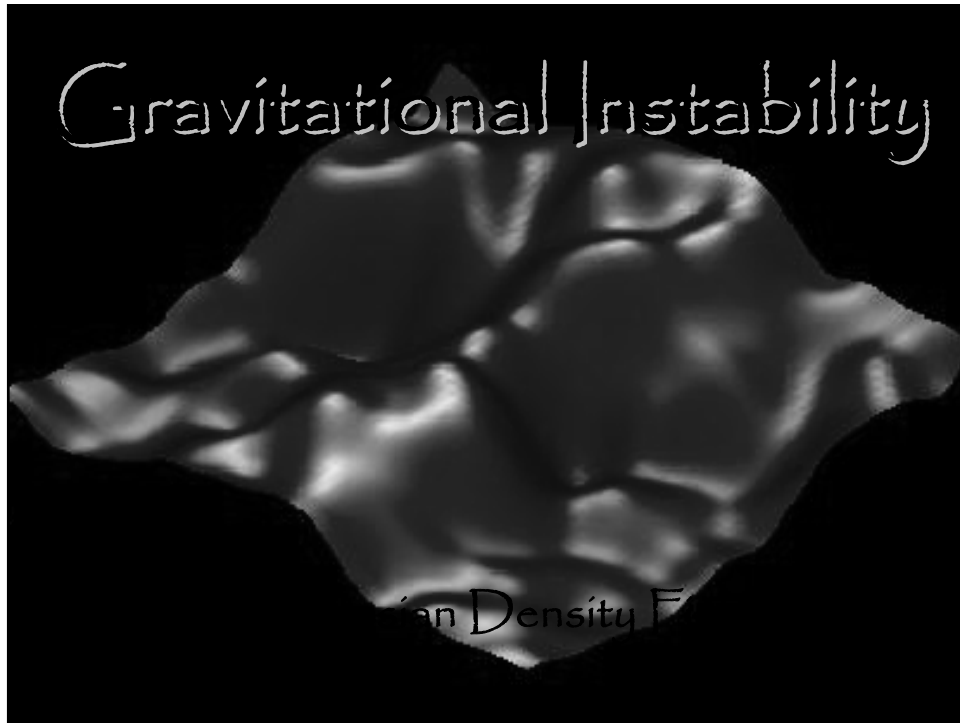
## Power Spectrum

# Gravitational Instability

$$\delta(\mathbf{x}, t) \equiv \frac{\rho(\mathbf{x}, t) - \bar{\rho}(t)}{\bar{\rho}(t)}$$

$$\delta(\mathbf{x}) = \int \frac{d\mathbf{k}}{(2\pi)^3} \hat{\delta}(\mathbf{k}) e^{-i\mathbf{k}\cdot\mathbf{x}}$$

... perturbations in the



## Gaussian Perturbations

$$P_N = \frac{\exp \left[ -\frac{1}{2} \sum_{i=1}^N \sum_{j=1}^N f_i (M^{-1})_{ij} f_j \right]}{[(2\pi)^N (\det M)]^{1/2}} \prod_{i=1}^N df_i$$

↑

$$M_{ij} \equiv \langle f(\mathbf{x}_i) f(\mathbf{x}_j) \rangle = \xi(\mathbf{x}_i - \mathbf{x}_j) = \xi(|\mathbf{x}_i - \mathbf{x}_j|)$$

Gaussian perturbations represent the simplest stochastic field of fluctuations imaginable. It is fully and completely characterized by its second-order moment, the autocorrelation function  $\xi(r)$ .

In fact, by concentrating on the contributions of the various scales and describing the field in terms of its Fourier components, we directly see that the FUNDAMENTAL function fully characterizing the Gaussian field

## Power Spectrum $P(k)$

$$(2\pi)^3 P(k_1) \delta_D(\mathbf{k}_1 - \mathbf{k}_2) = \langle \hat{f}(\mathbf{k}_1) \hat{f}^*(\mathbf{k}_2) \rangle$$

Arguably, the power spectrum is the single most important function for our understanding of the cosmic structure formation process.

## Power Spectrum

- Direct Characterization of contribution on different scales to inhomogeneous matter distribution
- First direct measure of inhomogeneities in spatial matter distribution
- Along with its Fourier transform, the autocorrelation function  $\xi(r)$
- For Gaussian primordial field, full characterization of density field
- Directly related to potential and velocity perturbations
- Encapsulates all relevant physical processes in early Universe affecting the primordial evolution density/potential/velocity perturbations
- Highly sensitive to constituency of Universe (nature dark matter, etc.)
- This is what the early (inflationary) Universe gives us !!!



# Cosmic Power Spectrum

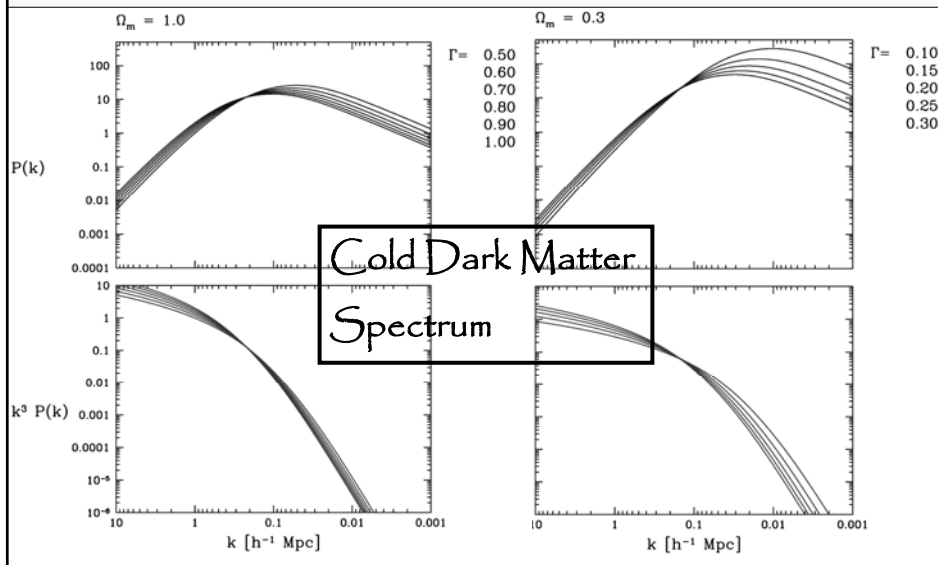
$$P(k) \propto \frac{k^n}{[1 + 3.89q + (16.1q)^2 + (5.46q)^3 + (6.71q)^4]^{1/2}} \times \frac{[\ln(1 + 2.34q)]^2}{(2.34q)^2},$$

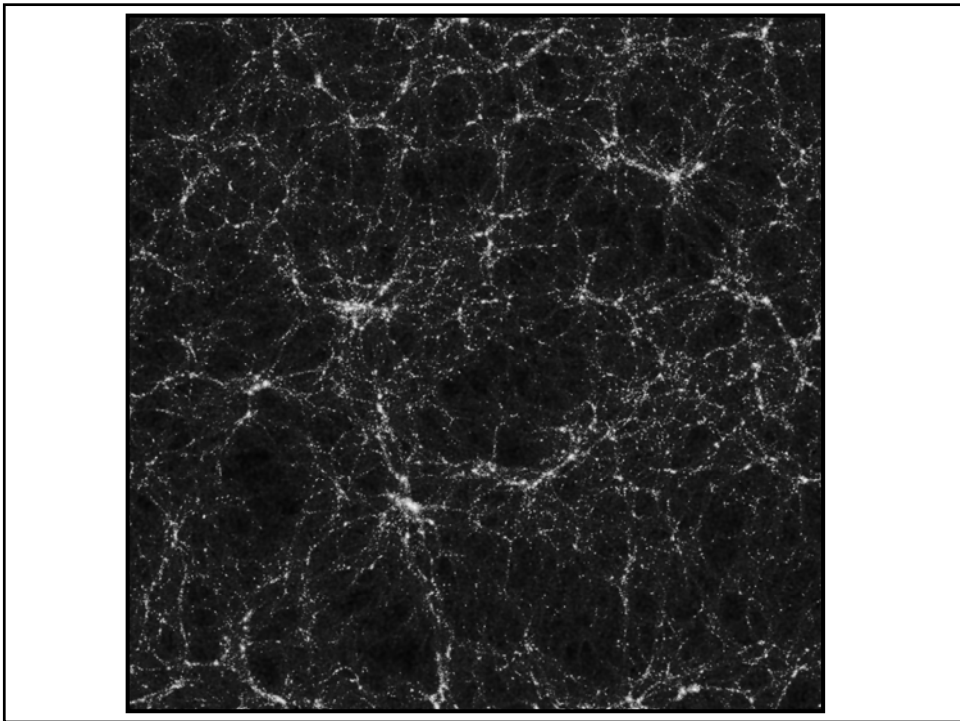
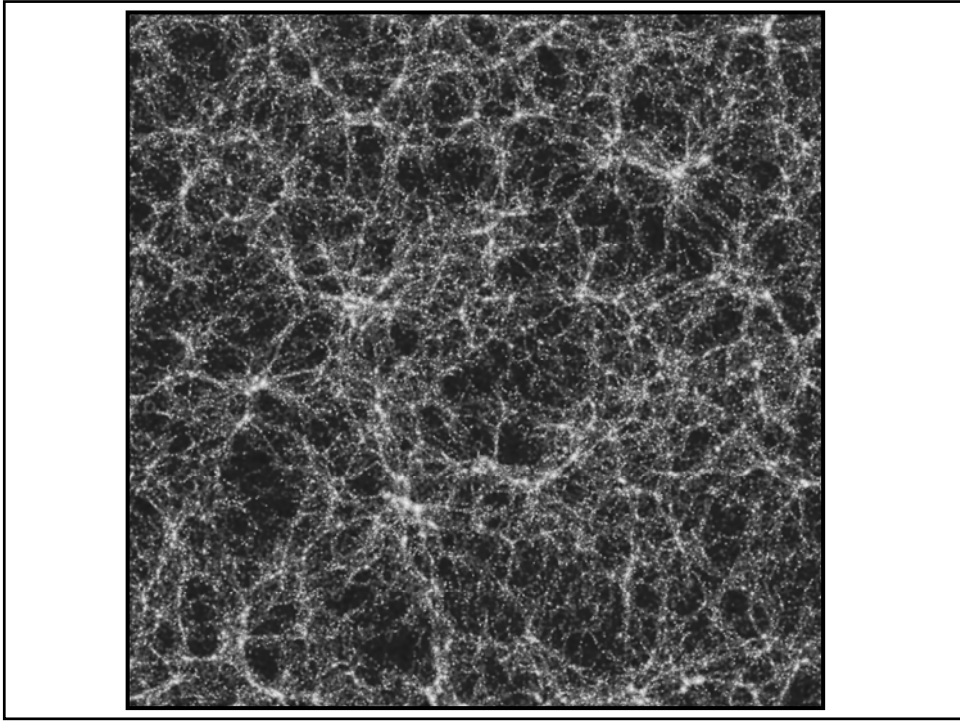
$$q = k/\Gamma$$

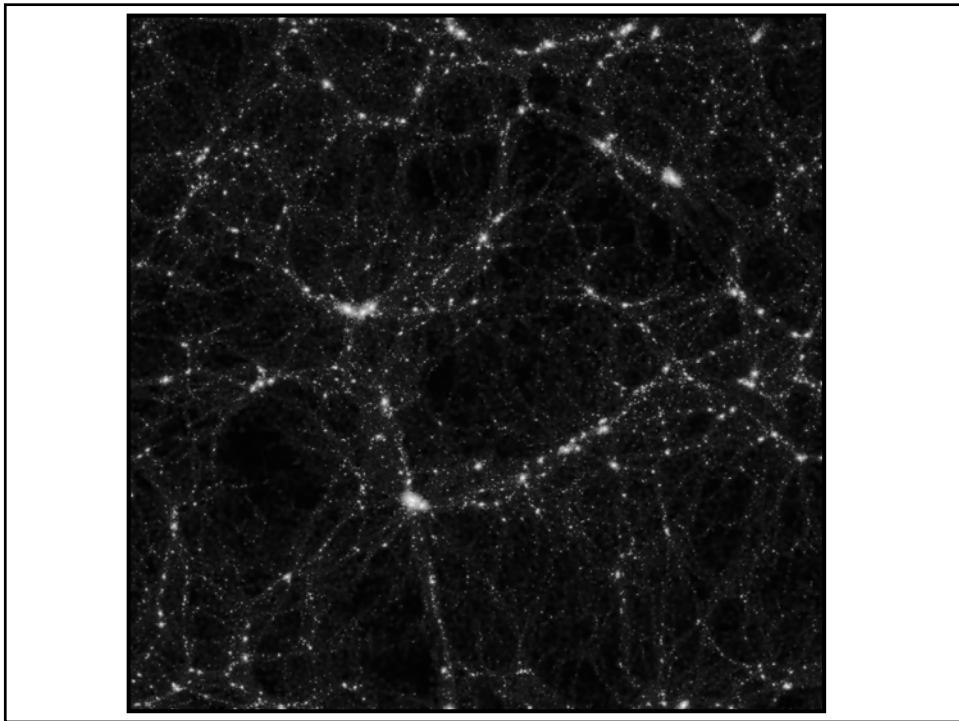
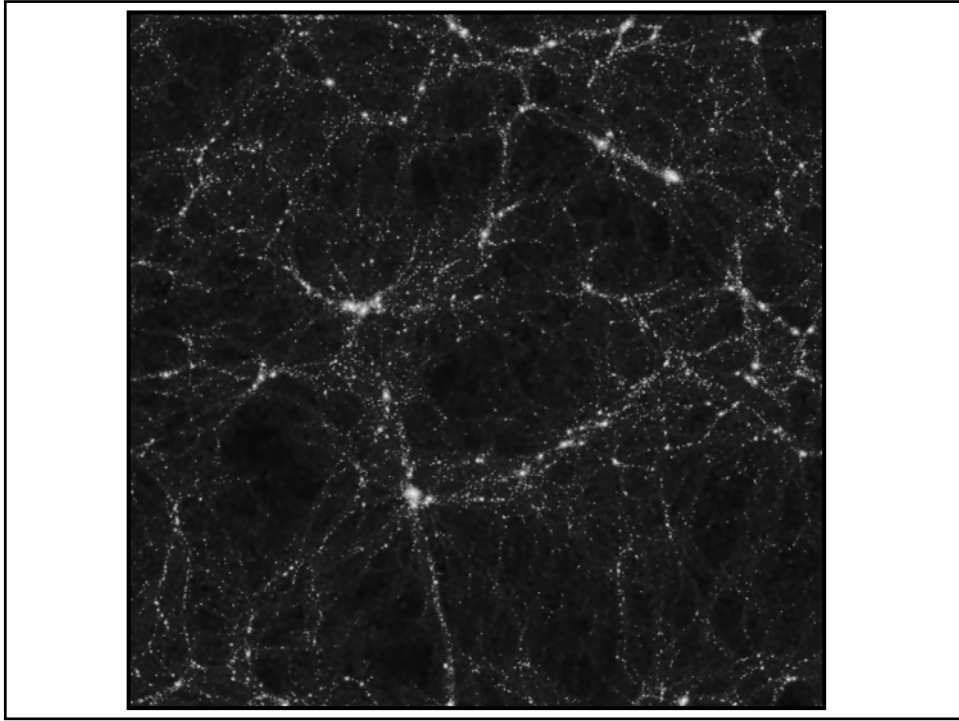
$$\Gamma = \Omega_0 h \exp(-\Omega_b - \Omega_b/\Omega_0)$$

Cold Dark Matter  
Spectrum

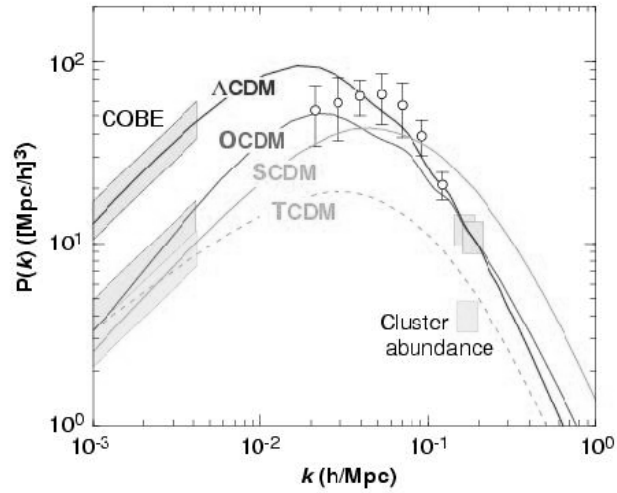
# Cosmic Power Spectrum



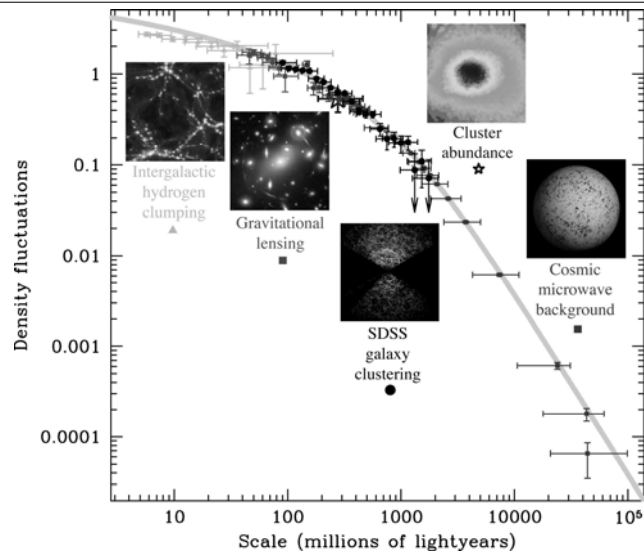




# Cosmic Power Spectrum



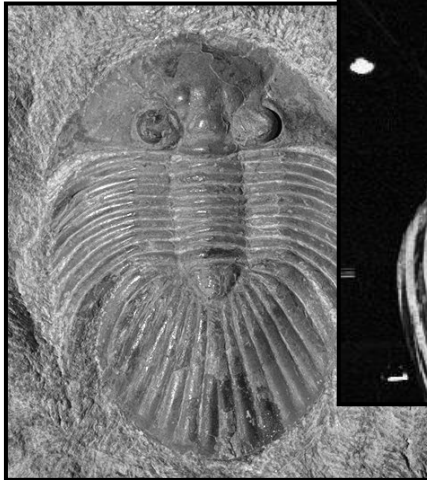
# Cosmic Power Spectrum



Cosmic

Fossils

Cosmic Fossils ?



# Cosmic Fossils

Which cosmic object contain direct information on emergence and growth of structure in the Universe ?

## Wanted:

- Structures in youthful evolutionary phase
- Direct link with their initial conditions
- On scales of Megaparsecs, and larger, gravitational collapse only just started

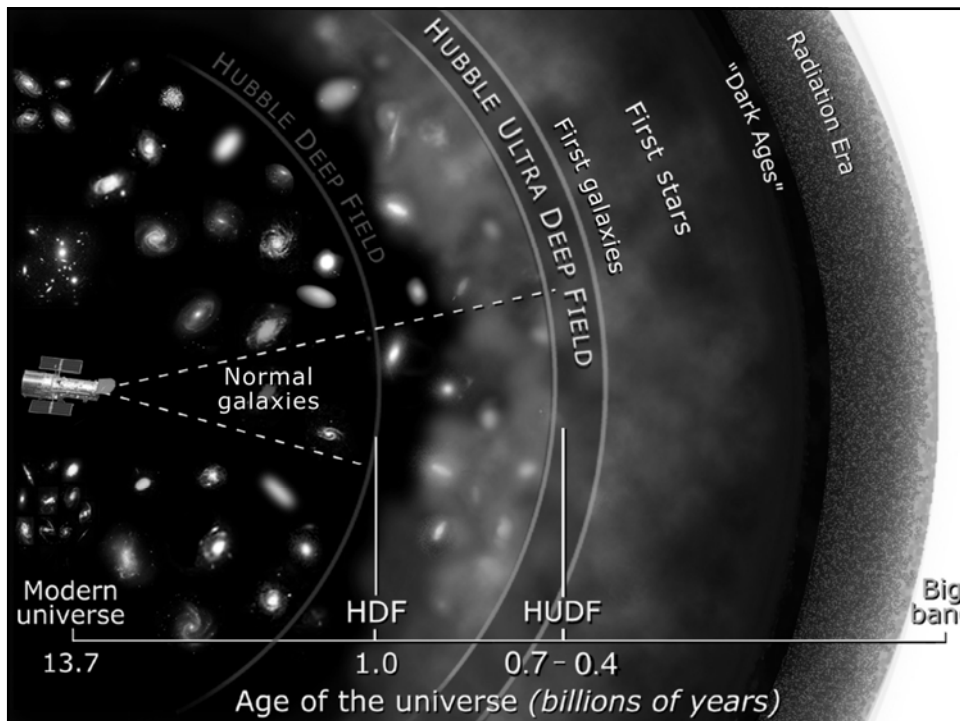
## Recall:

- visible (baryonic) matter but a fraction of total energy content Universe

$$\Omega_{rad} \approx 10^{-5}$$

$$\Omega_{matter} \approx 0.3$$

$$\Rightarrow \Omega_{\Lambda} \approx 0.7 \quad \Leftarrow$$



- Primordial Conditions:
  - temperature fluctuations in microwave background radiation
  - polarization Cosmic Microwave Background
  - treasure trove cosmological information
- Dynamics:
  - cosmic velocity flows
  - very difficult in practice, due to large uncertainties in distance estimate/measurements of galaxies, and hence the estimated deviations from Hubble expansion.
- Mass Distribution:
  - gravitational lensing of light by cosmic matter distribution
  - very promising, just started to yield significant results ...

