

## Probes Dark Energy

- **Supernovae Ia**  
probing luminosity distance – redshift relation
- **Clusters of Galaxies**  
number counts  $N(z)$ ,  
# formed clusters of galaxies as function of  $z$  sensitive to  $w$  &  $w'$
- **Cosmic Shear/Weak Lensing**  
measures angular diameter distance-redshift relation, in combination with structure growth
- **Baryonic Oscillations (BAO)**  
cosmic yardstick, curvature: residual imprint in galaxy distribution  
acoustic oscillations primordial baryon-photon plasma
- **Integrated Sachs Wolfe (ISW)**  
imprint foreground large scale structure on CMB,  
via evolving potential perturbations
- **Clustering**  
clustering correlation function/power spectrum,  
directly probing cosmological scenario, BAO wiggles
- **Growth of clustering:**  
evolving growth rate  $f(\Omega_m, z)$ , probed via influence of  
redshift distortions on correlation functions
- **Voids:**  
evolving void shapes,  
probing tidal force field generated by large scale mass distribution
- **Morphology and Topology**  
sensitivity of topology, measured by homology (Betti numbers)

## Dark Energy Probes: Comparison

Method	Strengths	Weaknesses	Systematics
<b>Weak Lensing</b>	Structure Growth + Geometric Statistical Power	CDM assumption	Image quality Photo-z
<b>Supernovae SNIa</b>	Purely Geometric Mature	Standard Candle assumption	Evolution Dust
<b>BAO (Baryonic Acoustic Oscillation)</b>	Largely Geometric Low systematics	Large samples required	Bias Nonlinearity
<b>Cluster Population N(z)</b>	Structure Growth + Geometric Xray+SZ+optical	CDM assumption	Determining mass Selection function

## Standard Candle & Cosmic Distances

# Robertson-Walker Metric

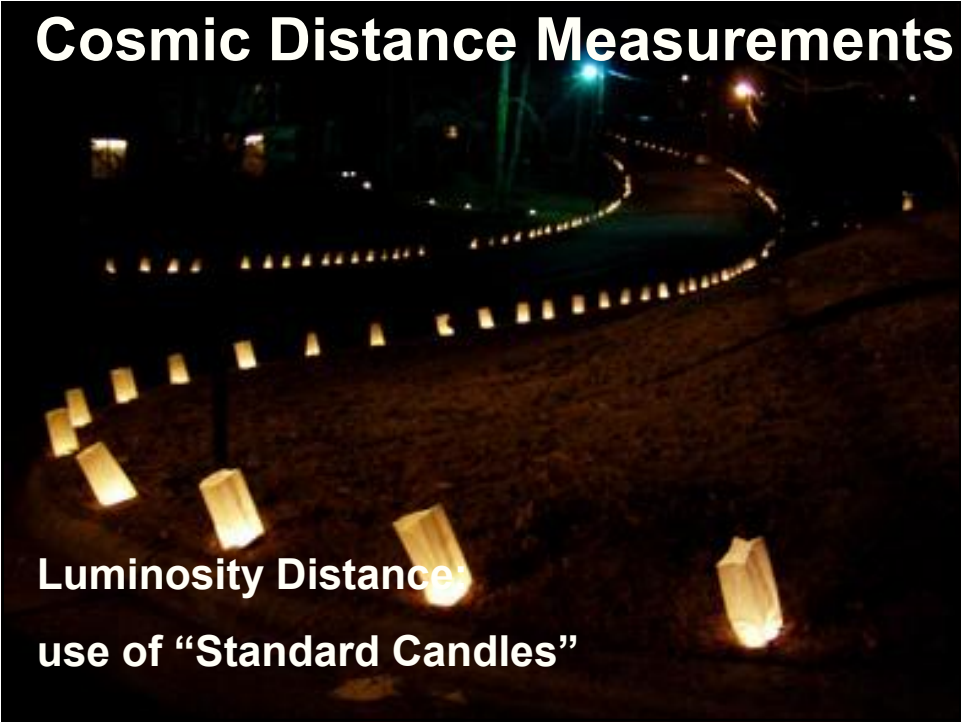
Distances in a uniformly curved spacetime is specified in terms of the Robertson-Walker metric. The spacetime distance of a point at coordinate  $(r, \theta, \phi)$  is:

$$ds^2 = c^2 dt^2 - a(t)^2 \left\{ dr^2 + R_c^2 S_k^2 \left( \frac{r}{R_c} \right) \left[ d\theta^2 + \sin^2 \theta d\phi^2 \right] \right\}$$

where the function  $S_k(r/R_c)$  specifies the effect of curvature on the distances between points in spacetime

$$S_k \left( \frac{r}{R_c} \right) = \begin{cases} \sin \left( \frac{r}{R_c} \right) & k = +1 \\ \frac{r}{R_c} & k = 0 \\ \sinh \left( \frac{r}{R_c} \right) & k = -1 \end{cases}$$

## Cosmic Distance Measurements



Luminosity Distance:  
use of “Standard Candles”



## Luminosity Distance

Definition cosmological luminosity distance:

$$l = \frac{L}{4\pi D_L^2}$$

for a source with INTRINSIC luminosity  $L$   
OBSERVED brightness  $l$

In a Robertson-Walker geometry, luminosity distance is

$$D_L = (1+z)D(z)$$

where  $D(z)$  is the cosmological distance measure

# Luminosity Distance

Cosmological distance measure:

$$D(z) = R_0 S_k \left( \frac{r}{R_0} \right)$$

with curvature term  $S_k(x) = \sin(x)$ ,  $x$ , or  $\sinh(x)$

$$r(z) = \frac{c}{H_0} \int_0^z dz' \left[ \sum_i \Omega_i (1+z')^{3+3w_i} - \frac{kc}{H_0 R_0} (1+z')^2 \right]^{-1/2}$$

Comoving radial distance  $r(z)$  at redshift  $z$

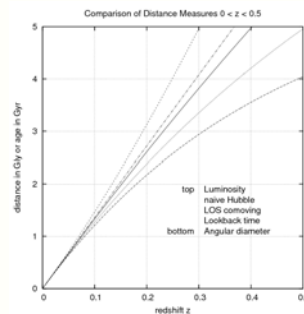
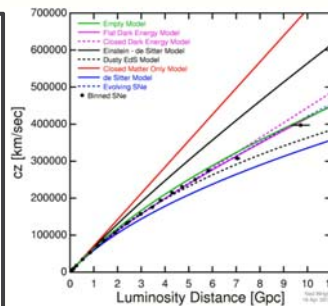
# Luminosity Distance

Luminosity Distance at low redshift:

$$D_L = \frac{c}{H_0} \left\{ z + z^2 \left( \frac{1-q_0}{2} \right) + O(z^3) \right\}$$

- with first term the linear Hubble expansion term
- second term the first acceleration/deceleration term:

$$D_L = \frac{1}{2} \sum_i \Omega_i (1+3w_i)$$



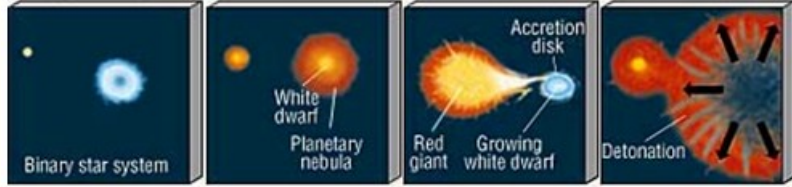
# Type Ia Supernovae

## Supernova Explosion & Host Galaxy

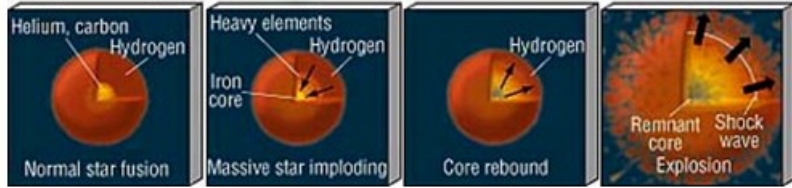


# Supernovae

(a) Type- I Supernova



(b) Type- II Supernova



Time →

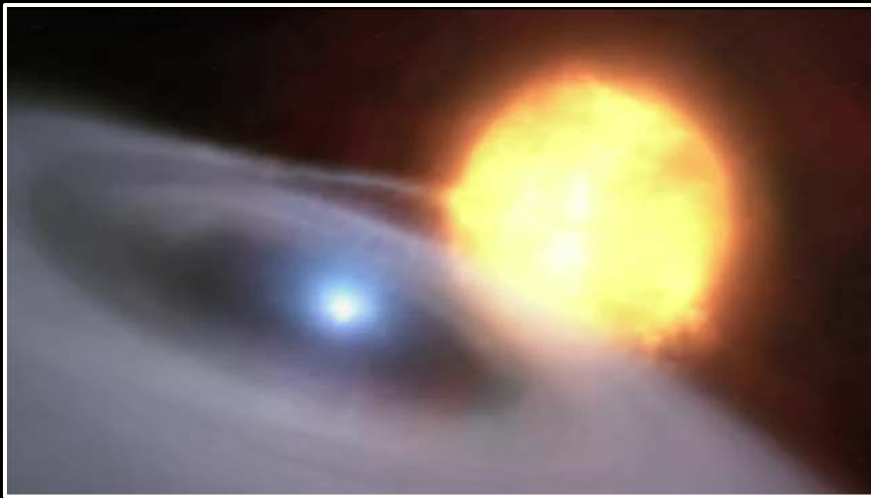
**Supernovae:**

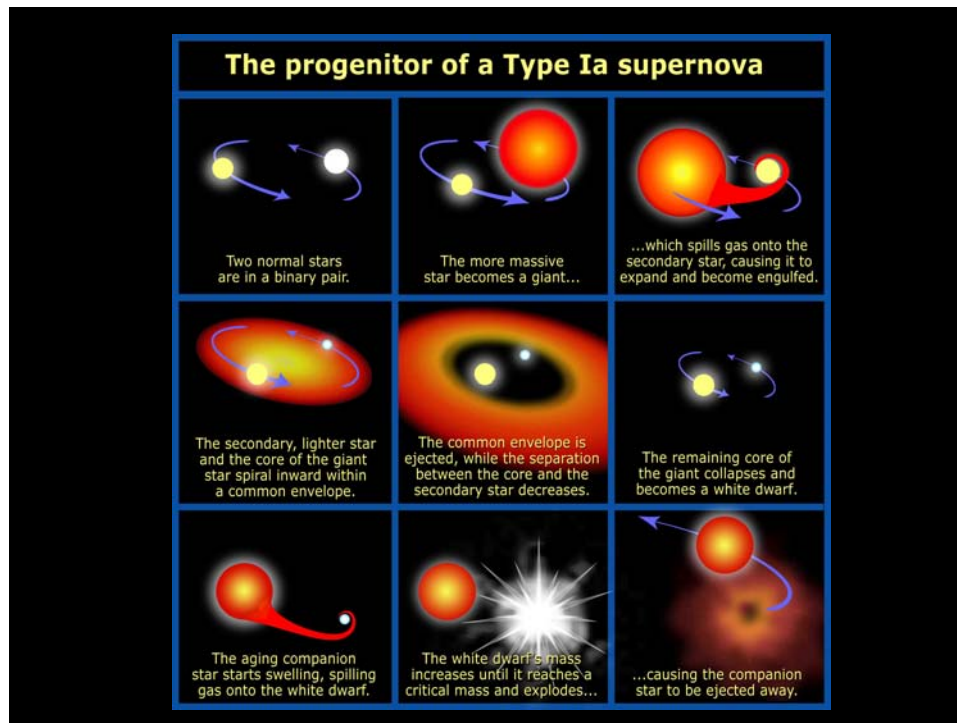
- gigantic stellar explosions
- within few months more radiation than Sun over entire lifetime
- shockwaves 5,000-30,000 km/s
- enrichment interstellar medium
- triggers star formation in surrounding ISM

**Supernovae, 4 types**

- (spectral absorption lines):
- SN II
  - SN Ia - no hydrogen
  - SN Ib
  - SN Ic - no helium

## Type Ia Supernova Explosion





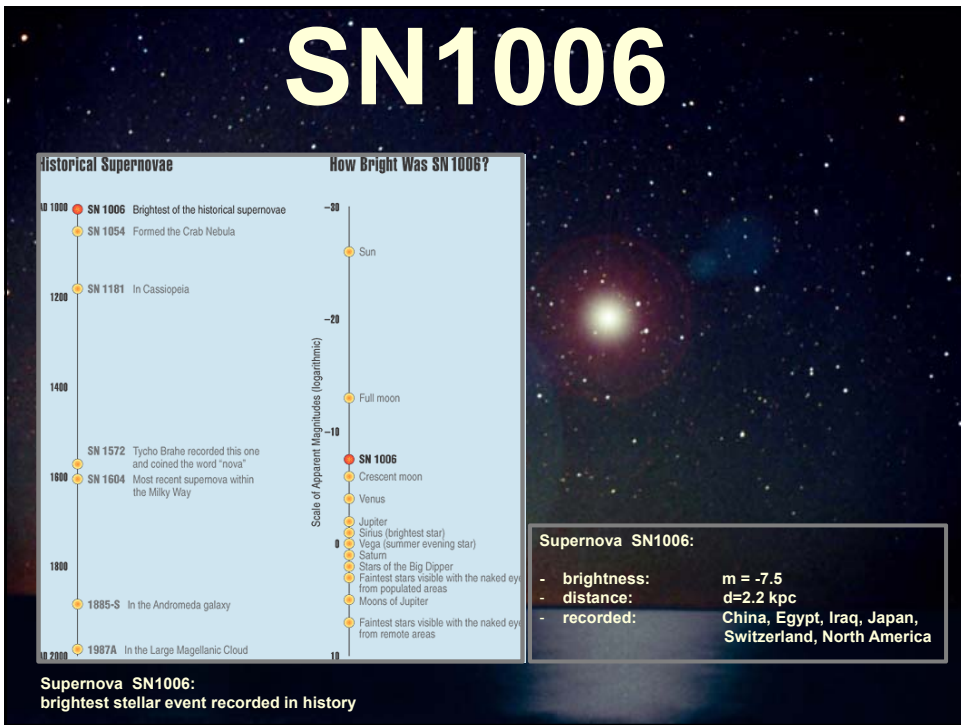
## Type Ia Supernova

- Amongst the most energetic explosions in our Universe:  
 $E \sim 10^{54}$  ergs
- During explosion the star is as bright as entire galaxy ! (ie.  $10^{11}$  stars)

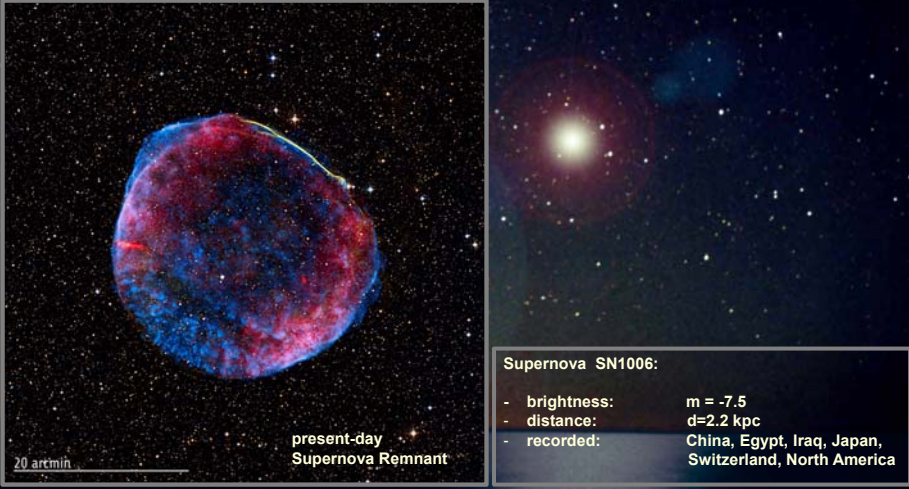
- Violent explosion Carbon-Oxygen white dwarfs:
- Embedded in binary, mass accretion from companion star
- When nearing Chandrasekhar Limit ( $1.38 M_{\odot}$ ), electron degeneracy pressure can no longer sustain star.
- while contracting under its weight, carbon fusion sets in, powering a catastrophic deflagration or detonation wave,
- leading to a violent explosion, ripping apart entire star

- Because exploding stars have nearly uniform progenitor ( $\sim 1.38 M_{\odot}$  white dwarf), their luminosity is almost the same:  
 $M \sim -19.3$   
 Standard Candle





# SN1006



present-day  
Supernova Remnant

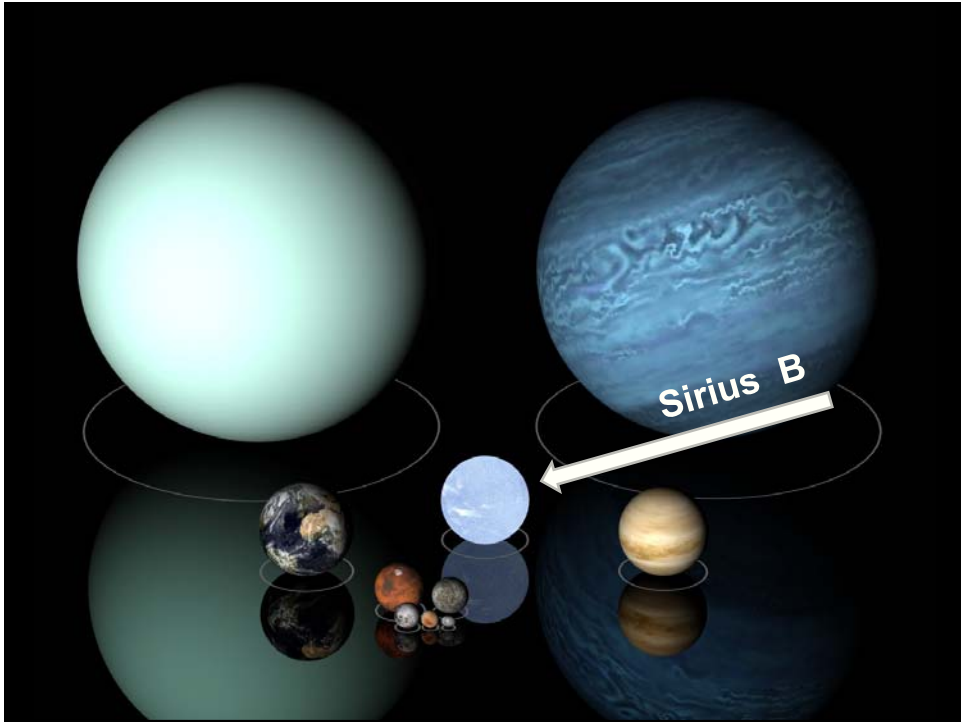
20 arcmin

Supernova SN1006:  
- brightness:  $m = -7.5$   
- distance:  $d = 2.2 \text{ kpc}$   
- recorded: China, Egypt, Iraq, Japan, Switzerland, North America

Supernova SN1006:  
brightest stellar event recorded in history

# White Dwarfs





Degenerate matter (helium, carbon or other possible reaction products)

Normal gas (50 km thick)

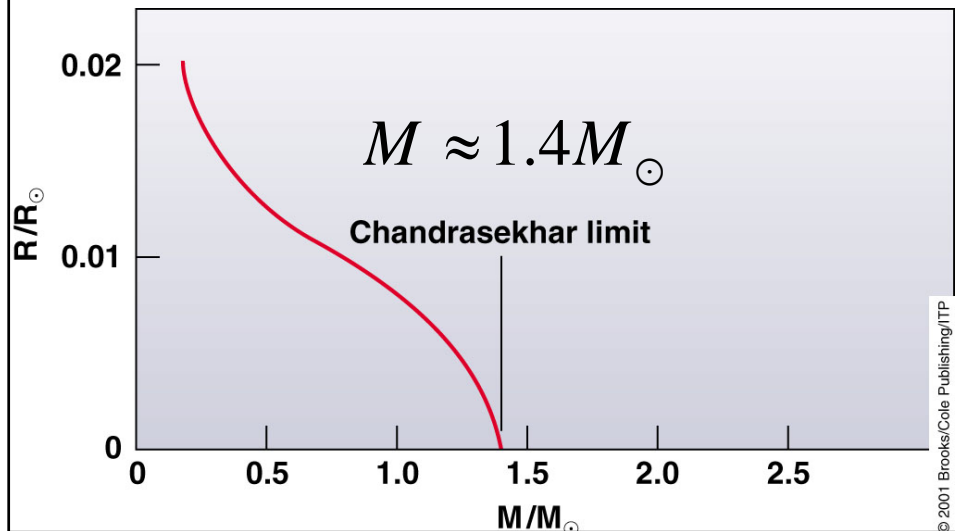
5000 to 6000 km

Regular gas: many unfilled energy levels. Particles free to move about and change energy levels.

