

# Central Theme: Cosmic Enigma

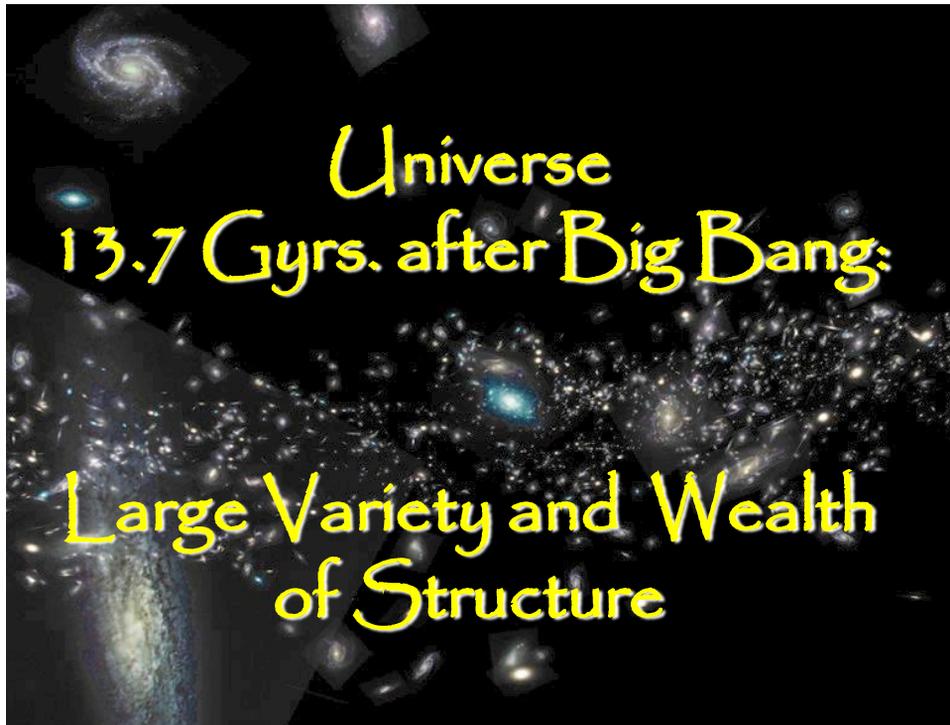
Universe

379,000 years after Big Bang

almost perfectly smooth

Microwave Background Radiation, surface of last scattering of cosmic photons is almost perfectly isotropic, all around the same temperature:

$T=2.725 \text{ K}$

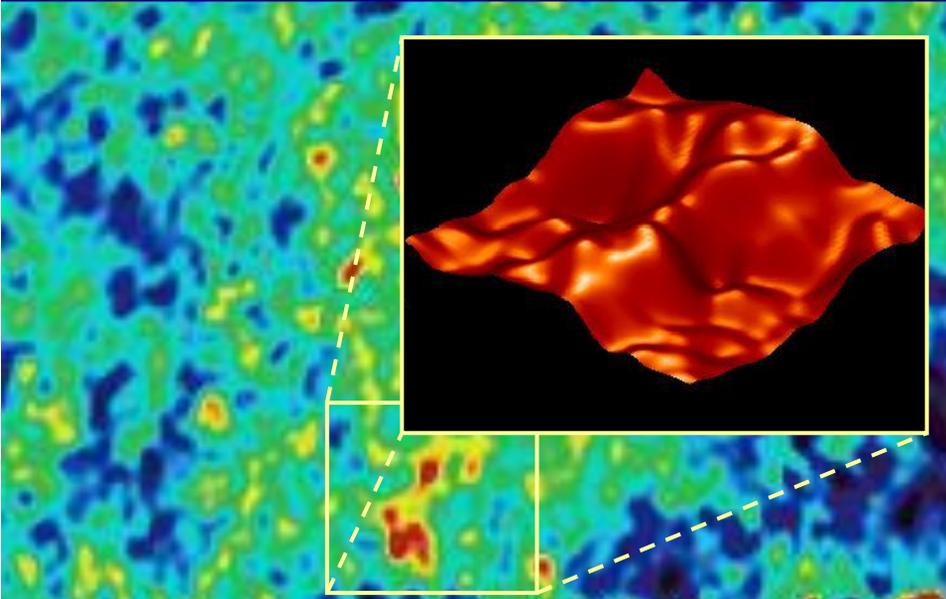


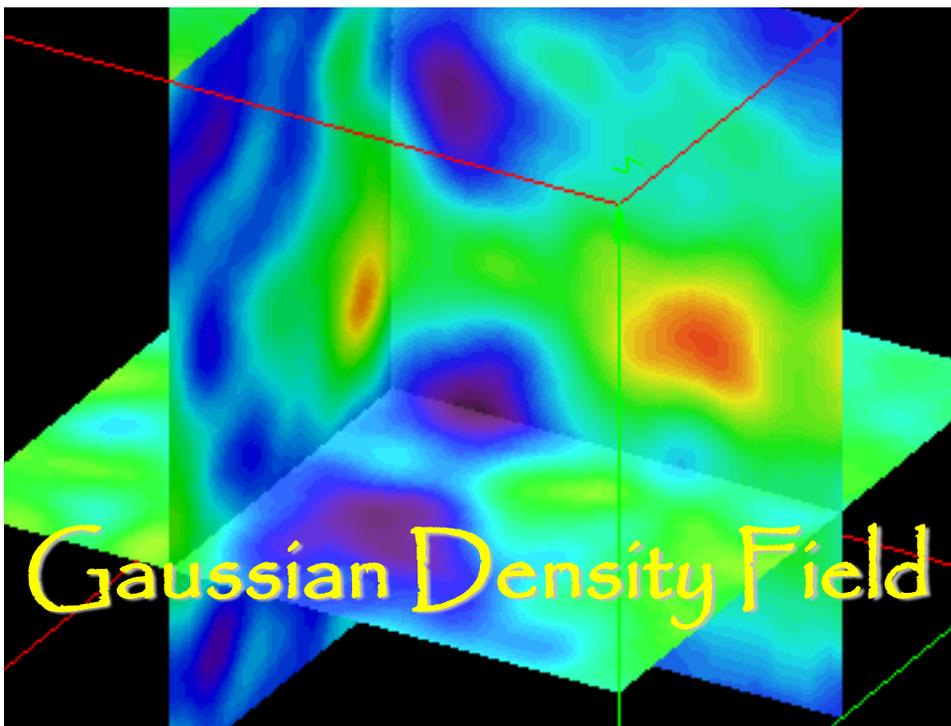
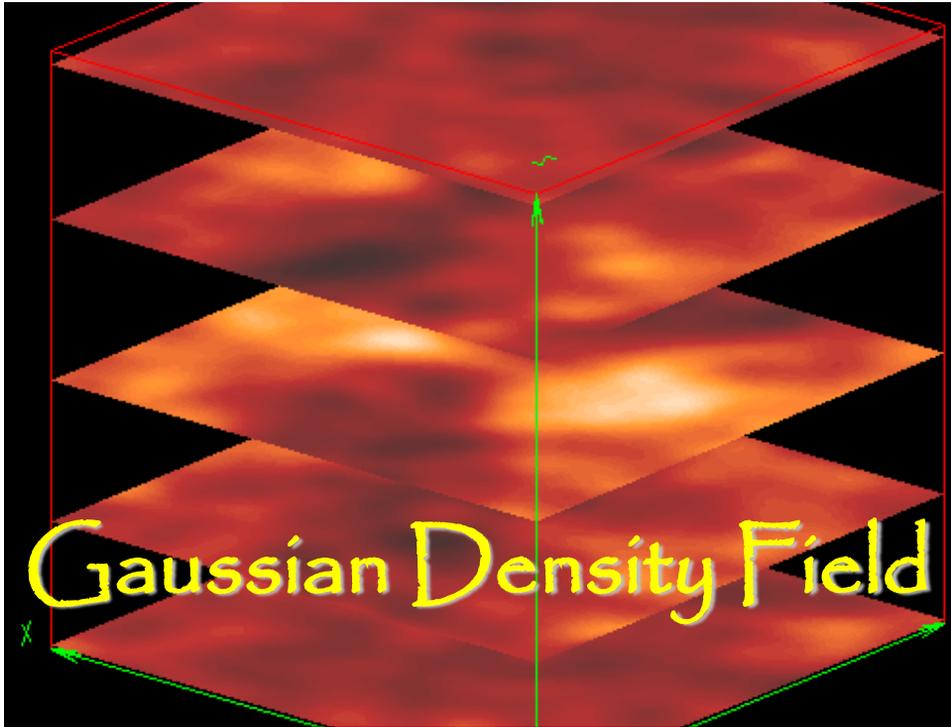
The Early Universe:  
Almost perfectly homogeneous and isotropic,  
without any discernable structure ...

How did the present wealth and variety of  
structure emerge out of  
an almost featureless, pristine early Universe  
?????

# Cosmic Paradigm: Gravitational Instability

## Primordial Gaussian Perturbations





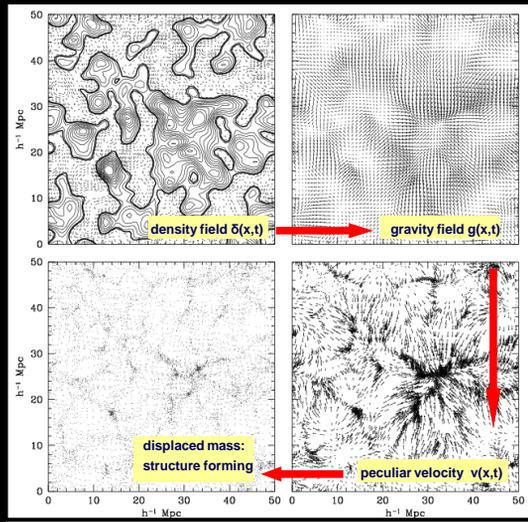
# Cosmic Structure Formation

The gravity perturbations induce cosmic flows of matter. High density regions start to contract and finally collapse, assembling more and more matter from their surroundings.

By contrast, as matter is moving out of them, low density regions turn into empty void regions.

Gradually, dependent on scale, we see the emergence of cosmic structures.

These days we can simulate the characteristics of the process through large computer simulations. Successful confrontation with the observational reality has given confidence in our understanding.



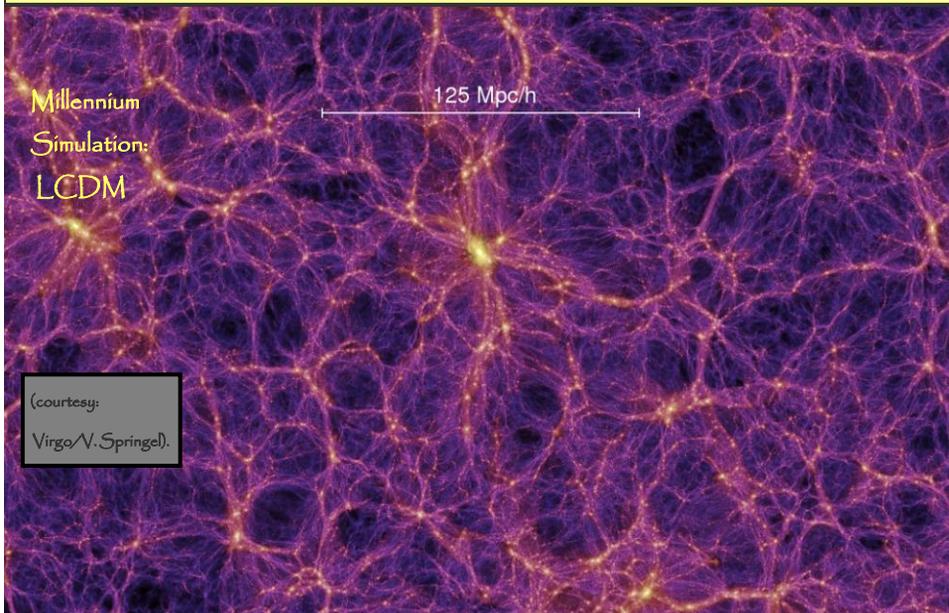
# Millennium Simulation

Millennium  
Simulation:  
LCDM

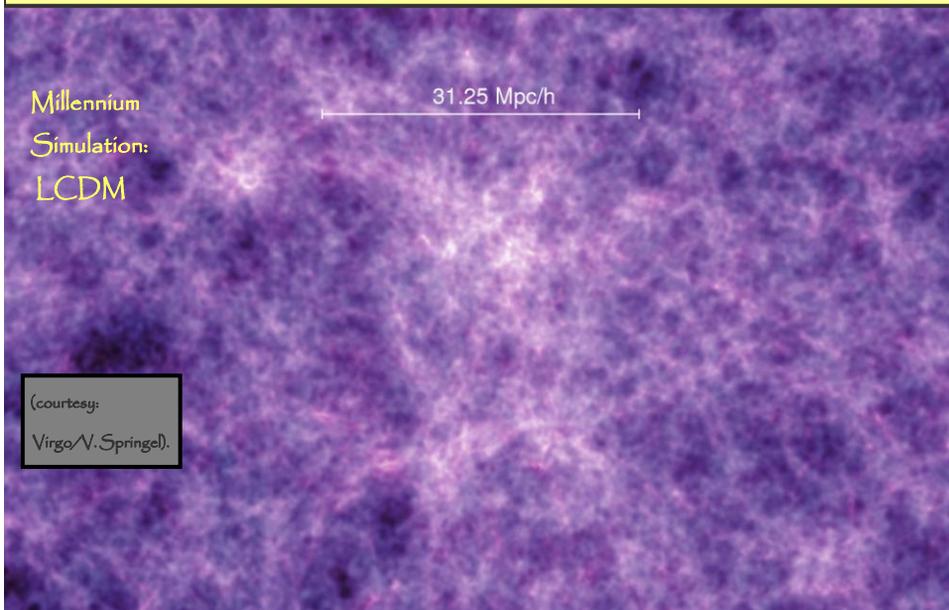
125 Mpc/h

(courtesy:  
Virgo/V. Springel).

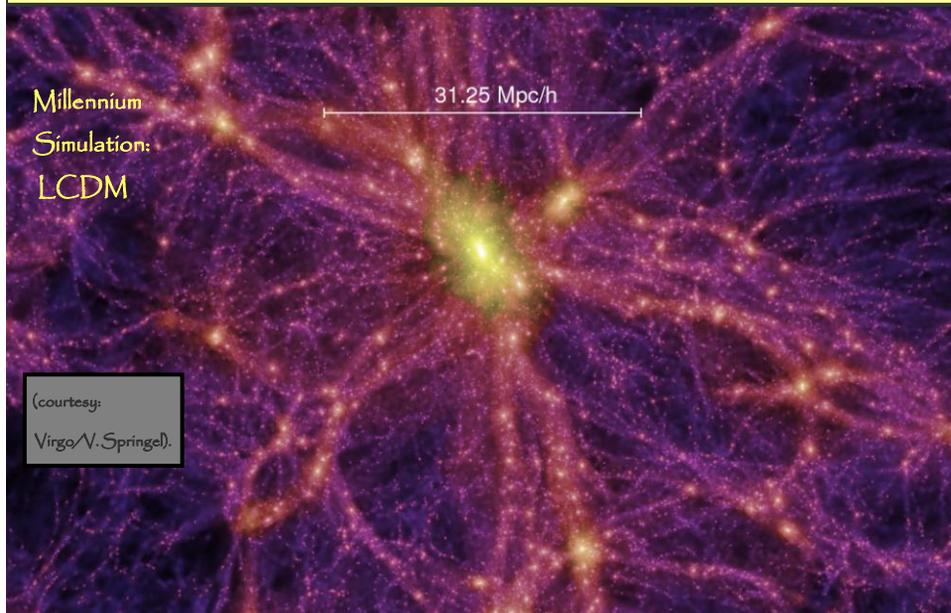
# Millennium Simulation



# Millennium Simulation

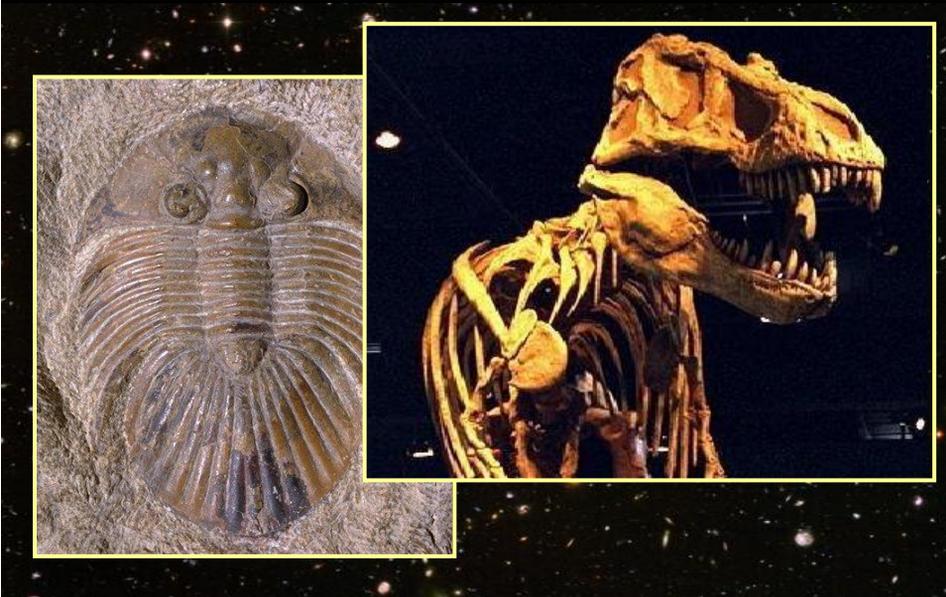


# Millennium Simulation



Cosmic  
Fossils

# Cosmic Fossils ?



## Cosmic Fossils

Which cosmic object contain direct information on emergence and growth of structure in the Universe ?

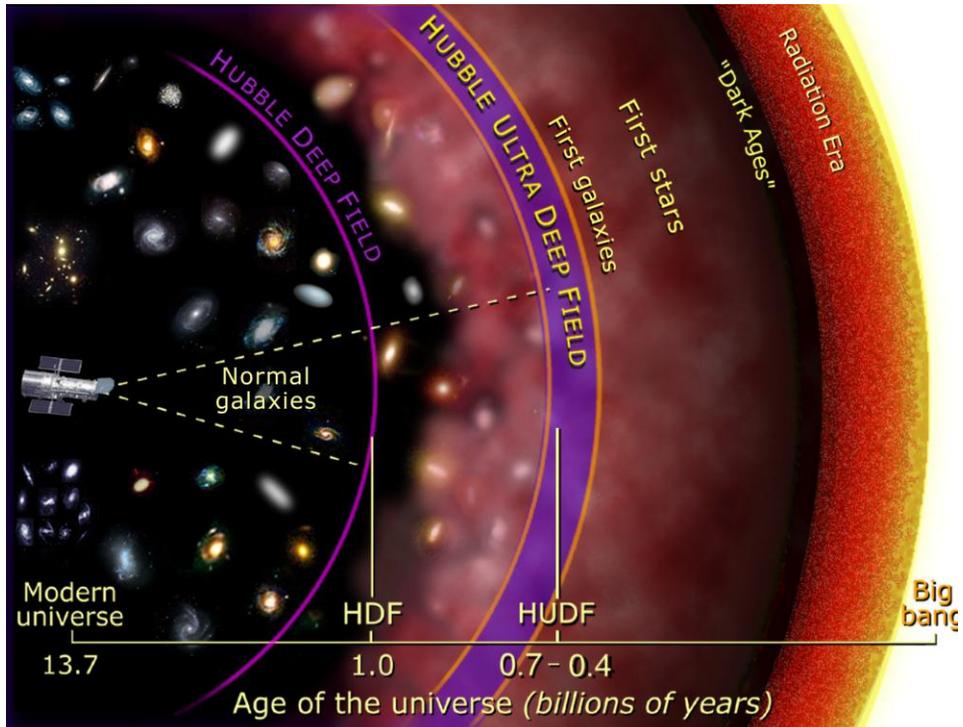
### Wanted:

- Structures in youthful evolutionary phase
- Direct link with their initial conditions
- On scales of Megaparsecs, and larger, gravitational collapse only just started

### Recall:

- visible (baryonic) matter but a fraction of total energy content Universe

$$\begin{aligned} \Omega_{rad} &\approx 10^{-5} \\ \Omega_{matter} &\approx 0.3 \\ \Rightarrow \Omega_{\Lambda} &\approx 0.7 \quad \leftarrow \end{aligned}$$



- Primordial Conditions:
  - temperature fluctuations in microwave background radiation
  - polarization Cosmic Microwave Background
  - treasure trove cosmological information
- Dynamics:
  - cosmic velocity flows
  - very difficult in practice, due to large uncertainties in distance estimate/measurements of galaxies, and hence the estimated deviations from Hubble expansion.
- Mass Distribution:
  - gravitational lensing of light by cosmic matter distribution
  - very promising, just started to yield significant results ...