- Galaxy Distribution:
  - galaxies supposed to be a fair reflection of underlying cosmic matter distribution
  - most detailed and investigated impression of cosmic matter distribution
    - nonlinear scales: tracing the Cosmic Web
    - Megaparsec linear scales: measuring the Power Spectrum
    - Gigaparsec linear scales: Baryonic Oscillations  
Primordial Power Spectrum
    - High redshift galaxies: tracing young Universe,  
early stages galaxy formation
  - But: formation and evolution of galaxies still a notoriously understudied problem, so that the relation between matter and galaxy distribution is as yet not unequivocally clear.
- Quasars & AGN
  - tracing the large scale matter distribution on scales of hundreds Mpc
  - but: largely unknown how they relate to the matter/galaxy distribution

- Clusters of Galaxies
  - spatial distribution tracer Cosmic Web
  - internal structure dictated by primordial perturbations
  - Hot intracluster gas ( $10^8$  K) - accurate tracer potential cluster
    - easily observable via X-rays
- Gaseous Cosmic Web
  - Baryonic gas traces the Cosmic Web:
 

Ly $\alpha$ forest	neutral hydrogen gas, mostly at high z
WHIM	shock-heated gas settled in cosmic web
- Distribution & Physical State Gas @ Dark Ages
  - First Stars & Galaxies
  - Reionization of baryonic gas: very sensitive measure cosmology
- Structure of Galaxies
  - Mass distribution galaxies
  - Internal phase-space structure galaxy haloes

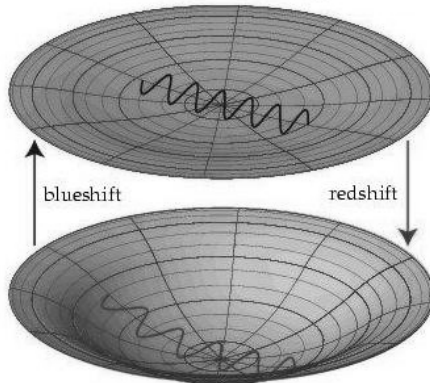
Embryonic Structure:

CMB:  
Rippling the Photons



# CMB Perturbations

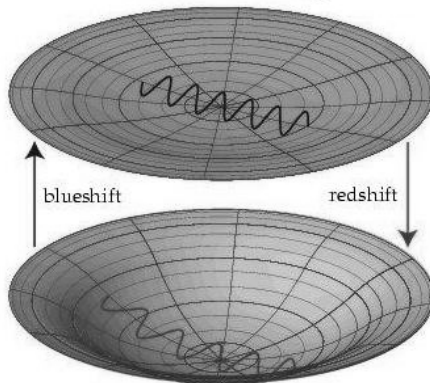
Metric Stretching



- As a result of perturbations in Gravitational potential photons experience frequency shift
- While travelling through perturbation:
  - Gravitational Redshift +
  - (Relativistic) Time Dilation
- Combined effect:  
Sachs-Wolfe Effect

# Sachs-Wolfe Effect

Metric Stretching



Sachs-Wolfe Effect

$$\frac{\Delta T}{T} \sim \frac{1}{3} \frac{\Delta \Phi}{c^2}$$

# Cosmic Microwave Background

COBE (1992):

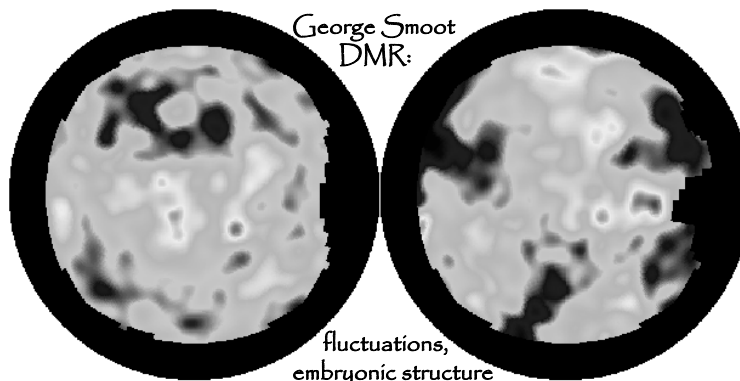
Accurate measurement  
Planck spectrum CMB

First detection angular  
temperature perturbations  
( $\theta \sim 7^\circ$ ): Sachs-Wolfe effect



## Primordial Anisotropies CMB sky

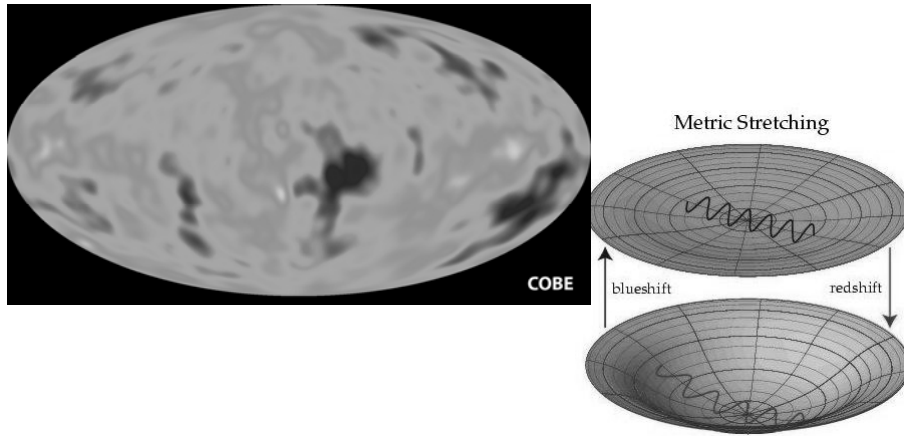
COBE-DMR Map of CMB Anisotropy



North Galactic Hemisphere      South Galactic Hemisphere

-100  $\mu\text{K}$   +100  $\mu\text{K}$

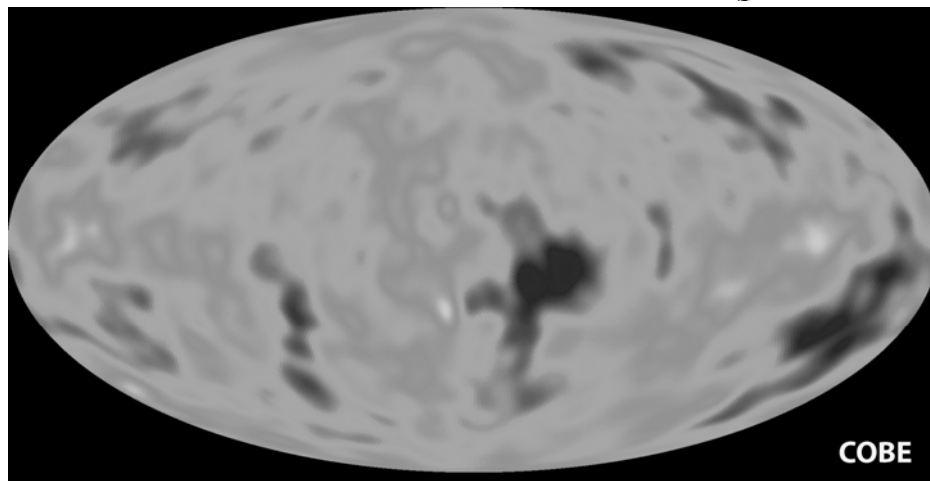
# Cosmic Microwave Background



Map of the Universe at Recombination Epoch:

- 379,000 years after Big Bang
- Superhorizon perturbations in gravitational potential (Sachs-Wolfe)
- $\Delta T/T < 10^{-5}$

# Cosmic Microwave Background

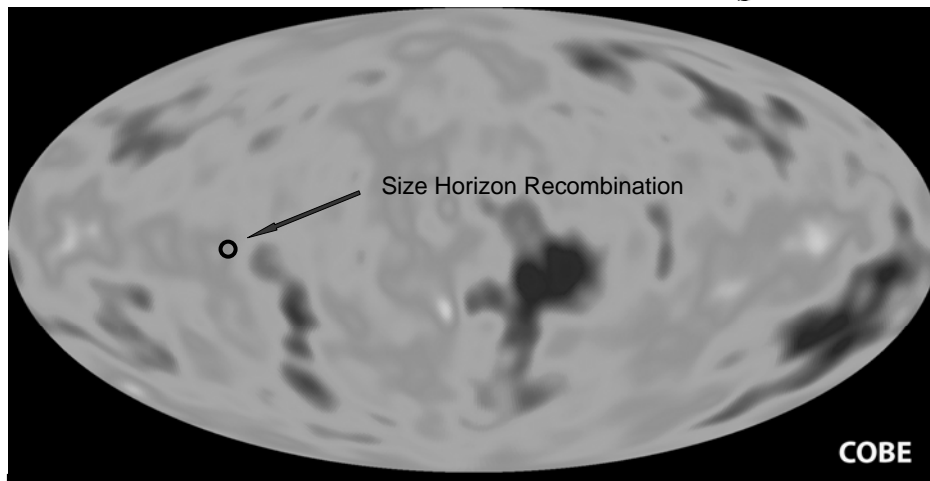


Map of the Universe at Recombination Epoch:

- 379,000 years after Big Bang
- Superhorizon perturbations in gravitational potential (Sachs-Wolfe)
- $\Delta T/T < 10^{-5}$

# Superhorizon Perturbations

## Cosmic Microwave Background

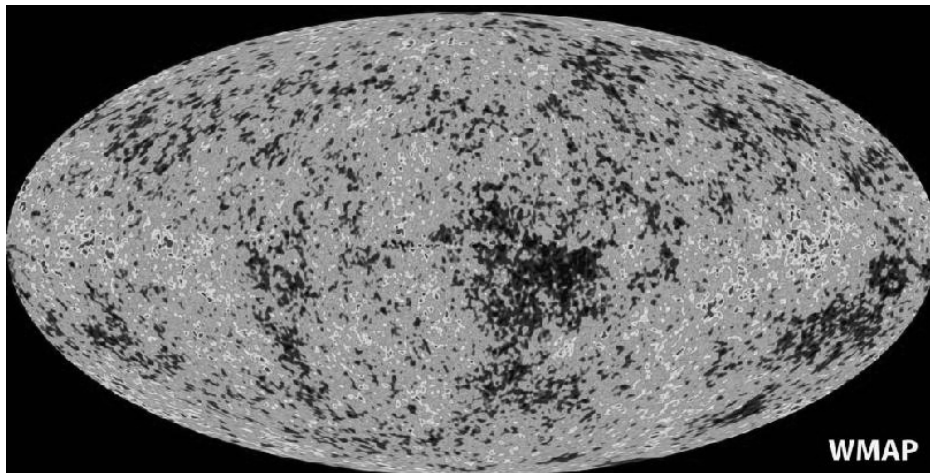


COBE measured fluctuations:  $> 7^\circ$   
Size Horizon at Recombination spans angle  $\sim 1^\circ$

How can it be that regions totally out of thermal contact, would have the same temperature ?

# Resolving Fluctuations

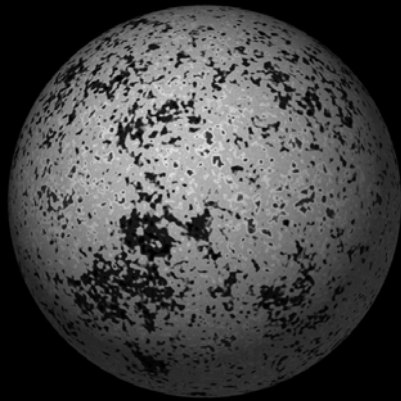
## Cosmic Microwave Background



Map of the Universe at Recombination Epoch:

- 379,000 years after Big Bang
- Subhorizon perturbations: primordial sound waves
- $\Delta T/T < 10^{-5}$

# Temperature Anisotropies

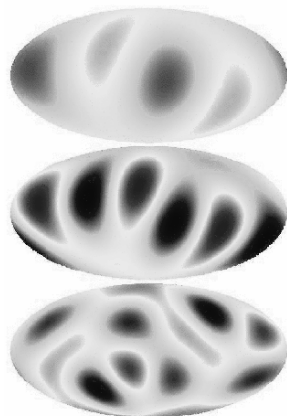


Temperature Perturbations in terms of Spherical Harmonics:

$$T(\theta, \phi) = \sum_{l,m} a_{lm} Y_l^m(\theta, \phi)$$

$$\phi \sim \frac{\pi}{l} \sim \frac{180^\circ}{l}$$

# Temperature Anisotropies

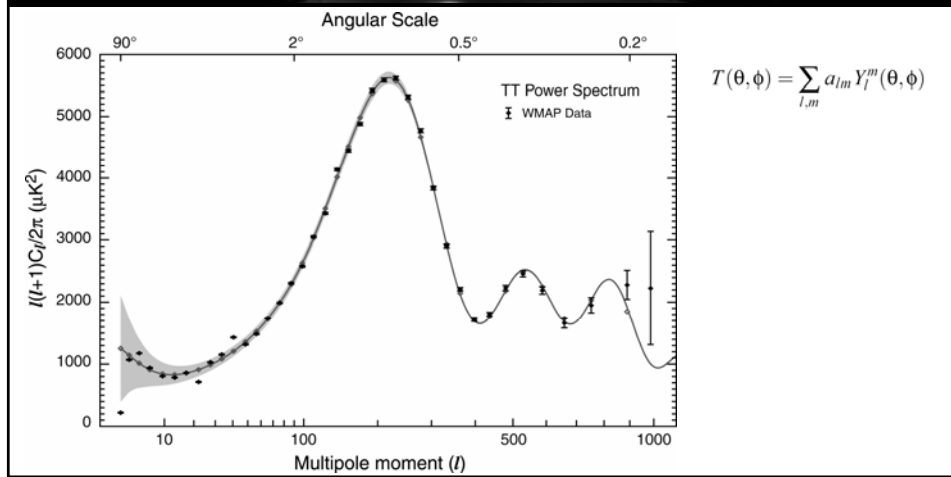


Temperature Perturbations in terms of Spherical Harmonics:

$$T(\theta, \phi) = \sum_{l,m} a_{lm} Y_l^m(\theta, \phi)$$

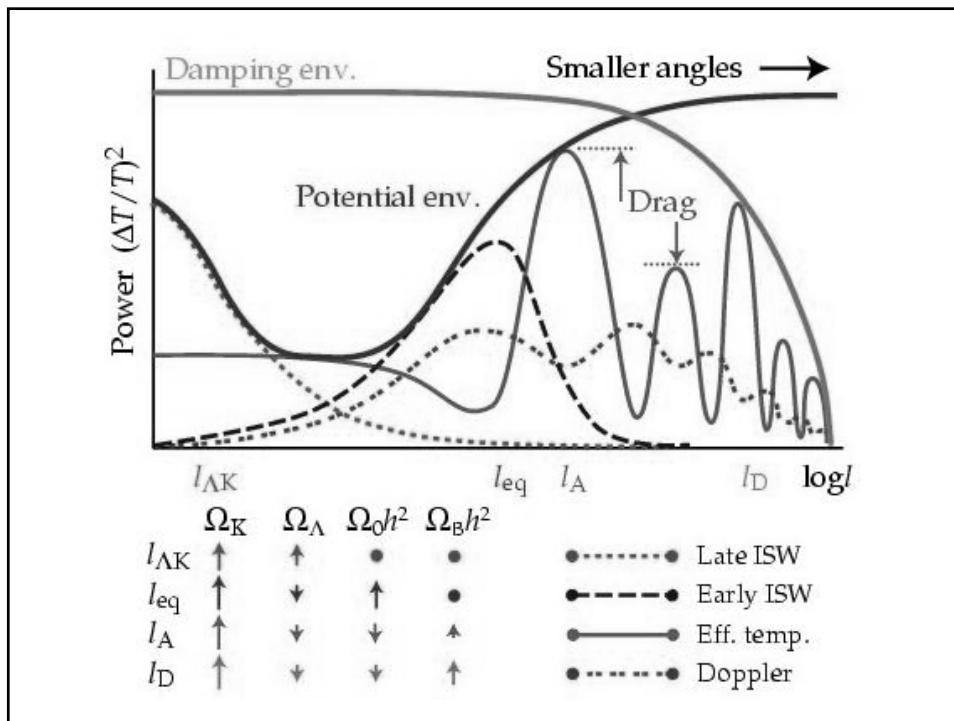
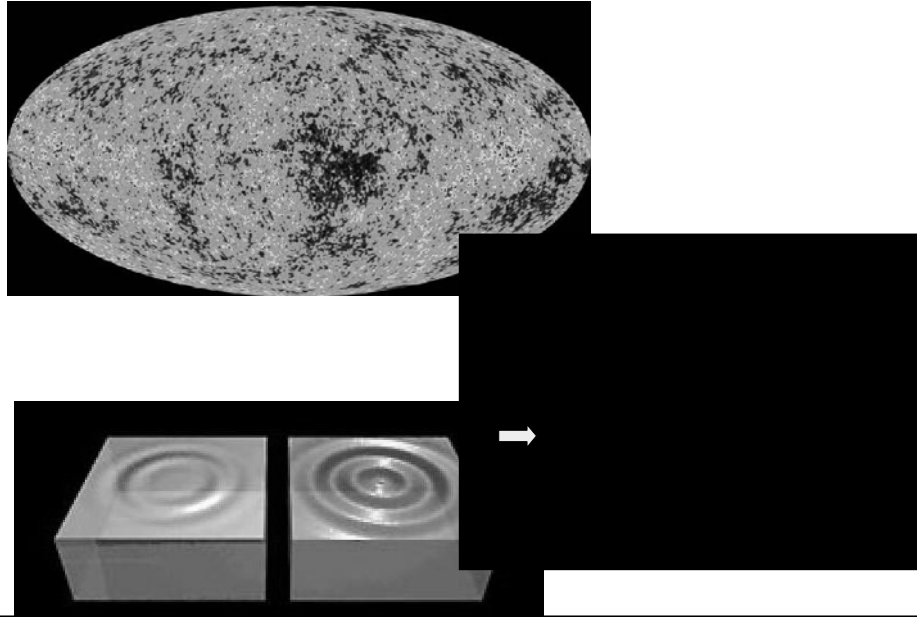
$$\phi \sim \frac{\pi}{l} \sim \frac{180^\circ}{l}$$

# CMB Power Spectrum



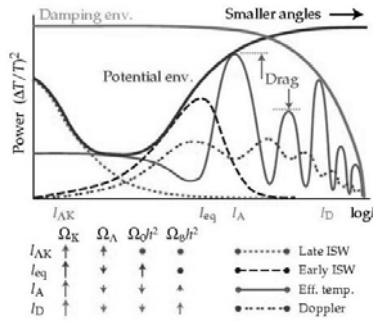
Music of the  
Spheres

# Cosmic Microwave Background





# Music of the Spheres

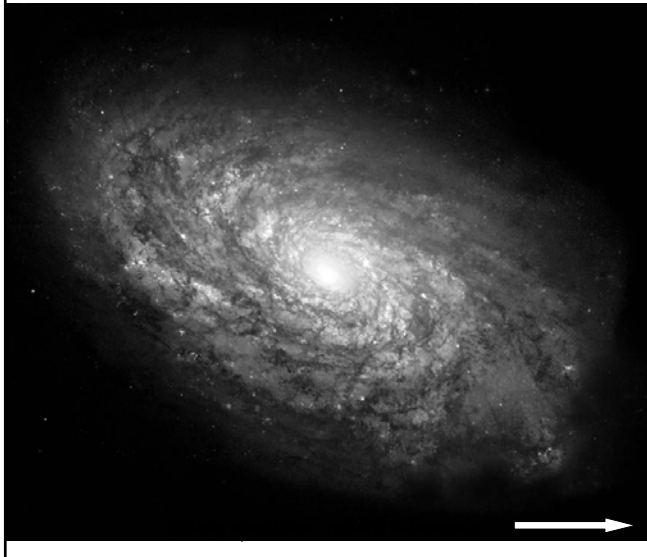


Total Angular CMB Spectrum  
modulated by combination of several effects,  
the Primary Perturbations

- 1) Sachs-Wolfe potential fluctuations,
- 2) Acoustic perturbations  
as the corresponding potential fluct.  
enter horizon and start to collapse
- 3) Integrated Sachs-Wolfe  
potential perturbations:
  - Early ISW: matter/radiation at recomb.
  - Late ISW: expansion influence curvature  
& cosmological constant
- 4) Doppler perturbations  
velocity fluct. accompanying potential pert.
- 5) Silk Damping  
radiation damping of fluctuations

# The Cosmic Web: Patterns Across the Universe

# A Universe of Galaxies

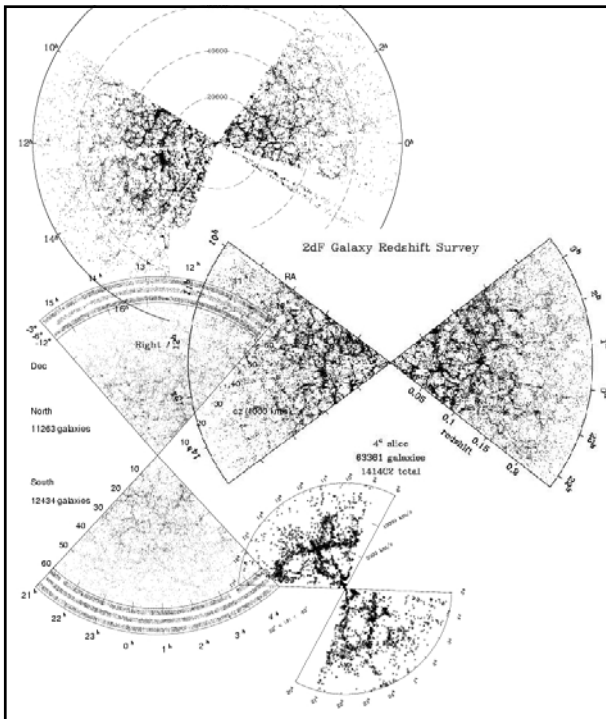
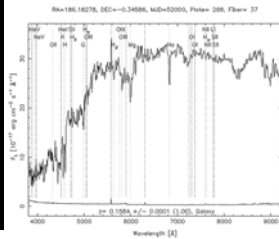


Used as point tracers of underlying cosmic density field.