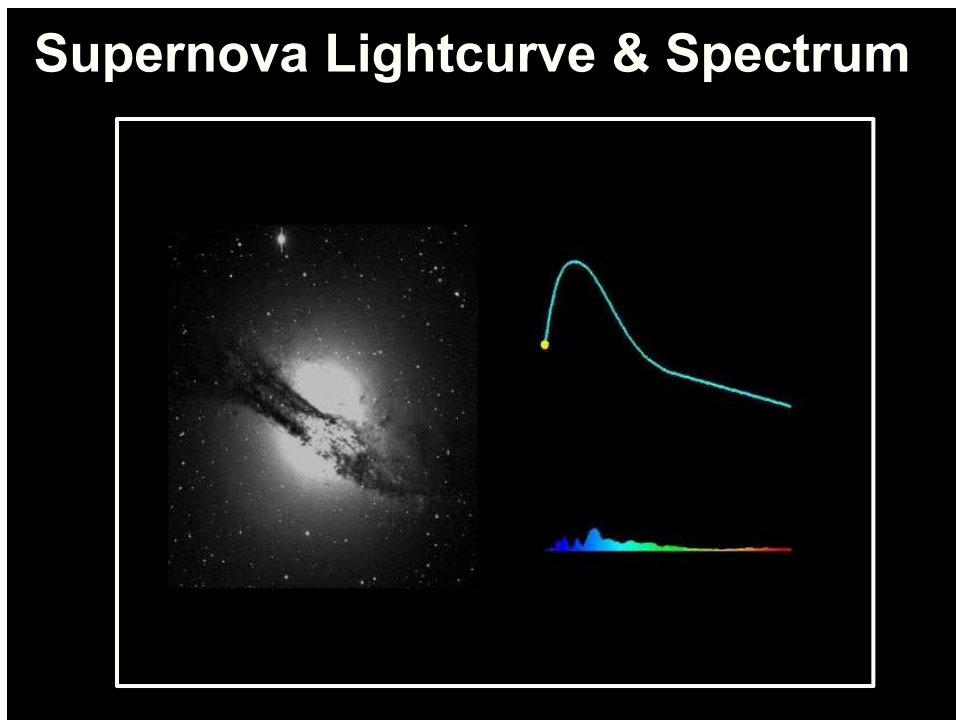
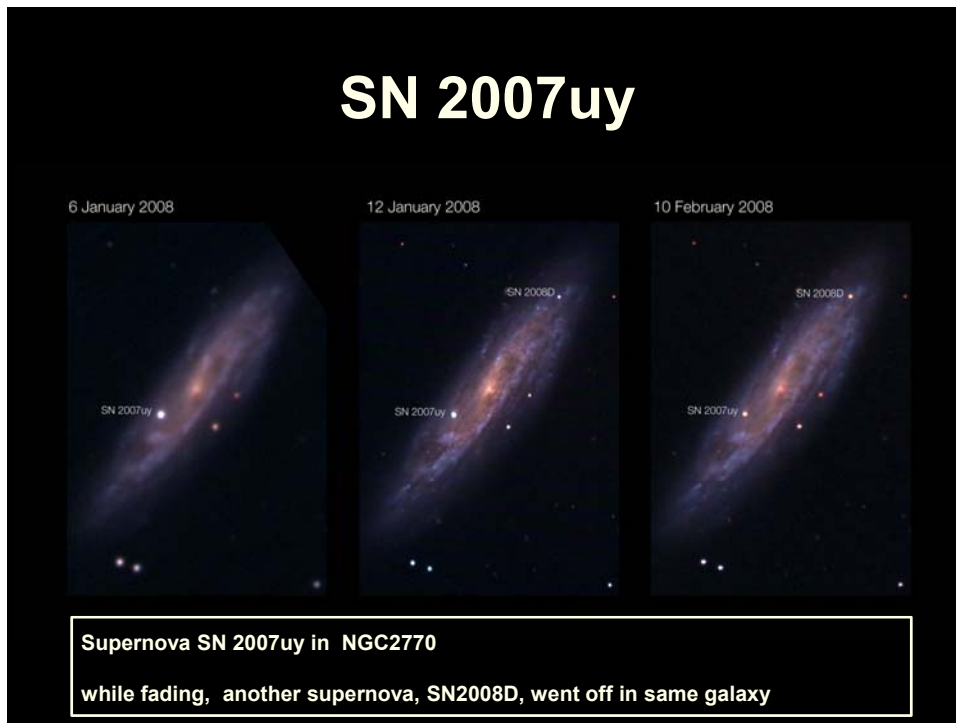
**Degenerate** gas: all lower energy levels filled with two particles each (opposite spins). Particles **locked** in place.

## Chandrasekhar Mass Limit

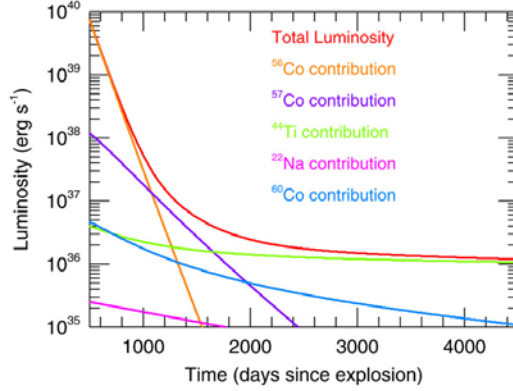
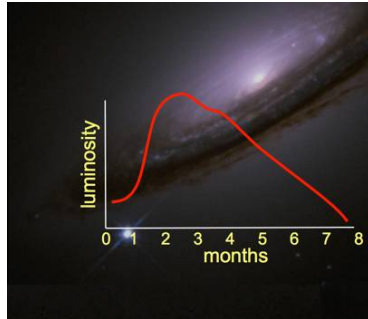
What is the maximum mass that can be supported by the dense compact material of a white dwarf star?



## Supernova Lightcurves



# Supernova Lightcurve

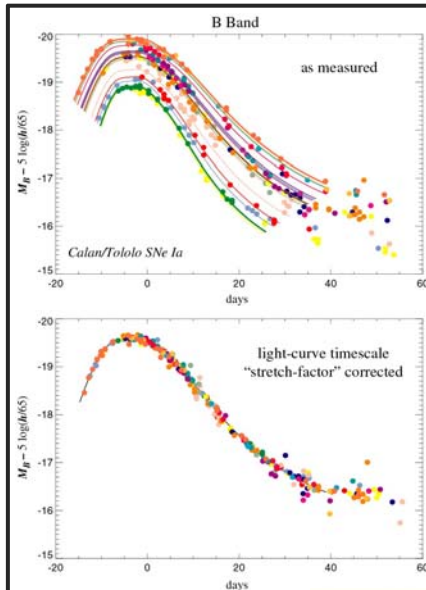


Type Ia supernovae follow a characteristic light curve—the graph of luminosity as a function of time—after the explosion.

This luminosity is generated by the radioactive decay of Nickel-56 through Cobalt-56 to Iron-56.

Maximum absolute magnitude of about -19.3.

# the Phillips Relation



Relationship between

- peak luminosity of a Type Ia supernova
- speed of luminosity evolution after maximum light.

Mark Phillips (1993):

- on the basis of Calan/Tololo Supernova Survey
- the faster a supernova fades after peak,
- the fainter its intrinsic peak luminosity
- reduces scatter in Hubble diagram to  $\sigma < 0.2$  mag
- heuristic relationship, as yet not theoretically “understood”

# Supernova Teams: Practical Aspects

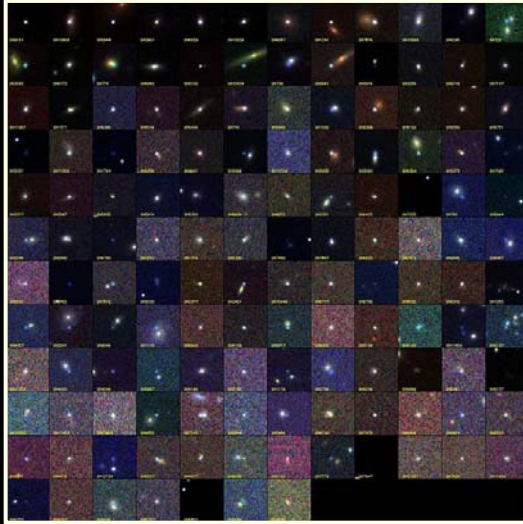
## Supernova Cosmology Project

Success of Supernova Projects built on 3 major developments:

- **the introduction in the 1980s of large mosaic charge-coupled device (CCD) cameras on 4-meter class telescopes:**
  - systematic search of thousands of galaxies over large area of sky for rare supernova events
- **dramatic increase in computing power in the 1980s:**
  - enabling vast amount of data processing for automated search of supernovae amongst the huge number of galaxies monitored
- **Supernovae Ia as standard candles**
  - Calan/Tololo Supernova Search: accurate light curves & spectra
  - Phillips relation

## High-z Supernova Search Team

## Supernova Cosmology Project



diligently monitoring millions of galaxies, in search for that one explosion ...