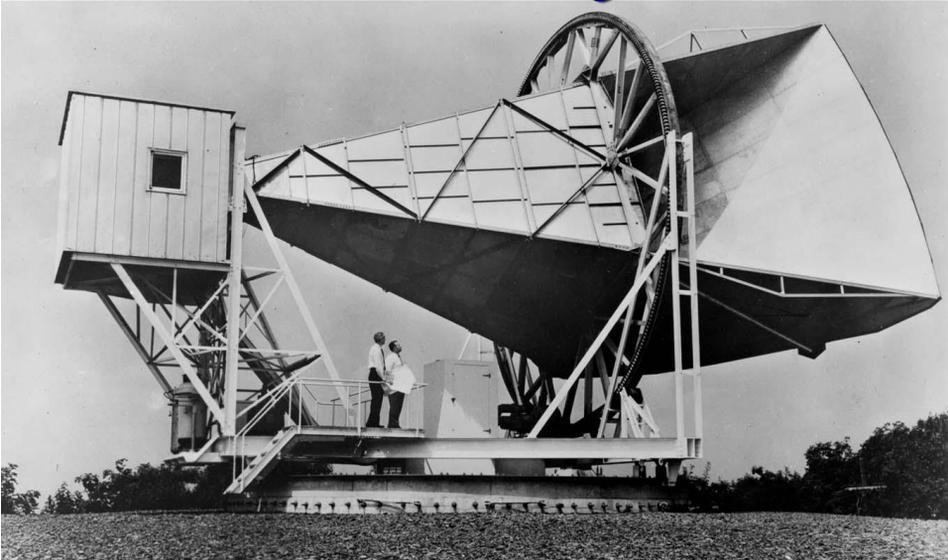
- Galaxy Distribution:
  - galaxies supposed to be a fair reflection of underlying cosmic matter distribution
  - most detailed and investigated impression of cosmic matter distribution
    - nonlinear scales: tracing the Cosmic Web
    - Megaparsec linear scales: measuring the Power Spectrum
    - Gigaparsec linear scales: Baryonic Oscillations  
Primordial Power Spectrum
    - High redshift galaxies: tracing young Universe, early stages galaxy formation

But: formation and evolution of galaxies still a notoriously understood problem, so that the relation between matter and galaxy distribution is as yet not unequivocally clear.
- Quasars & AGN
  - tracing the large scale matter distribution on scales of hundreds Mpc
  - but: largely unknown how they relate to the matter/galaxy distribution

- Clusters of Galaxies
  - spatial distribution tracer Cosmic Web
  - internal structure dictated by primordial perturbations
  - Hot intracluster gas. ( $10^8$  K) - accurate tracer potential cluster
    - easily observable via X-rays
- Gaseous Cosmic Web
  - Baryonic gas traces the Cosmic Web:
    - Ly $\alpha$  forest      neutral hydrogen gas, mostly at high z
    - WHIM              shock-heated gas settled in cosmic web
- Distribution & Physical State Gas @ Dark Ages
  - First Stars & Galaxies
  - Reionization of baryonic gas: very sensitive measure cosmology
- Structure of Galaxies
  - Mass distribution galaxies
  - Internal phase-space structure galaxy haloes

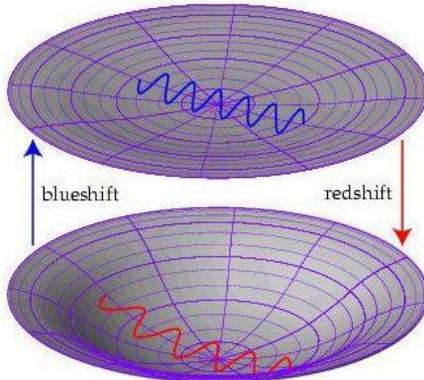
# Embryonic Structure: CMB: Rippling the Photons

## Cosmic Microwave Background: Discovery



# CMB Perturbations

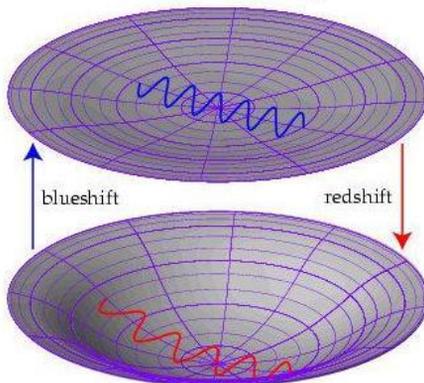
Metric Stretching



- As a result of perturbations in Gravitational potential photons experience frequency shift
- While travelling through perturbation:
  - Gravitational Redshift +
  - (Relativistic) Time Dilation
- Combined effect: Sachs-Wolfe Effect

# Sachs-Wolfe Effect

Metric Stretching



Sachs-Wolfe Effect

$$\frac{\Delta T}{T} \sim \frac{1}{3} \frac{\Delta \Phi}{c^2}$$

# Cosmic Microwave Background

## COBE (1992):

Accurate measurement  
Planck spectrum CMB

First detection angular  
temperature perturbations  
( $\theta \sim 7^\circ$ ): Sachs-Wolfe effect



# Cosmic Microwave Background

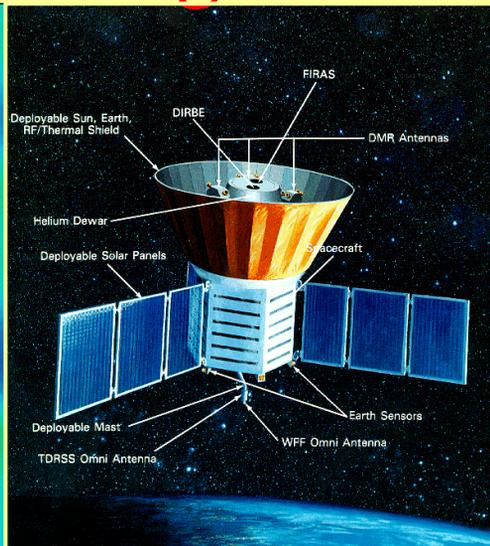
## COBE (1992):

Three instruments:

FIRAS: **Mather**  
Far-Infrared Absolute  
Spectrophotometer

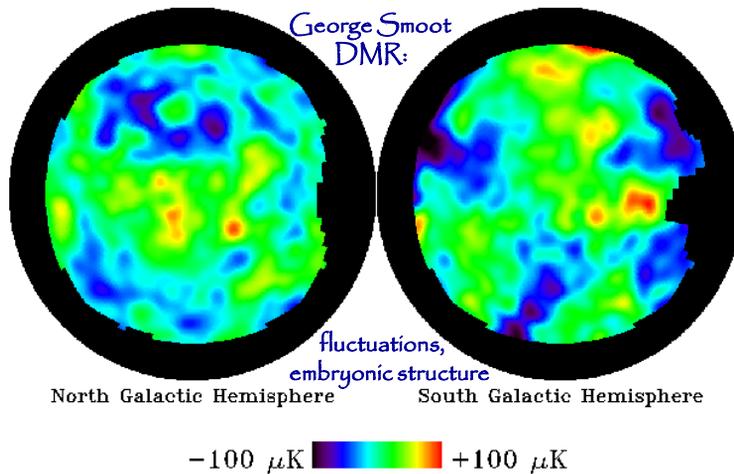
DIRBE: **Hauser**  
Diffuse Infrared Background  
Experiment

DMR: **Smoot**  
Differential Microwave  
Radiometer

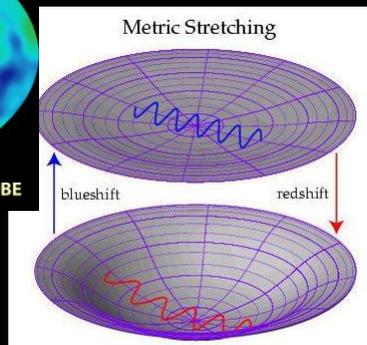
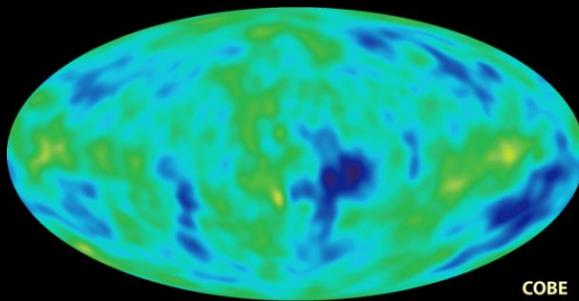


# Primordial Anisotropies CMB sky

COBE-DMR Map of CMB Anisotropy



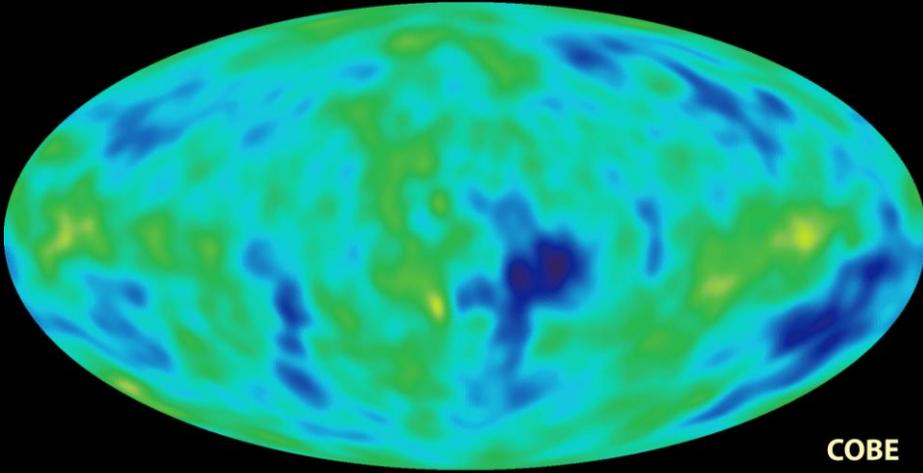
## Cosmic Microwave Background



Map of the Universe at Recombination Epoch:

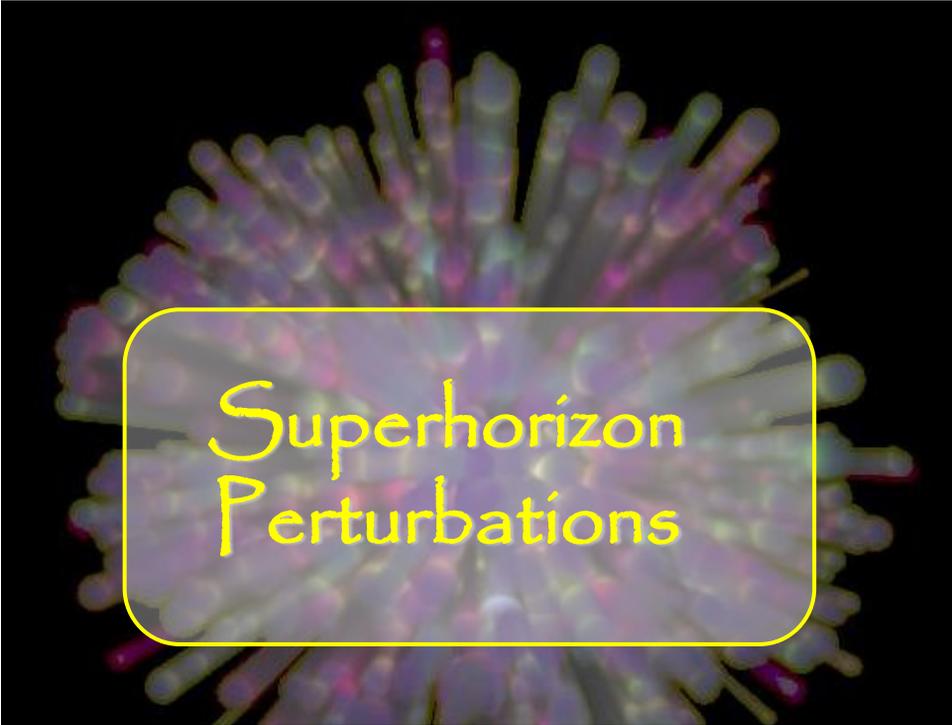
- 379,000 years after Big Bang
- Superhorizon perturbations in gravitational potential (Sachs-Wolfe)
- $\Delta T/T < 10^{-5}$

# Cosmic Microwave Background



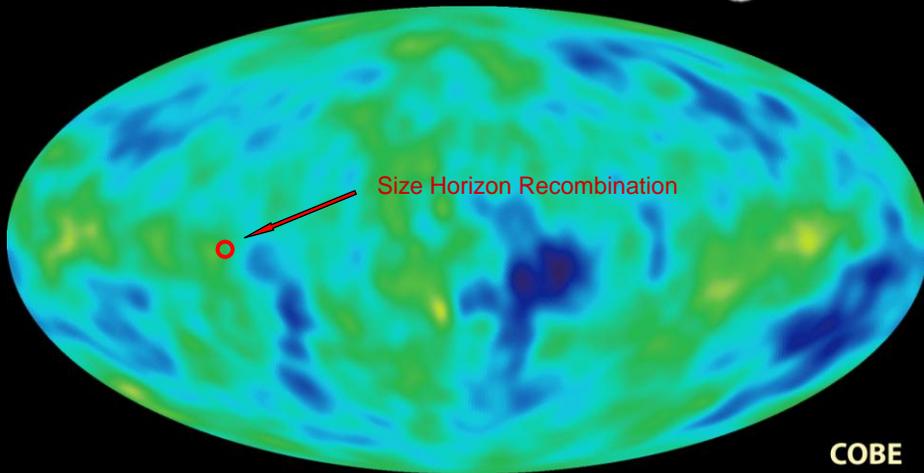
Map of the Universe at Recombination Epoch:

- 379,000 years after Big Bang
- Superhorizon perturbations in gravitational potential (Sachs-Wolfe)
- $\Delta T/T < 10^{-5}$



Superhorizon  
Perturbations

# Cosmic Microwave Background



COBE measured fluctuations:  $> 7^\circ$   
Size Horizon at Recombination spans angle  $\sim 1^\circ$

How can it be that regions totally out of thermal contact, would have the same temperature?

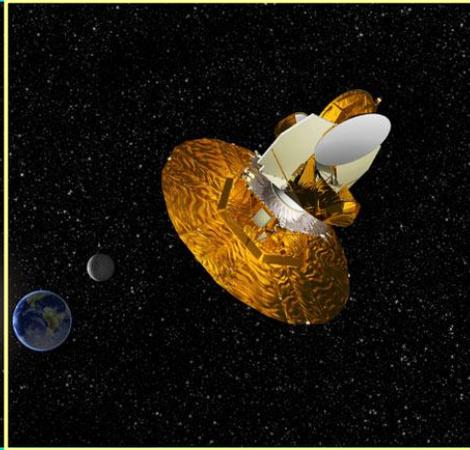
Resolving  
Fluctuations

# Cosmic Microwave Background

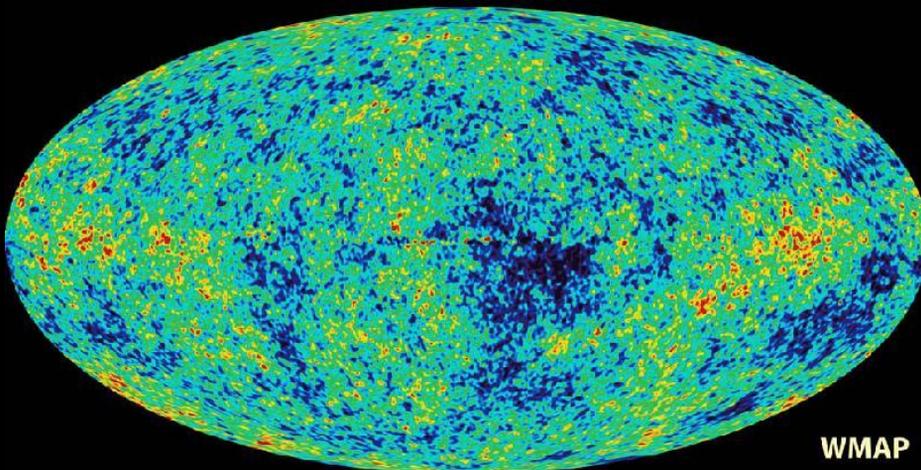
## WMAP (2001):

Detailed map sub-degree  
angular temperature  
perturbations ( $\theta < 1^\circ$ )

Angular Power Spectrum:  
Precision Cosmology



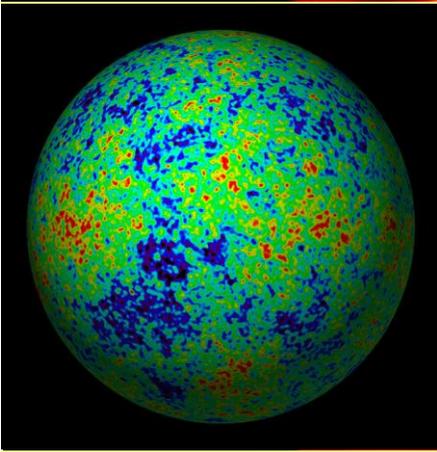
## Cosmic Microwave Background



Map of the Universe at Recombination Epoch:

- 379,000 years after Big Bang
- Subhorizon perturbations: primordial sound waves
- $\Delta T/T < 10^{-5}$

# Temperature Anisotropies

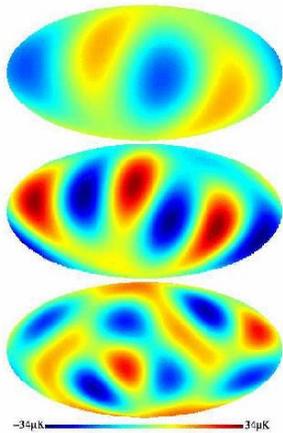


Temperature Perturbations in terms of  
Spherical Harmonics:

$$T(\theta, \phi) = \sum_{l,m} a_{lm} Y_l^m(\theta, \phi)$$

$$\phi \sim \frac{\pi}{l} \sim \frac{180^\circ}{l}$$

# Temperature Anisotropies

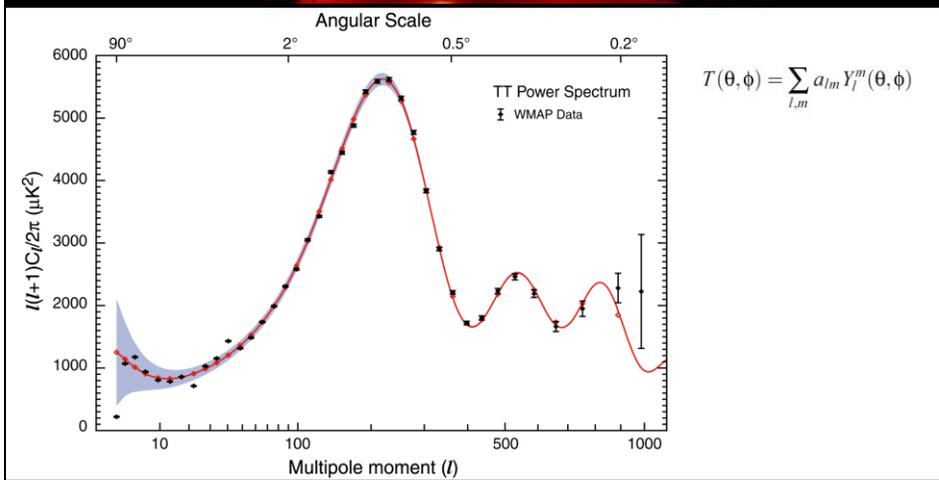


Temperature Perturbations in terms of  
Spherical Harmonics:

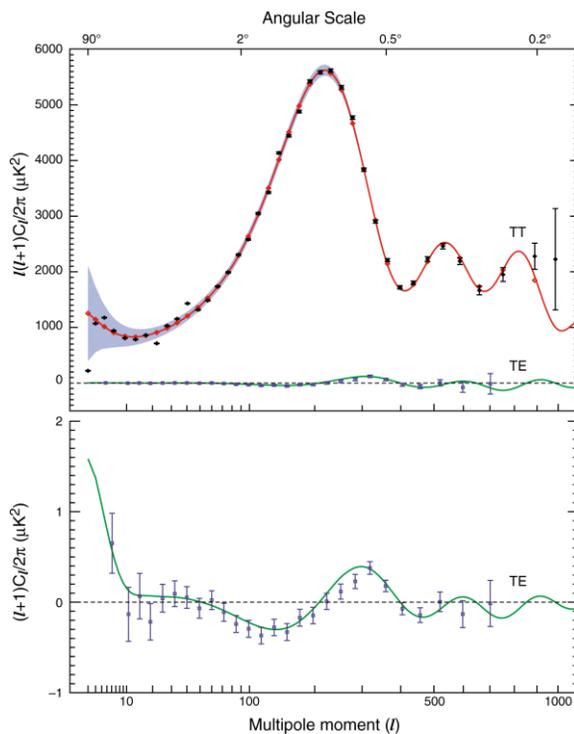
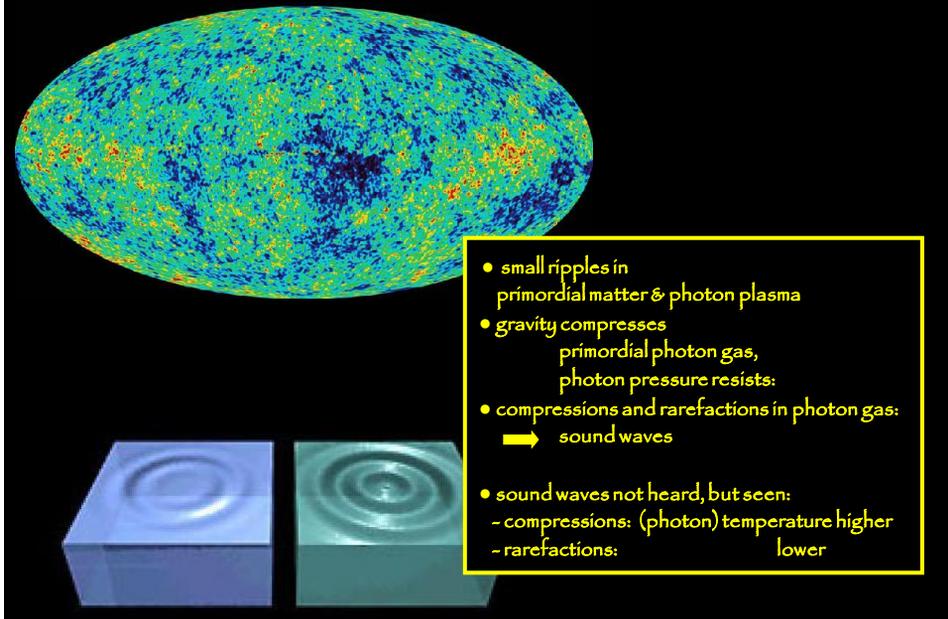
$$T(\theta, \phi) = \sum_{l,m} a_{lm} Y_l^m(\theta, \phi)$$

$$\phi \sim \frac{\pi}{l} \sim \frac{180^\circ}{l}$$

# CMB Power Spectrum



# Cosmic Microwave Background



CMB

Angular power spectrum

WMAP3

Temperature fluctuations

Temperature-Polarization

$$C_l \propto \langle a_{lm} a_{lm}^* \rangle$$

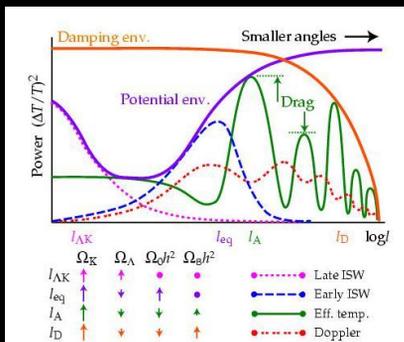
$$C_l \propto l(l+1)$$

$$P(k) \propto k$$

# Harmonic Signature

- Identify structure and composition of the Universe
  - through detailed examination of the pattern of overtones on the fundamental frequency
  - much like using them for a music instrument
- Observed frequency spectrum consistent with inflationary origin:
  - spectrum of cosmic sound has harmonics at **integer ratios of fundamental**
- Without inflation, fluctuations should have been generated at intermediate times
- This would have destroyed the harmonic structure of the peaks (like drilling holes in an organ pipe)