Intention is to map this cosmic matter field on Megaparsec scales.

"LSS" still reflects conditions primordial Universe:

Cosmic Fossil



Development of our Megaparsec cosmos worldview over the past two decades. A compilation of the galaxy distribution charted in four major galaxy redshift survey campaigns:

- 1) The CfA/SSRS survey
- 2) The LCRS (Las Campanas redshift survey)
- 3) 2dFGRS (2dF galaxy redshift survey)
- 4) SDSS Sloan Digital Sky Survey

Over the past two decades we have witnessed a paradigm shift in our perception of the Megaparsec scale structure in the Universe. As increasing elaborate galaxy redshift surveys charted ever larger regions in the nearby Universe, an intriguingly complex and salient foamlike network came to unfold and establish itself as the quintessential characteristic of the cosmic matter and galaxy distribution.

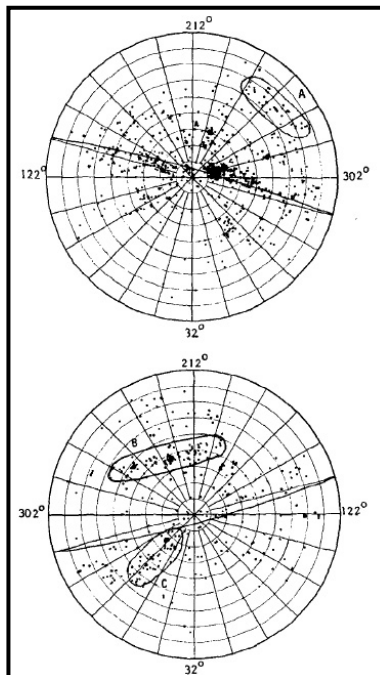
In a great many physical systems, the spatial organization of matter is one of the most readily observable manifestations of the forces and processes forming and moulding them. Richly structured morphologies are usually the consequence of the complex and nonlinear collective action of basic physical processes.

The vast Megaparsec cosmic web is undoubtedly one of the most striking examples of complex geometric patterns found in nature. In its own right, the vast dimensions and intricate composition of the cosmic foam make it one of the most imposing and intriguing patterns existing in the Universe. Its wide-ranging importance stems from its status as a cosmic fossil. On a scale of tens up to a few hundred Megaparsecs it is still relatively straightforward to relate the configuration at the present cosmic epoch to that of the primordial matter distribution from which it emerged. With the cosmic foam seemingly representing this phase, it assumes a fundamental role in the quest for understanding the origin of all structures in the Universe.

While its complex cellular morphology involves one of the most outstanding and evident aspects of the Cosmic foam, it has also remained one defying simple definitions which may be the cause of it having remained one of the least addressed aspects. The geometry of the cosmic foam may be described as a nontrivial stochastic assembly of various anisotropic and asymmetric elements. A major deficiency in the vast majority of studies on the large scale distribution of galaxies has been the lack of suitable quantitative and statistical characterizations of the truly fundamental aspects of the cosmic foam geometry.

# The Cosmic Web: A Census

# Sky Maps: world all around us



## Early Views

Shapley-Ames catalog (1932) of nearby galaxies:

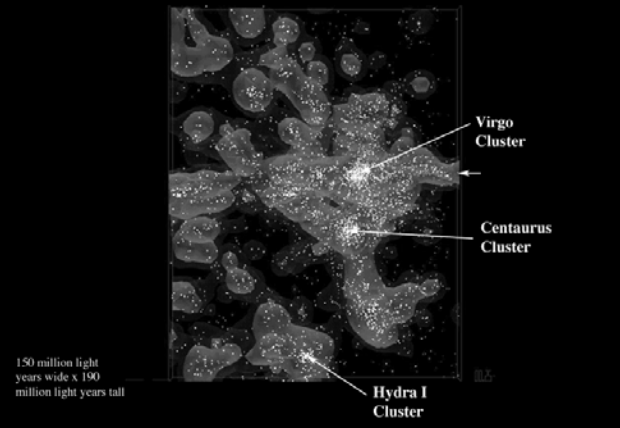
All-sky survey of galaxies to  $m=18.3$

$$\delta > -23^\circ$$

- numerous concentrations:  
groups and clusters (incl. Virgo cluster)
- asymmetry between north and south:  
many more galaxies on northern sky
- conspicuous concentration along a line  
running through richest nearby cluster,  
the Virgo cluster:
- The Supergalactic Plane  
(first identified by de Vaucouleurs:  
the plane of our own Local Supercluster)

# The Local Supercluster

End-on View of the Local Supercluster:

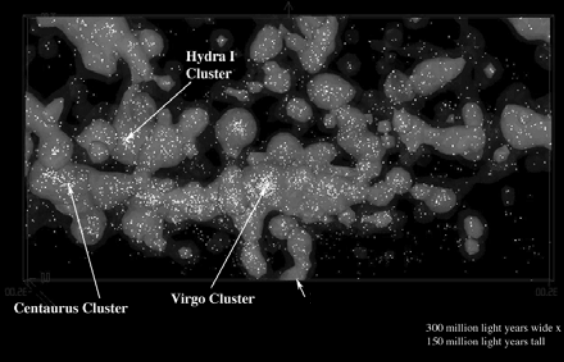


Courtesy: B. Tully

Our Local Group finds itself located at the outer region of a large supercluster region, the "Local Supercluster", a large flattened mass concentration  $\sim 10 h^{-1}$  Mpc in size, centered on one rich cluster, the Virgo cluster

# The Local Supercluster

Polar View of Local Supercluster:

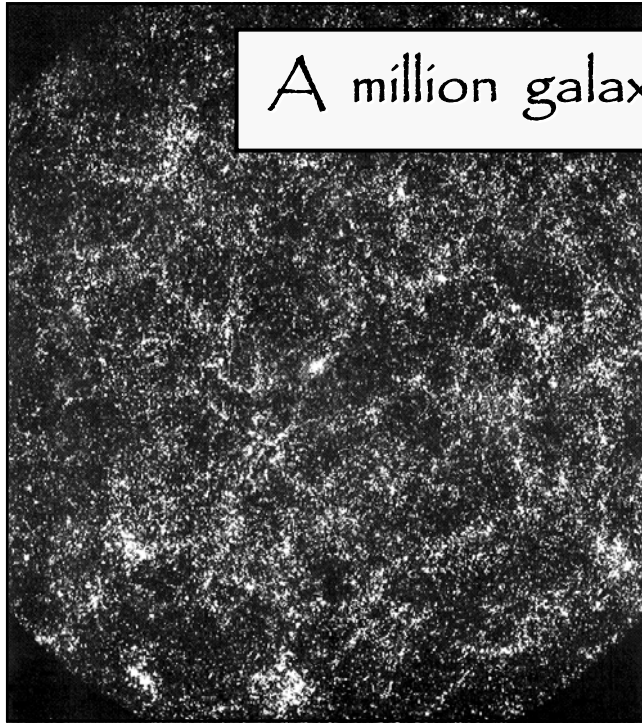


Courtesy: B. Tully

Our Local Group finds itself located at the outer region of a large supercluster region,

- the "Local Supercluster",
- a large flattened mass concentration  $\sim 10 h^{-1}$  Mpc in size,
- centered on one rich cluster, the Virgo cluster

## A million galaxies



### Shane-Wirtanen map:

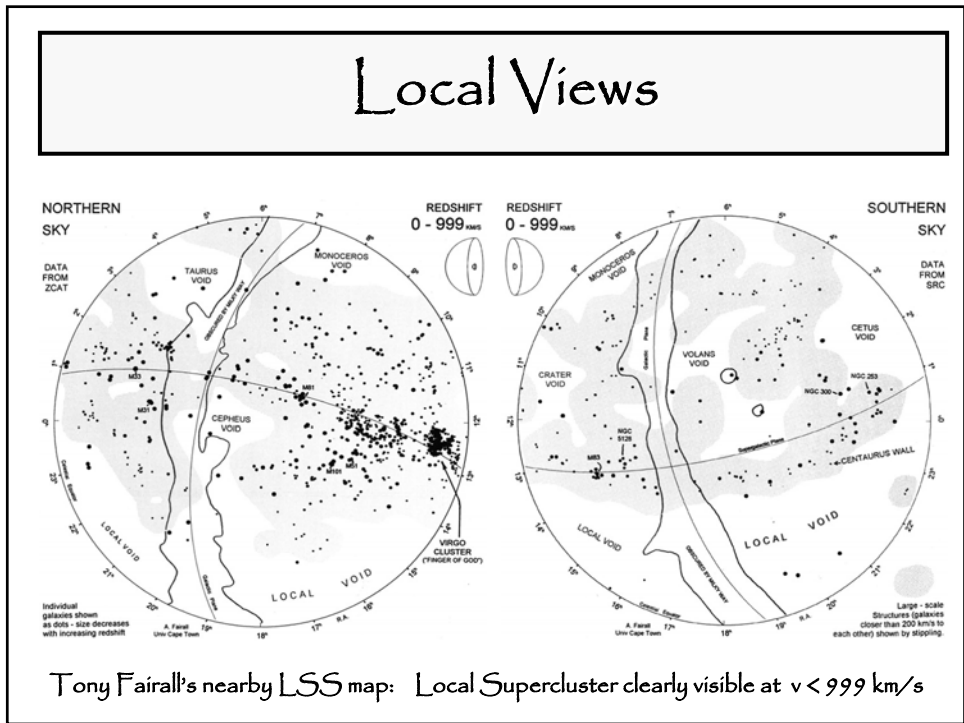
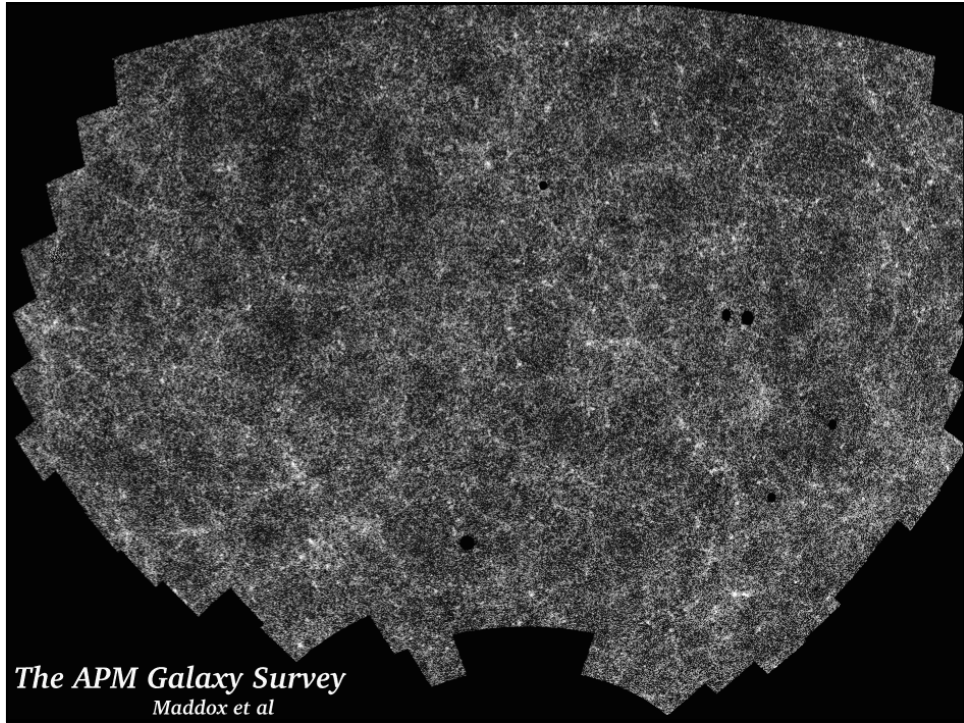
On the basis of the Shane-Wirtanen counts, P.J.E. Peebles produced a map of the sky distribution of 1 million galaxies on the sky:

- Clearly visible are clusters
- hint of filamentary LSS features, embedding clusters

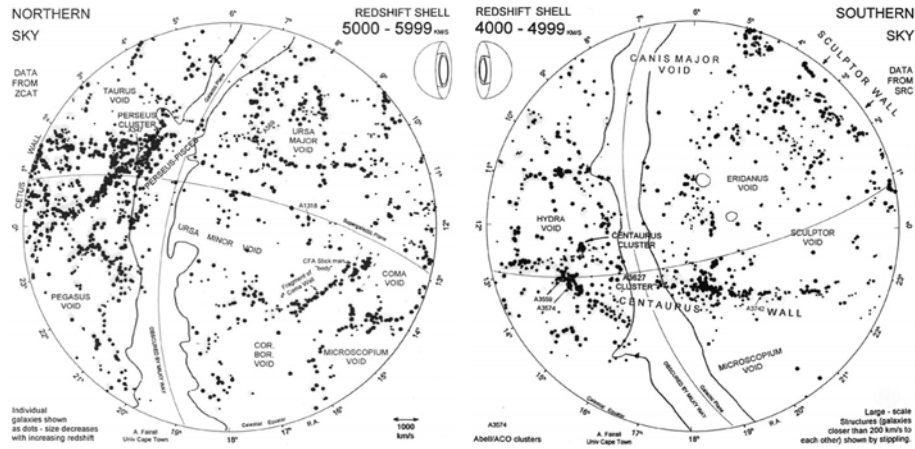
## APM survey

- Sky map:
  - $2 \times 10^6$  galaxies
  - $17 < m < 20.5$
- Uniformly defined
- Sky region: 4300 sq. deg.
  - 185 UK Schmidt plates,  $6^\circ \times 6^\circ$
- Large inhomogeneities, hints of weblike patterns, with clusters at densest regions.

courtesy: S. Maddox, G. Efstathiou,  
W. Sutherland, D. Loveday



# Local Views: Moving into Foam



Tony Fairall's nearby LSS map: at  $cz=5000-5999$  km/s clear views of local cosmic web

## 2MASS survey

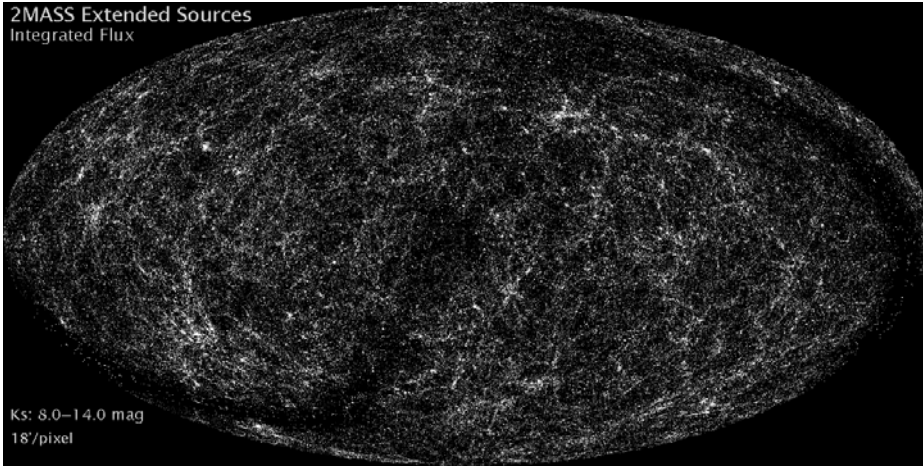
- 2MASS all-sky survey:  
ground-based near-infrared survey whole sky,  
 $J(1.2 \mu\text{m})$ ,  $H(1.6 \mu\text{m})$ ,  $K(2.2 \mu\text{m})$
- 2MASS extended source catalog (XSC):  
1.5 million galaxies
- unbiased sample nearby galaxies
- photometric redshifts: depth in 2MASS maps,  
"cosmic web" of (nearby) superclusters spanning  
the entire sky.

courtesy: T. Jarrett



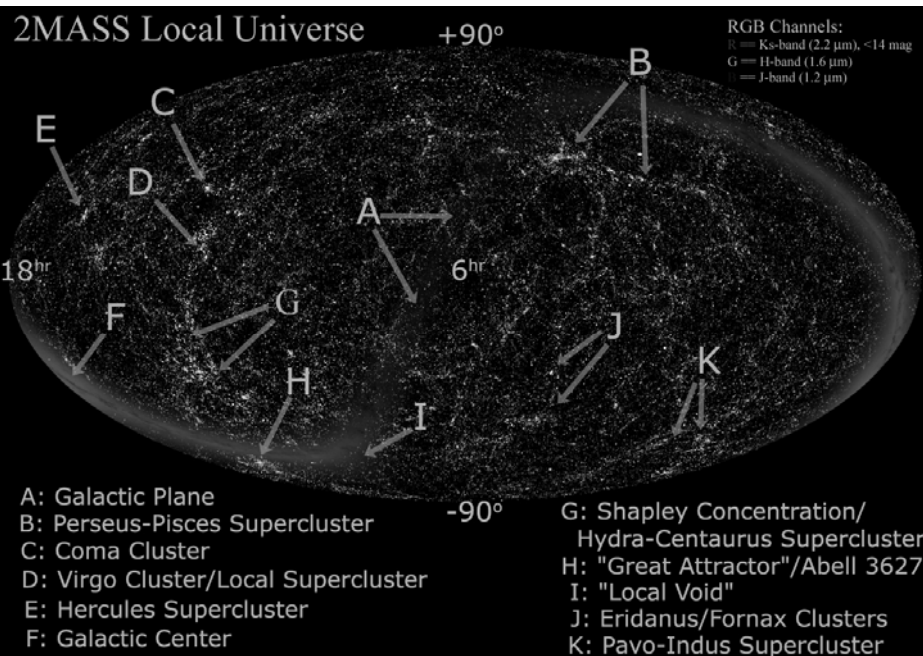
# The Cosmic Web

2MASS Extended Sources  
Integrated Flux



Looking around us we already see the unmistakable signatures of an intriguing foamlike matter distribution in our immediate Cosmic Vicinity.

## Identity of Local Structures along local Cosmic Web.

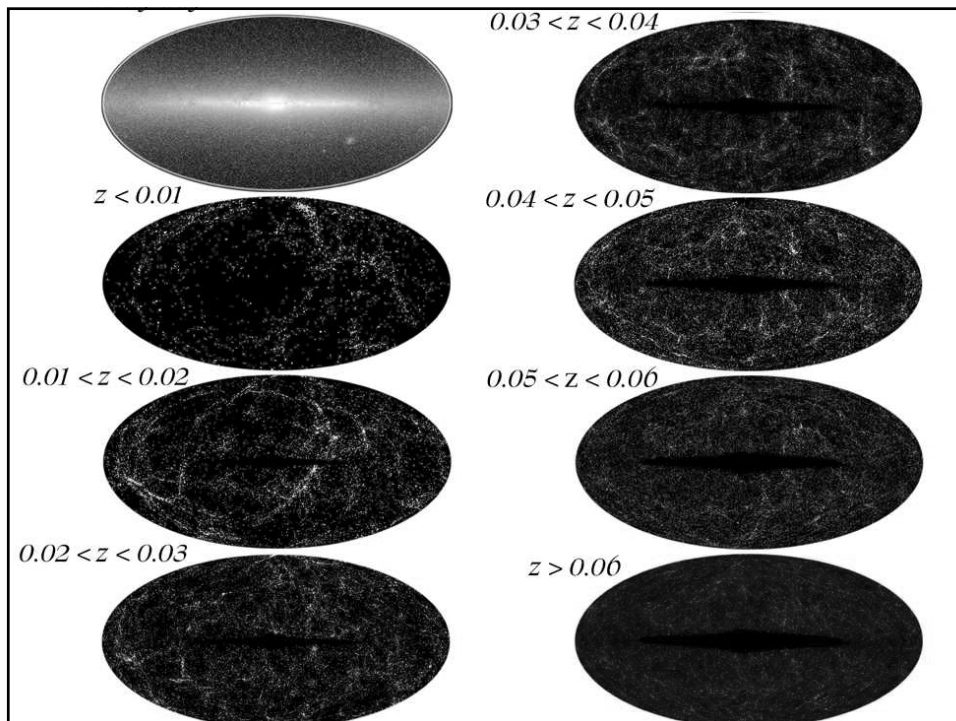


# The Cosmic Web

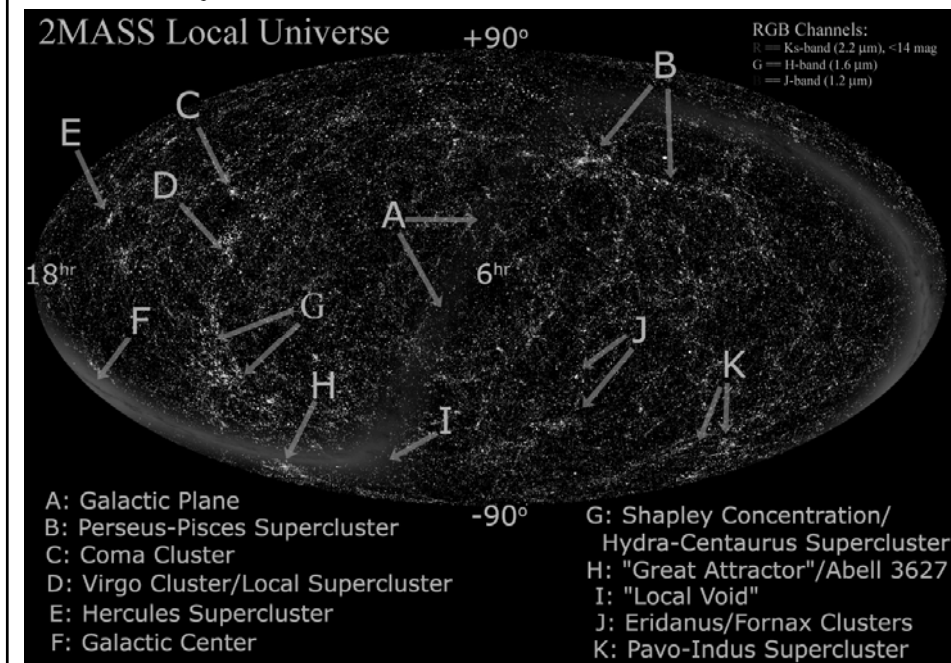


2MASS: the cumulative view.