## High-z Supernova Search Team

## Supernova Cosmology Project

### Challenges to be dealt with by Supernova Teams:

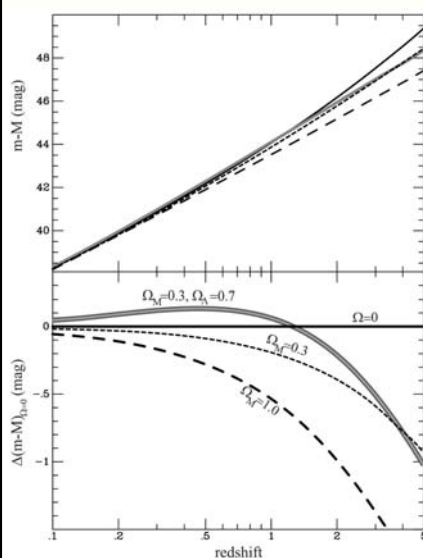
- Huge logistic (and political) issue of assuring vast amounts of (strongly contested) observing time on a range of telescopes (incl. 4-m ones for probing high-z universe)
- Dealing with a range of astronomical effects that would render any subtle cosmological signature insignificant:
  - Influence of dust: affecting brightness of supernovae
  - Abundance effects: poorly understood influence of heavy chemical elements on supernova lightcurves
  - ....
- Results put under heavy scrutiny through large range of tests dealing with each imaginable pitfall and artefact
- Absolutely crucial that two competing teams reached same conclusion independently !!!!

## High-z Supernova Search Team



# Cosmic Acceleration

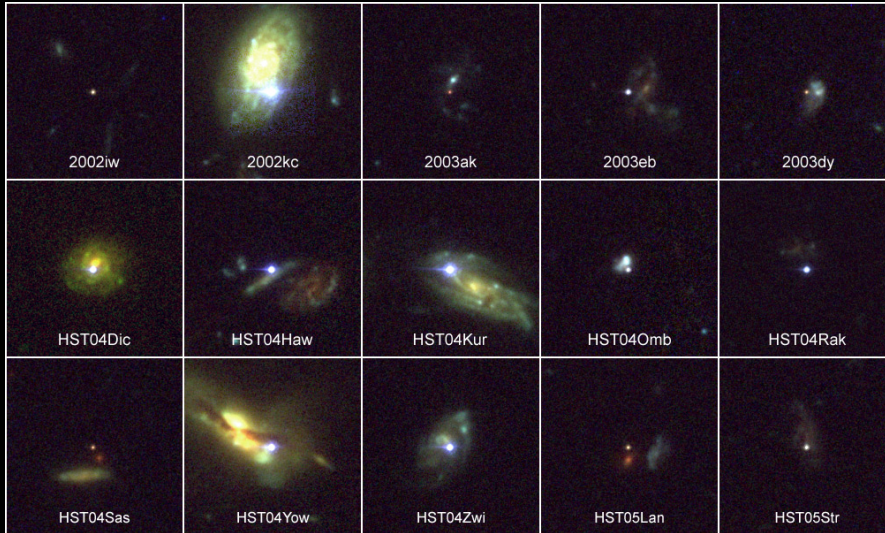
## Cosmic Acceleration



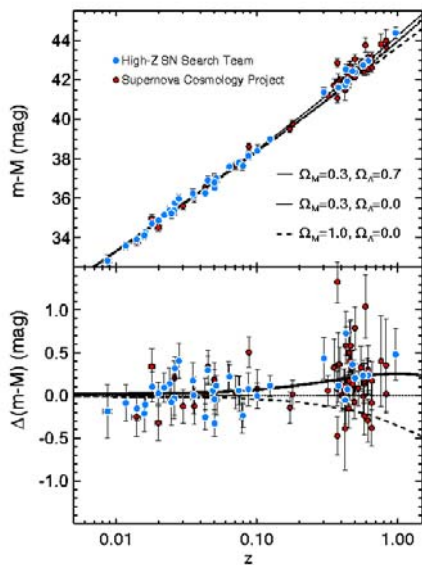
### Hubble Diagram high-z SNIa

- distance vs. redshift  $z$   
 $m-M$  vs. redshift  $z$
- determine:
  - absolute brightness of supernova Ia
  - from dimming rate (Phillips relation)
- measure:
  - apparent brightness of explosion
- translates into:
  - luminosity distance of supernova
  - dependent on acceleration parm.  $q$

# High-z SNIa: sample



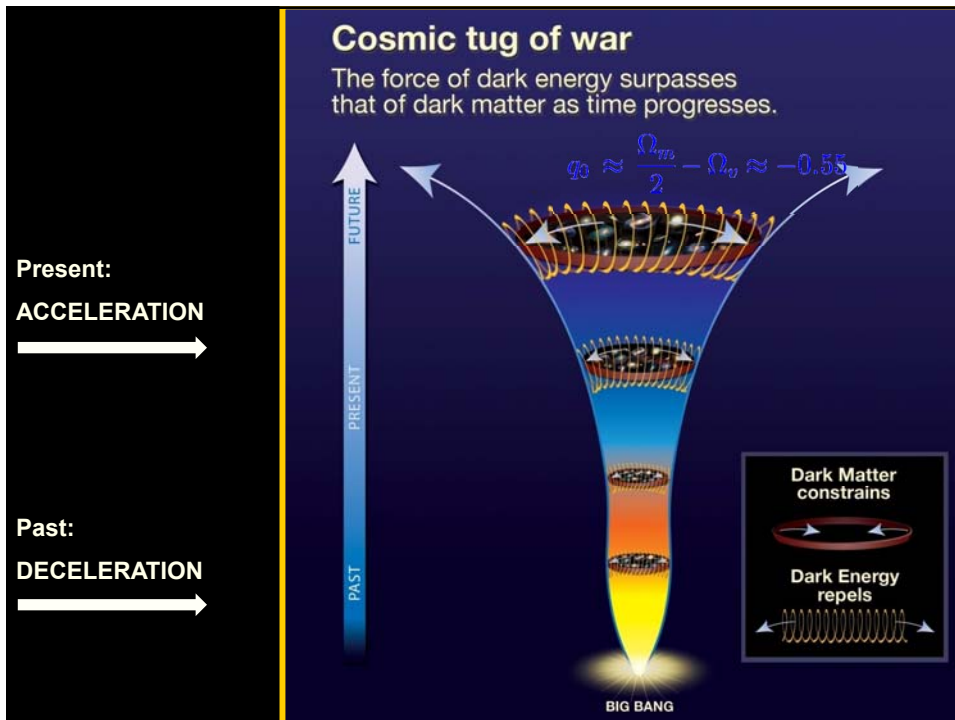
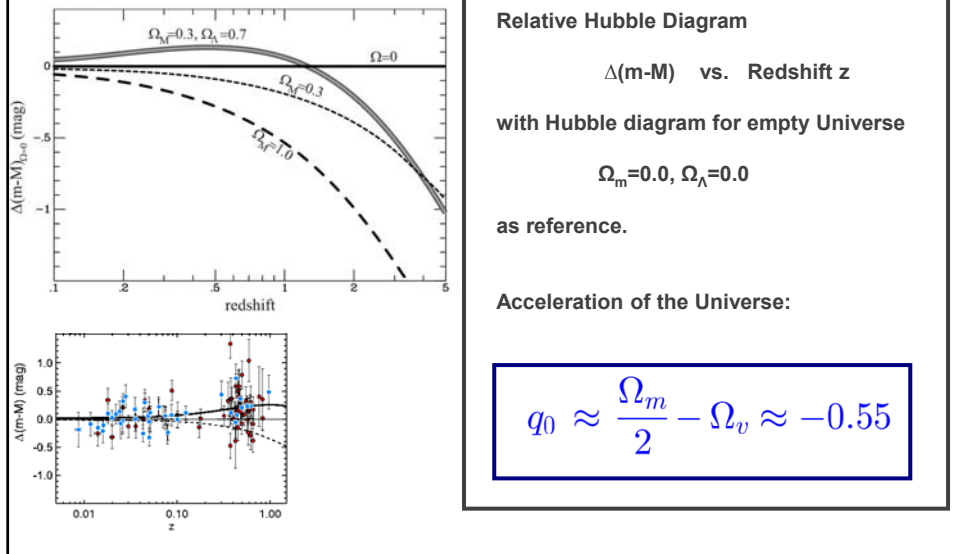
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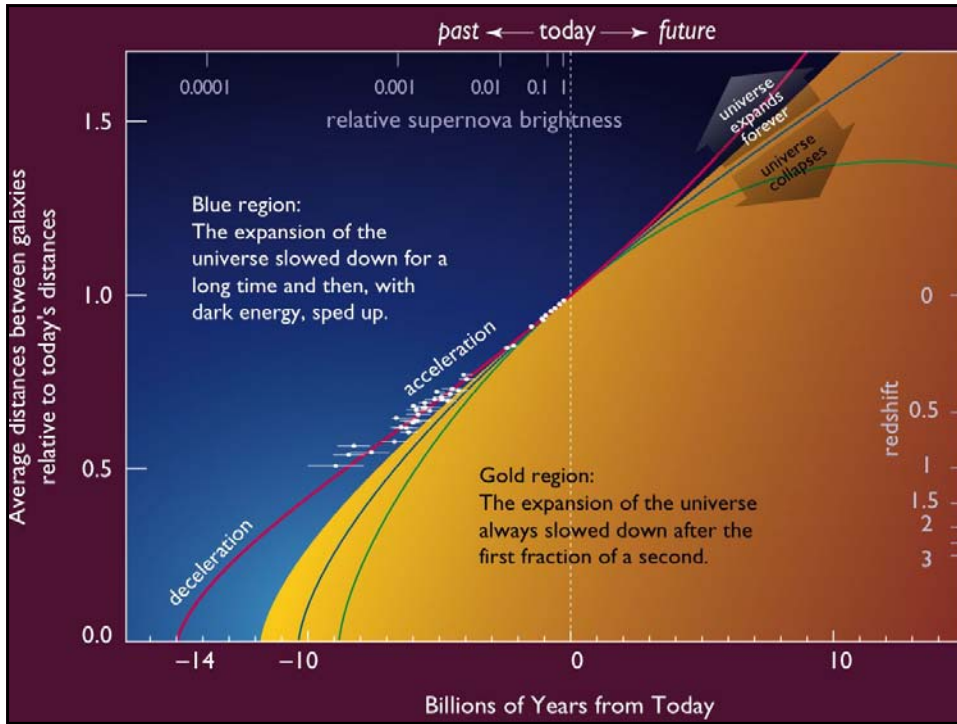