## Music of the Spheres

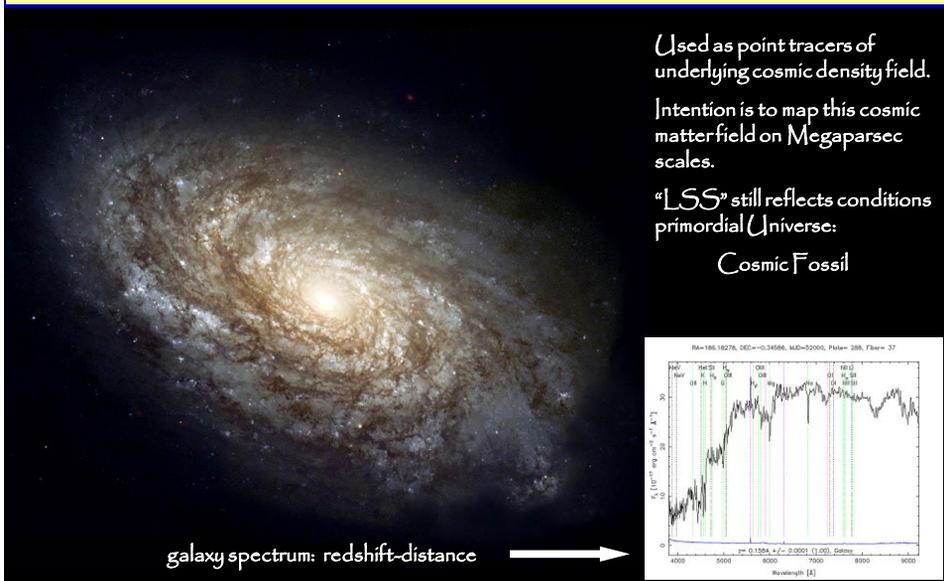


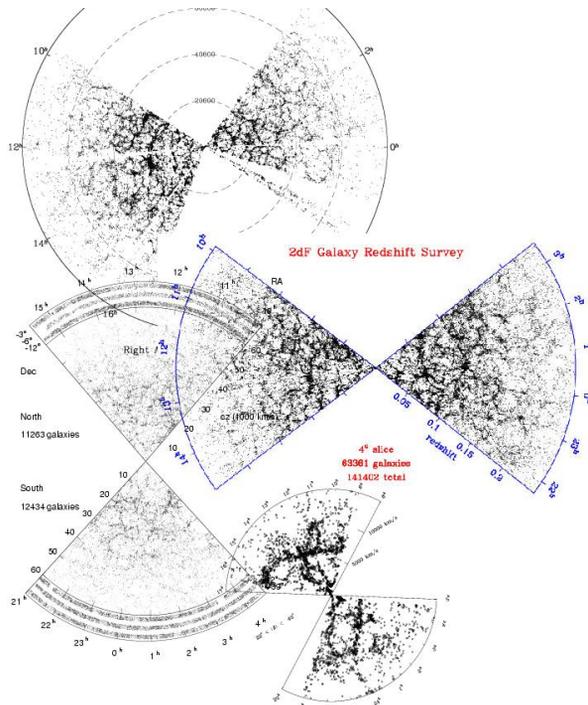
### Total Angular CMB Spectrum modulated by combination of several effects, the Primary Perturbations

- Sachs-Wolfe potential fluctuations,
- Acoustic perturbations  
as the corresponding potential fluct.  
enter horizon and start to collapse
- Integrated Sachs-Wolfe  
potential perturbations:
  - **Early ISW**: matter/radiation at recomb.
  - **Late ISW**: expansion influence curvature  
& cosmological constant
- Doppler perturbations  
velocity fluct. accompanying potential pert.
- Silk Damping**  
radiation damping of fluctuations

# The Cosmic Web: Patterns Across the Universe

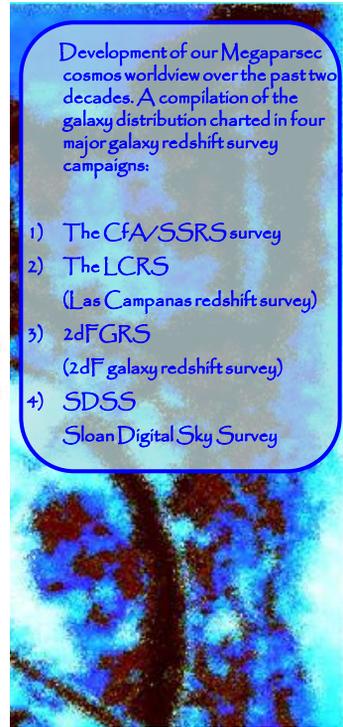
## A Universe of Galaxies





Development of our Megaparsec cosmos worldview over the past two decades. A compilation of the galaxy distribution charted in four major galaxy redshift survey campaigns:

- 1) The CfA/SSRS survey
- 2) The LCRS (Las Campanas redshift survey)
- 3) 2dFGRS (2dF galaxy redshift survey)
- 4) SDSS Sloan Digital Sky Survey



Over the past two decades we have witnessed a paradigm shift in our perception of the Megaparsec scale structure in the Universe. As increasing elaborate galaxy redshift surveys charted ever larger regions in the nearby Universe, an intriguingly complex and salient foamlke network came to unfold and establish itself as the quintessential characteristic of the cosmic matter and galaxy distribution.

In a great many physical systems, the spatial organization of matter is one of the most readily observable manifestations of the forces and processes forming and moulding them. Richly structured morphologies are usually the consequence of the complex and nonlinear collective action of basic physical processes.

The vast **Megaparsec cosmic web** is undoubtedly one of the most striking examples of **complex geometric patterns** found in nature. In its own right, the vast dimensions and intricate composition of the cosmic foam make it one of the most imposing and intriguing patterns existing in the Universe. Its wide-ranging importance stems from its status as a cosmic fossil. On a scale of **tens** up to a **few hundred Megaparsecs** it is still relatively straightforward to relate the configuration at the present cosmic epoch to that of the primordial matter distribution from which it emerged. With the cosmic foam seemingly representing this phase, it assumes a fundamental role in the quest for understanding the origin of all structures in the Universe.

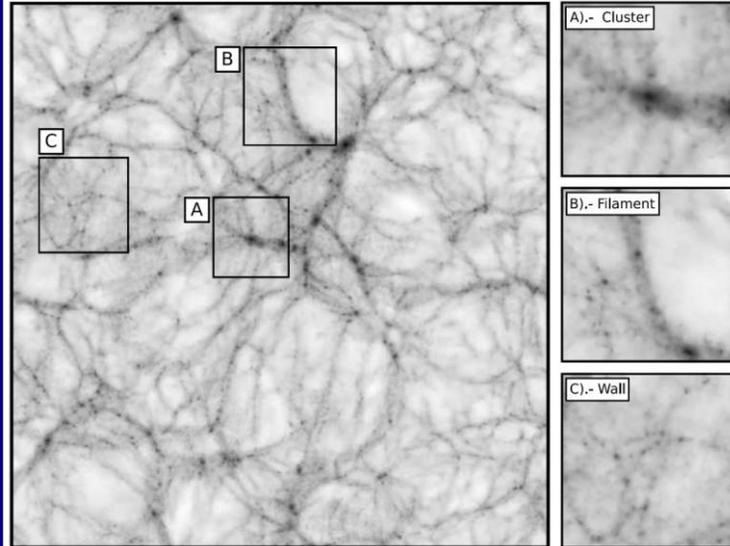
While its complex cellular morphology involves one of the most outstanding and evident aspects of the Cosmic foam, it has also remained one defying simple definitions which may be the cause of it having remained one of the least addressed aspects. The geometry of the cosmic foam may be described as a nontrivial stochastic assembly of various **anisotropic** and **asymmetric** elements. A major deficiency in the vast majority of studies on the large scale distribution of galaxies has been the lack of suitable quantitative and statistical characterizations of the truly fundamental aspects of the cosmic foam geometry.

# The Cosmic Web

Stochastic  
Spatial  
Pattern of

- Clusters,
- Filaments &
- Walls  
around
- Voids

in which matter,  
(DM, gas, gal's)  
has agglomerated



## Galaxy Surveys:

## Luminosity Function

## Galaxy Surveys

- Galaxies, Groups, Clusters & Superclusters:

Tracers of Structure in the Universe

- discrete tracers of underlying density field:

$$n(\vec{x}) \leftrightarrow \rho(\vec{x})$$

- Fair or Biased Tracer ?

## Galaxy Surveys

- Ideal Sample:
  - all sample points have exactly the same properties over complete "survey volume"
- However ...
  - galaxies have different luminosities, sizes, etc.:
  - systematic influence on distribution as function of depth
  - do galaxy properties depend on environment?

## Galaxy Surveys

- Various selection criteria:
  - + magnitude-limited
  - + angular diameter - limited
- Galaxy distribution as tracer cosmic structure:
  - + requirement to understand selection  $\psi(r, \theta, \varphi, \nu, T)$ :
    - sampling rate of galaxies at distance  $r$
    - sky position  $\theta, \varphi$
    - frequency  $\nu$
    - galaxy type  $T$
- Most convenient and best controlled:
  - + selection on basis luminosity/brightness

## Luminosity Function

Large variety of galaxies

- ranging from dwarfs to giant ellipticals
- large range of luminosity/brightness

Luminosity distribution:

$$dn(L) = \phi(L)dL$$

number of galaxies with luminosity

$$[L, L + dL]$$

PS. Luminosity distribution may depend on various galaxy properties, such as morphological type

# Schechter Luminosity Function

Very good approximate expression for the galaxy luminosity distribution:

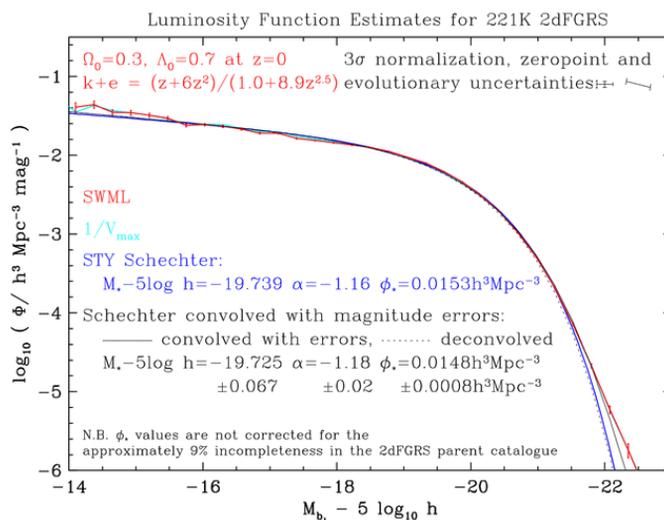
- Schechter Luminosity Function:

$$\phi(L)dL = \phi^* \left( \frac{L}{L_*} \right)^\alpha e^{-L/L_*} d \left( \frac{L}{L_*} \right)$$

- Parameterized by 3 parameters:

$\phi^*$ : normalization density parameter  
 $L_*$ : characteristic luminosity  
 $\alpha$ : faint-end slope

## Schechter Function



## Schechter Luminosity Function

- Mean space density gal's:

$$n(L)dL = \int_0^{\infty} \phi(L)dL = \phi^* \int_0^{\infty} s^{\alpha} e^{-s} ds = \phi^* \Gamma(\alpha + 1)$$

- Gamma function:  $\Gamma(z) = \int_0^{\infty} t^{z-1} e^{-t} dt$

- Notice:  $\alpha < -1$   
(infinite contribution faint gal's)

- Mean Luminosity (from cosmic volume)

$$\langle L \rangle = \int_0^{\infty} L \phi(L) dL = \phi^* L_* \int_0^{\infty} s^{(\alpha+1)} e^{-s} ds = \phi^* L_* \Gamma(\alpha + 2)$$

- divergent only if  $\alpha < -2$

## Schechter Luminosity Function

- 2dFGRs luminosity function:

$$M_* = -19.725$$

$$\alpha = -1.18$$

$$\phi^* = 0.0148 \text{ Mpc}^{-3}$$

- Faint Galaxies dominate number density !!!!!

Bright Galaxies determine the luminosity (stars)  
in a cosmic volume !!!!!

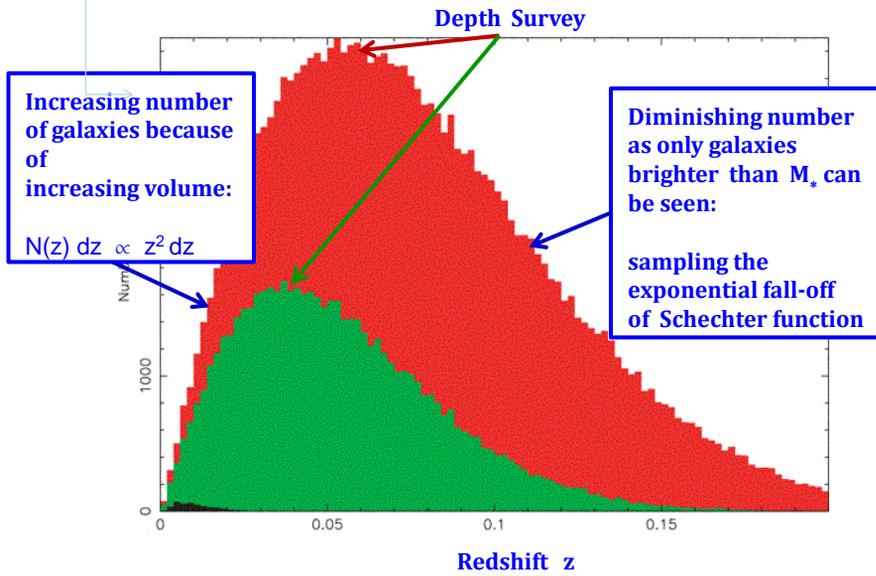
## Survey Depth

- Most galaxy surveys defined by apparent magnitude limit  $m_{\text{lim}}$
- All galaxies having an apparent brightness higher than that corresponding to  $m_{\text{lim}}$  are included in survey
- Depends on
  - intrinsic brightness/absolute magnitude  $M$
  - (luminosity) distance  $d_L$
  - (- k-correction: shift galaxy spectrum as function redshift  $z$ )
- Absolute Magnitude  $\longleftrightarrow$  Apparent Magnitude
 
$$M = m - 5 \log d_L(z) - 25 - k(z)$$

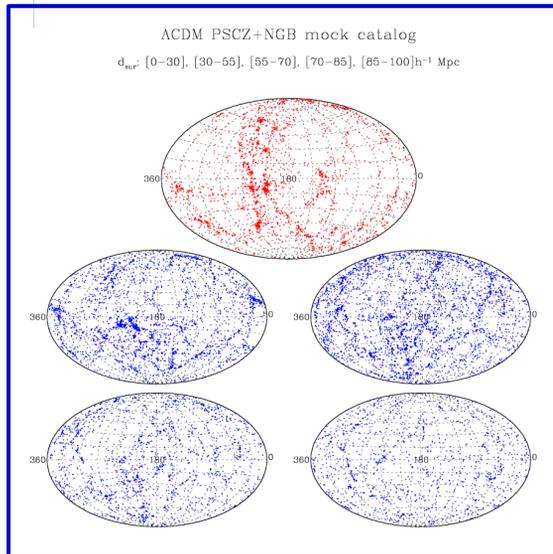
## Survey Depth

- For a survey with magnitude limit  $m_{\text{lim}}$ :
- At distance  $d_L$  (Mpc) one can see galaxies brighter than:
 
$$M = m_{\text{lim}} - 5 \log d_L(z) - 25 - k(z)$$
- Survey Depth  $d_{\text{sur}}$ :  
distance out to which one can see an  $M_*$  galaxy:
 
$$\log d_{\text{sur}} = 0.2(m_{\text{lim}} - M) + 5 + 0.2k(z)$$

# Survey Depth



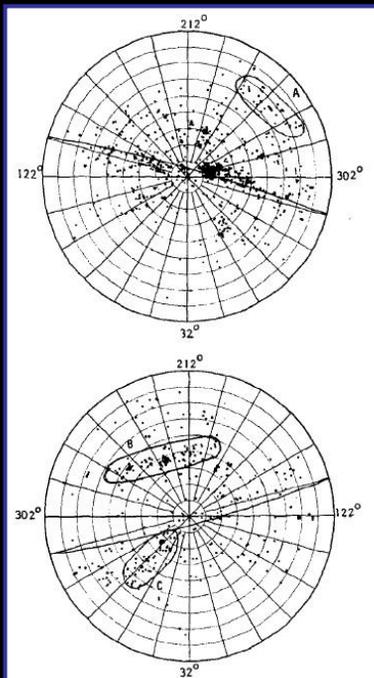
# Survey Depth



**Theoretical Example:**

Galaxies in PSCZ catalogue, at different depths

# Sky Maps: world all around us



## Early Views

Shapley-Ames catalog (1932) of nearby galaxies:

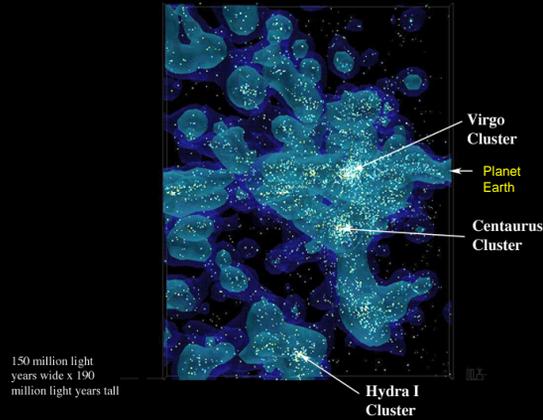
All-sky survey of galaxies to  $m=18.3$

$$\delta > -23^\circ$$

- numerous concentrations:  
groups and clusters (incl. Virgo cluster)
- asymmetry between north and south:  
many more galaxies on northern sky
- conspicuous concentration along a line  
running through richest nearby cluster,  
the Virgo cluster:
- The Supergalactic Plane  
(first identified by de Vaucouleurs:  
the plane of our own Local Supercluster)

# The Local Supercluster

## End-on View of the Local Supercluster:

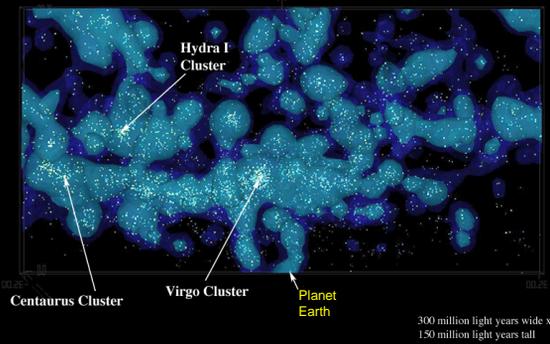


Our Local Group finds itself located at the outer region of a large supercluster region,

- the "Local Supercluster",
- a large flattened mass concentration  $\sim 10 h^{-1}$  Mpc in size,
- centered on one rich cluster, the Virgo cluster

# The Local Supercluster

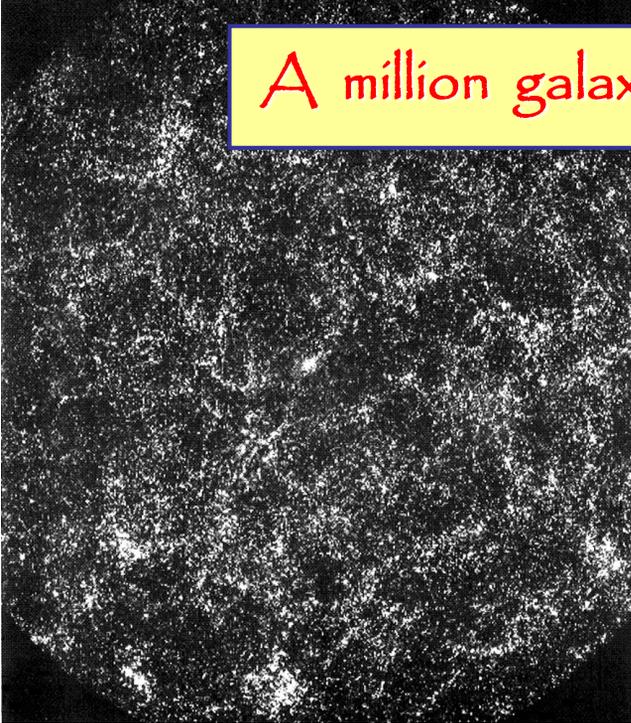
## Polar View of Local Supercluster:



Our Local Group finds itself located at the outer region of a large supercluster region,

- the "Local Supercluster",
- a large flattened mass concentration  $\sim 10 h^{-1}$  Mpc in size,
- centered on one rich cluster, the Virgo cluster

## A million galaxies



### Shane-Wirtanen map:

On the basis of the Shane-Wirtanen counts, P.J.E. Peebles produced a map of the sky distribution of 1 million galaxies on the sky:

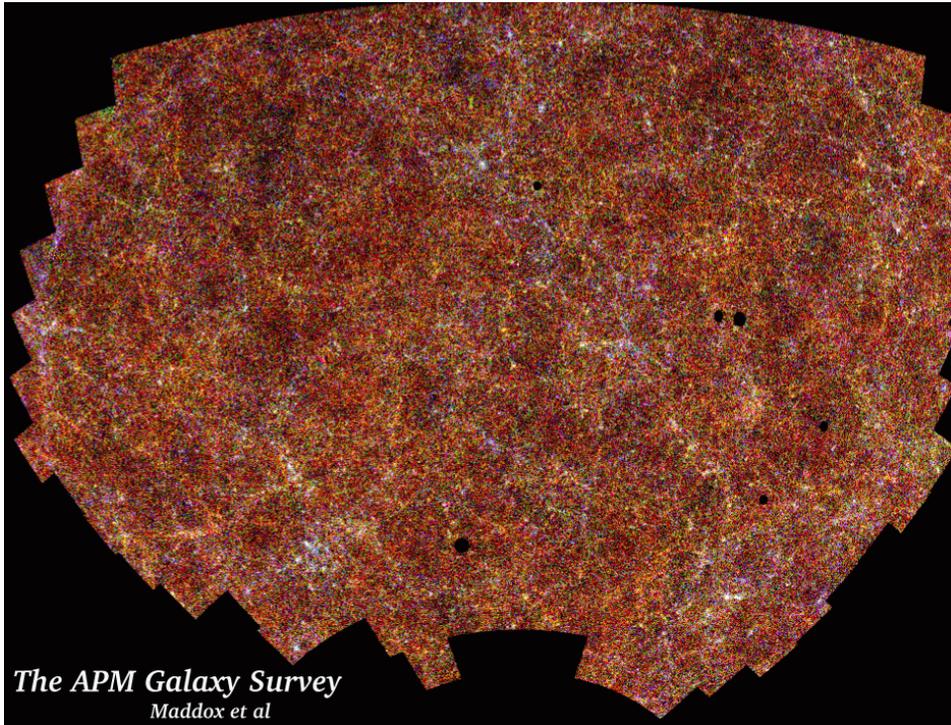
- Clearly visible are clusters
- hint of filamentary LSS features, embedding clusters

## APM survey

- Sky map:
  - $2 \times 10^6$  galaxies
  - $17 < m < 20.5$
- Uniformly defined
- Sky region: 4300 sq. deg.  
185 UK Schmidt plates,  $6^\circ \times 6^\circ$
- Large inhomogeneities, hints of weblike patterns, with clusters at densest regions.

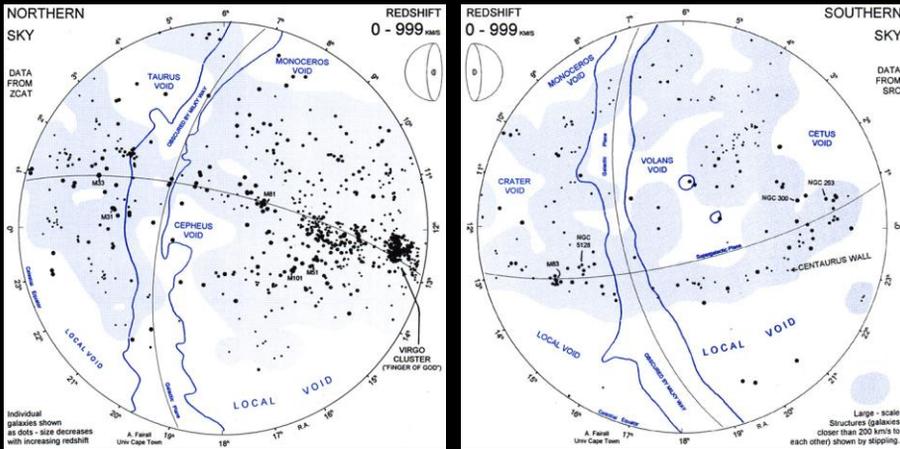
courtesy:

S. Maddox, G. Efsthathiou,  
W. Sutherland, D. Loveday



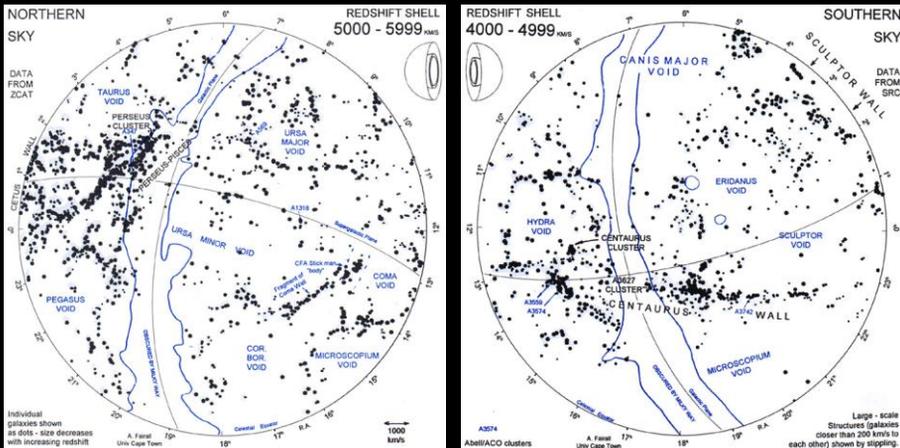
# Maps of the Local Universe

# Local Views



Tony Fairall's nearby LSS map: Local Supercluster clearly visible at  $v < 999$  km/s

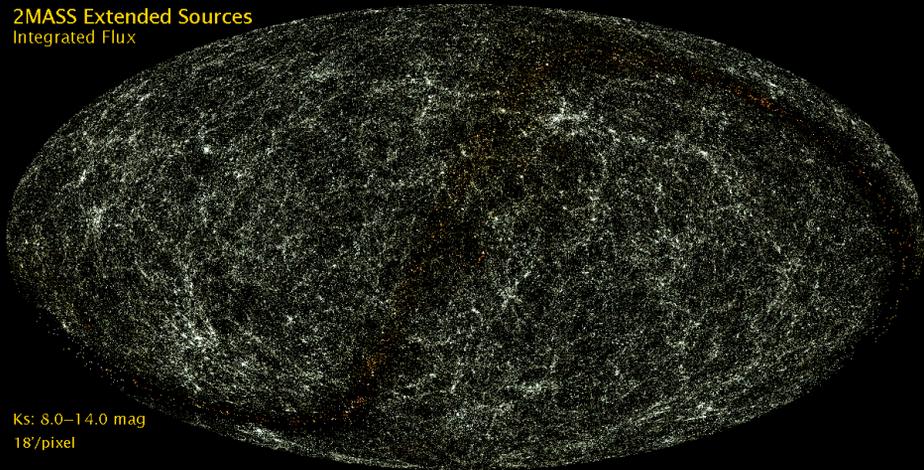
# Local Views: Moving into Foam



Tony Fairall's nearby LSS map: at  $cz=5000-5999$  km/s clear views of local cosmic web

# The Cosmic Web

2MASS Extended Sources  
Integrated Flux



Ks: 8.0–14.0 mag  
18"/pixel

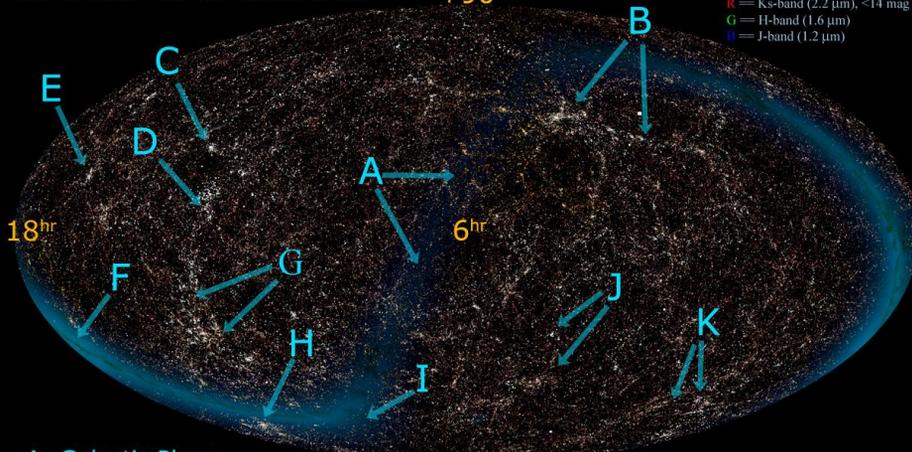
Looking around us we already see the unmistakable signatures of an intriguing foamlke matter distribution in our immediate Cosmic Vicinity.

## Identity of Local Structures along local Cosmic Web.

2MASS Local Universe

+90°

RGB Channels:  
R = Ks-band (2.2  $\mu\text{m}$ ), <14 mag  
G = H-band (1.6  $\mu\text{m}$ )  
B = J-band (1.2  $\mu\text{m}$ )



A: Galactic Plane  
B: Perseus-Pisces Supercluster  
C: Coma Cluster  
D: Virgo Cluster/Local Supercluster  
E: Hercules Supercluster  
F: Galactic Center

-90°

G: Shapley Concentration/  
Hydra-Centaurus Supercluster  
H: "Great Attractor"/Abell 3627  
I: "Local Void"  
J: Eridanus/Fornax Clusters  
K: Pavo-Indus Supercluster

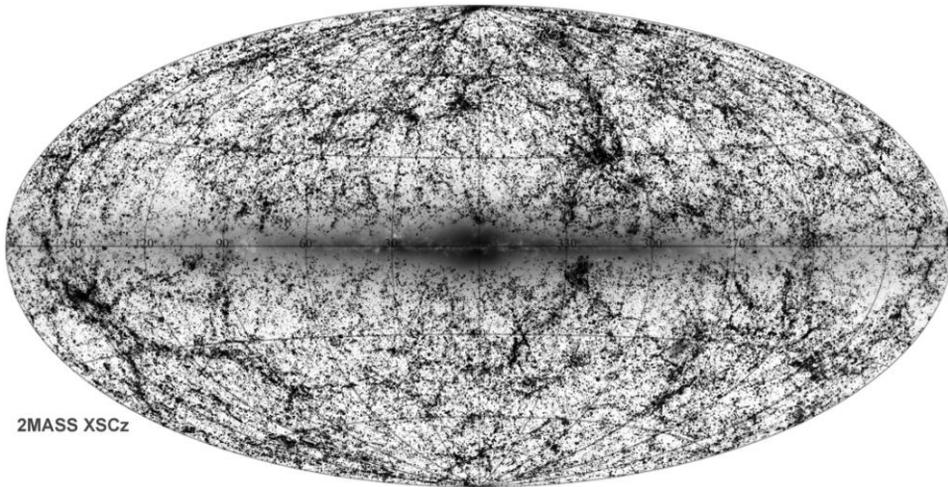
## 2MASS survey

- 2MASS all-sky survey:  
ground-based near-infrared survey whole sky,  
J( $1.2\ \mu\text{m}$ ), H( $1.6\ \mu\text{m}$ ), K( $2.2\ \mu\text{m}$ )
- 2MASS extended source catalog (XSC):  
1.5 million galaxies
- unbiased sample nearby galaxies
- photometric redshifts: depth in 2MASS maps,  
“cosmic web” of (nearby) superclusters spanning  
the entire sky.

courtesy:

T. Jarrett

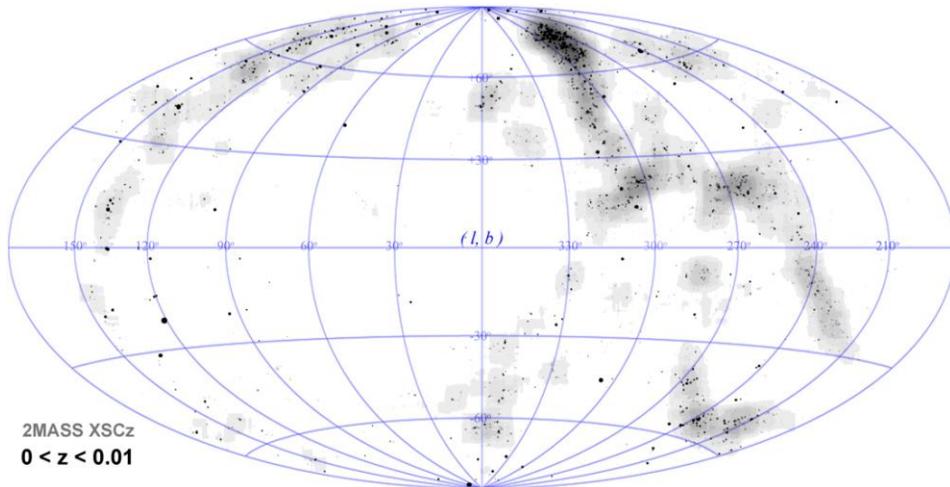
## 2MASS Cosmic Web



2MASS XSCz

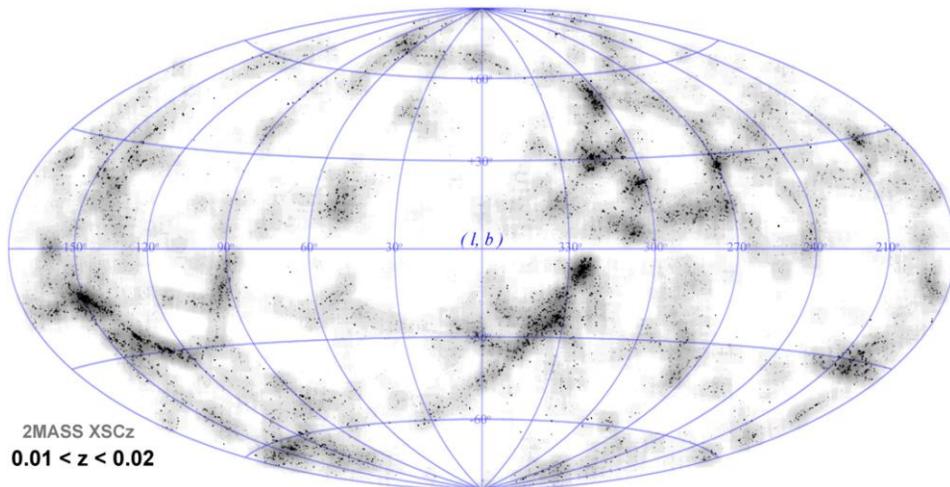
Looking around us we already see the unmistakable signatures of an intriguing weblike matter distribution in our immediate Cosmic Vicinity.

# 2MASS Cosmic Web



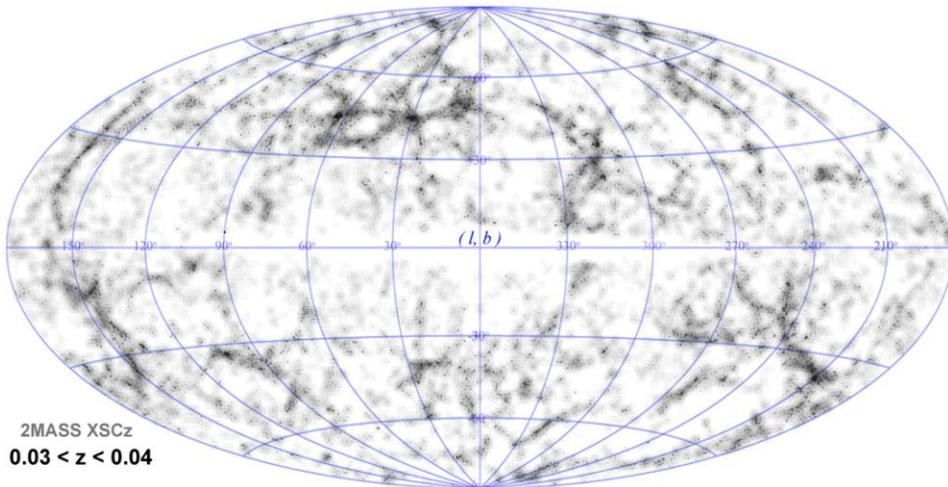
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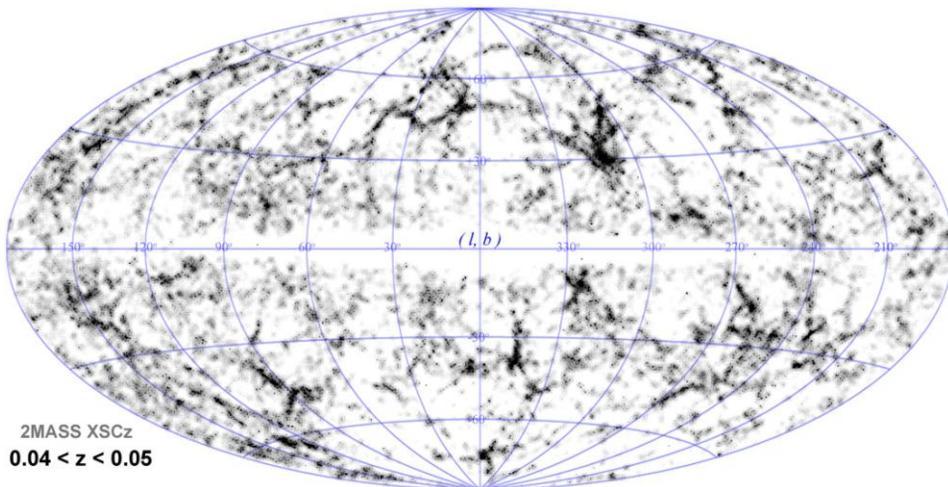
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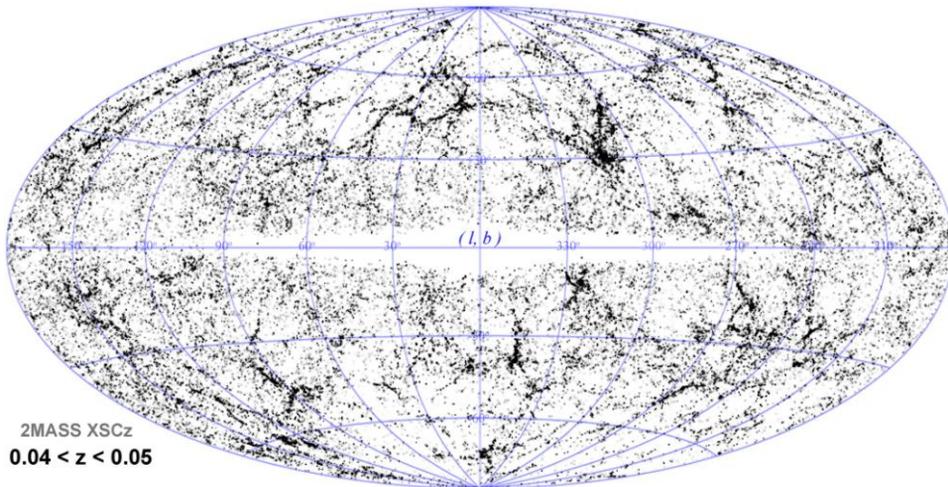
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# 2MASS Cosmic Web



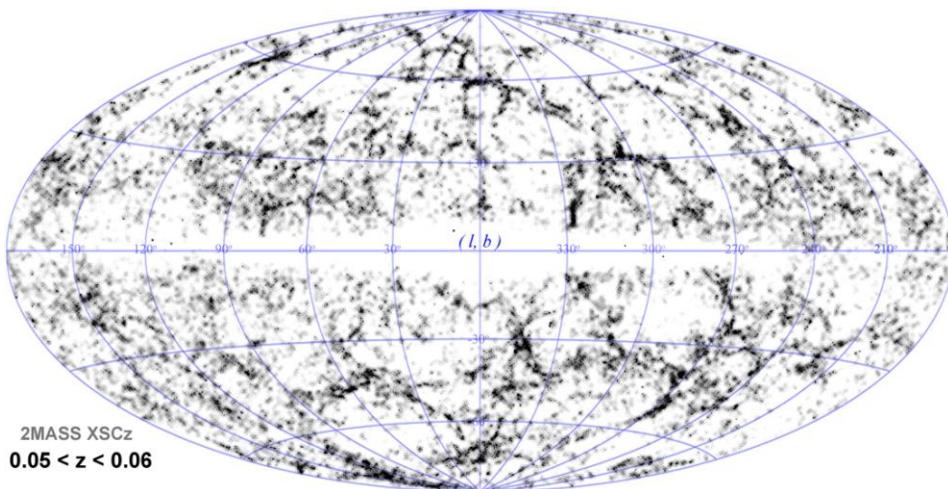
Looking around us we already see the unmistakable signatures of an intriguing weblike matter distribution in our immediate Cosmic Vicinity.