Moving outward we see the unfolding of the local cosmic foam.



## Identity of Local Structures along local Cosmic Web.



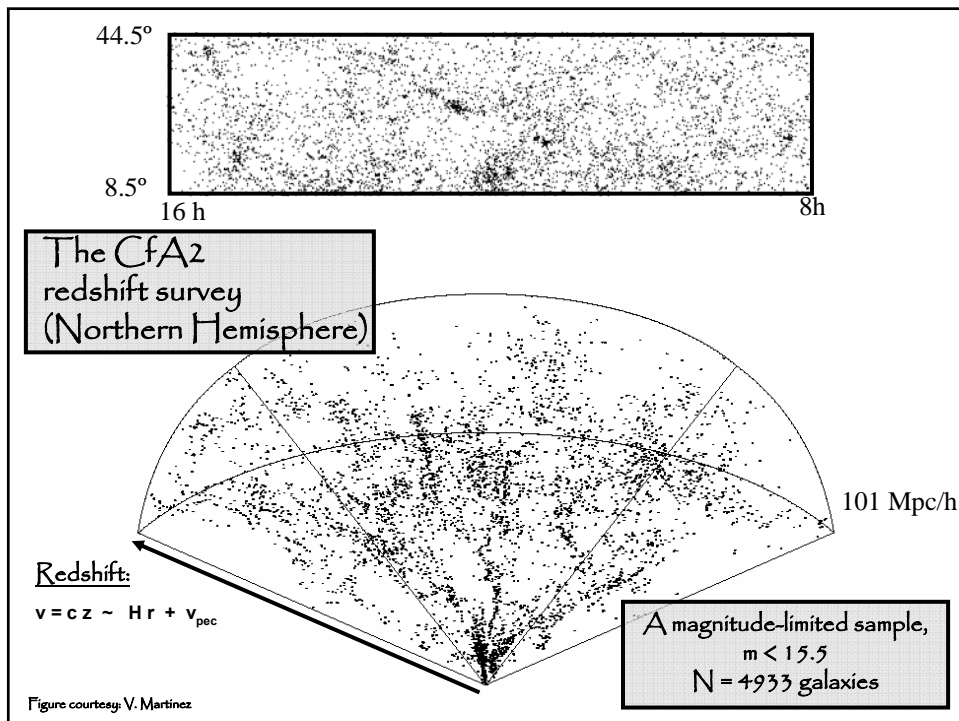
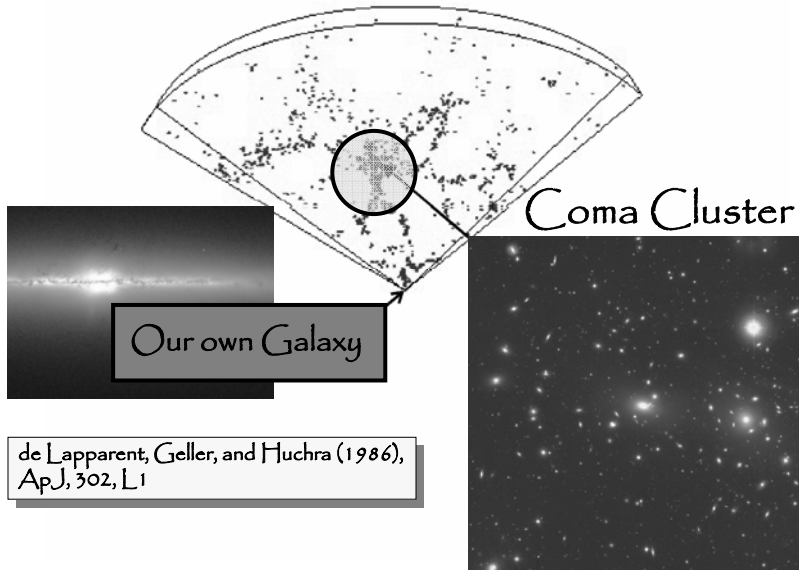
# Maps of the Local Universe

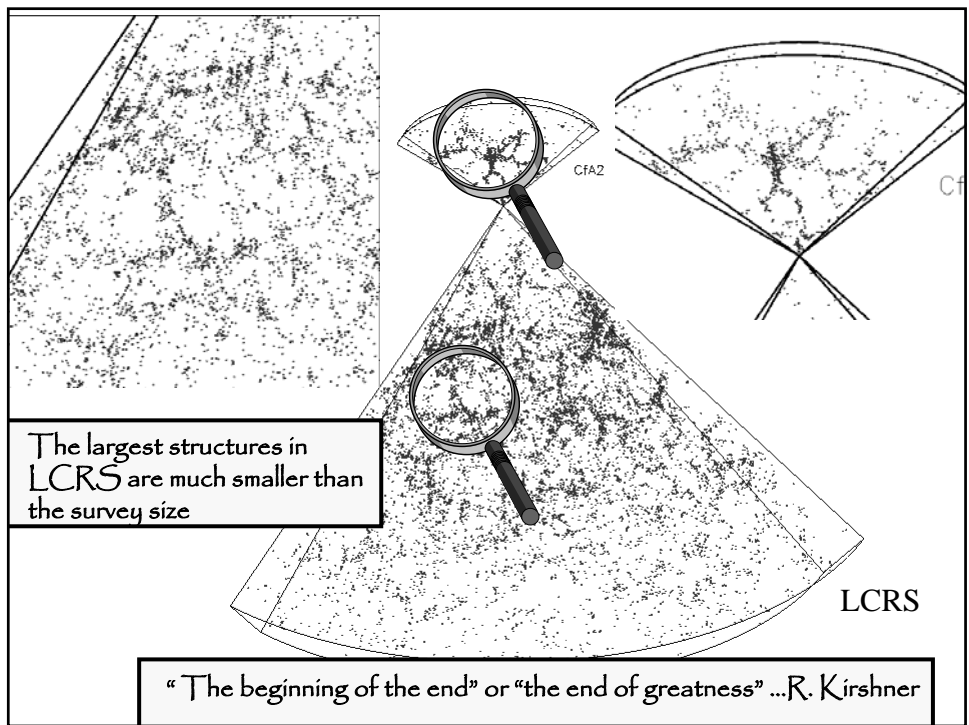
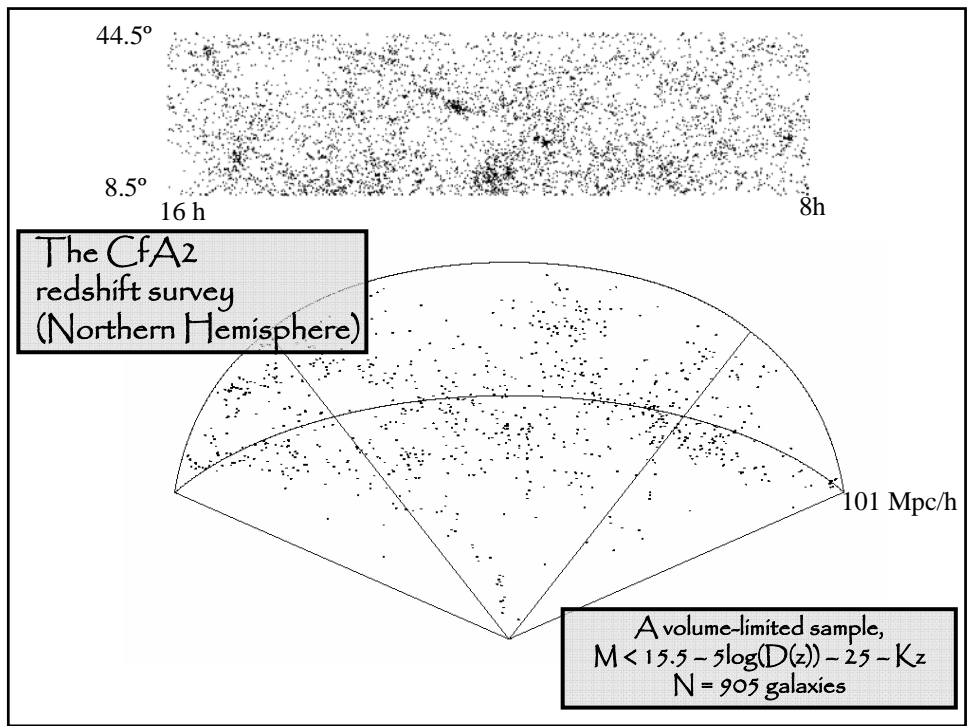
The Cosmic Web Revealed:

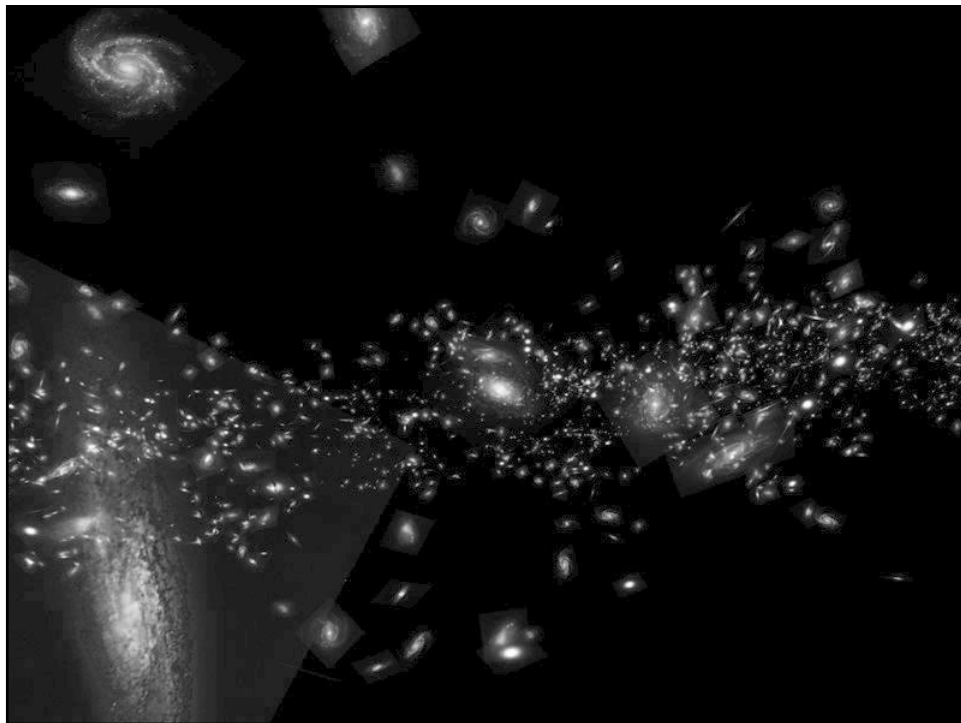
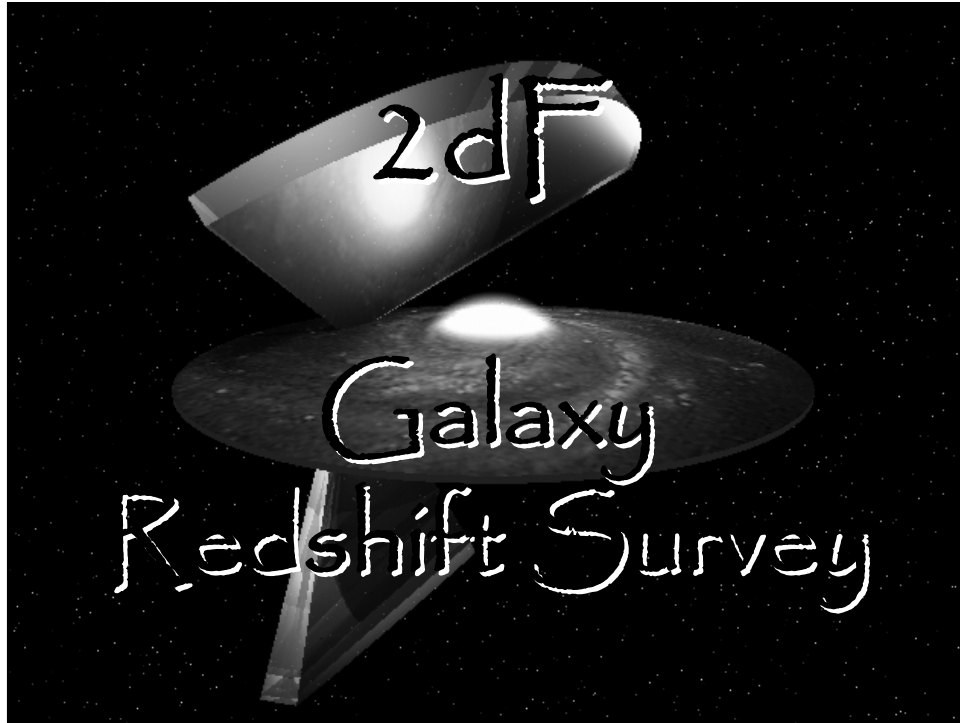
The CfA2 and SDSS  
survey slices

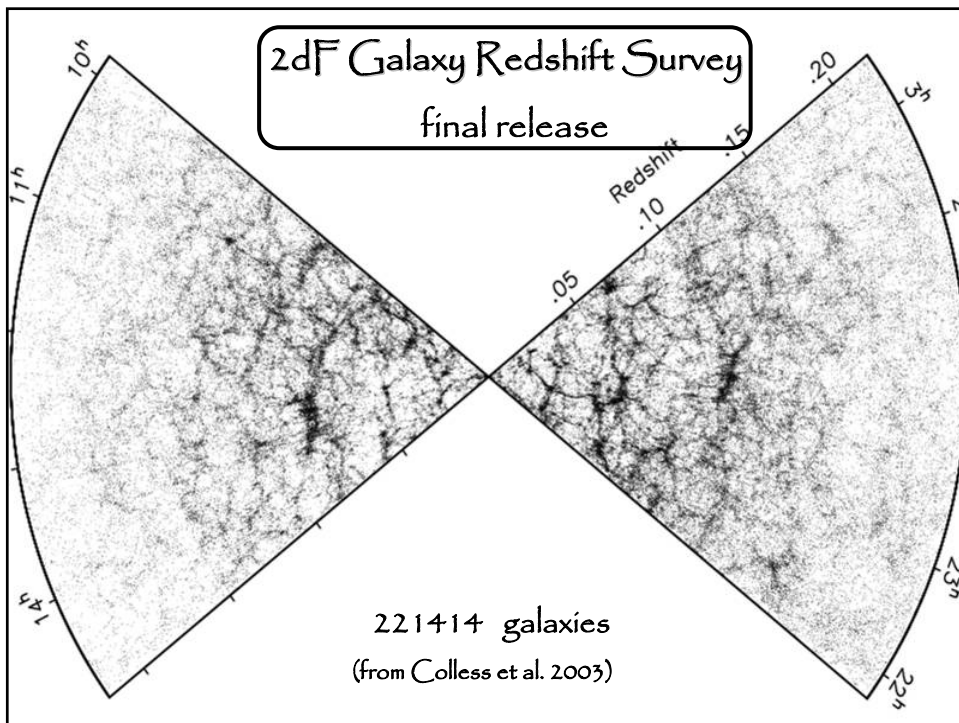
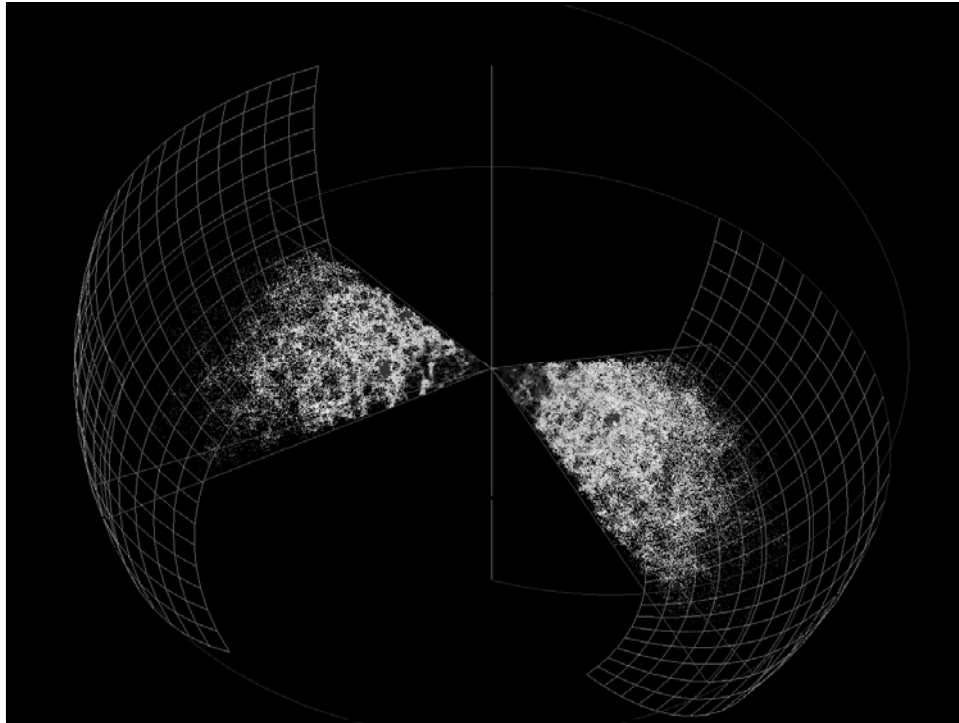
(de Lapparent, Geller, Huchra, ...  
1986, ...)