## Hubble Diagram high-z SNIa

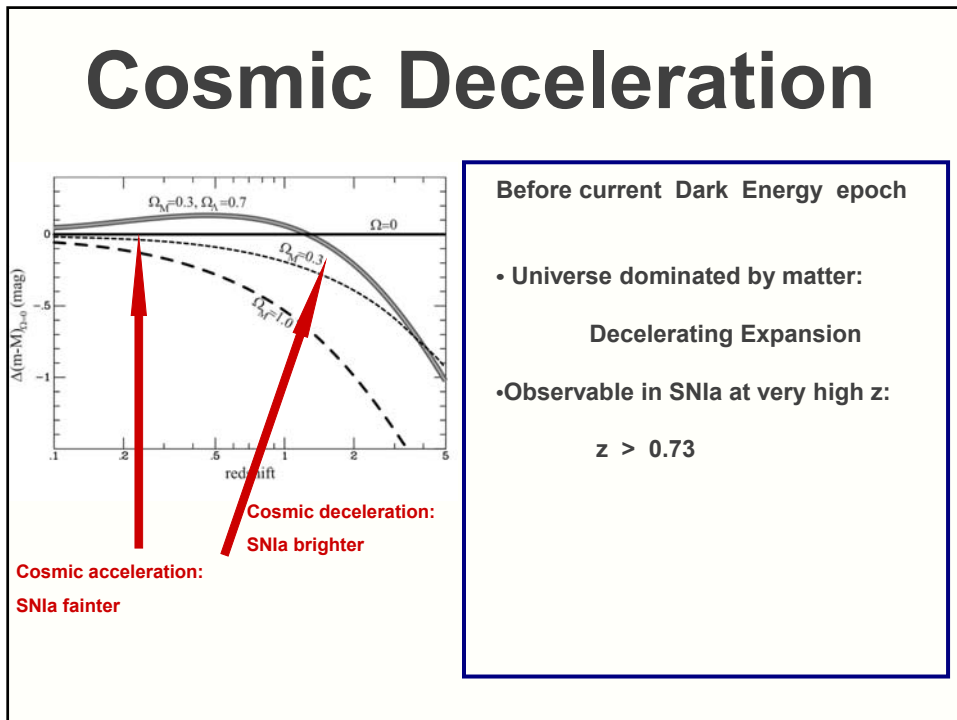
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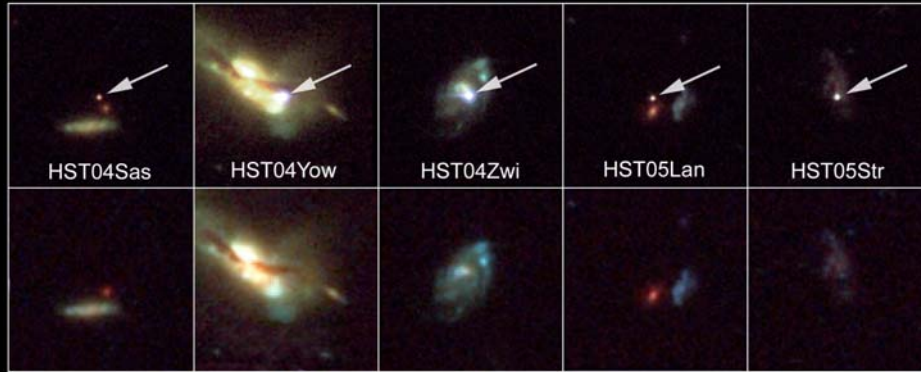




# Cosmic Deceleration



# Beyond Acceleration: SNe Ia at $z > 0.7$



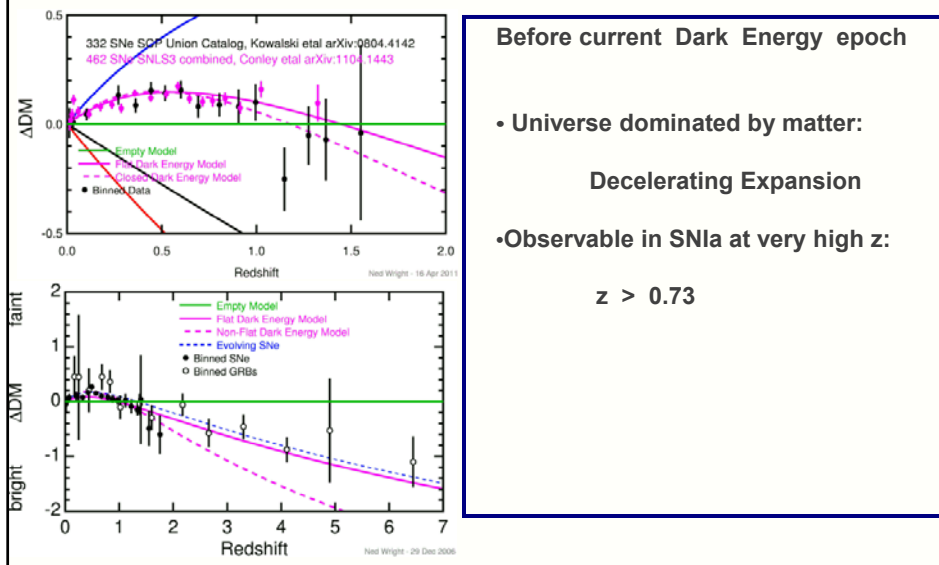
Five high-z SNIa, images HST-ACS camera

SNIa and host galaxies

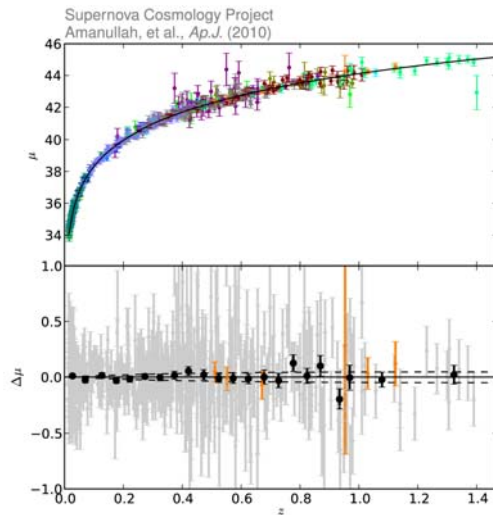
lower panel: before

top panel: after explosion)

# Cosmic Deceleration



# Union2: state-of-the-art SNIa compilation



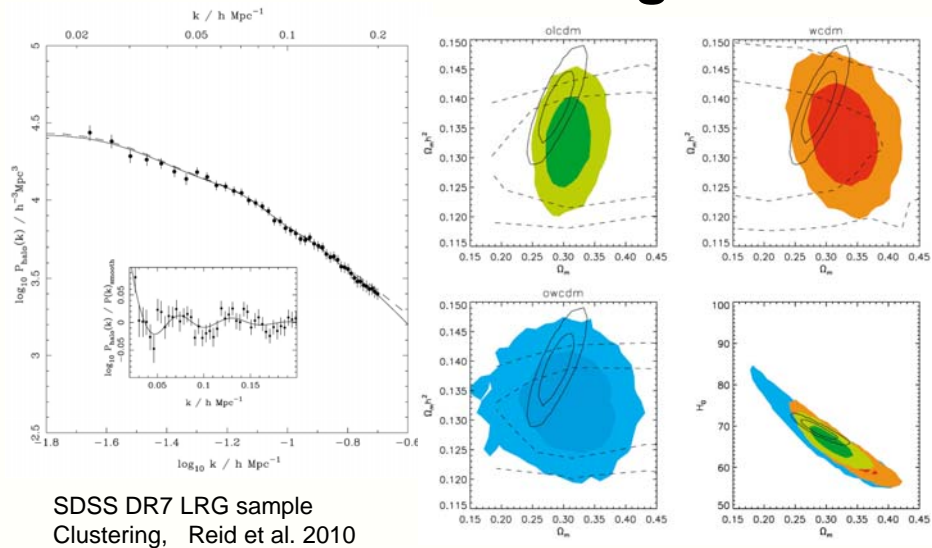
SCP Union2.1 SN Ia  
compilation:

719 SNe, 17 datasets  
(557 used)  
6  $z > 1$  SN Ia

Amanullah et al. 2010

# Clustering

## Cosmic Constraints LSS Clustering

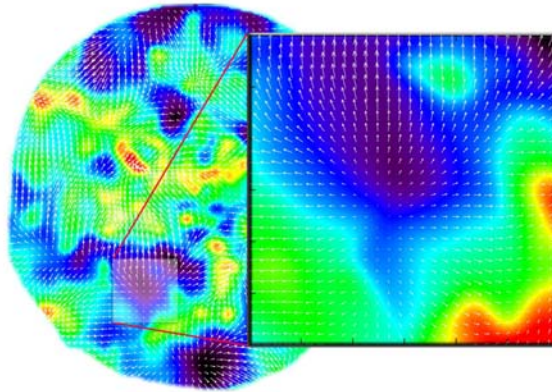


## Structure Growth Factor

# Large Scale Flows

## Large-Scale Flows:

- On large (Mpc) scales, structure formation still in linear regime
- Structure buildup accompanied by displacement of matter:
  - Cosmic flows
- Directly related to cosmic matter distribution



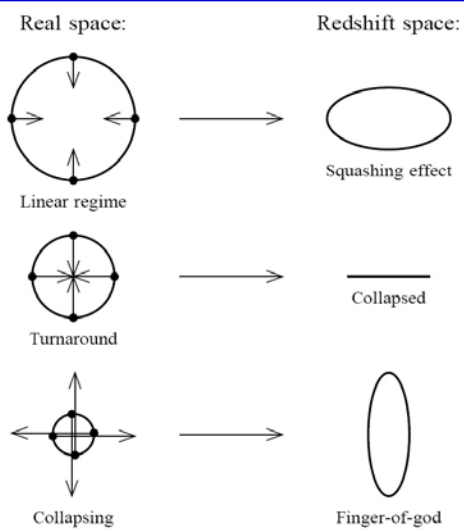
$$\mathbf{v}(\mathbf{x}, t) = \frac{H}{4\pi} \frac{f(\Omega_m)}{b} a \int d\mathbf{x}' \delta_{gal}(\mathbf{x}', t) \frac{(\mathbf{x}' - \mathbf{x})}{|\mathbf{x}' - \mathbf{x}|^3}$$