# 2MASS Cosmic Web



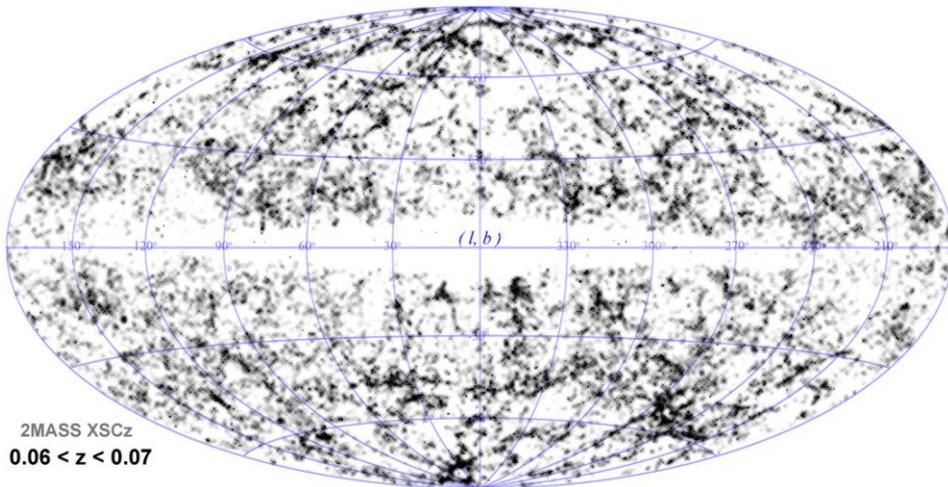
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# 2MASS Cosmic Web



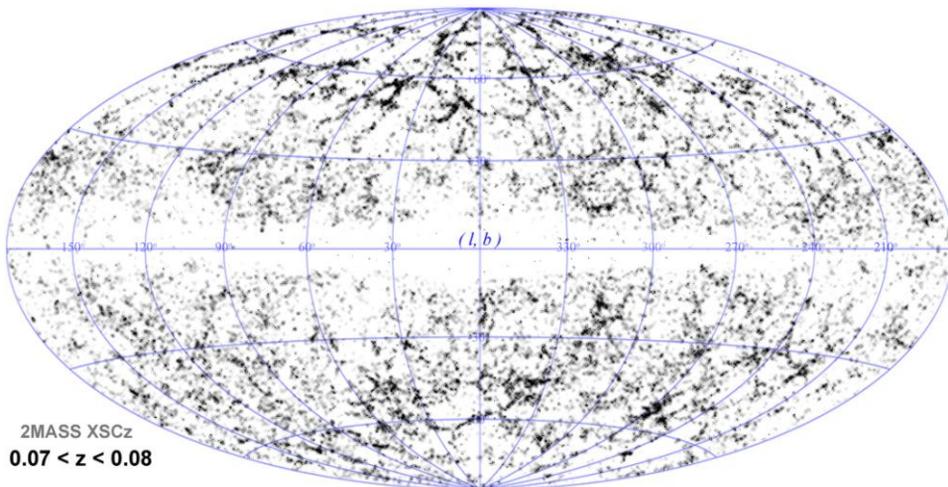
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Looking around us we already see the unmistakable signatures of an intriguing weblike matter distribution in our immediate Cosmic Vicinity.

# 2MASS Cosmic Web



Looking around us we already see the unmistakable signatures of an intriguing weblike matter distribution in our immediate Cosmic Vicinity.



# Galaxy Redshift Surveys

## Galaxy Redshift Surveys

- For obtaining 3D maps of the galaxy distribution:

measure spatial location of galaxies:

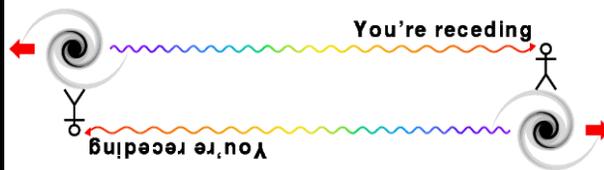
- position on the sky  $(\alpha, \delta)$
- distance  $r$

- Determination real distance  $r$  of galaxy very cumbersome, reasonably accurate estimates only for nearby gal's ...
- Common approximate method:  
exploit Hubble expansion of the Universe

## Galaxy Redshift Surveys

$$1 + z = \frac{1}{a} \iff \begin{cases} \lambda_{em} = \lambda_0 \\ \lambda_{obs} = \frac{a(t_{obs})}{a(t_{em})} \lambda_0 \end{cases}$$

$$z \equiv \frac{\lambda_{obs} - \lambda_{em}}{\lambda_{em}}$$



## Galaxy Redshift Surveys

- Hubble Expansion:

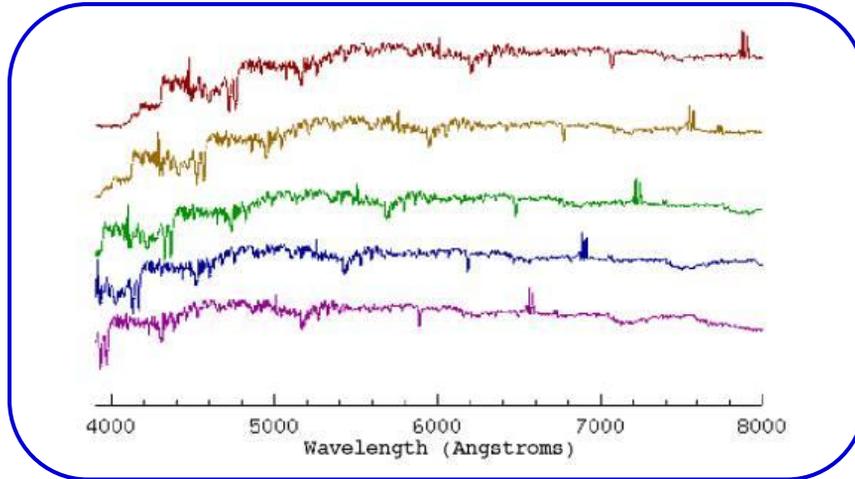
$$cz = Hr \quad (z \ll 1)$$

galaxy at distance  $r$   
 has redshift  $z$   
 ( $c$ : vel. light;  $H$ : Hubble constant)

- Redshift of galaxies can be much more easily determined than distance:

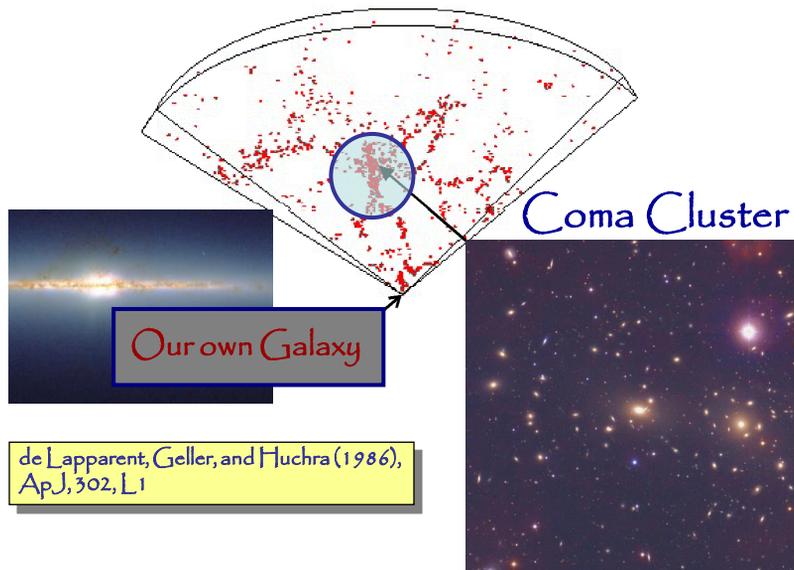
Galaxy Spectrum

# Galaxy Redshift Surveys



Examples of redshifted galaxy spectra

# Mapping the Universe



## Redshift Space Distortions

### Redshift Distortions

- In reality, galaxies do not exactly follow the Hubble flow:

In addition to the cosmological flow, there are locally induced velocity components in a galaxy's motion:

$$cz = Hr + v_{pec}$$

the galaxy's peculiar velocity  $v_{pec}$

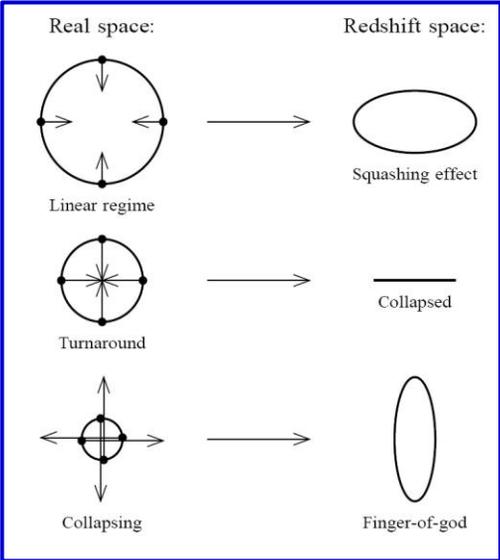
- As a result, maps on the basis of galaxy  $z$  do not reflect the galaxies' true spatial distribution

# Redshift Distortions

Origin of peculiar velocities:

three regimes

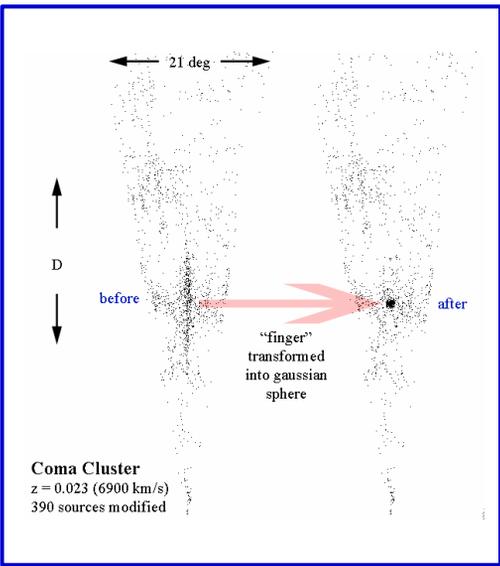
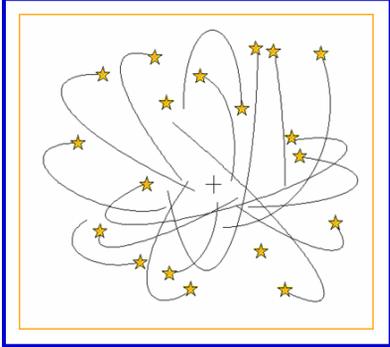
- very high-density virialized cluster (core) regions:  
"thermal" motion in cluster, up to > 1000 km/s
- "Fingers of God"**
- collapsing overdensity (forming cluster):  
inflow/infall velocity
- Large scales:  
(linear, quasi-linear) cosmic flow, manifestation of structure growth



# Fingers of God

$$cz = Hr_{clust} + \frac{\vec{v}_{gal} \cdot \vec{r}_{gal}}{r_{gal}}$$

Galaxy velocity component along line of sight



# Fingers of God

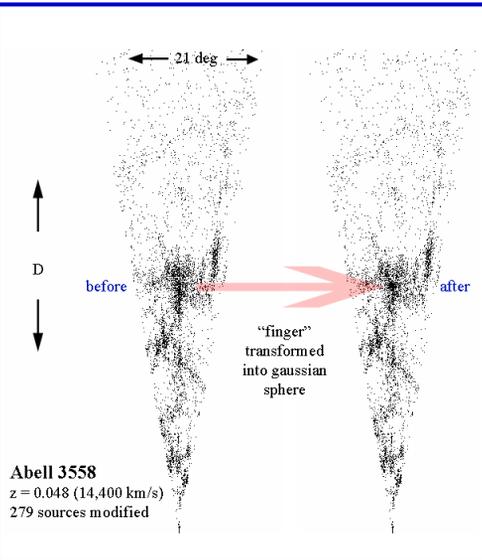
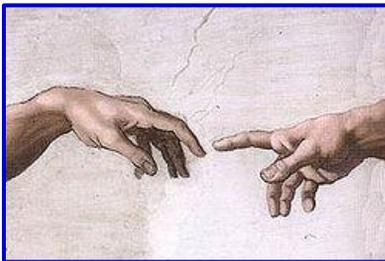
## Clusters of galaxies:

Mass:  $10^{14} - 10^{15} M_{\odot}$   
 Radius:  $\sim 1.5$  Mpc  
 Overdensity  $\Delta \sim 1000$

Thermal velocity:  $\sim 1000$  km/s

Internal cluster galaxy velocities  
 visible in projection along line of sight

→ "Finger of God"



# Nonlinear Infall Pattern

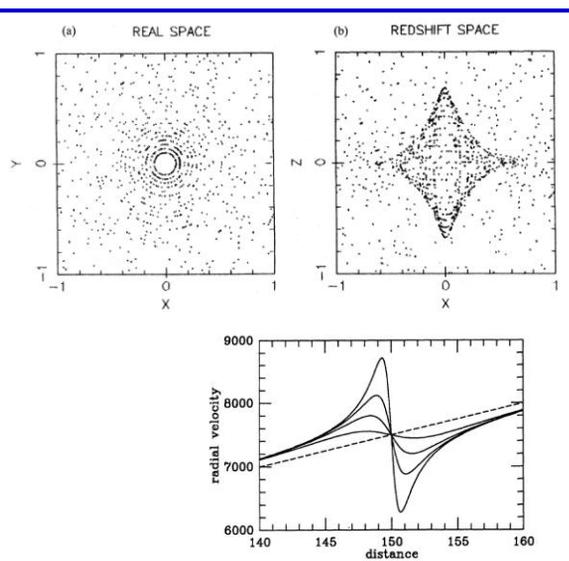
## Cluster Infall:

Matter in surroundings falling  
 in onto cluster:

- infall velocities up to 1000 km/s  
 radially declining:
- velocities decrease as distance  
 to cluster centre increases
- projected radial velocity  
 function of angle & distance  
 wrt. cluster centre.



- triple-value region redshift space:  
 - within turnaround radius,  
 a particular redshift  $z$   
 may correspond to 3 spatial  
 positions



## Nonlinear Infall Pattern

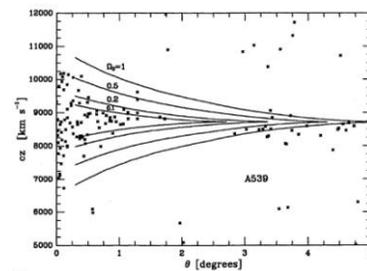
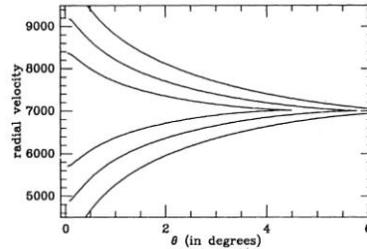
### Cluster Caustics:

Three-value region cluster infall:

Projection onto restricted cone-shaped redshift space regions around clusters

Enclosed within caustic surfaces

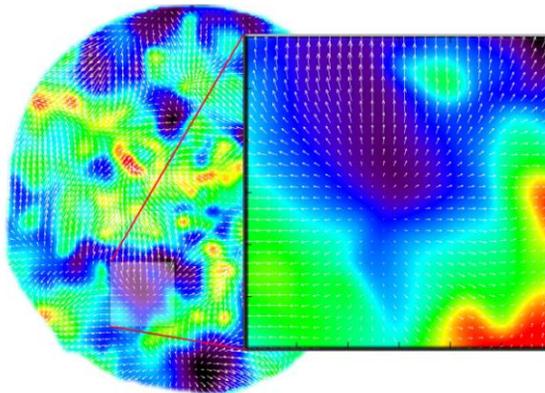
Position caustics dependent on  $\Omega_m$



## Large Scale Flows

### Large-Scale Flows:

- On large (Mpc) scales, structure formation still in linear regime
- Structure buildup accompanied by displacement of matter:
  - Cosmic flows
- Directly related to cosmic matter distribution
- In principle possible to correct for this distortion, ie. to invert the mapping from real to redshift space
- Condition: entire mass distribution within volume should be mapped



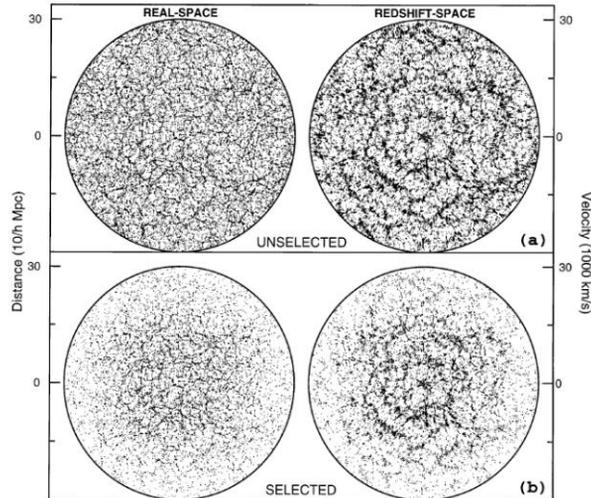
$$\mathbf{v}(\mathbf{x}, t) = \frac{H}{4\pi} \frac{f(\Omega_m)}{b} a \int d\mathbf{x}' \delta_{gal}(\mathbf{x}', t) \frac{(\mathbf{x}' - \mathbf{x})}{|\mathbf{x}' - \mathbf{x}|^3}$$

# Large Scale Flows

## Large-Scale Flows:

The induced large scale peculiar velocities translate into extra contributions to the redshift of the galaxies

Compare  
"real space" structure vs.  
"redshift space" structure



Magnitude vs. Volume Limited

# Magnitude vs. Volume limited Surveys

- Two different sampling approaches for analysis spatial structure from galaxy redshift catalogue:
- Volume-limited surveys:
  - uniform spatial coverage, including all galaxies within volume to depth  $d_s$
  - all galaxies with an absolute brightness  $>$  survey limit  $M_s$
$$M_s = m_{\text{lim}} - 5 \log d_s - 25 - k(z)$$
  - diminishing sampling density & spatial resolution as one wishes to include larger volume (excluding all galaxies  $M > M_s$ )
- Magnitude-limited survey
  - include all galaxies with apparent magnitude brighter than  $m_s$
  - assures optimal use of spatial galaxy catalogue
  - at the price of a non-uniform spatial coverage & diminishing resolution towards higher depths

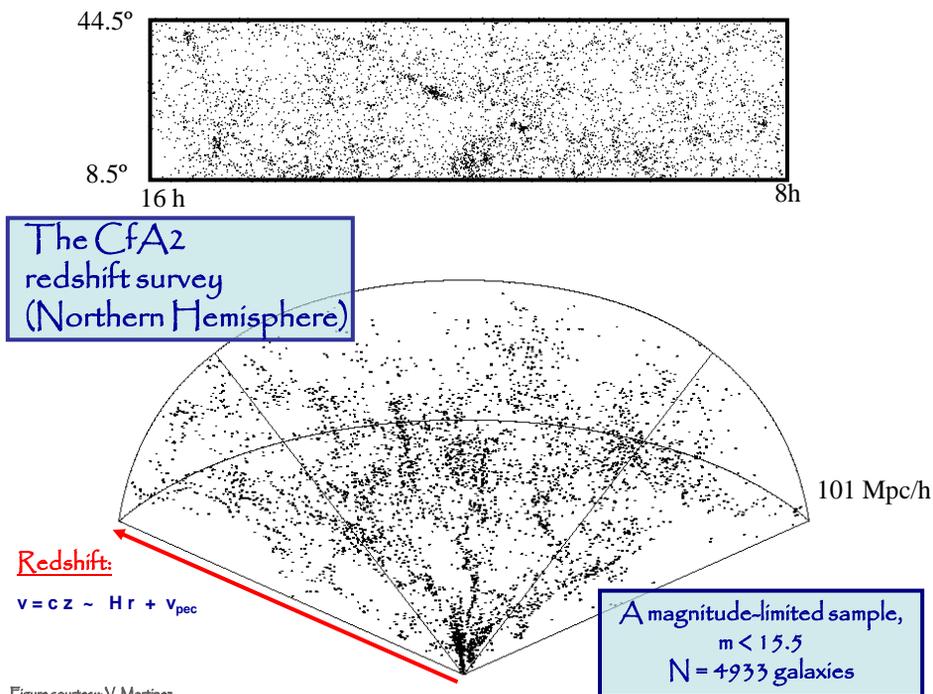
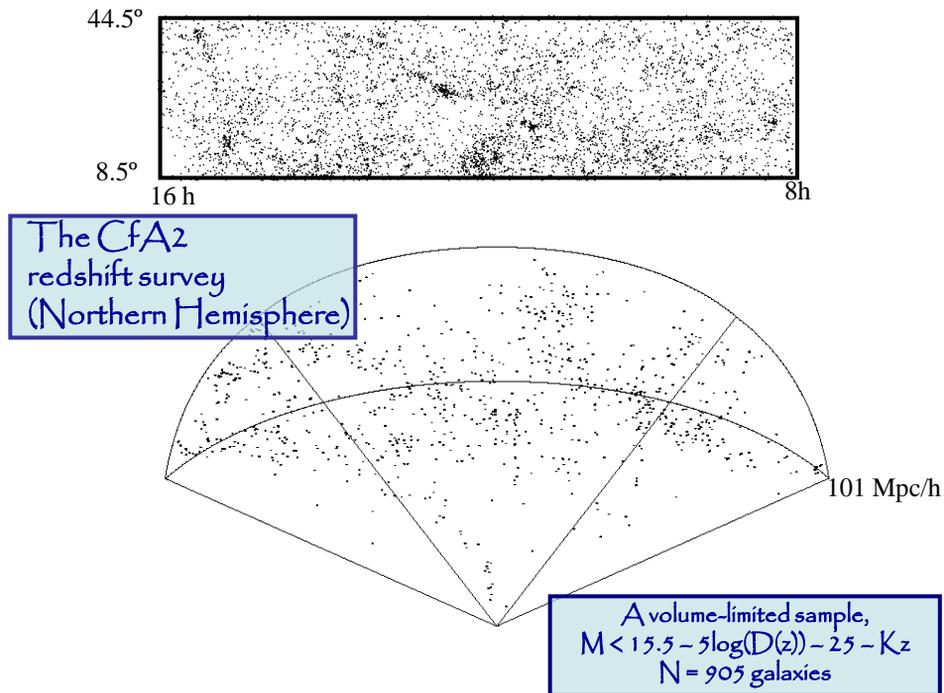


Figure courtesy: V. Martinez



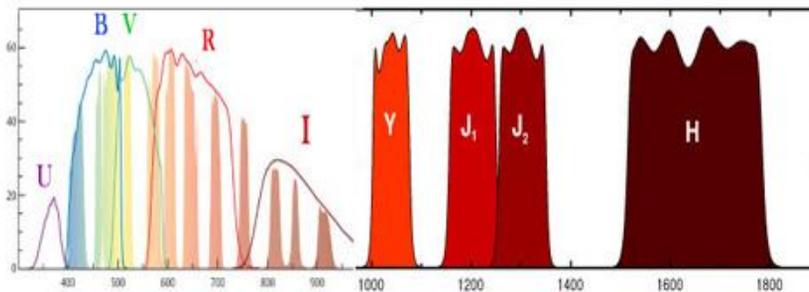
## Photometric Redshifts

# Photometric Redshifts

- Instead of measuring the electromagnetic spectrum of the galaxies in a survey, one may get a good estimate of the redshift on the basis of the photometry and colours of the objects.