# Mapping the Universe







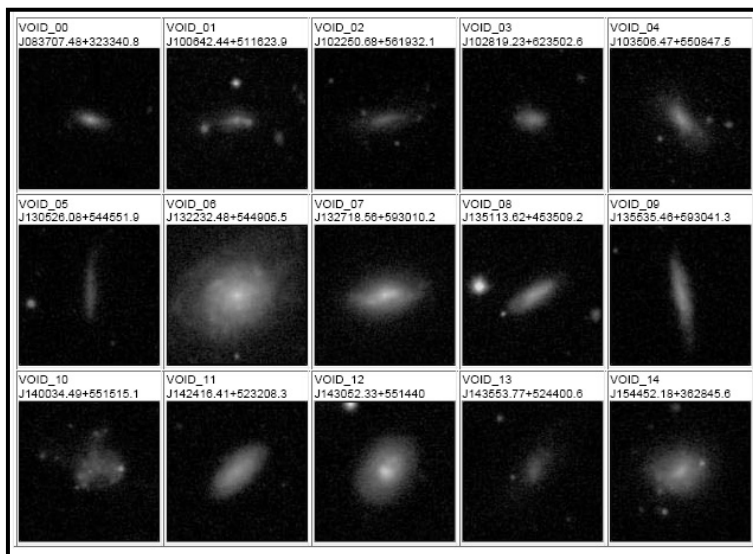


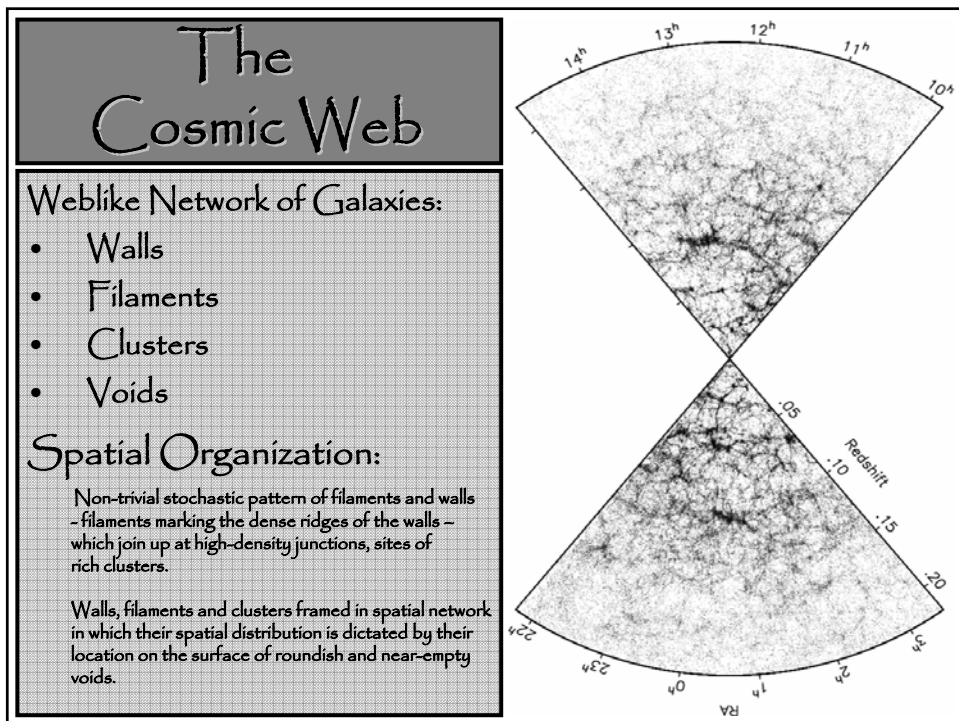


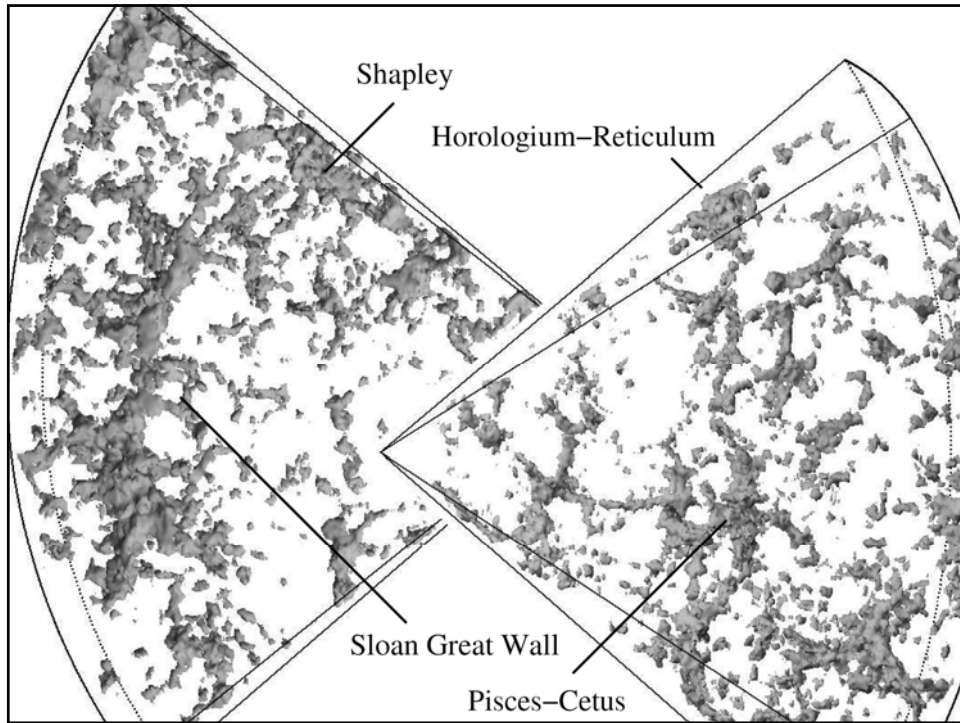
# SDSS survey

- Largest and most systematic (digital!) sky survey in history of astronomy.
- Images sky in 5 photometric bands !!!!  
Down to apparent magnitude  $r \sim 23.1$
- Covers  $\sim 25\%$  of the sky: 8452 sq. deg.
- With 2dFGRS, the SDSS will produce the most extensive map of the spatial structure of our cosmic neighbourhood.
- Million galaxies subsequently selected for measuring redshift  $z$ : electromagnetic spectrum
- Total:
  - sky survey:  $10^8$  stars,  $10^8$  galaxies,  $10^5$  quasars
  - spectroscopy:  $10^6$  galaxies,  $10^5$  quasars,  $10^5$  stars

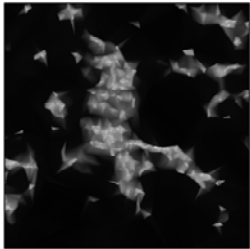
# SDSS survey



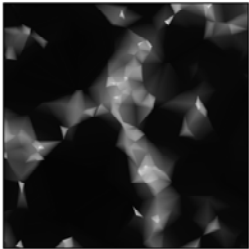




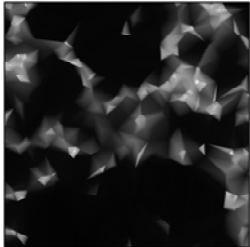
**cluster:**



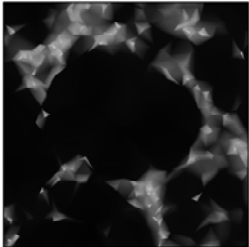
**filaments:**



**wall:**



**void:**



Foam Elements  
in the 2dFGRS

- + Walls
- + Filaments
- + Clusters
- + Voids

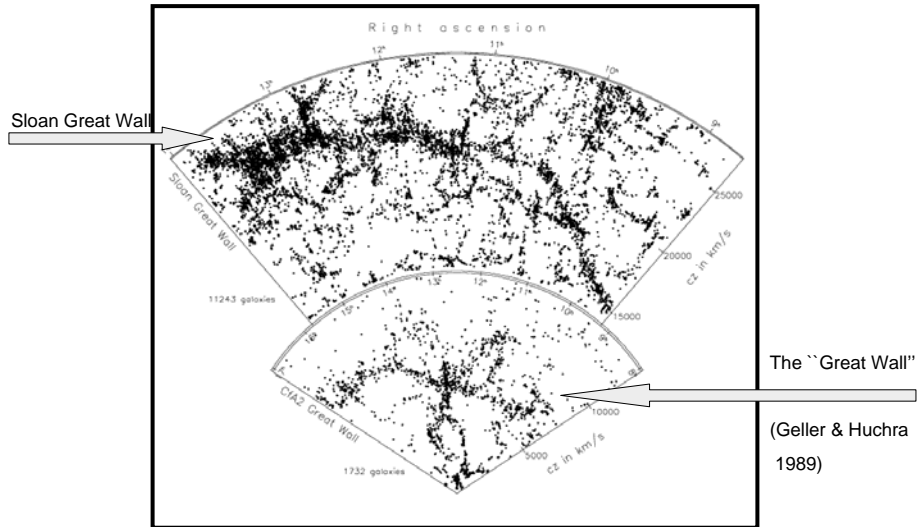
# The Elements

# The Cosmic Web

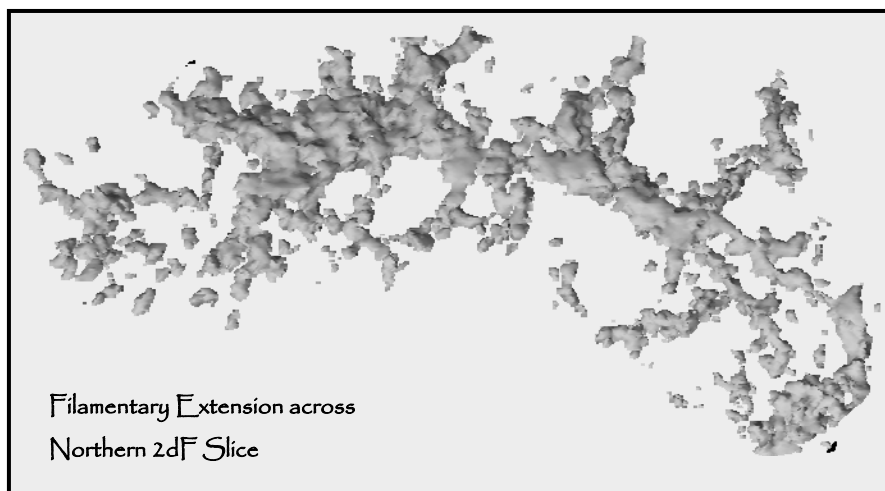
## Walls and Filaments

From the Millennium Simulation;  
V. Springel & GIF consortium

# Walls and Filaments



# Walls and Filaments



DTFE rendering: W. Schaap

# Walls and Filaments

## Pisces-Perseus Supercluster

Canonic example of a strongly flattened supercluster consisting of

- sheet-like central region, dense filamentary boundary ridge
- Relative proximity ( $d \sim 55h^{-1}$  Mpc),
- Characteristic & salient filamentary morphology,
- Favourable orientation.

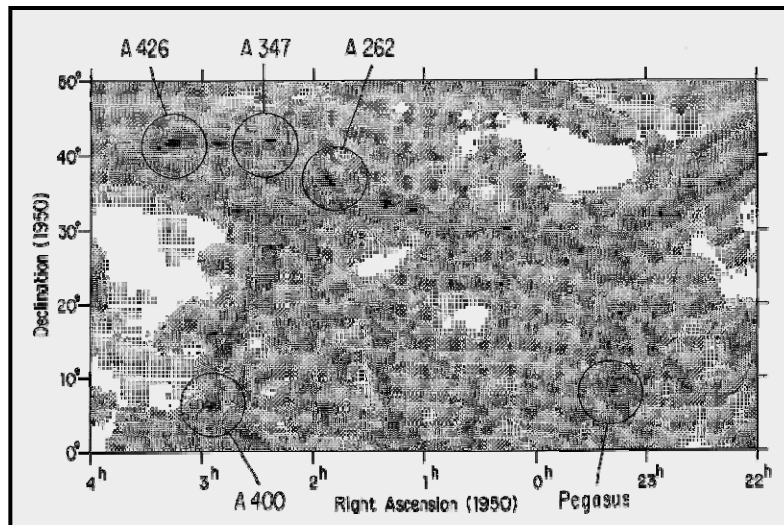
Northern boundary: ridge south-westward of Perseus cluster (A426)

Dimensions Ridge:  $5h^{-1}$  Mpc wide

$50h^{-1}$  Mpc length; possible  $140h^{-1}$  Mpc extension

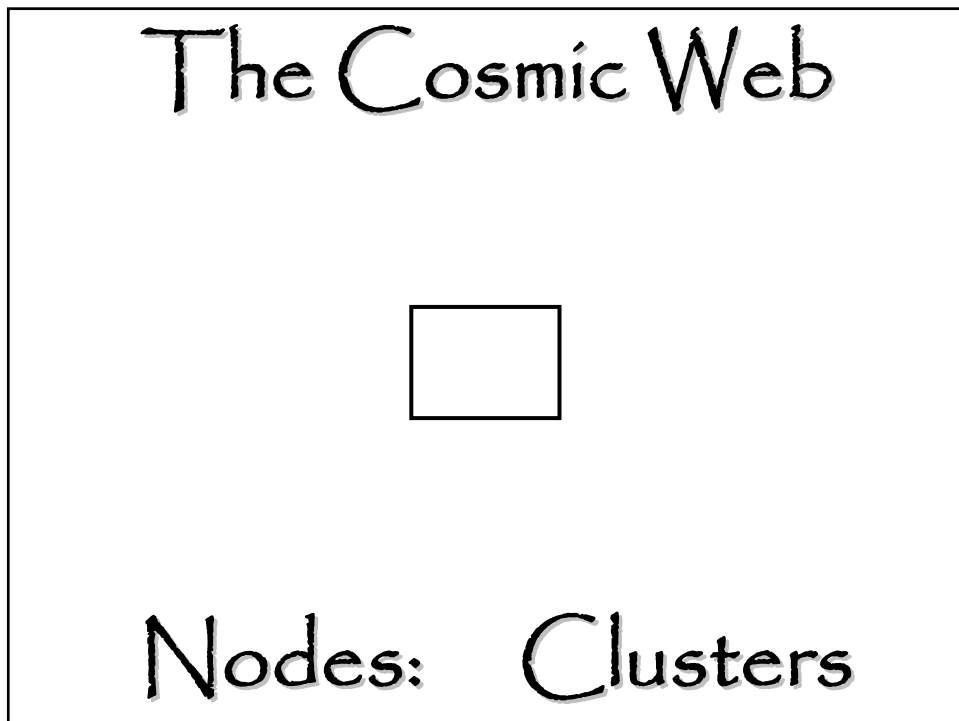
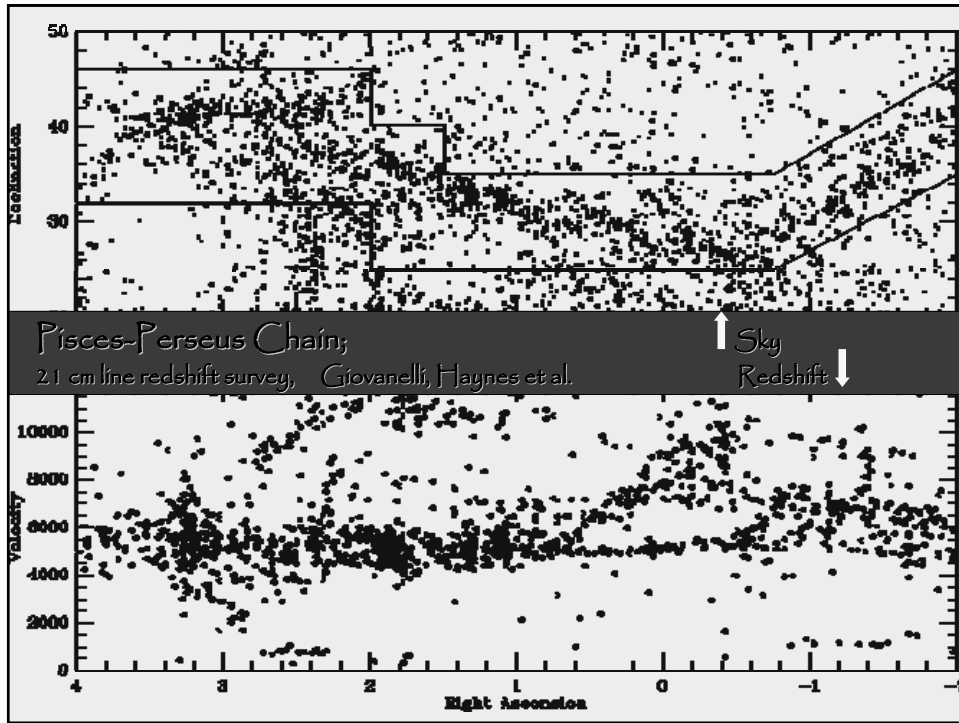
Along Ridge: high density clusters, incl. A462, A347, A262

# Walls and Filaments

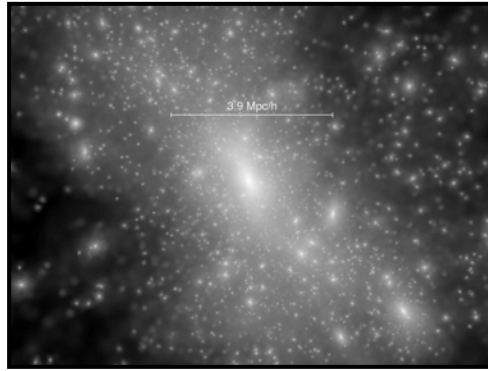


Pisces-Perseus Chain;

21 cm line redshift survey,  
Giovanelli & Haynes

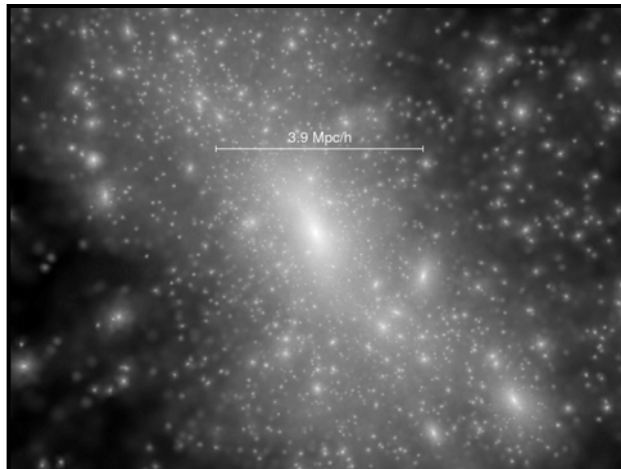


# The Cosmic Web



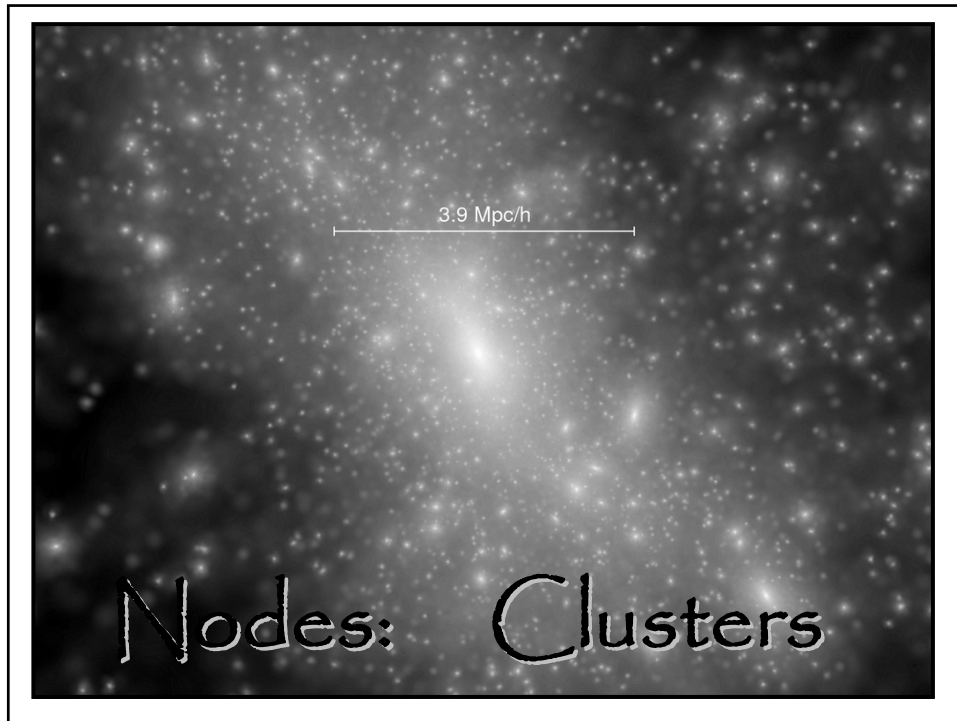
Nodes: Clusters

# The Cosmic Web



Nodes: Clusters





## Clusters of Galaxies

- Assemblies of up to 1000s of galaxies within a radius of only  $1.5-2h^{-1}$  Mpc,
- Representing overdensities of  $\delta \sim 1000$
- Galaxy move around with velocities  $\sim 1000$  km/s
- They are the most massive, and most recently, fully collapsed structures in our Universe.

# Clusters of Galaxies



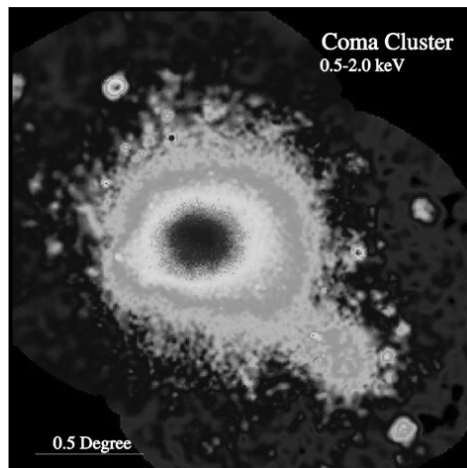
Courtesy:  
O. Lopez-Cruz

Coma Cluster

# Clusters of Galaxies X-ray intracluster gas

Baryonic matter in clusters is not only confined to galaxies. On the contrary, about 2 to 5 times more baryonic mass is in the form of a diffuse hot X-ray emitting intracluster gas, trapped and heated to a temperature of the order of  $10^8$  K by the gravitational potential of the cluster. At such high temperatures, this gas is a fully ionized plasma, producing powerful X-ray emission, bremsstrahlung radiation induced by the electron-ion interactions.

ROSAT X-ray image Coma Cluster



# Clusters of Galaxies: Gravitational Lenses

A highly promising method to determine the amount and distribution of

matter in the Universe

looks at the way it affects

the trajectories of photons.