# Redshift Distortions

## Origin of peculiar velocities:

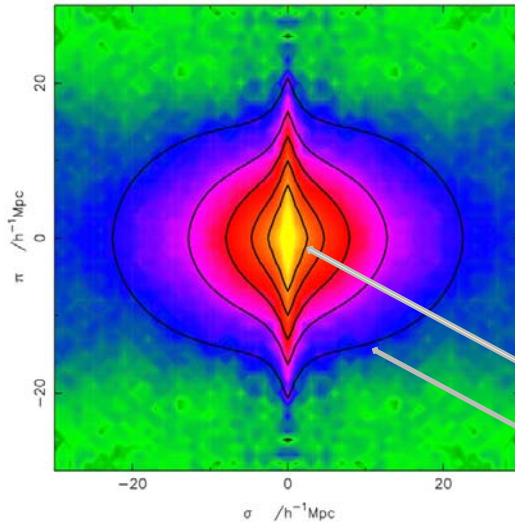
### three regimes

- very high-density virialized cluster (core) regions: "thermal" motion in cluster, up to > 1000 km/s
- "Fingers of God"
- collapsing overdensity (forming cluster): inflow/infall velocity
- Large scales: (linear, quasi-linear) cosmic flow, manifestation of structure growth





## sky-redshift space 2-pt correlation function $\xi(\sigma, \pi)$



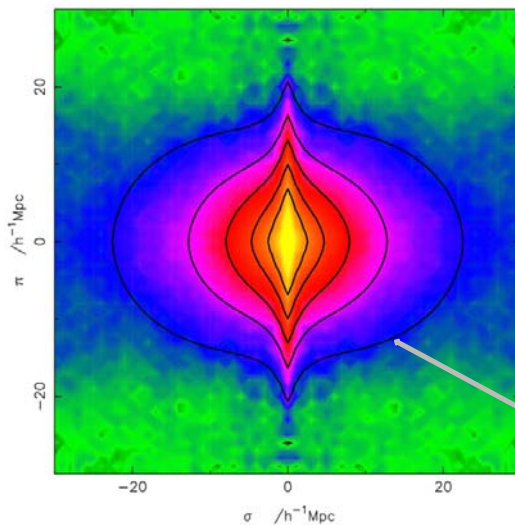
Correlation function determined in sky-redshift space:

$$\xi(\sigma, \pi)$$

sky position:  $\sigma = (\alpha, \delta)$   
redshift coordinate:  $\pi = cz$

Close distances:  
distortion due to non-linear  
Finger of God  
Large distances:  
distortions due to large-scale  
flows

## Redshift Space Distortions Correlation Function



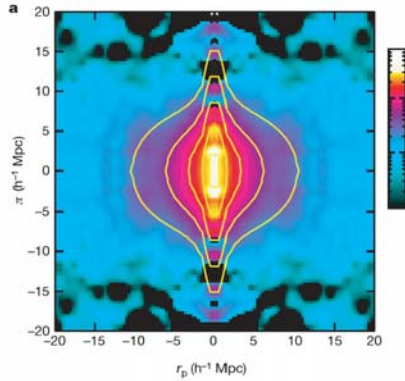
On average,  $\xi_s(s)$  gets amplified wrt.  $\xi_r(r)$

Linear perturbation theory (Kaiser 1987):

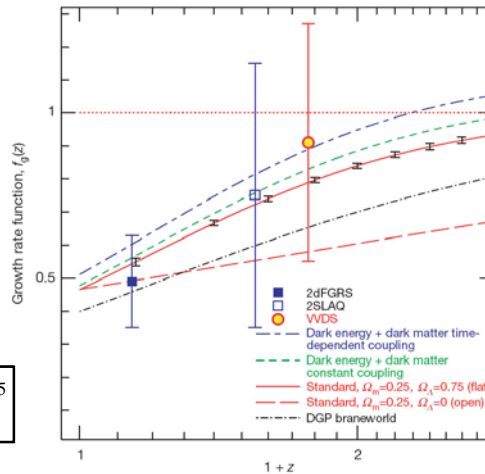
$$\xi_s(s) = \left(1 + \frac{2}{3}\Omega^{0.6} + \frac{1}{5}\Omega^{1.2}\right)\xi_r(s)$$

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# Evolution Growth Rate



Linder 2008  
Guzzo et al. 2008

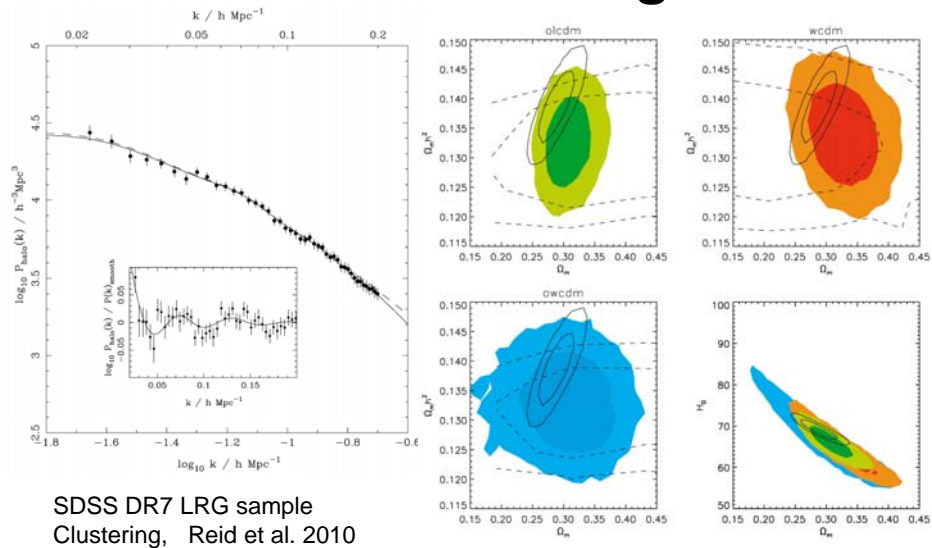


$$f(\Omega_m, \Omega_\Lambda) = \frac{a}{D} \frac{dD}{da} \approx \Omega_m^{0.55}$$

Peebles growth rate factor

# Galaxy & Cluster Clustering

# Cosmic Constraints LSS Clustering



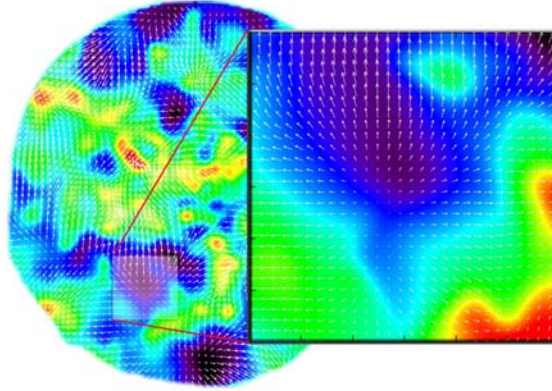
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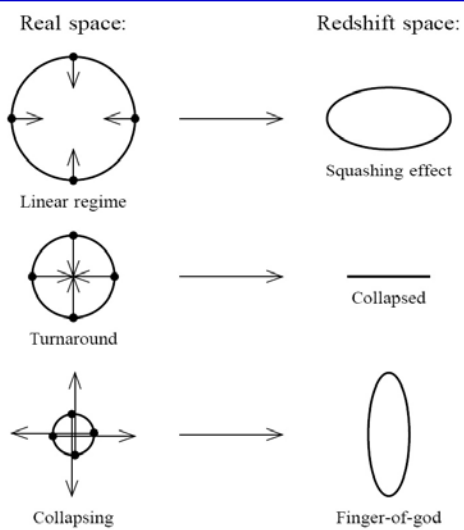
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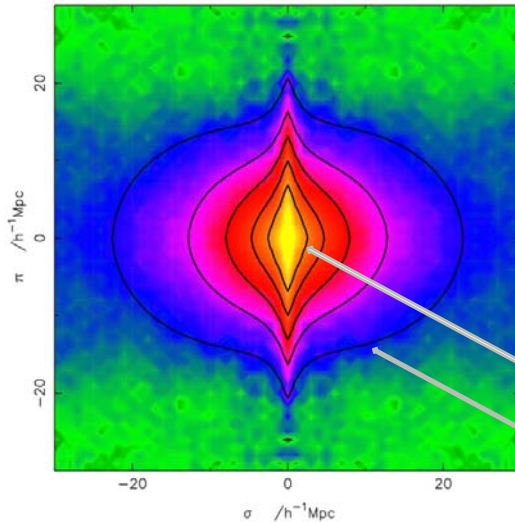
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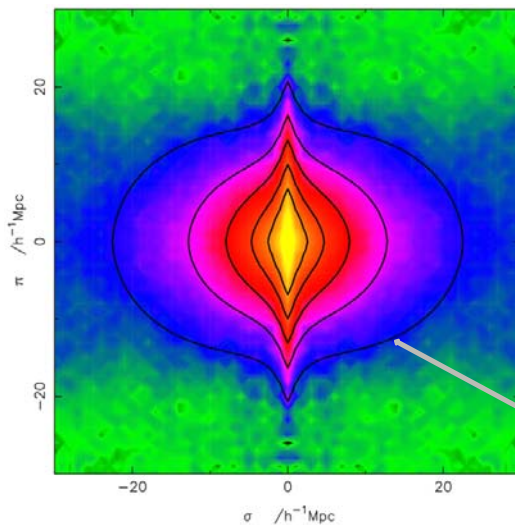
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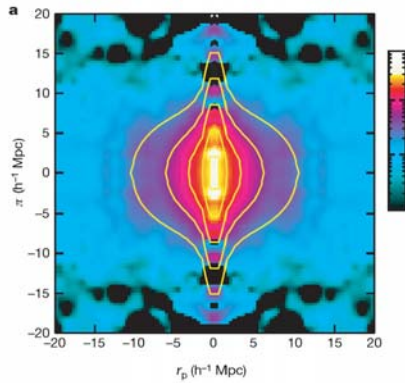
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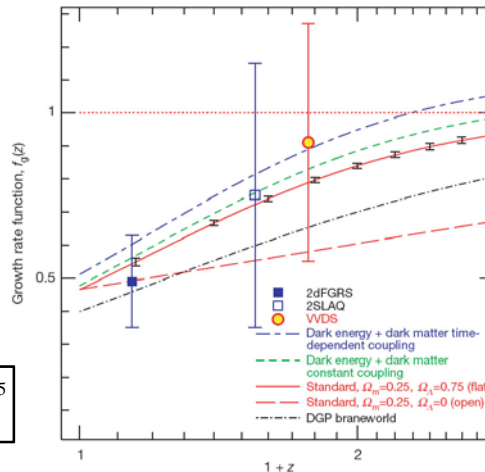
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Linder 2008  
Guzzo et al. 2008