COMBO-17

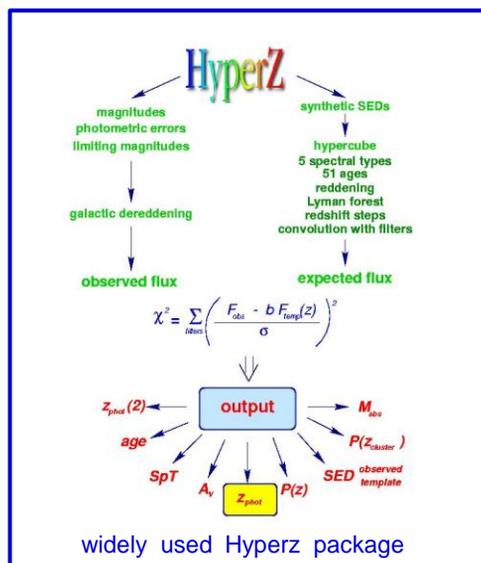
+ 4



# Photometric Redshifts

Practical Implementation:

- Photometric redshifts determined by fitting to standard SED (SED: spectral energy distribution)
- Taking into account:
  - spectral type
  - reddening
  - Lyman $\alpha$  forest (high z!)
  - filters
- Accuracy (typical):
  - $\Delta z \sim 0.1$



# Photometric Redshifts

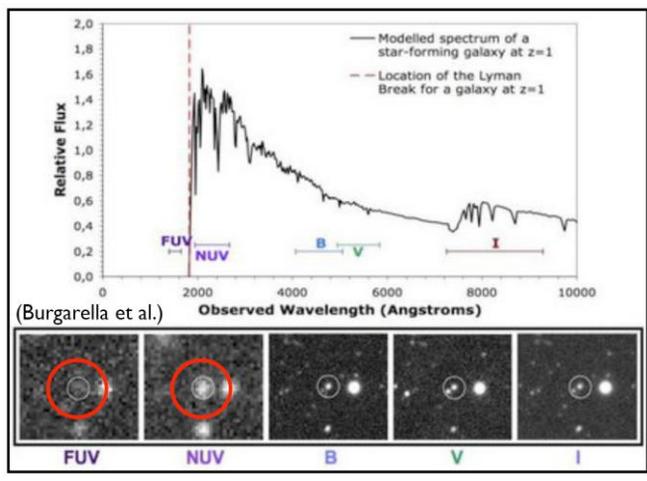
## Photometric Redshifts

Technique widely used for identifying high  $z$  objects

For example, Lyman break results

in

FUV-NUV dropouts (1400-1800 Å) for  $z \sim 0.5-1.0$

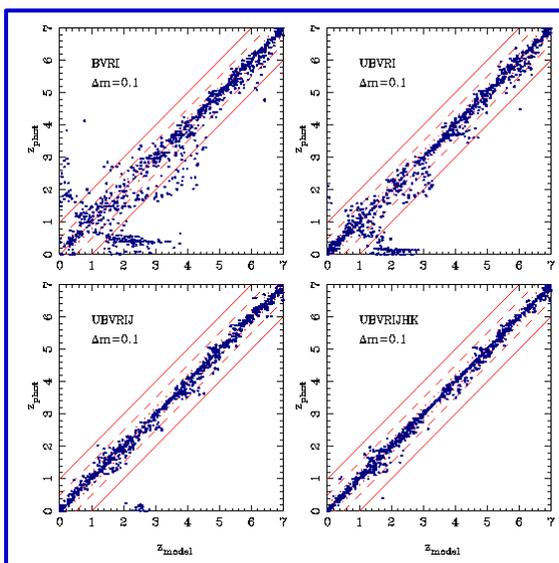


Below the Lyman break at 912 Å, hydrogen absorbs galaxy light

# Photometric Redshifts

## Photometric Redshifts:

- Accuracy (typical):  $-\Delta z \sim 0.1$
- Accuracy higher as more bands are used
- Bands to be chosen to take into account spectral characteristics/features
- eg. low  $z$ : UV still weak point

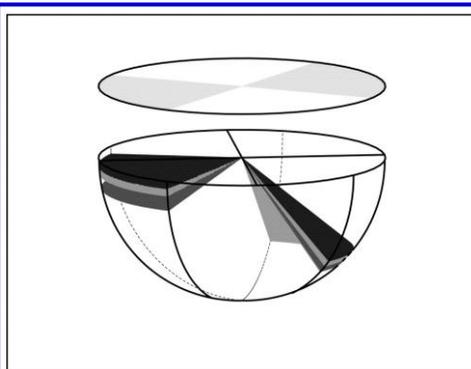


# Survey Geometry

## Survey Geometry

### Practical Limitations

- Limited telescope time
- Limited detector sensitivity
- How to optimally sample structure in Universe?
- Devise survey geometry that reveals optimal amount of information on question at hand
  - Patterns galaxy distribution
  - Distribution high-density peaks
  - Density Field

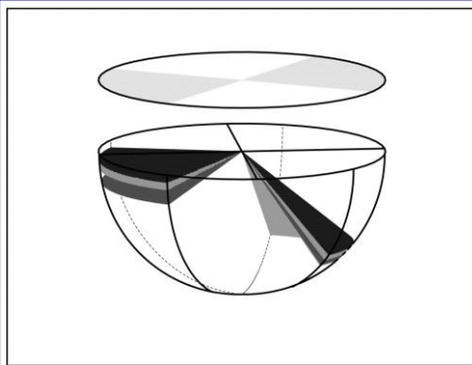


Sky Location  
2-D LCRS survey slices

## Survey Geometry

### Survey Geometry:

- Slice Surveys:
  - thin stripe on sky
  - very sensitive to reveal patterns galaxy distribution
- Pencil-beam surveys
  - very narrow region on sky
  - very deep
  - strategy to probe largest structures
  - structure at high  $z$  (early times)



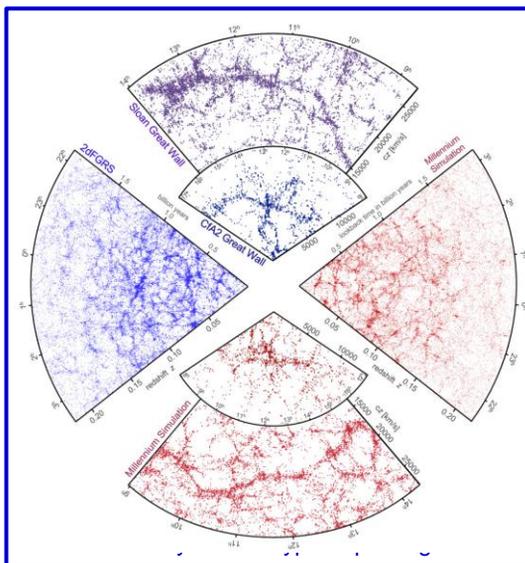
Sky Location  
2-D LCRS survey slices

## Survey Geometries

### Examples of

### Slice Redshift Surveys:

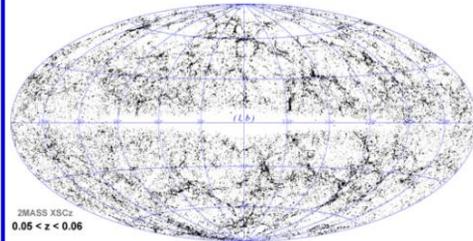
From  
CfA2-2dFGRS-SDSS



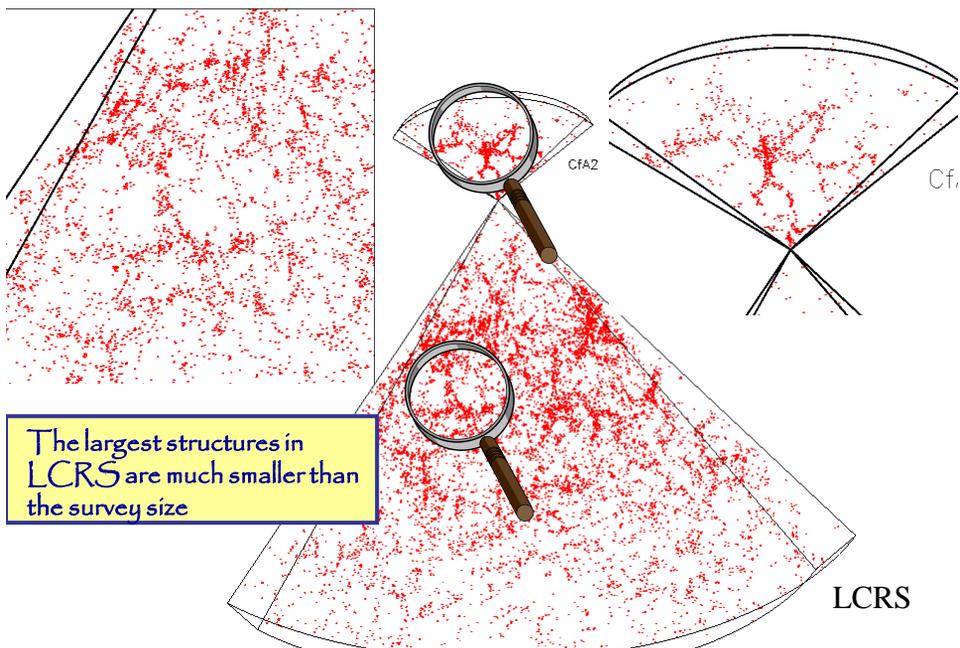
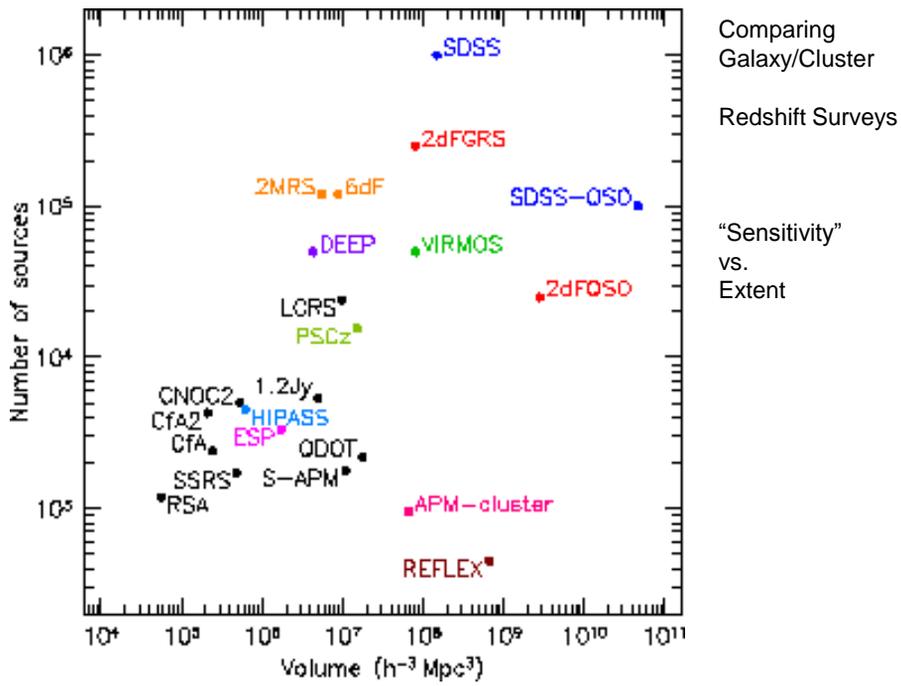
## Survey Geometry

Survey Geometry:

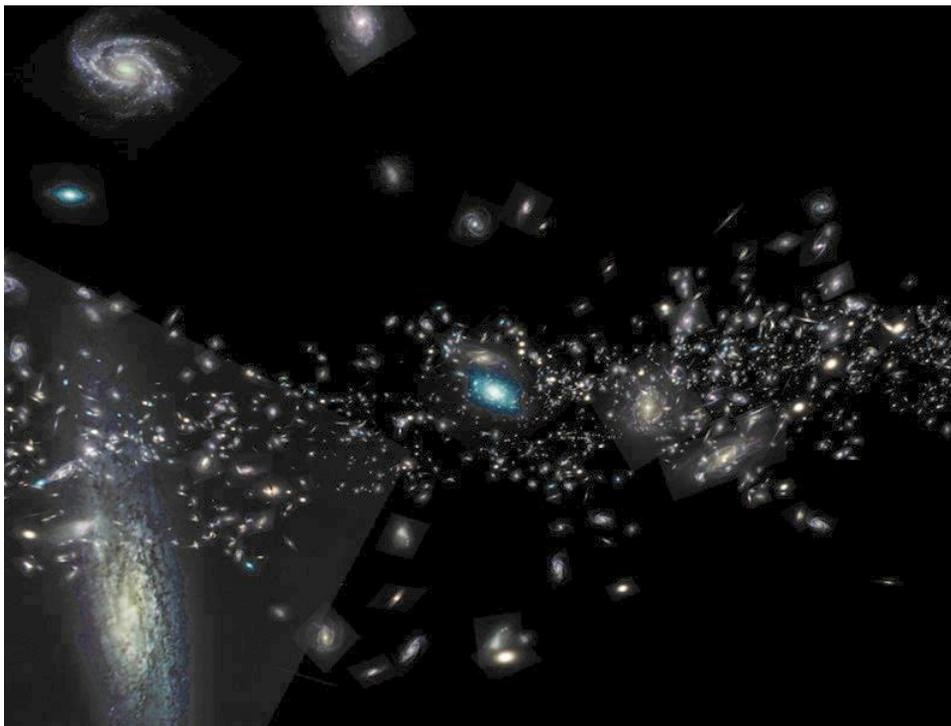
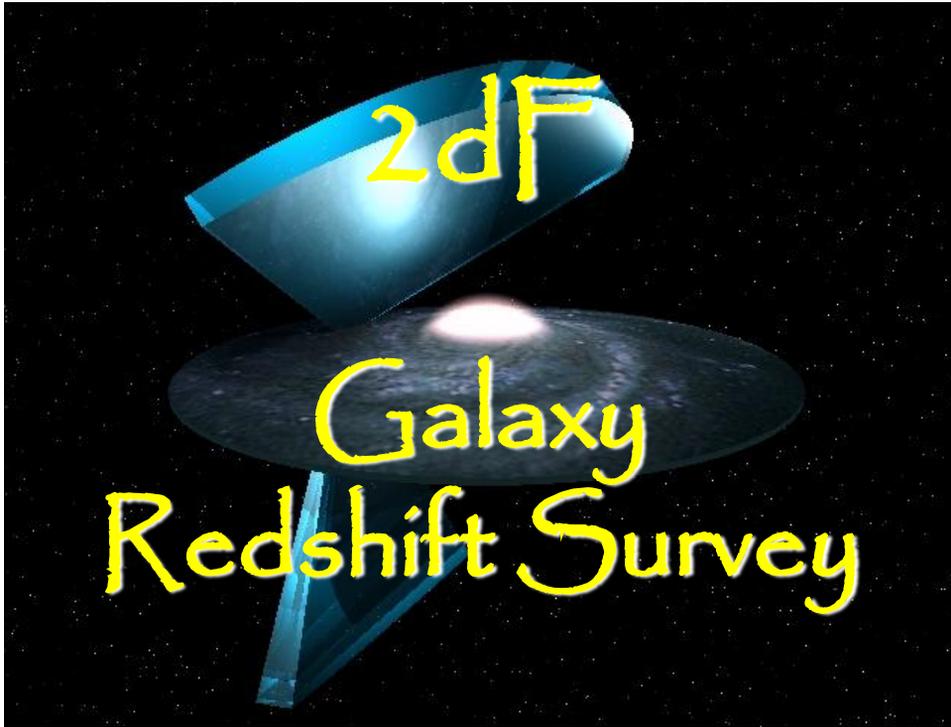
- Sparse Sample:
  - sampling density field
  - on scales  $\gg$  intergalaxy distance
- Full-sky surveys
  - necessary to probe dynamics cosmic regions

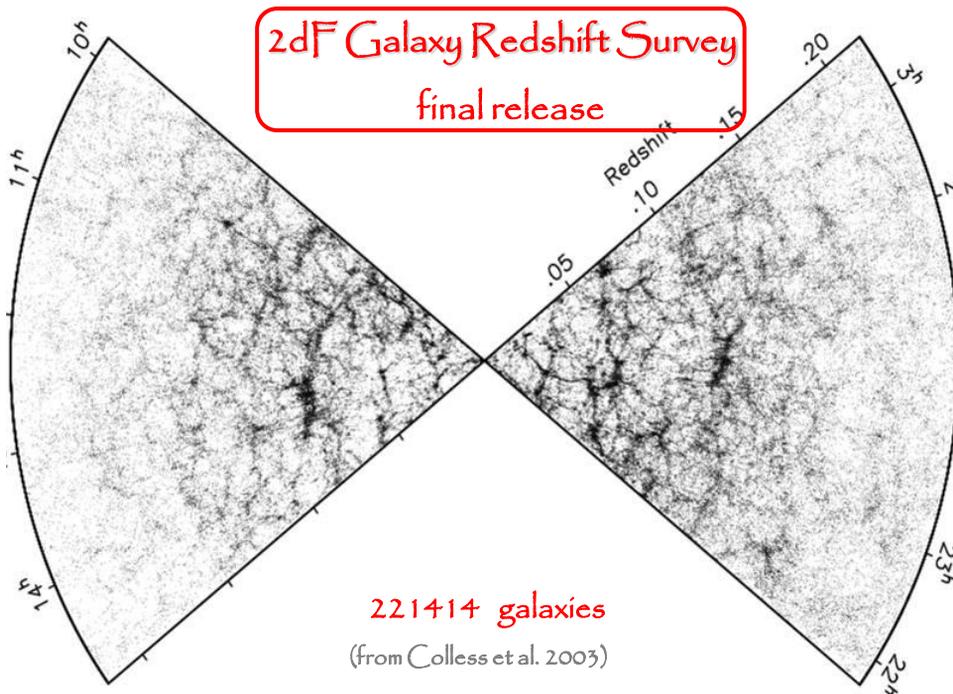
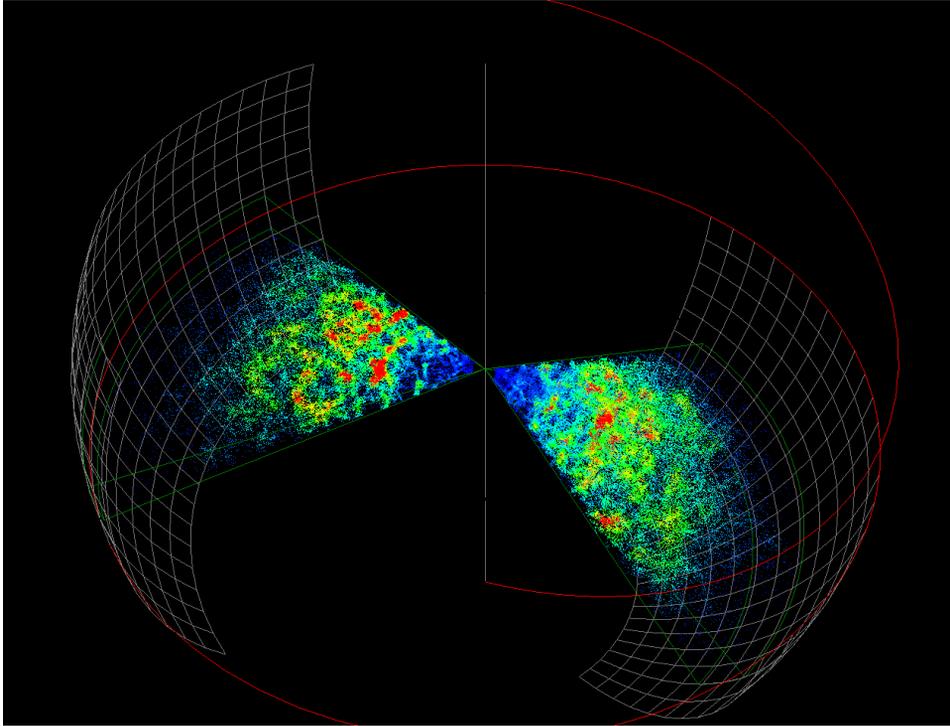