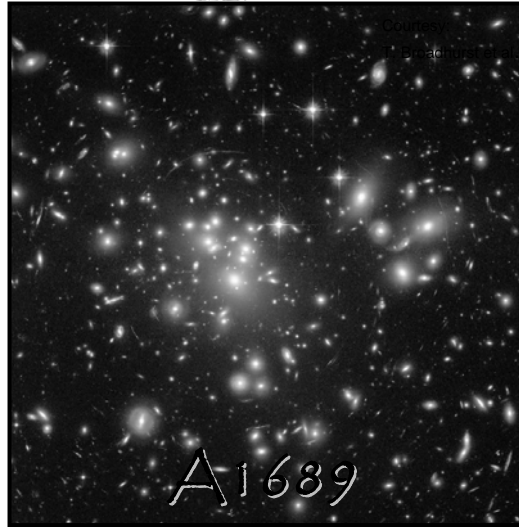
According to

Einstein's theory of

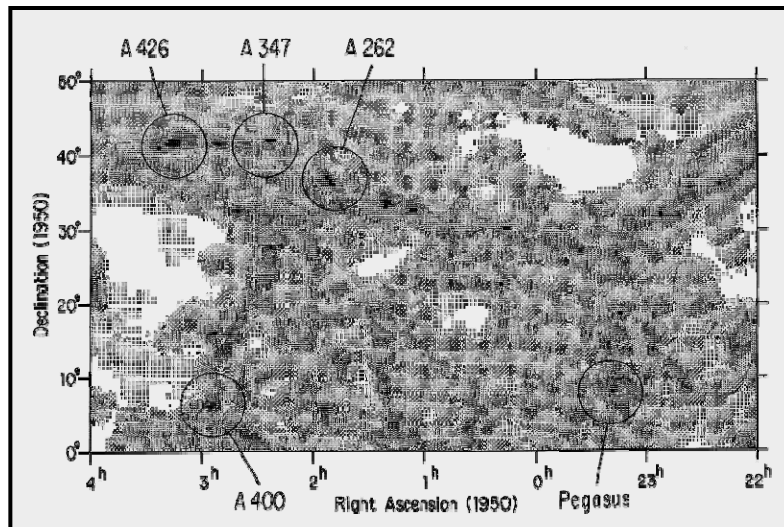
General Relativity,

gravitational potential wells will bend and focus light. Dark matter concentrations act as a

Gravitational Lens.



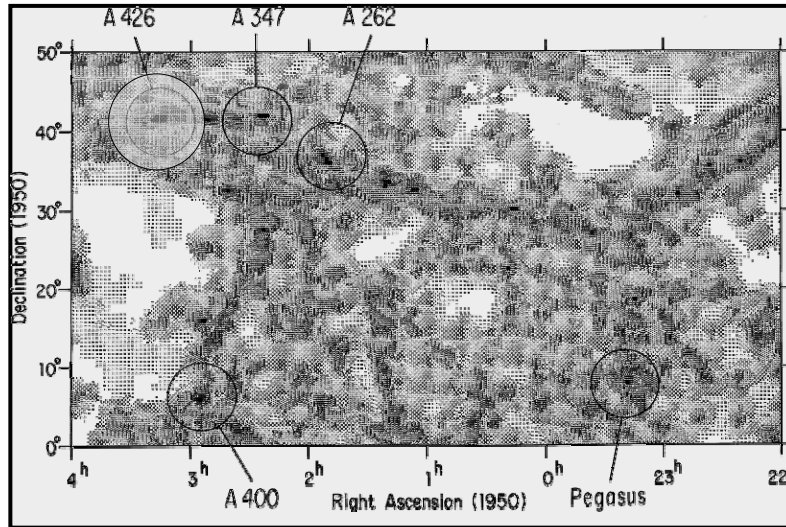
# Cosmic Web & Clusters



Pisces-Perseus Chain;

21 cm line redshift survey,  
Giovanelli & Haynes

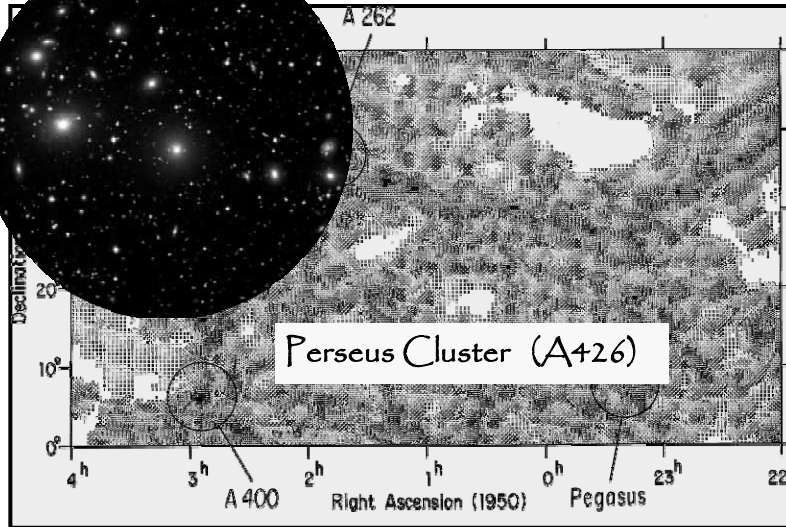
# Cosmic Web & Clusters



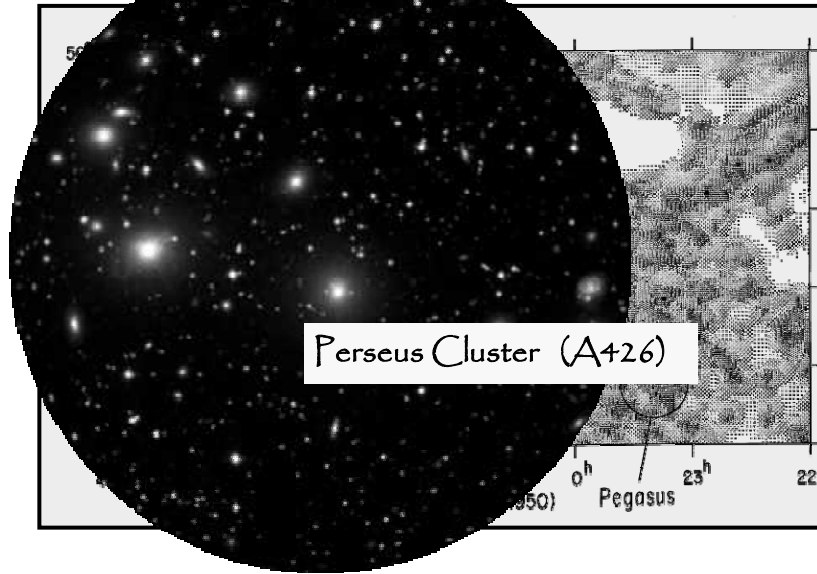
Pisces-Perseus Chain;

21 cm line redshift survey,  
Giovanelli & Haynes

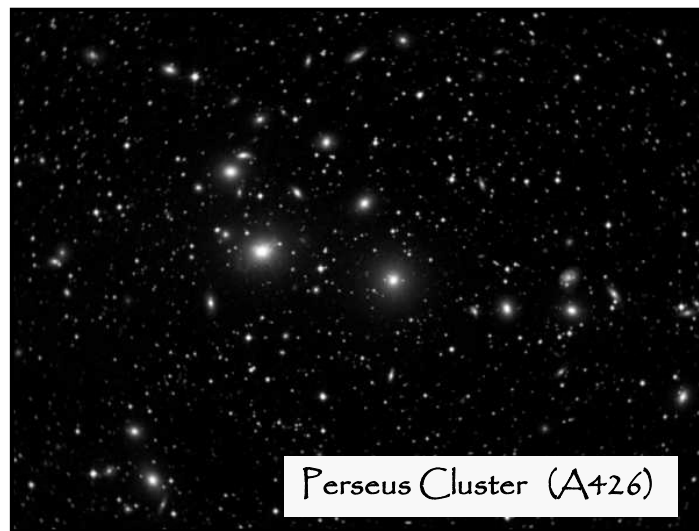
# Cosmic Web & Clusters

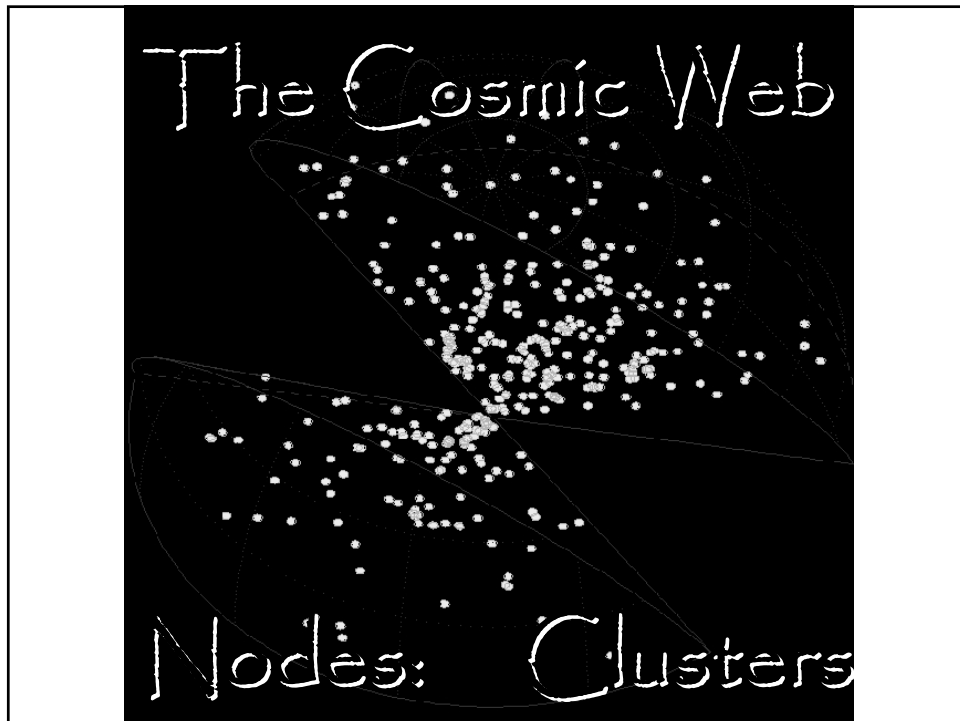
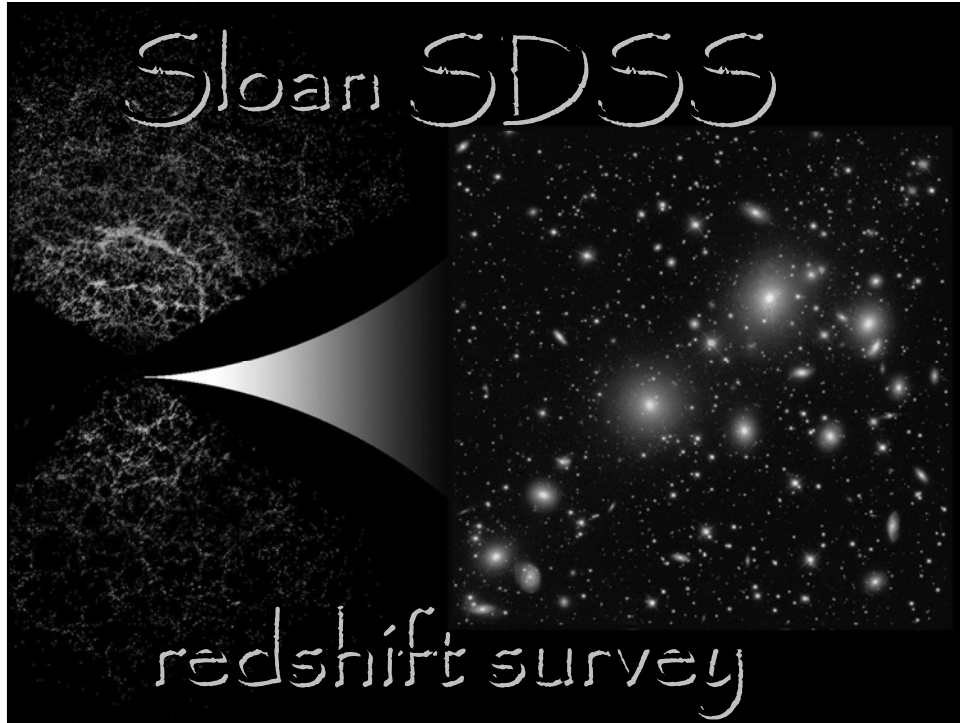


# Cosmic Web & Clusters

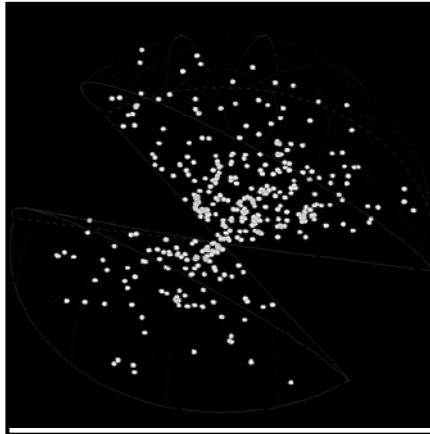


# Cosmic Web & Clusters





# The Cosmic Web



The spatial cluster distribution.

The full volume of the X-ray cluster REFLEX cluster survey within a distance of  $600h^{-1}$  Mpc. The REFLEX galaxy cluster catalogue contains all clusters brighter than an X-ray flux of  $3 \times 10^{-16}$  ergs  $\text{cm}^{-2}$  over a large part of the in the southern sky. The missing part of hemisphere delineates the region highly obscured by the Galaxy.

REFLEX: Boehringer et al. (2001)

Courtesy: Borgani & Guzzo (2001)

Nodes: Clusters

# The Cosmic Web

Nodes: Clusters

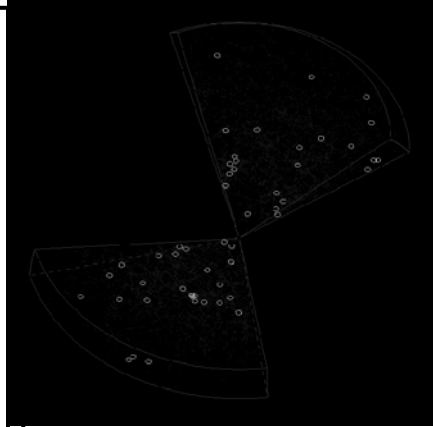
# The Cosmic Web

The spatial cluster distribution and relation to Cosmic Web.

The green circles mark the positions of REFLEX X-ray clusters in the northern and southern slices of the Las Campanas redshift survey (LCRS, Shectman et al. 1996), out to a maximum distance of  $600h^{-1}$  Mpc. Underlying, in blue, the galaxies in the LCRS delineate a foamlike distribution of filaments, walls and voids.

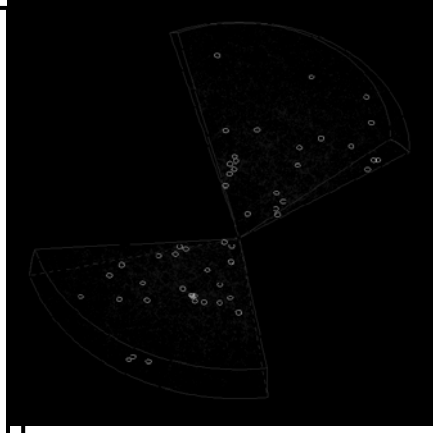
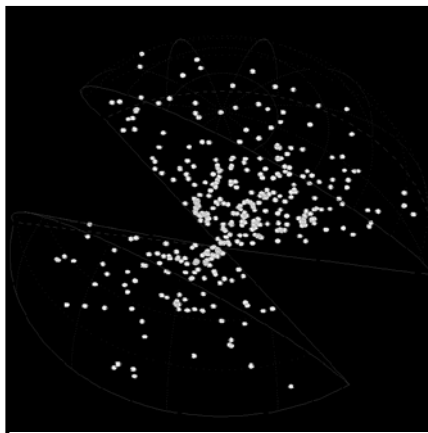
REFLEX: Boehringer et al. (2001)

Courtesy: Borgani & Guzzo (2001)



Nodes: Clusters

# The Cosmic Web



Nodes: Clusters



# The Cosmic Web

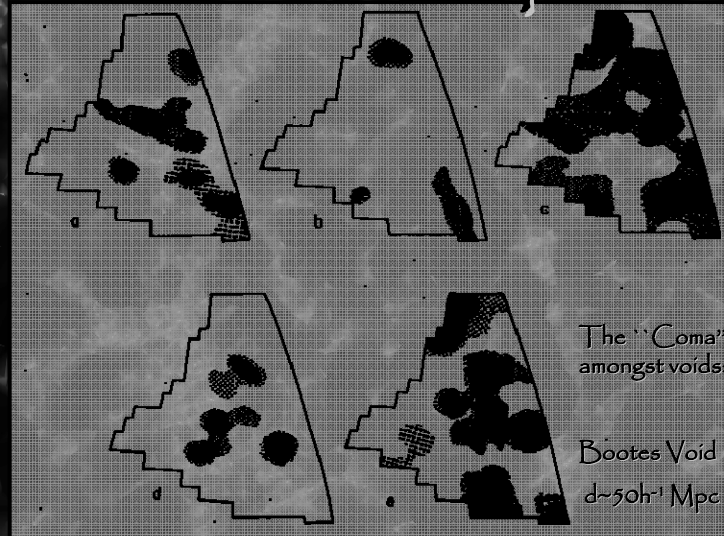
## Voids

## Voids in Space

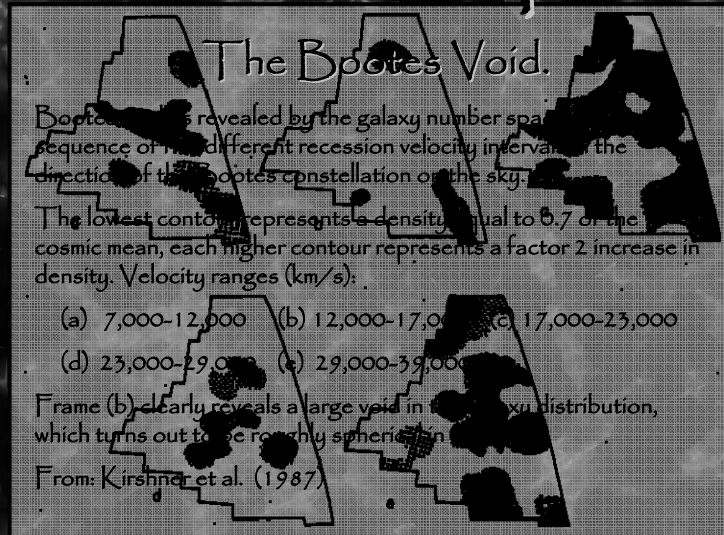
Voids in the 6dF redshift survey,

Detected by A. Fairall

# Voids in Space



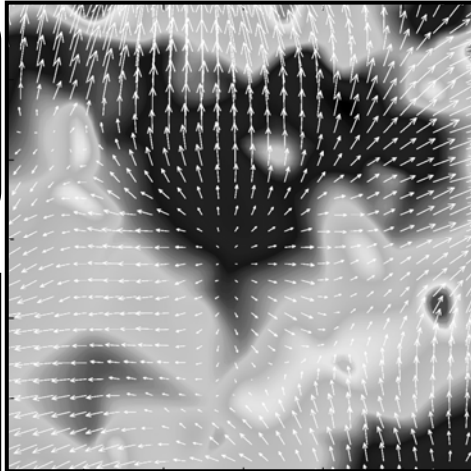
# Voids in Space



# Voids in Space

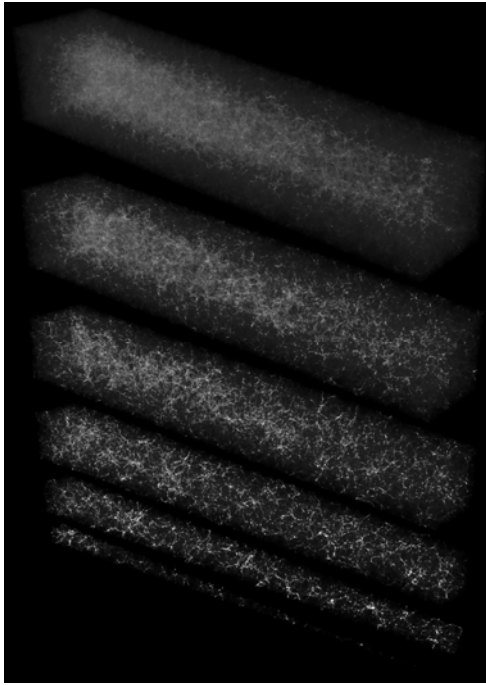
**Void Dynamics:**  
Voids exert a repulsing dynamical influence over their surroundings.

Sculptor Void



PSCz: DTFE density & velocity field  
(F. Romano-Diaz)

# Web in Depth



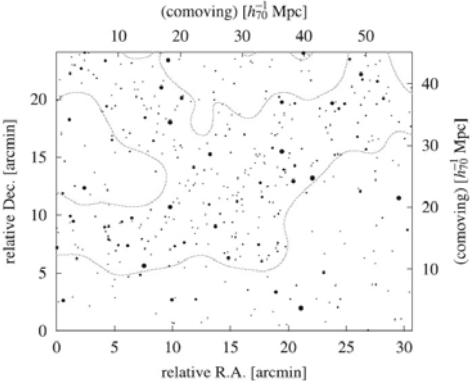
## Far Away, Long Ago

Various surveys are attempting to trace the large scale structure out to large cosmic depths/redshifts.

- Is cosmic web truly universal
- What about the scales of the web (characteristic, largest structures, ...)
- Evolution of Megaparsec scale matter distribution.

Simulation of VIRMOS redshift survey, web out to large redshift

## Far Away, Long Ago

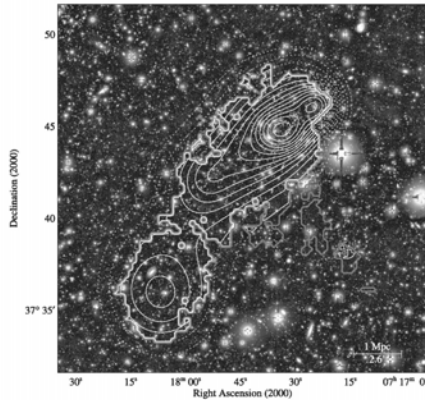


Various surveys are attempting to trace the large scale structure out to large cosmic depths/redshifts.