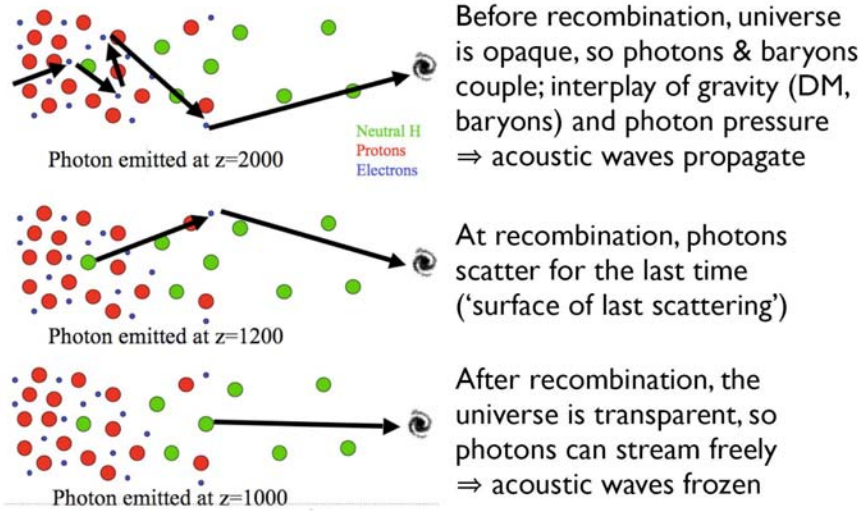
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Peebles growth rate factor

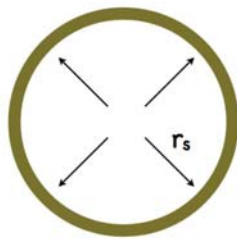
**BAO:**

**Baryonic Acoustic Oscillations**

# BAO

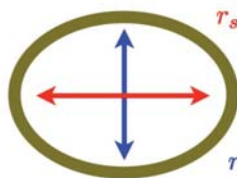


## BAO as cosmological tools



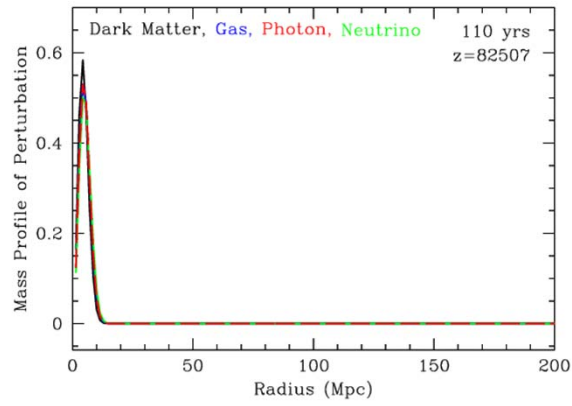
Until recombination, the sound wave travels a distance of:

$$r_s = \int_{z_{rec}}^{\infty} \frac{c_s(z)}{H(z)} dz$$

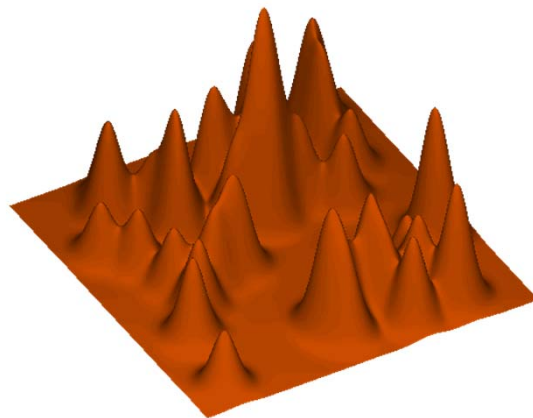


This distance can be accurately determined from the CMB power spectrum, and was found to be  $147 \pm 2$  Mpc.

## Measuring BAO



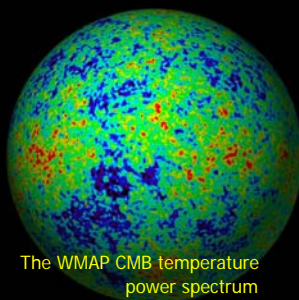
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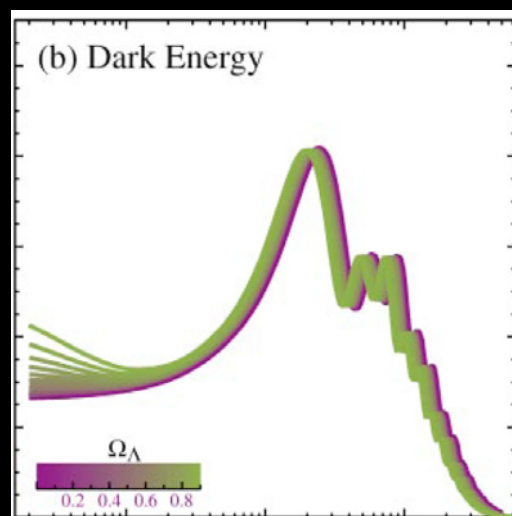


# ISW: Integrated Sachs Wolfe Effect

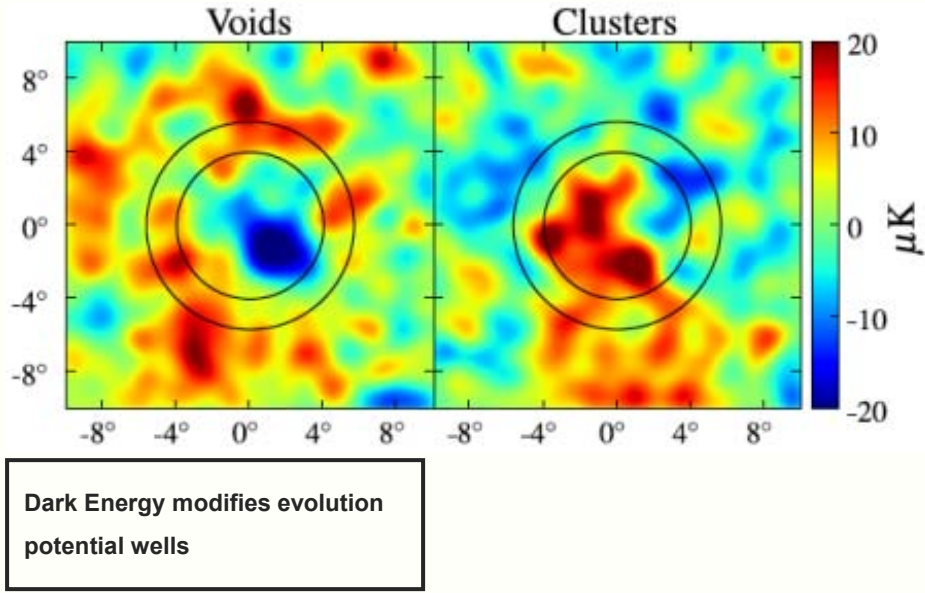
## Dark Energy & CMB: ISW



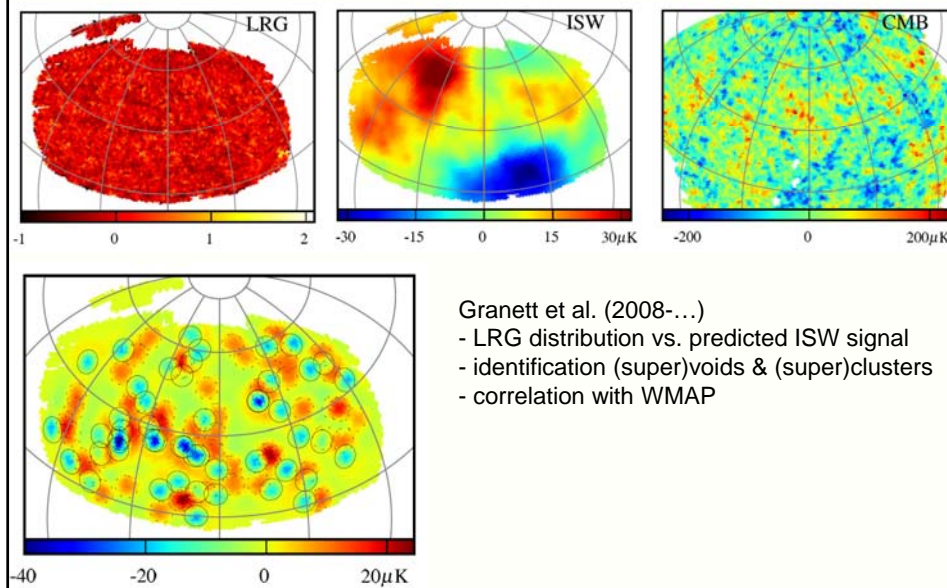
Dark Energy modifies evolution  
potential wells