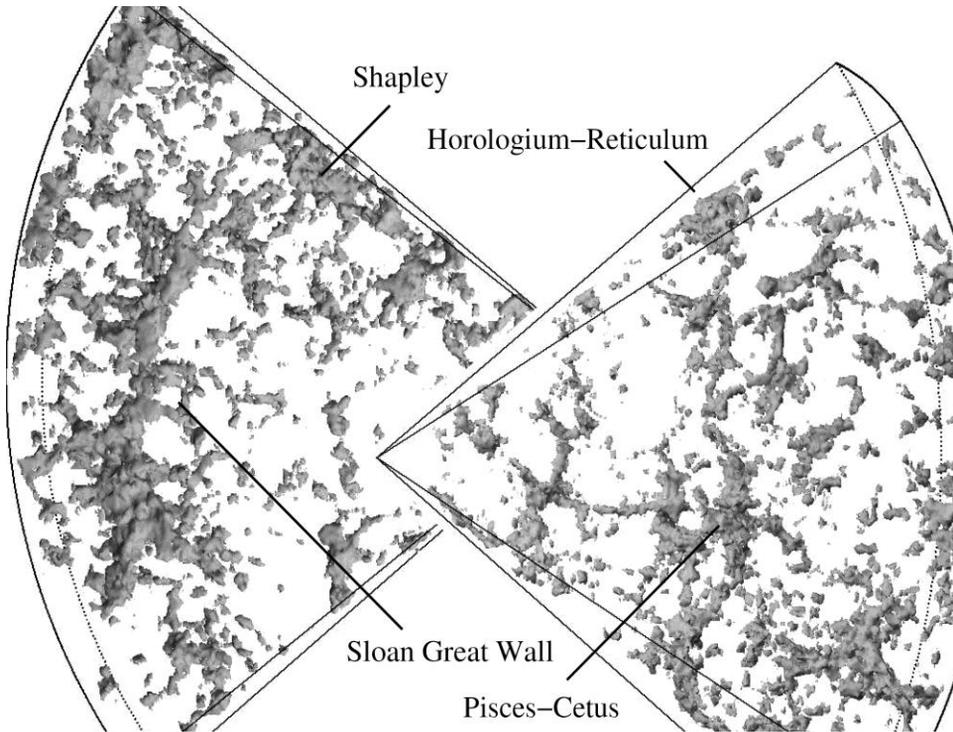
# Galaxy Redshift Surveys: Overview



“The beginning of the end” or “the end of greatness” ...R. Kirshner







## SDSS survey

- Largest and most systematic (digital!) sky survey in history of astronomy.
- Images sky in 5 photometric bands !!!!  
Down to apparent magnitude  $r \sim 23.1$
- Covers  $\sim 25\%$  of the sky: 8452 sq. deg.
- With 2dFGRS, the SDSS will produce the most extensive map of the spatial structure of our cosmic neighbourhood.
- Million galaxies subsequently selected for measuring redshift  $z$ : electromagnetic spectrum
- Total:
  - sky survey:  $10^8$  stars,  $10^8$  galaxies,  $10^5$  quasars
  - spectroscopy:  $10^6$  galaxies,  $10^5$  quasars,  $10^5$  stars

## SDSS survey

Specially dedicated  
2.5m wide-angle telescope  
Apache Point Observatory (New Mexico)



# SDSS survey

Aims to sample 25% of the sky:  
DR7 - 8423 sq. deg.

Photometric system 5 filters:

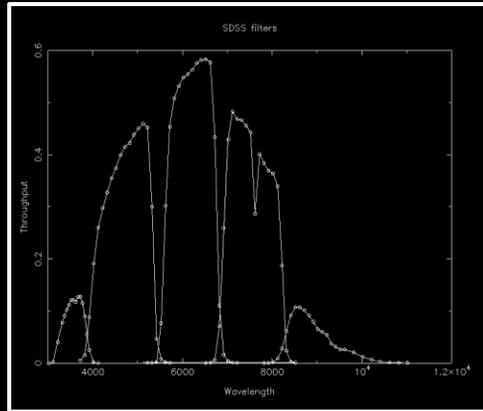
	$\lambda$	$m_{\text{lim}}$
u	354 nm	24.4
g	476 nm	25.3
r	628 nm	25.1
i	769 nm	24.4
z	925 nm	22.9

Driftscan mode

- 5 filters:
- 30 CCD chips, 5 rows of 6
- S/N ~ 5
- CCD chip: 2048x2048 pixels  
120 Mbyte

Spectroscopy

- up to 640 (fibers) per recording
- per night 6-9 recordings



# SDSS survey

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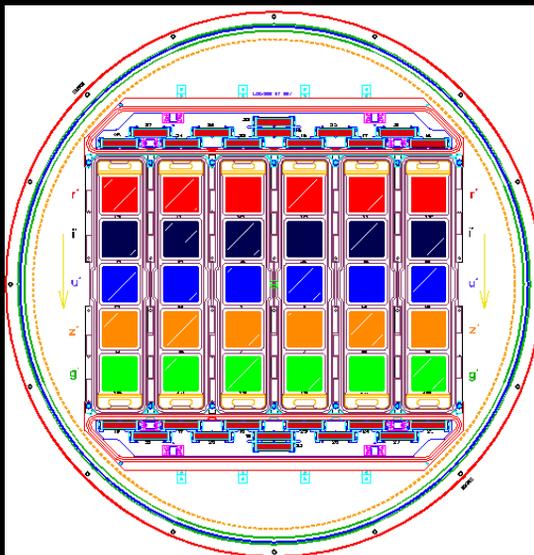
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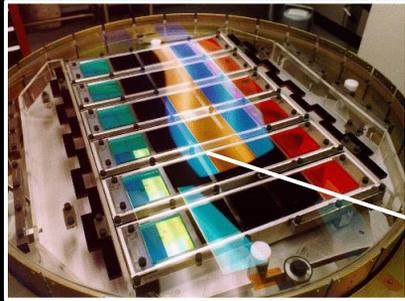
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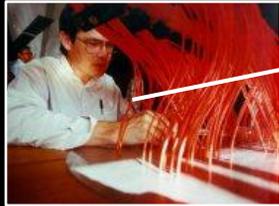


# SDSS survey

5-color  
Camera  
30 CCD  
chips

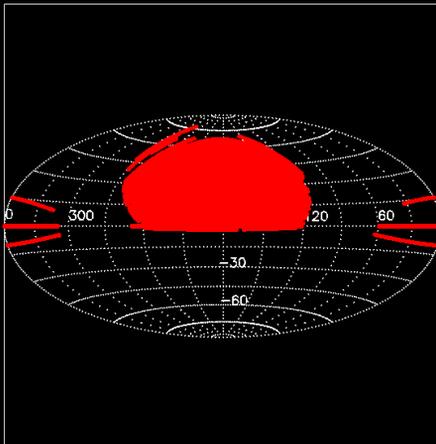


Fiber  
Spectrograph

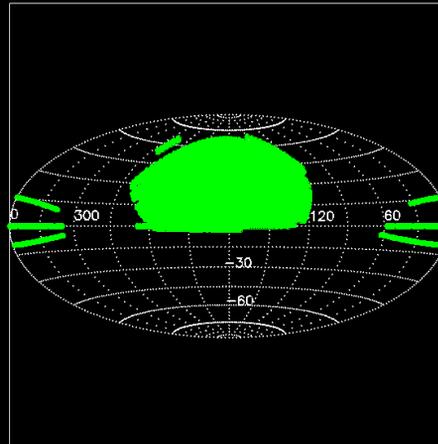


# SDSS survey

SDSS Data Release 7 (2008):



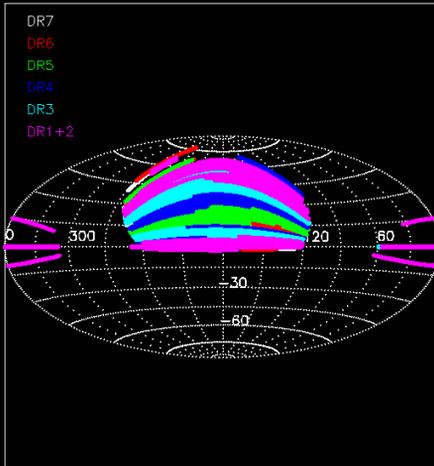
SDSS Legacy Imaging Sky Coverage:  
8423 sq. deg.



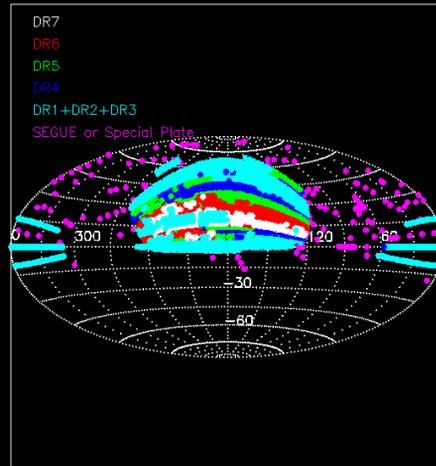
SDSS Legacy Spectral Sky Coverage:  
8032 sq. deg.

# SDSS survey

SDSS Data Release 1-7 (2000-2008)

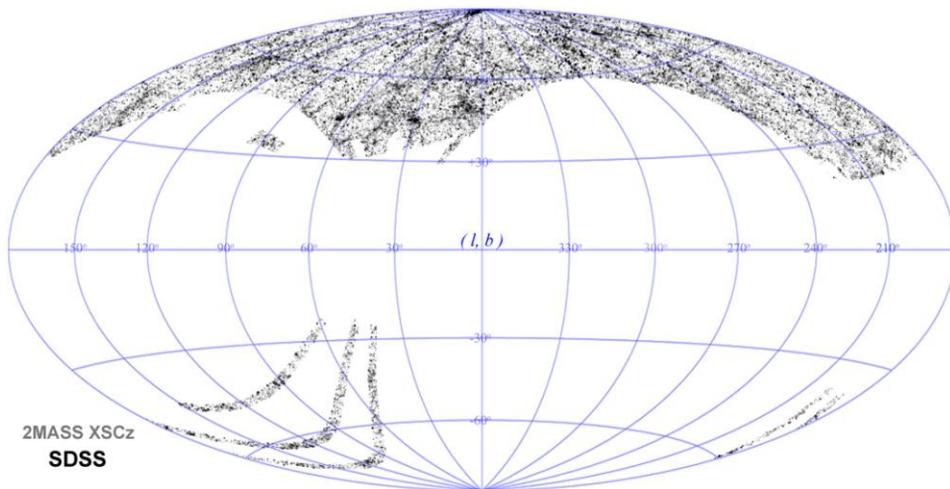


SDSS Legacy Imaging Sky Coverage:  
8423 sq. deg.



SDSS Legacy Spectral Sky Coverage:  
8032 sq. deg.

## SDSS Galactic region



comparison 2MASS

# SDSS survey

- Imaging:  
230 million objects

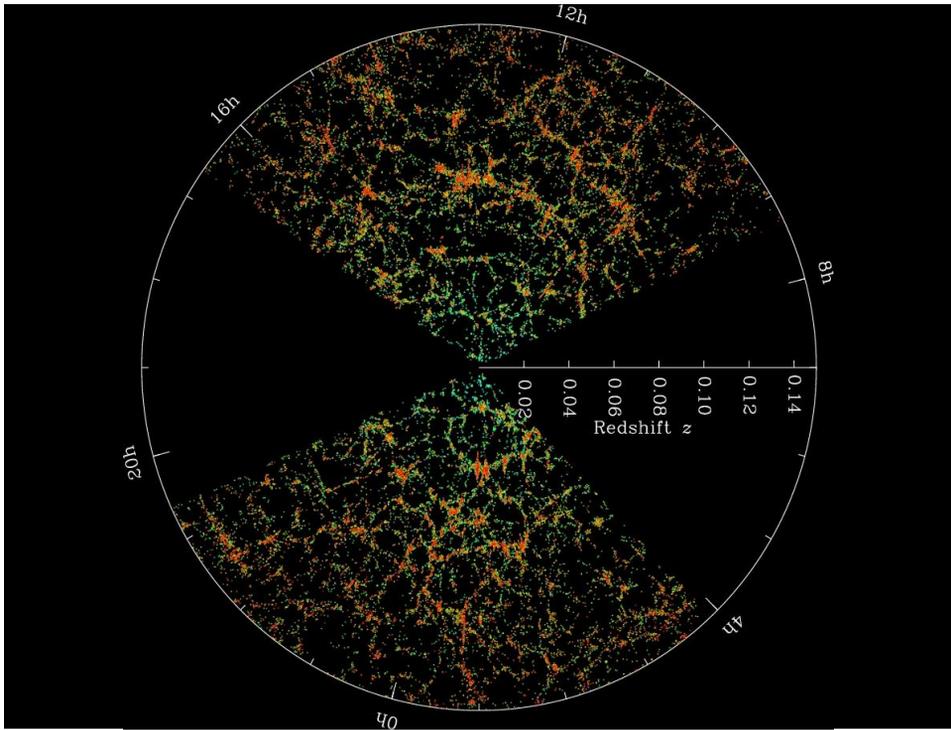
- Spectroscopic (Redshift) survey:

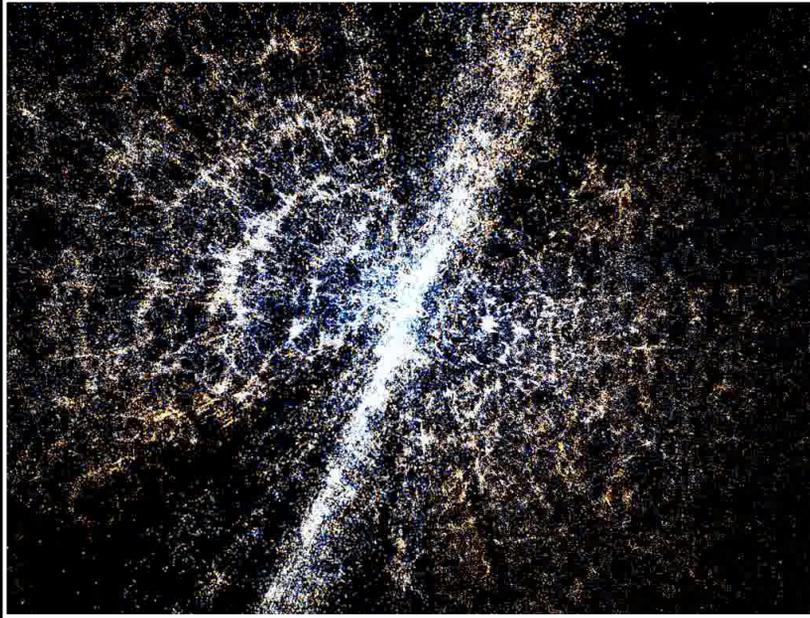
magnitude limit:  
galaxies: (Petrosian)  $r < 17.7$   
quasars  $i < 19.1 / i < 20.2$  ( $z > 2.3$ )

objects: 928,567 galaxies  
109,862 quasars  $z < 2.3$   
8,802 quasars  $z > 2.3$

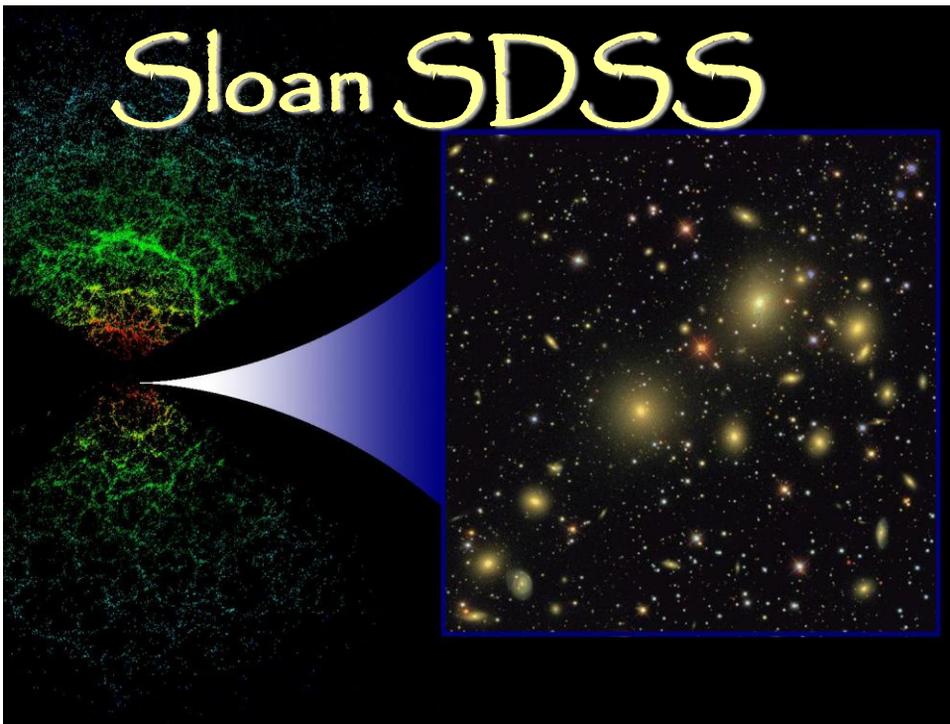


VOID_00 J083707.48+323340.8	VOID_01 J100542.44+511623.9	VOID_02 J102250.68+561932.1	VOID_03 J102819.23+623502.6	VOID_04 J103506.47+550847.6
VOID_05 J130526.08+544551.9	VOID_06 J132232.48+544906.5	VOID_07 J132718.56+593010.2	VOID_08 J135113.62+463509.2	VOID_09 J135635.46+593041.3
VOID_10 J140034.49+551515.1	VOID_11 J142416.41+523208.3	VOID_12 J143052.33+551440	VOID_13 J143553.77+524400.6	VOID_14 J154452.18+362845.6





# The Elements: Clusters



# Clusters of Galaxies

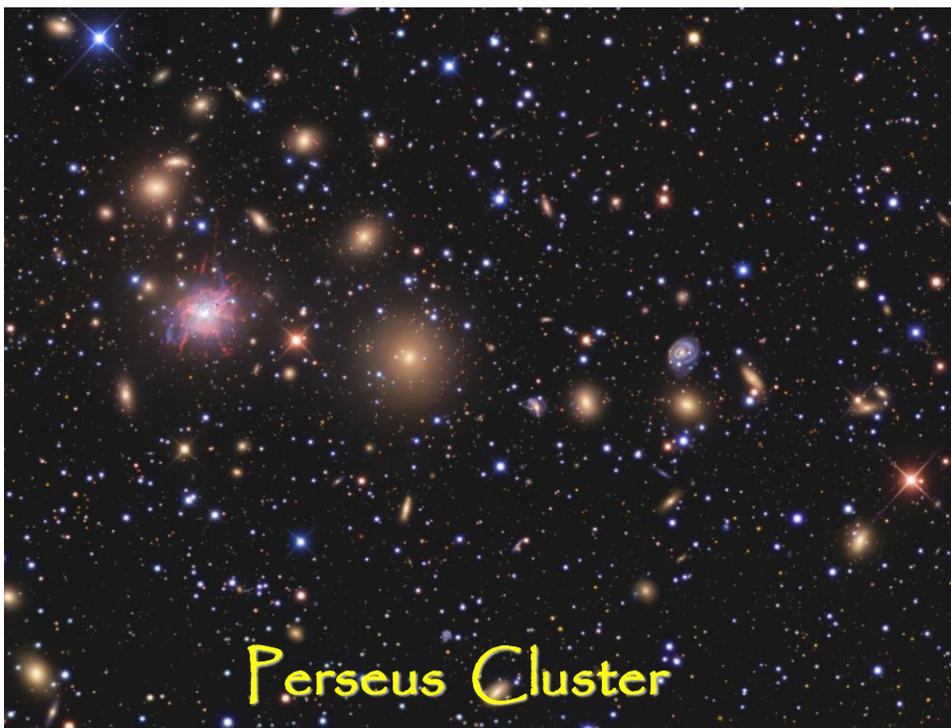
- Assemblies of up to 1000s of galaxies within a radius of only  $1.5-2h^{-1}$  Mpc,
- Representing overdensities of  $\delta \sim 1000$
- Galaxy move around with velocities  $\sim 1000$  km/s
- They are the most massive, and most recently, fully collapsed structures in our Universe.