- Is cosmic web truly universal
- What about the scales of the web (characteristic, largest structures, ...)
- Evolution of Megaparsec scale matter distribution.

Subaru Survey: Amazing prominent large scale distribution of Ly $\alpha$  emitting galaxies.  
A filament at redshift  $z \sim 3$ ?

# Far Away, Long Ago



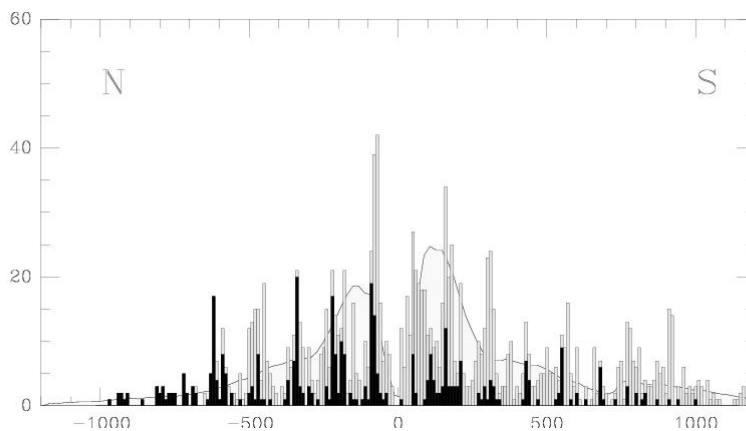
Various surveys are attempting to trace the large scale structure out to large cosmic depths/redshifts.

- Is cosmic web truly universal?
- What about the scales of the web (characteristic, largest structures, ...)
- Evolution of Megaparsec scale matter distribution.

Elbeling et al. (2004):

A filamentary structure in between two rich clusters.

# Far Away, Long Ago

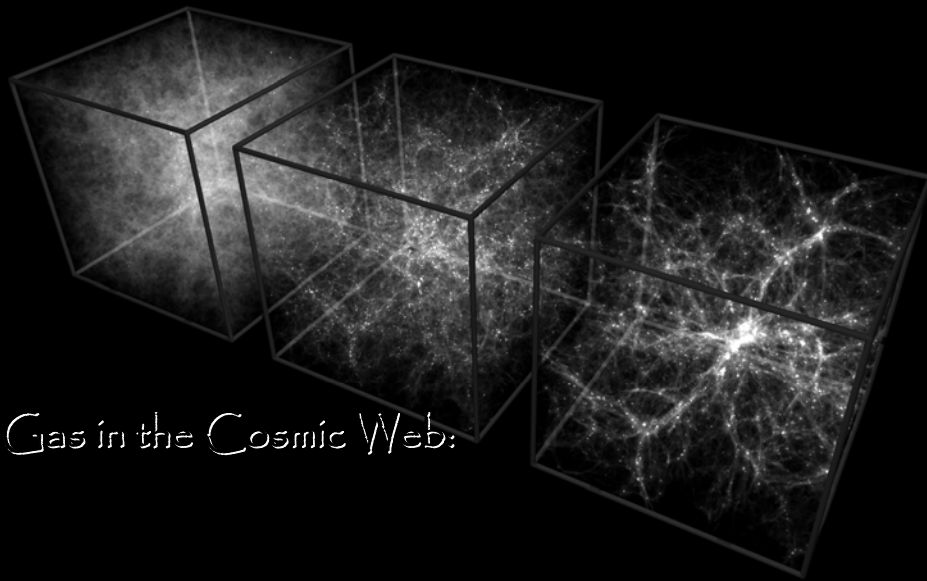


Deep pencil beam survey (Broadhurst et al):

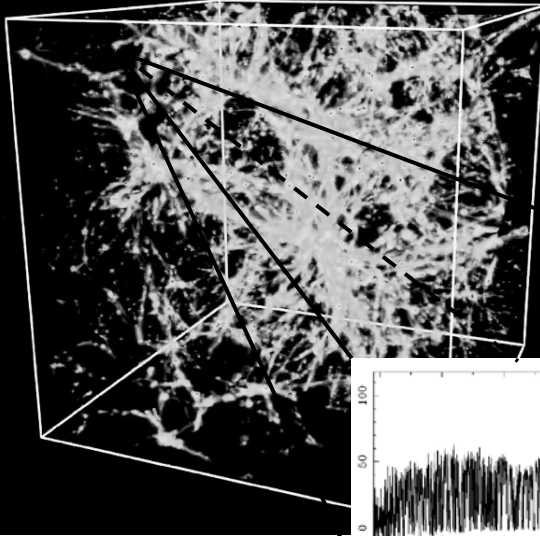
A semi-regular pattern of redshift spikes along line of sight, indicating the passage of l.o.s. through sheets, filaments and clusters. Suggestions for a characteristic scale of  $\sim 120h^{-1}$  Mpc should be ascribed to the 1-D character of the redshift skewer through 3-D structure.

# The Gastrophysical Web

## The Gastrophysical Web



# The Gastrophysical Web

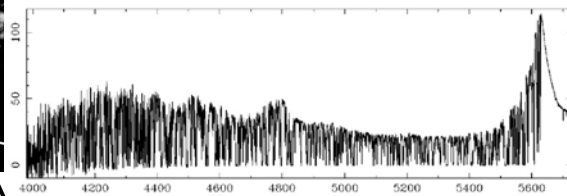


## The Ly $\alpha$ forest:

...s in the intergalactic medium  
...y traces the density fluctuations  
...dark matter distribution.

D absorption lines arise due to  
...e of sight intersection by the  
...l hydrogen component

...olumn density absorption lines  
...ated with sheets and filaments in  
...Cosmic Web"



# Web Dynamics

# Cosmic Migration Flows

CMB Dipole:

We move wrt Universe:  $v \sim 620$  km/s

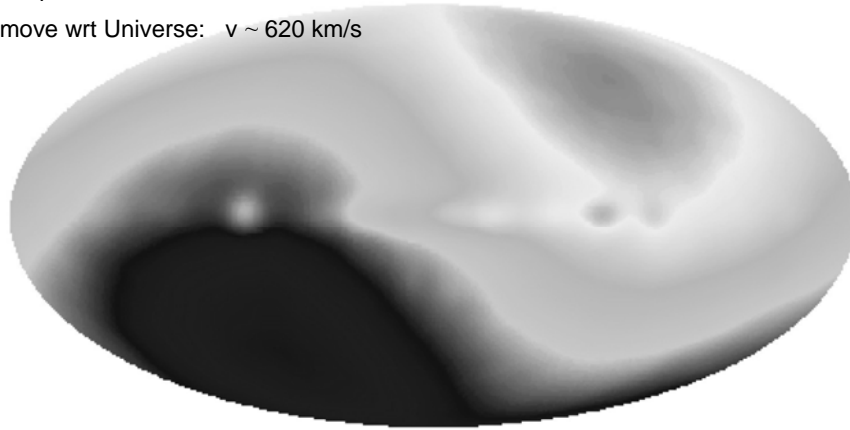
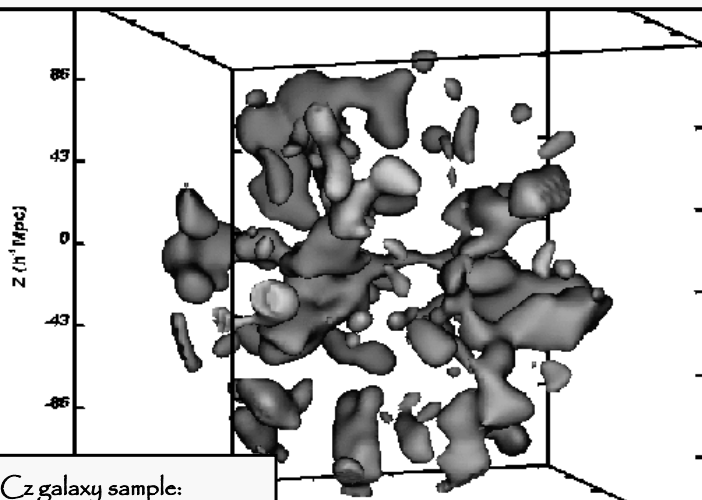


Figure 11. The Cosmic Microwave Background dipole as measured by the DMR instrument of the COBE microwave background satellite (see also Kogut et al. 1993)

# Cosmic Migration Flows



PSCz galaxy sample:  
Density field



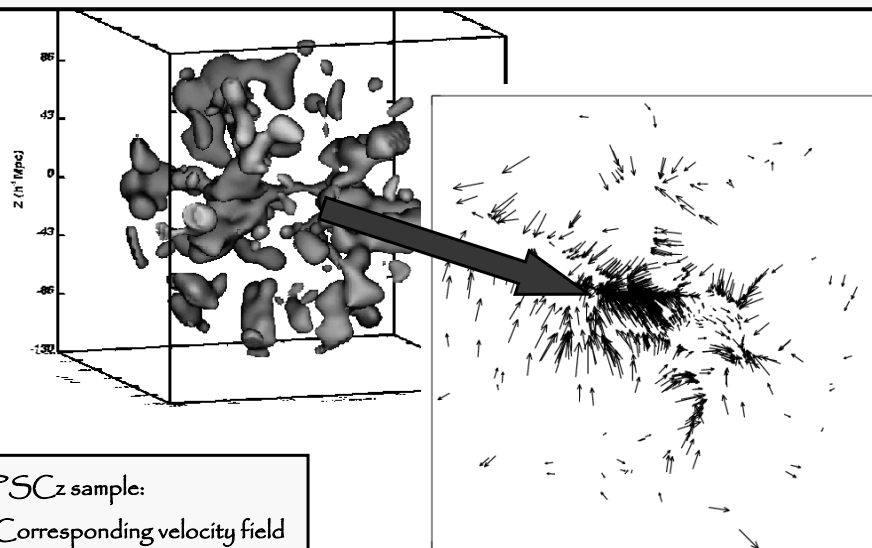
# Cosmic Migration Flows

$$\mathbf{v} = \frac{H f}{4\pi G \rho_u} \mathbf{g} = \frac{2 f}{3H\Omega} \mathbf{g}$$

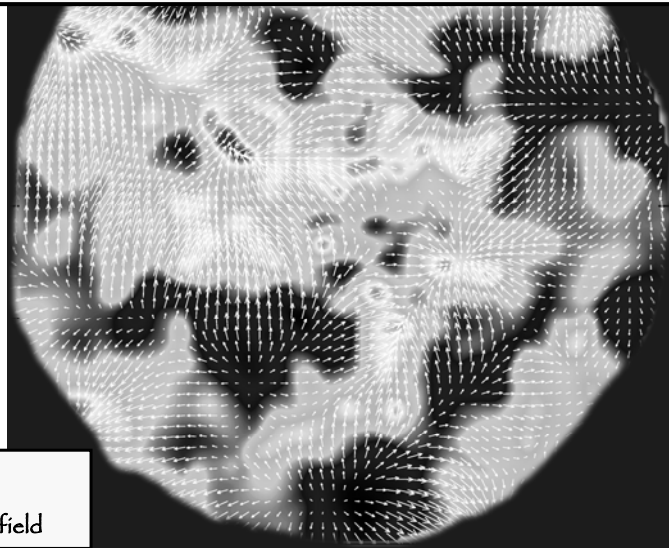


$$\mathbf{v}(\mathbf{x}, t) = \frac{H}{4\pi} \frac{f(\Omega_m)}{b} a \int d\mathbf{x}' \delta_{gal}(\mathbf{x}', t) \frac{(\mathbf{x}' - \mathbf{x})}{|\mathbf{x}' - \mathbf{x}|^3} \quad (158)$$

# Cosmic Migration Flows

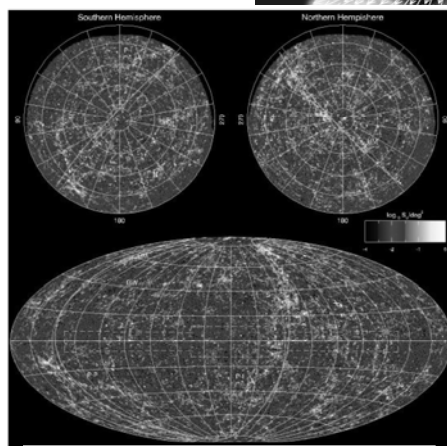


# Cosmic Migration Flows

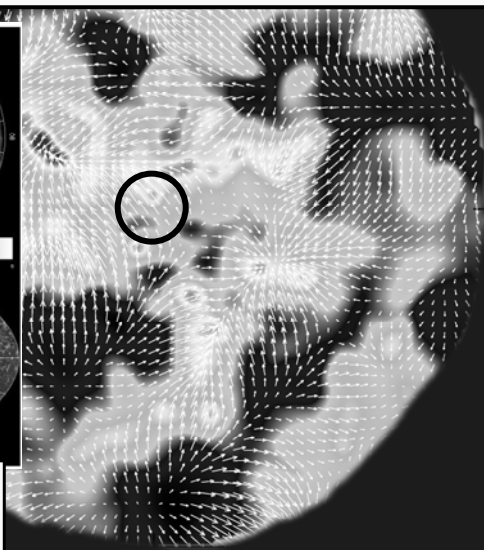


PSCz sample,  
Map Density & Flow field

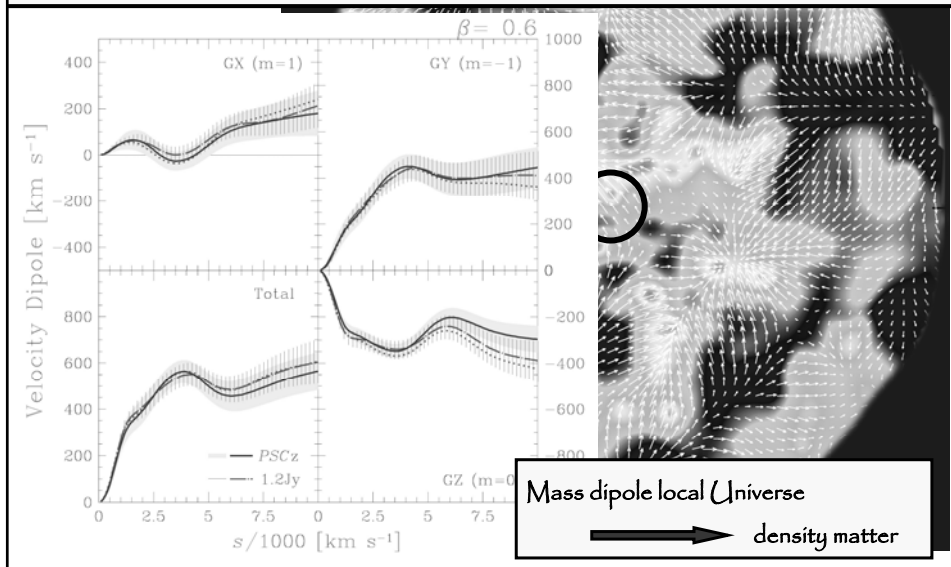
# Cosmic Migration Flows



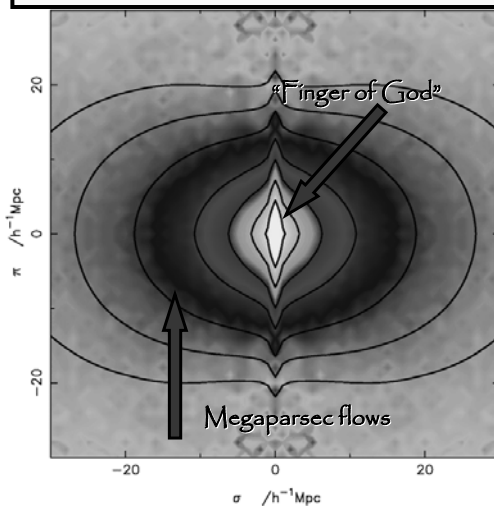
PSCz sample & 2MASS sky  
Flow around Local Group



# Cosmic Migration Flows



## the Web: Migration Flows



Large scale flows lead to redshift distortions:

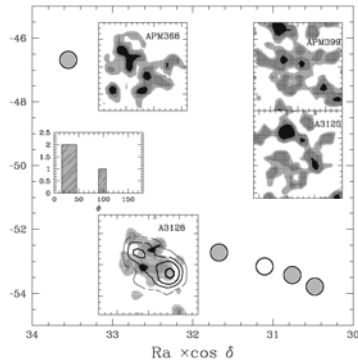
$$cz = Hr + v_{\text{pec}}$$

These flows are part of the assembly of large scale structures, and reach largest values as matter is transported along the filaments into the clusters.

When mapping the galaxy distribution in redshift space, this induces a distortion:

- Flattening along  $z$  as matter flows into Megaparsec features ( $v < 600 \text{ km/s}$ ).
- Extension due to thermal motions inside cluster ( $v \sim 1000 \text{ km/s}$ ): "Fingers of God"

# Web Dynamics: Alignments



Of outmost importance for understanding the dynamical origin of the cosmic web is that of alignments between and around clusters of galaxies.

The presence of such alignments is an indication for the tidal origin of the cosmic web with the clusters as the dominant tidal agents.

This forms an essential ingredient of the "Cosmic Web" theory of Bond et al.

Work by various groups, most notably Plionis and collaborators, indicate that indeed clusters, and galaxies around them, reveal significant alignments.

Plionis 2005

# Cosmic Shear & Gravitational Lensing

# Gravitational Lensing

A highly promising method to determine the amount and distribution of matter in the Universe does not concentrate on the way in which Dark Matter affects

- the motions of galaxies and the intracluster gas,

but instead looks at the way it affects

- the trajectories of photons.

According to Einstein's theory of general relativity, gravitational potential wells will bend and focus light. Dark matter concentrations will therefore act

Gravitational Lens

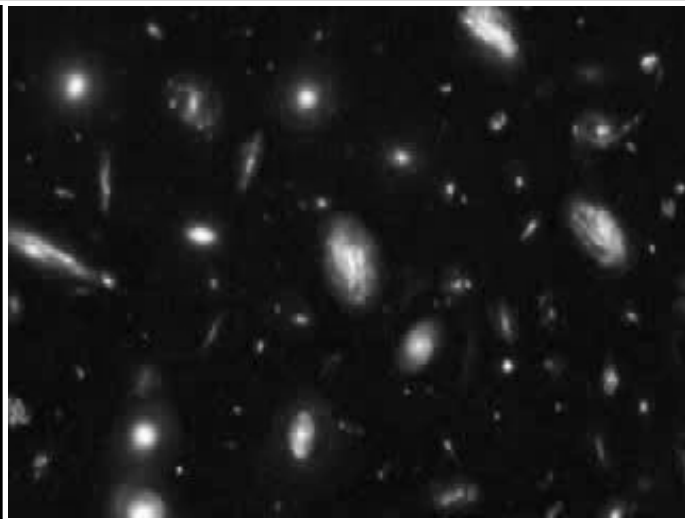


A1689, HST, Broadhurst et al.

# Gravitational Lensing

Illustration:

Mass passing in front of background of galaxies, distorting their received images.