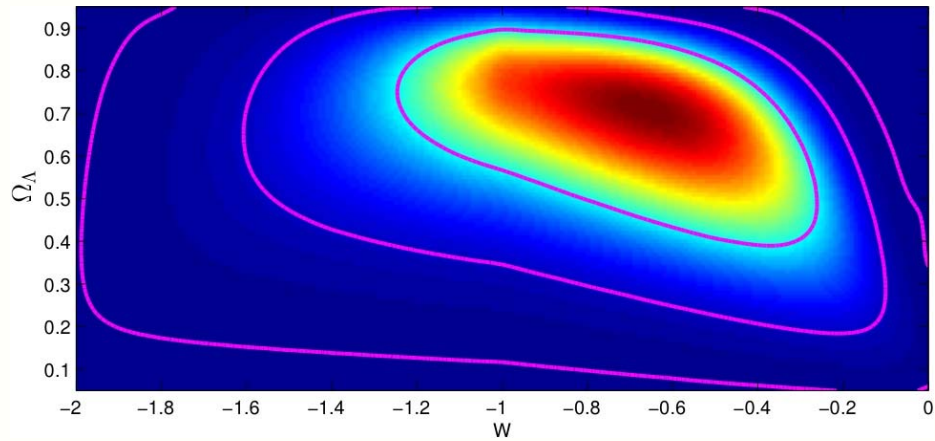
# Dark Energy: ISW



## ISW & identified voids/clusters



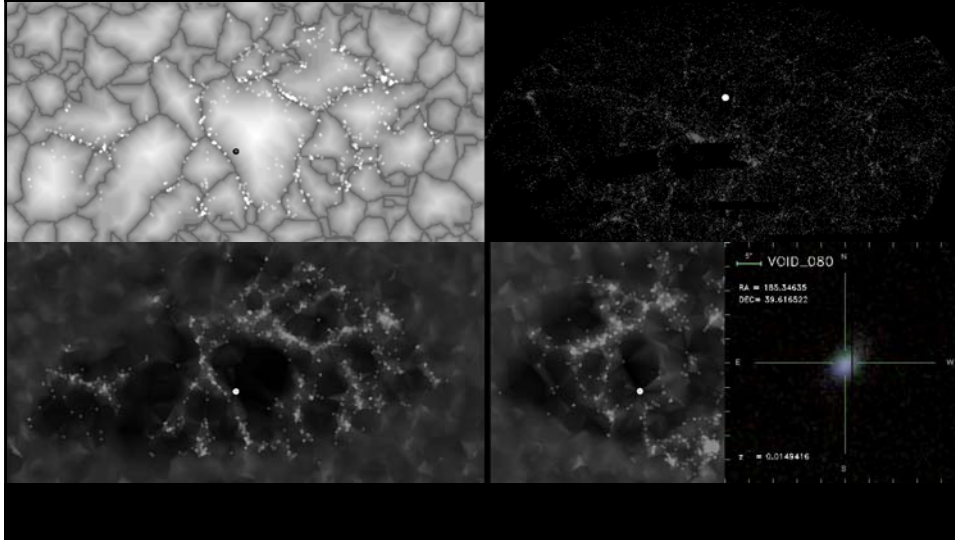
## Dark Energy: ISW



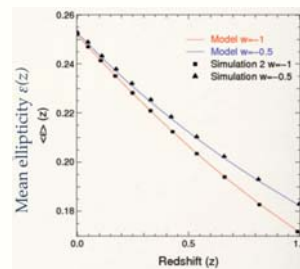
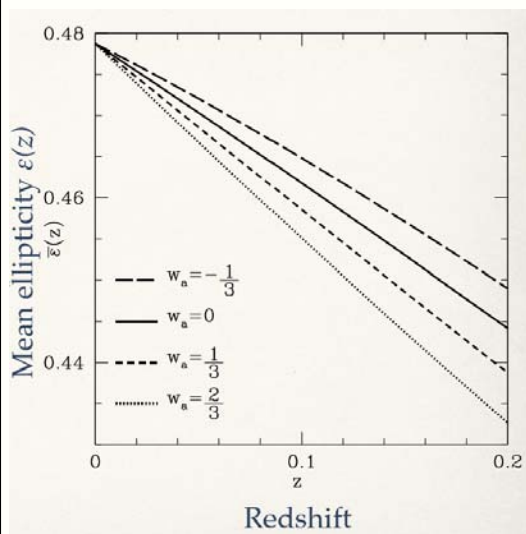
Dark Energy modifies evolution  
potential wells

**Cosmic Voids:**  
**Shape of Voids**

# Cosmic Voids



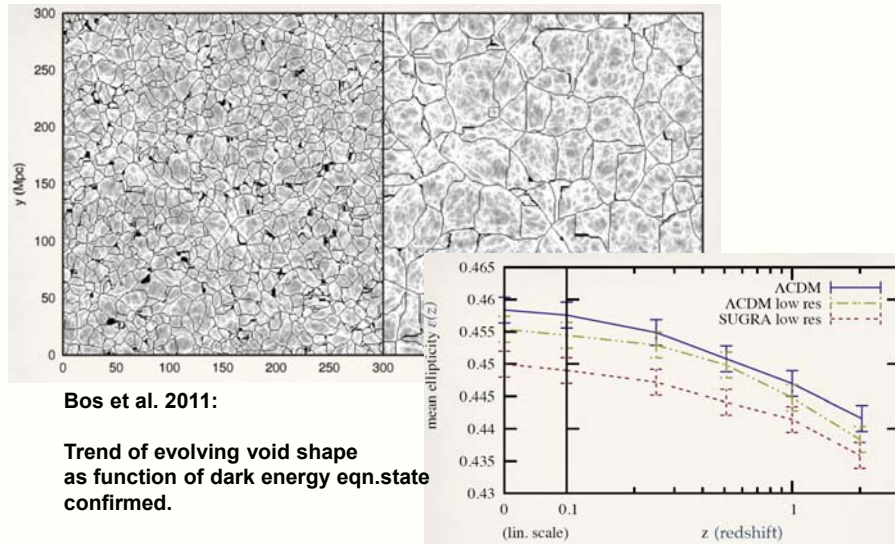
## Evolving Void Shapes



Evolution of void shape  
sensitive probe of dark energy:

Park & Lee 2007  
Lavaux & Wandelt 2010

# Evolving Void Shapes



## Future Experiments

# Euclid

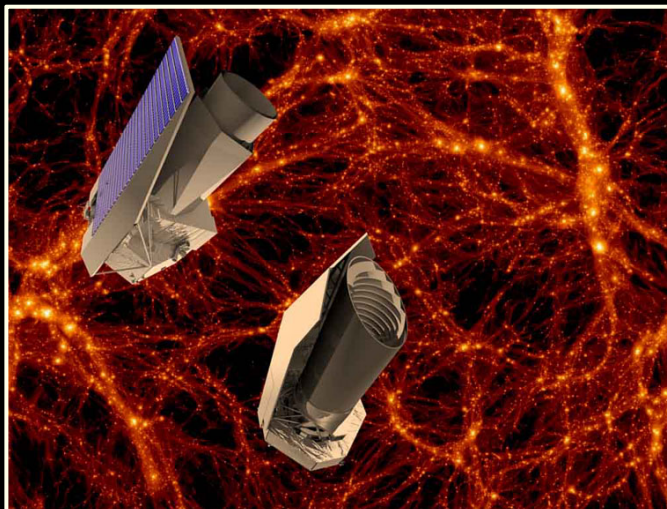
Euclid:  
father of geometry



## ESA Cosmic Vision 2020-2025

- 1.2 m Korsch telescope
- visible light:
  - m=24.5 CCD imaging
- IR (Y,J,H) band photometer
- spectrometer 108 bright gals
  
- 15,000 sq. deg. survey
- 40 sq. deg. deep survey
  
- Combination:
  - DUNE      grav. Lensing
  - SPACE     BAO

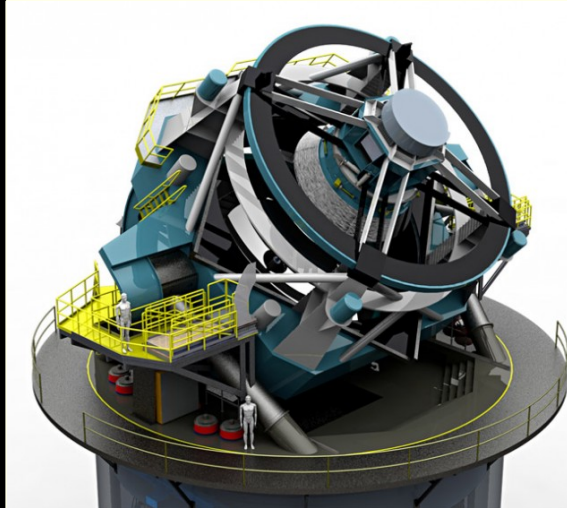
# Euclid



## ESA Cosmic Vision 2020-2025

- 1.2 m Korsch telescope
- visible light:
  - m=24.5 CCD imaging
- IR (Y,J,H) band photometer
- spectrometer 108 bright gals
  
- 15,000 sq. deg. survey
- 40 sq. deg. deep survey
  
- Combination:
  - DUNE      grav. Lensing
  - SPACE     BAO

# LSST: Large Synoptic Survey Telescope



8.4 m primary mirror  
widefield survey telescope

- El Penon, Chile  
2682 m. mountain
- start operation: 2015
- 3.5 deg. angle of view
- 3.2 Gigapixel prime focus  
digital camera
- 200,000 images per year
- 30 Tbyte per night
- partial funding Bill Gates

Summary

# Take-Home Facts

## 1. Strong evidence Accelerated Expansion

- since supernova discovery, 100s SNIa observed over broader range redshifts
- based solely upon supernova Hubble diagram, independent of General Relativity, very strong evidence expansion Universe accelerated recently

## 2. Dark energy as cause cosmic acceleration

- within general relativity, accelerated expansion cannot be explained by any known form of matter or energy
- it can be accommodated by a nearly smooth form of energy with large negative pressure, Dark Energy, that accounts for about 73% of the universe.

## 3. Independent evidence dark energy

- Cosmic Microwave Background and Large Scale Structure data provide independent evidence, within context of  $\Lambda$ CDM model of structure formation, that the universe is filled with a smooth medium accounting for 73% of the total energy content of the universe.
- that came to dominate the dynamics of the universe once all observed structure had formed

# Take-Home Facts

## 4. Vacuum energy as dark energy

- simplest explanation for dark energy is the energy associated with the vacuum
- mathematically equivalent to a cosmological constant
- However, most straightforward calculations of vacuum energy density from zero-point energies of all quantum fields lead to estimates which are a bit too large, in the order of  $\sim 10^{120}$

## 5. Dark theories of Dark Energy

- There is no compelling theory of dark energy
- Beyond vacuum energy, many intriguing ideas: light scalar fields, additional spatial dimensions, etc.
- Many models involve time-varying dark energy

## 6. New Gravitational Theories ?

- alternatively, cosmic acceleration could be a manifestation of gravitational physics beyond General Relativity
- however, as yet there is no self-consistent model for new gravitational physics that is consistent with large body of data that constrains theories of gravity.



# Take-Home Facts

**7. Dark destiny**

**8. At the nexus of many physical mysteries**

**9. Two big questions**

- a) Is dark energy something different than vacuum energy
- b) Does General Relativity self-consistently describe cosmic acceleration ?

**10. Probing Dark Energy**