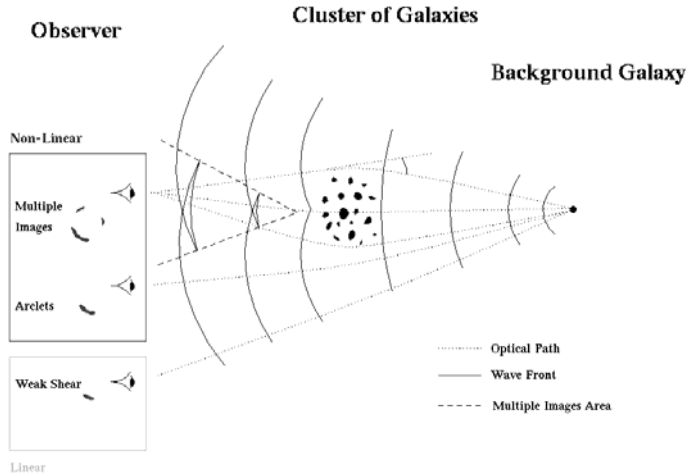


# Clusters: Gravitational Lensing

Illustration:

Dependent on whether the light passes within Einstein radius or outside, we deal with:

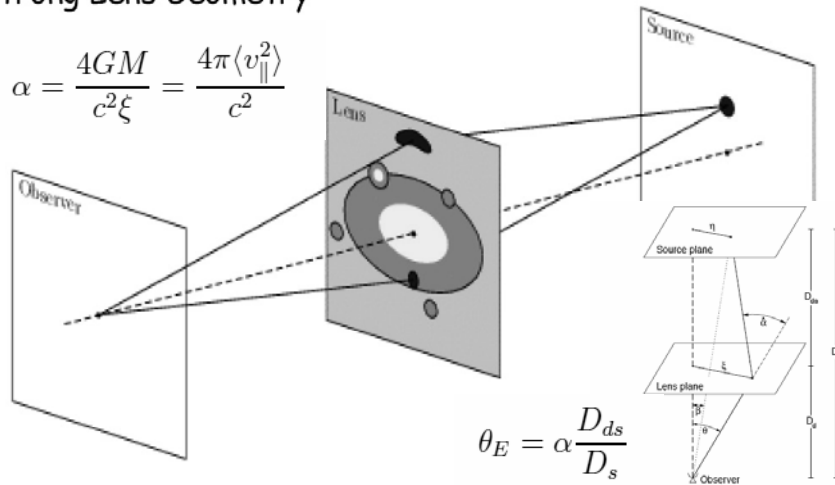
- **Strong Lensing:**  
nonlinear distortions
- **Weak Lensing:**  
linear distortions



# Gravitational Strong Lensing

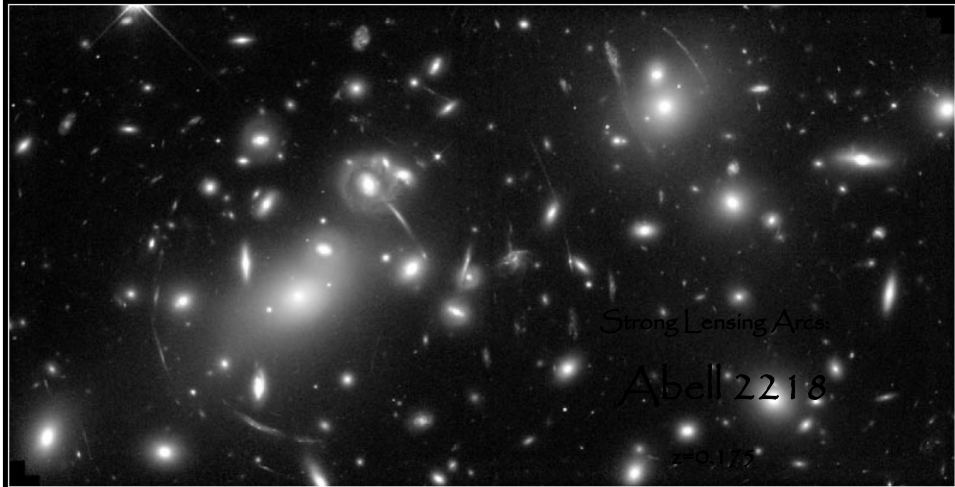
Strong Lens Geometry

$$\alpha = \frac{4GM}{c^2\xi} = \frac{4\pi\langle v_{\parallel}^2 \rangle}{c^2}$$



$$\theta_E = \alpha \frac{D_{ds}}{D_s}$$

# Clusters: Gravitational Lensing

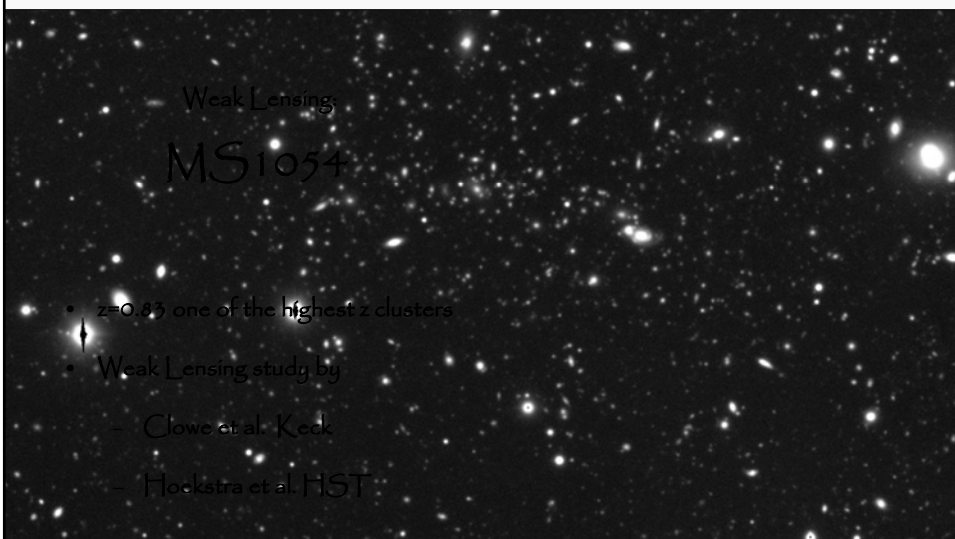


**Galaxy Cluster Abell 2218**

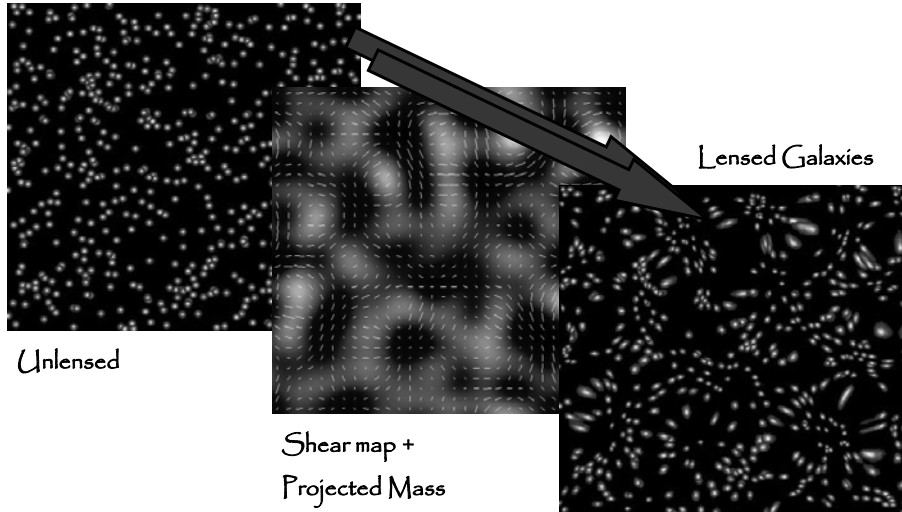
HST • WFPC2

NASA, A. Fruchter and the ERO Team (STScI) • STScI-PRC00-08

# Clusters: Gravitational Weak Lensing



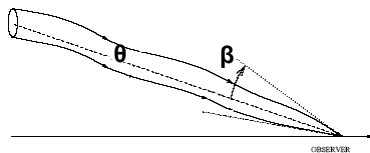
# Gravitational Weak Lensing



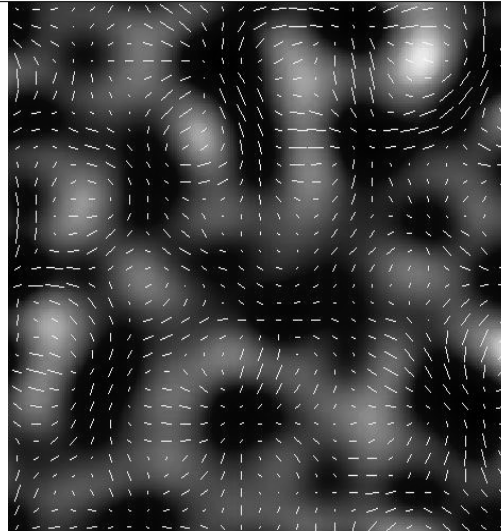
# Gravitational Lensing

$$A_{ij} \equiv \frac{\partial \beta_i}{\partial \theta_j} = \begin{pmatrix} 1 - \kappa & 0 \\ 0 & 1 - \kappa \end{pmatrix} + \begin{pmatrix} -\gamma_1 & \gamma_2 \\ \gamma_2 & \gamma_1 \end{pmatrix}$$

Magnification                  Shear



$$\begin{aligned} \kappa &= \frac{1}{2} (\phi_{,11} + \phi_{,22}) \\ \gamma_1 &= \frac{1}{2} (\phi_{,11} - \phi_{,22}) \\ \gamma_2 &= \phi_{,12} \\ \phi_{,ij} &= \frac{\partial^2 \phi}{\partial \theta_i \partial \theta_j} \end{aligned}$$





# Gravitational Lensing

$$\kappa = \frac{1}{2}(\phi_{,11} + \phi_{,22})$$

$$\gamma_1 = \frac{1}{2}(\phi_{,11} - \phi_{,22})$$

$$\gamma_2 = \phi_{,12}$$

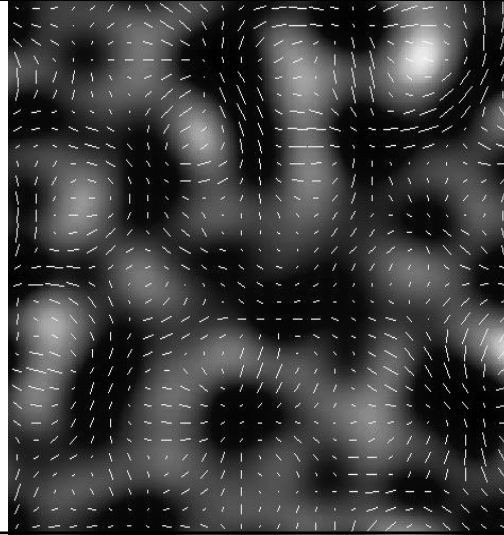
$$\phi_{,ij} = \frac{\partial^2 \phi}{\partial \theta_i \partial \theta_j}$$

Lensing Potential

related to

Peculiar Gravitational Potential

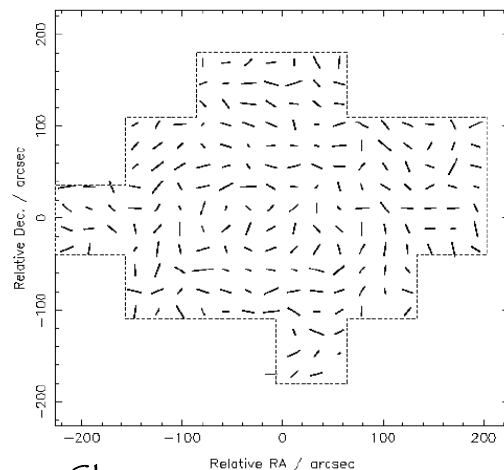
$$\phi(\mathbf{r}) = \frac{2}{c^2} \int_0^r dr' \Phi(r') \left( \frac{1}{r} - \frac{1}{r'} \right)$$



# Clusters: Gravitational Lensing

MS1054

- $z=0.83$  one of the highest  $z$  clusters
- Studied by
  - Clowe et al. Keck
  - Hockstra et al. HST

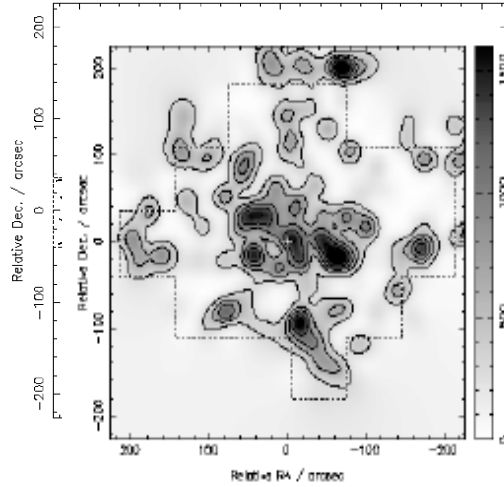


Shear map

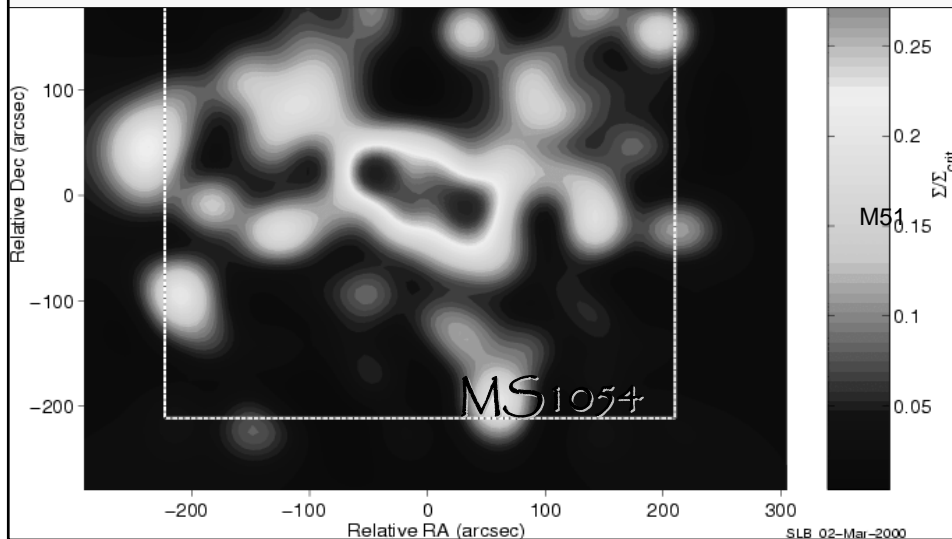
# Clusters: Gravitational Lensing

MS1054

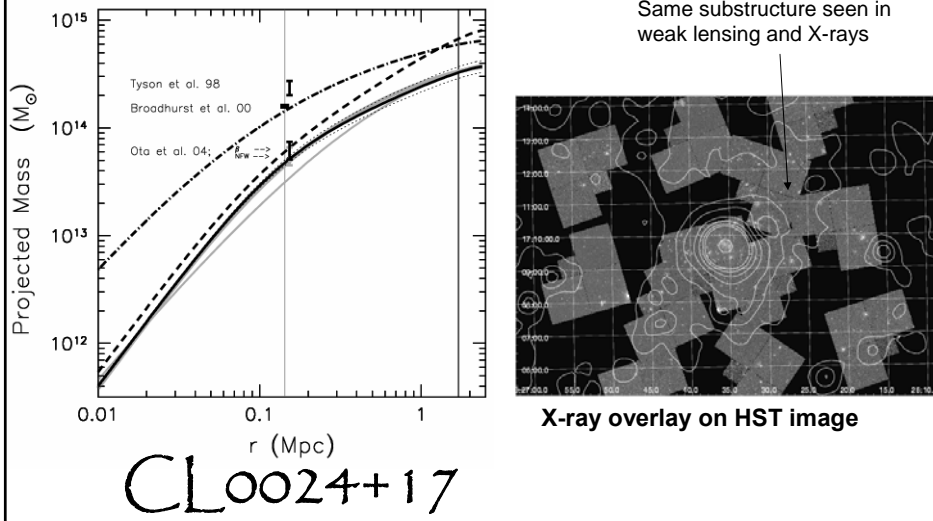
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  - Hoekstra et al. HST



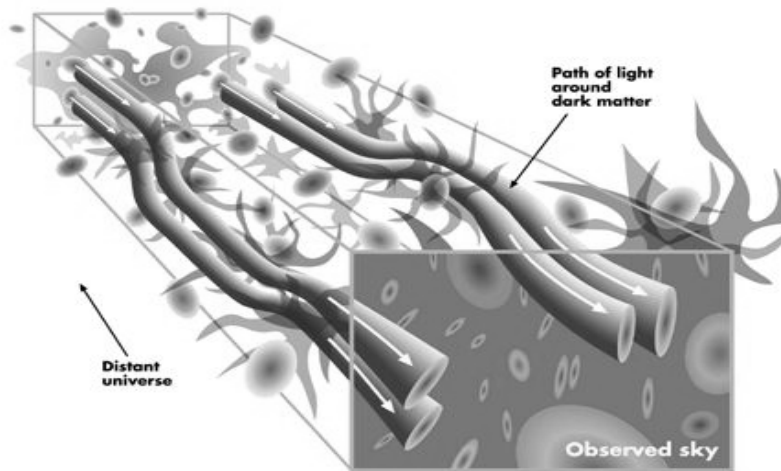
# Clusters: Gravitational Lensing



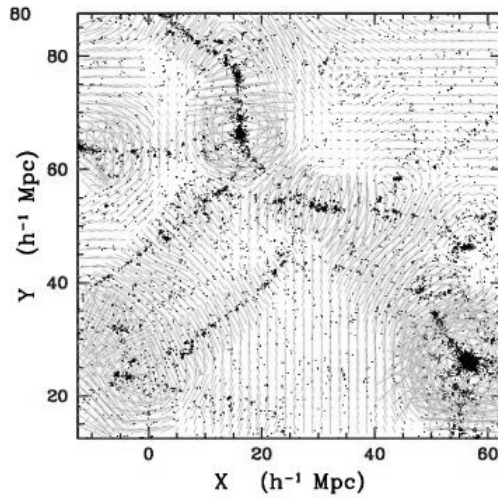
# Clusters: Comparison Lensing & X-ray



# Cosmic Shear



# the Web: Shear Distortions & Lensing



Large scale tidal shear distorts the paths of photons as they travel from their source to the observer.

This effect is known as "gravitational lensing". For moderate distortions, outside the Einstein radius ("weak lensing"),

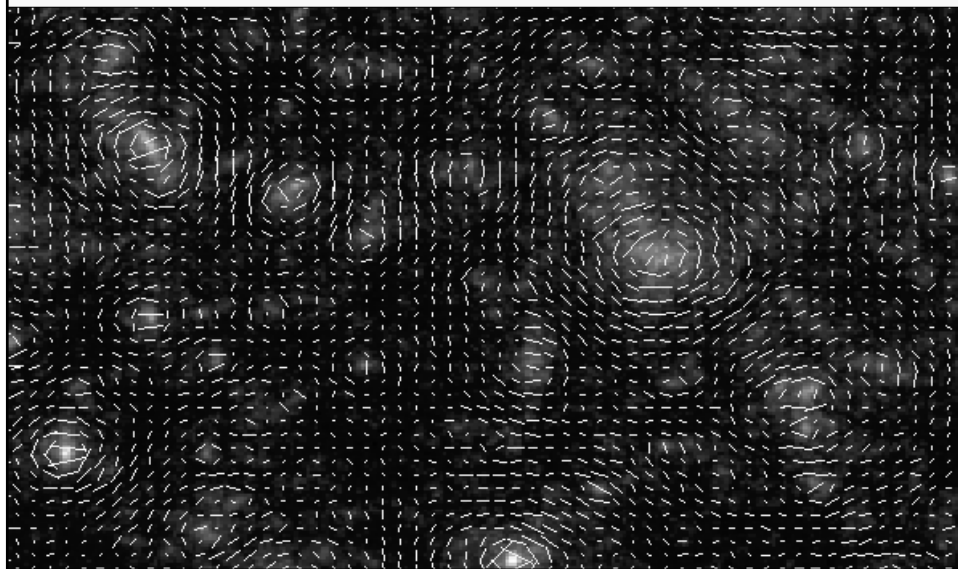
the distortions of galaxy shapes can be measured and inverted to yield the (projected) distorting mass distribution.

Clusters are outstanding, representing major potential wells.

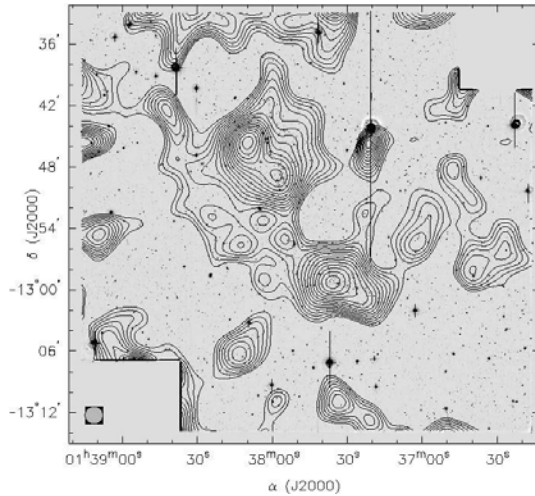
But also the generic Megaparsec matter distribution "lenses":

Cosmic Shear

## Cosmic Shear



## the Web: Shear Distortions & Lensing



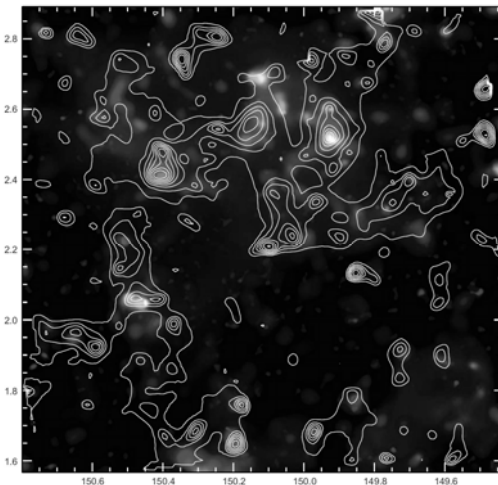
Although the cosmic shear due to a filament is considerably weaker than that of the clusters, recently

Dietrich, Schneider & Romano-Díaz (2004)

succeeded in mapping the filament between A222 and A333 on the basis of the measured lensing.

This shows that filaments are shown to be genuine dynamical entities.

## the Web: Shear Distortions & Lensing



First genuine map

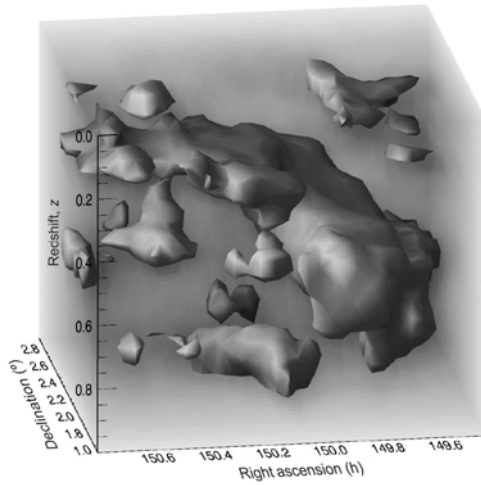
Large Scale

Cosmic Dark Matter distribution  
by means of weak lensing:

Clearly visible is the filamentary  
Weblike nature of the mass  
Distribution.

Massey et al. 2007

# the Web: Shear Distortions & Lensing



First genuine map  
Large Scale  
Cosmic Dark Matter distribution  
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Massey et al. 2007