# Clusters of Galaxies



Courtesy:  
O. Lopez-Cruz

Coma Cluster

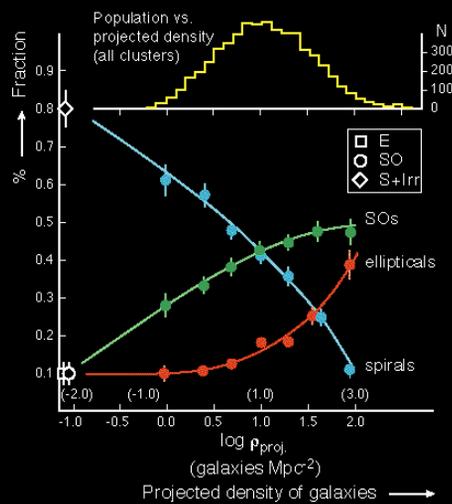




## Density-Morphology Relation

Outstanding relation between cosmic environment and galaxies:

- Density-Morphology Relation
- Dense regions (clusters):  
early-type galaxies  
(ellipticals, SO, ...)
- Lower Density areas:  
late-type galaxies  
(spirals, irregulars)
- From clusters to voids
- reflection of effects  
galaxy interactions  
(more frequent high densities)

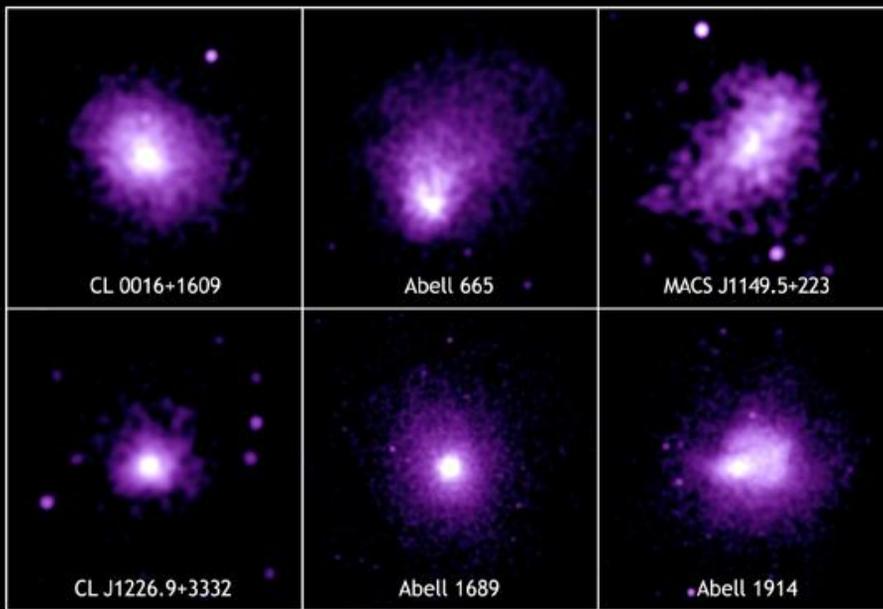
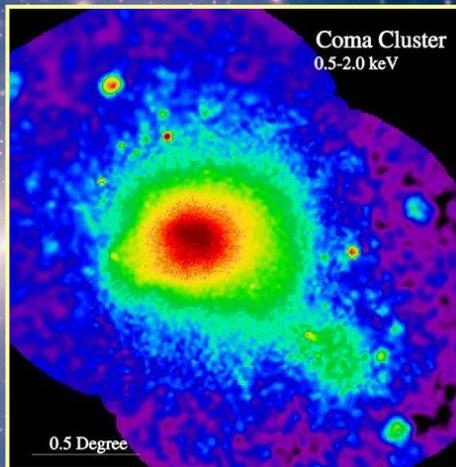


# Clusters of Galaxies

## X-ray intracluster gas

Baryonic matter in clusters is not only confined to galaxies. On the contrary, about 2 to 5 times more baryonic mass is in the form of a **diffuse hot X-ray emitting intracluster gas**, trapped and heated to a temperature of the order of  $10^8$  K by the gravitational potential of the cluster. At such high temperatures, this gas is a fully ionized plasma, producing powerful X-ray emission, bremsstrahlung radiation induced by the electron-ion interactions.

ROSAT X-ray image Coma Cluster



# Clusters of Galaxies: Gravitational Lenses

A highly promising method to determine the amount and distribution of

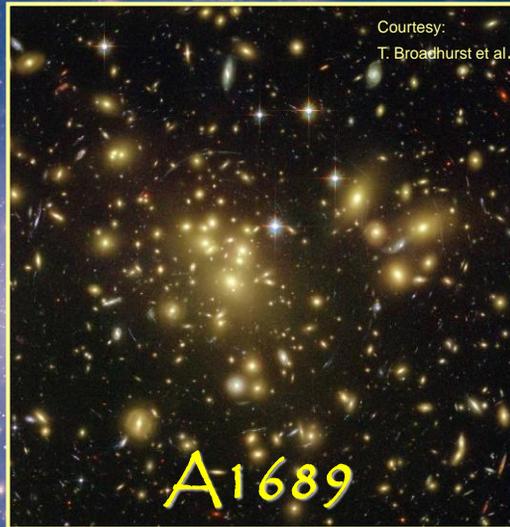
matter in the Universe looks at the way it affects the trajectories of photons.

According to

Einstein's theory of General Relativity,

gravitational potential wells will bend and focus light. Dark matter concentrations act as a

**Gravitational Lens.**



# Clusters of Galaxies: Dark Matter Map

A highly promising method to determine the amount and distribution of

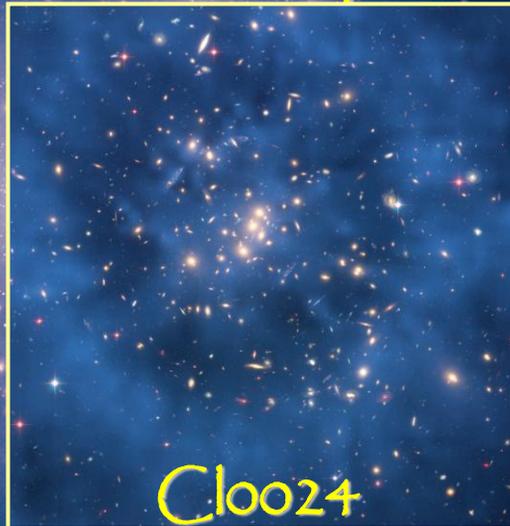
matter in the Universe looks at the way it affects the trajectories of photons.

According to

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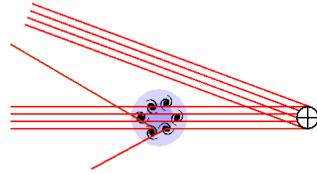
gravitational potential wells will bend and focus light. Dark matter concentrations act as a

**Gravitational Lens.**

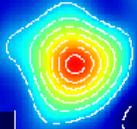


# Clusters of Galaxies: Sunyaev-Zeldovich

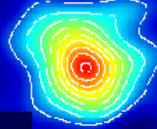
Sunyaev-Zel'dovich effect:  
scattering through inverse Compton  
of CMB photons by  
hot intracluster electrons



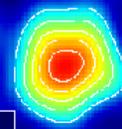
Abell 1914  $z=0.17$



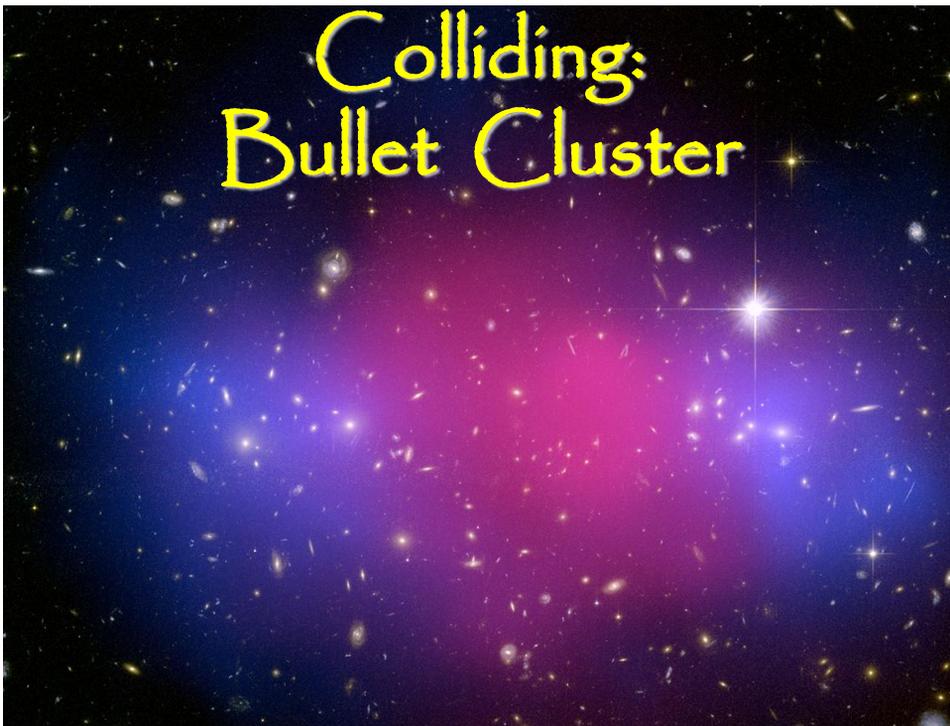
CL0016+16  $z=0.54$



MS1054-C0321  $z=0.83$



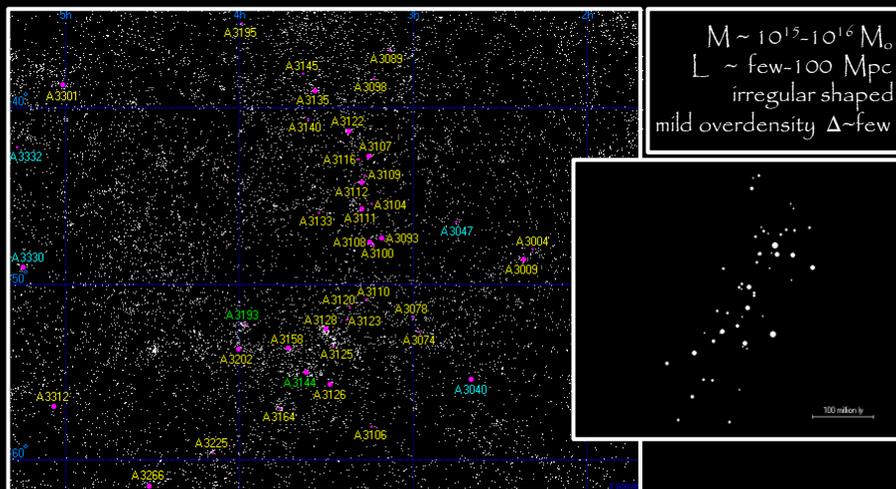
# Colliding: Bullet Cluster



# The Elements: Superclusters

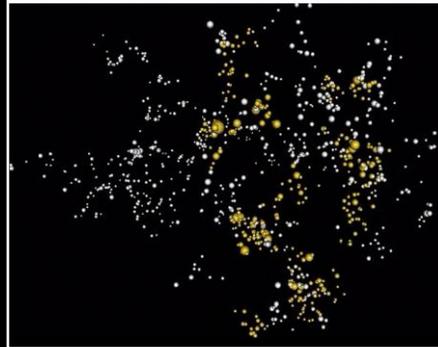
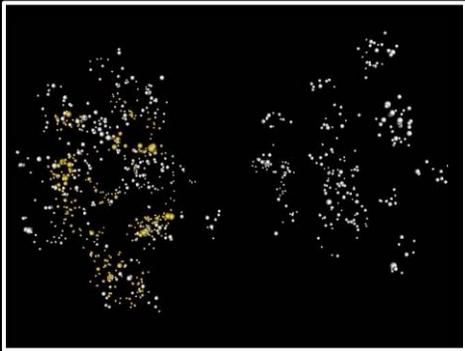
## Superclusters

Large groups of clusters & galaxies (1-dozens)

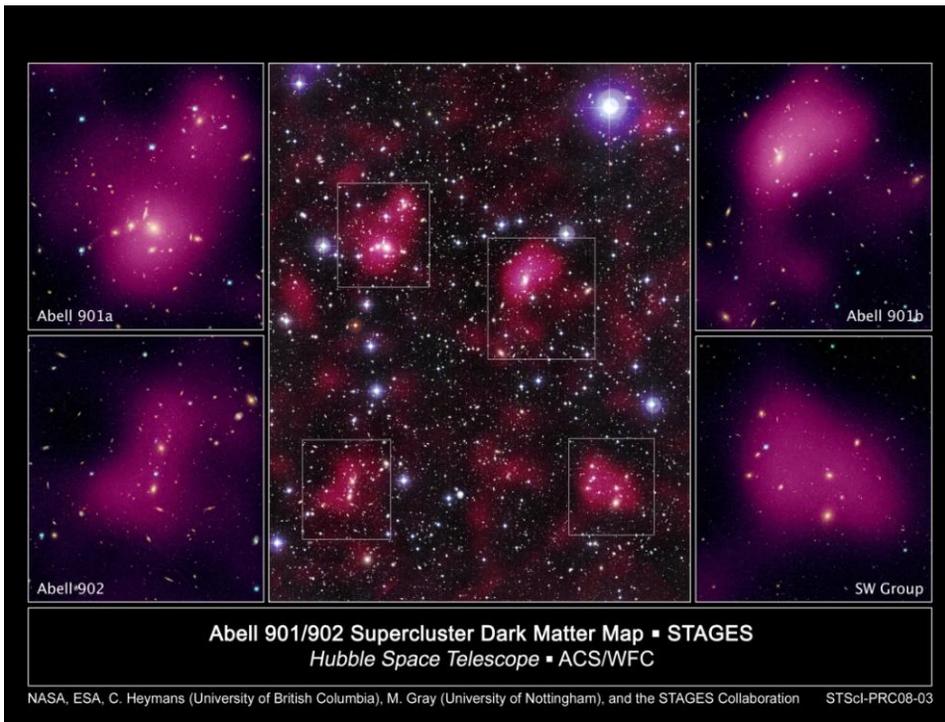


# Superclusters:

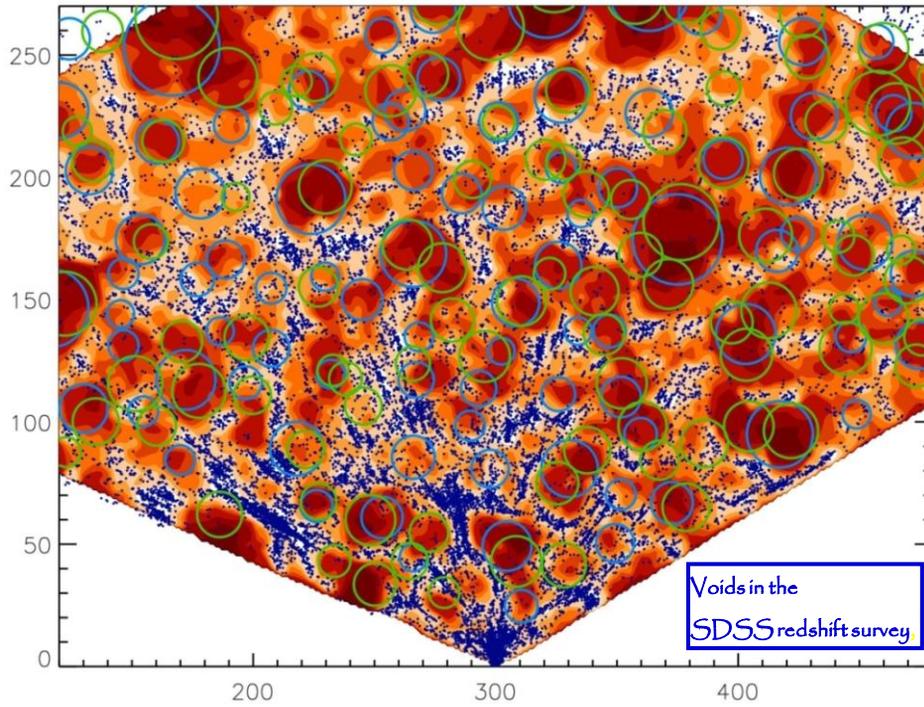
Einasto et al. sample  
 X-ray clusters (yellow) and  
 Abell clusters (white)



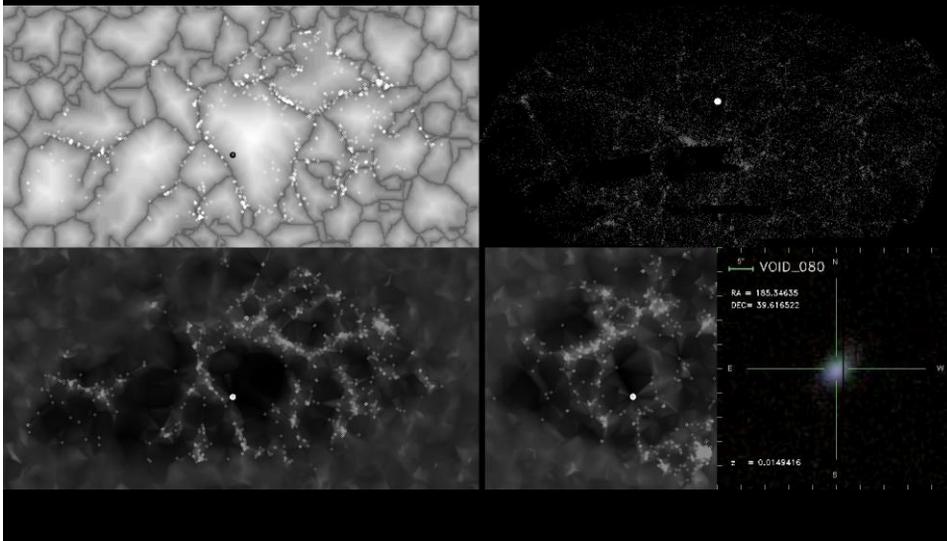
superclusters are not isolated single objects,  
 but integral components in the pervasive  
 Cosmic Web



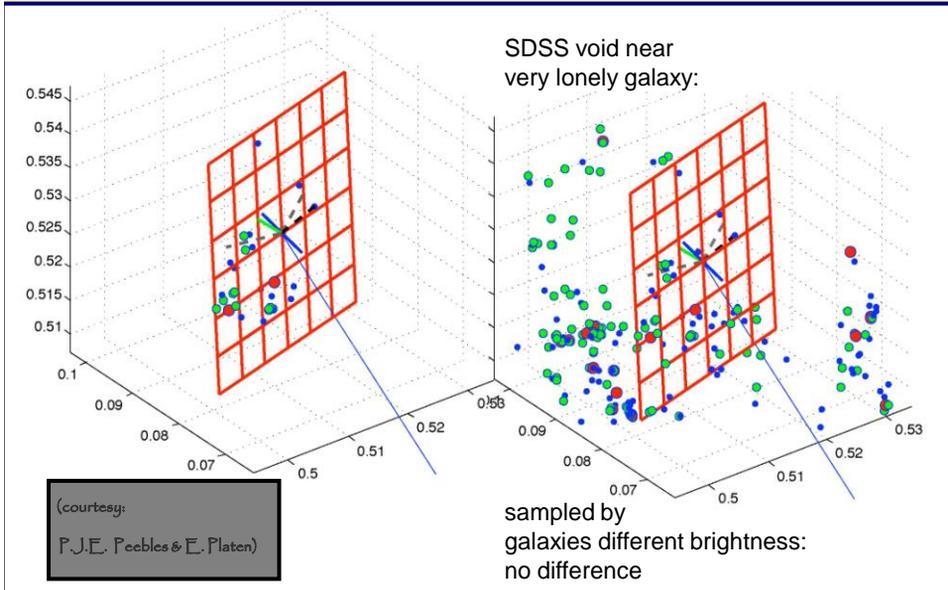




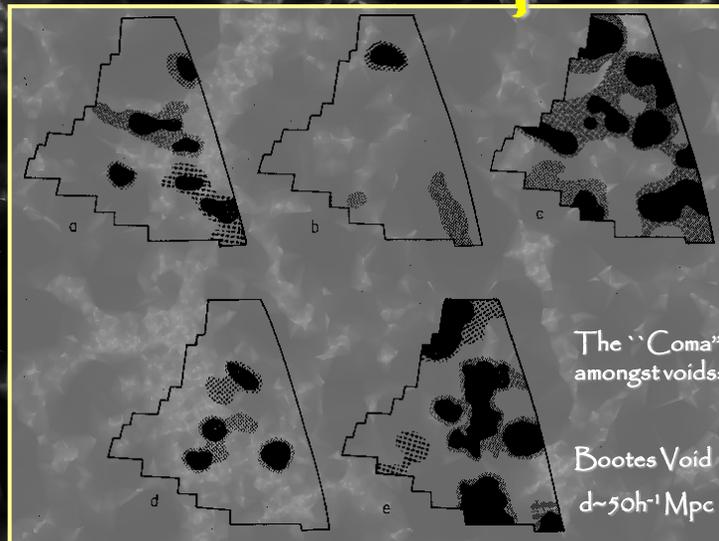
# SDSS Voids



# SDSS Voids



## Voids in Space



# Voids in Space

## The Bootes Void.

Bootes void as revealed by the galaxy number space density in a sequence of five different recession velocity intervals in the direction of the Bootes constellation on the sky.

The lowest contour represents a density equal to 0.7 of the cosmic mean, each higher contour represents a factor 2 increase in density. Velocity ranges (km/s):

- (a) 7,000-12,000 (b) 12,000-17,000 (c) 17,000-23,000  
(d) 23,000-29,000 (e) 29,000-39,000

Frame (b) clearly reveals a large void in the galaxy distribution, which turns out to be roughly spherical in outline.

From: Kirshner et al. (1987)

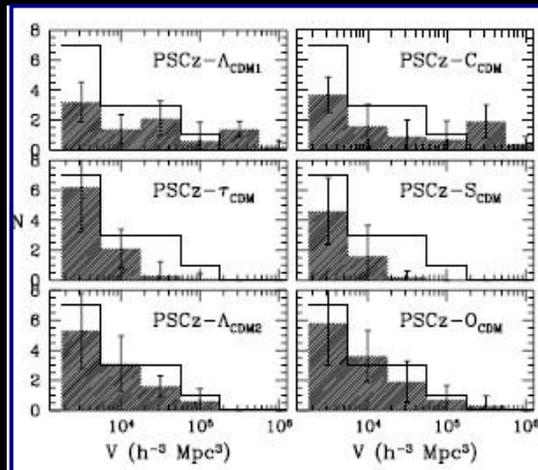
## Void Size & Volume

### Void Size

Void size distribution  
dependent on cosmology:

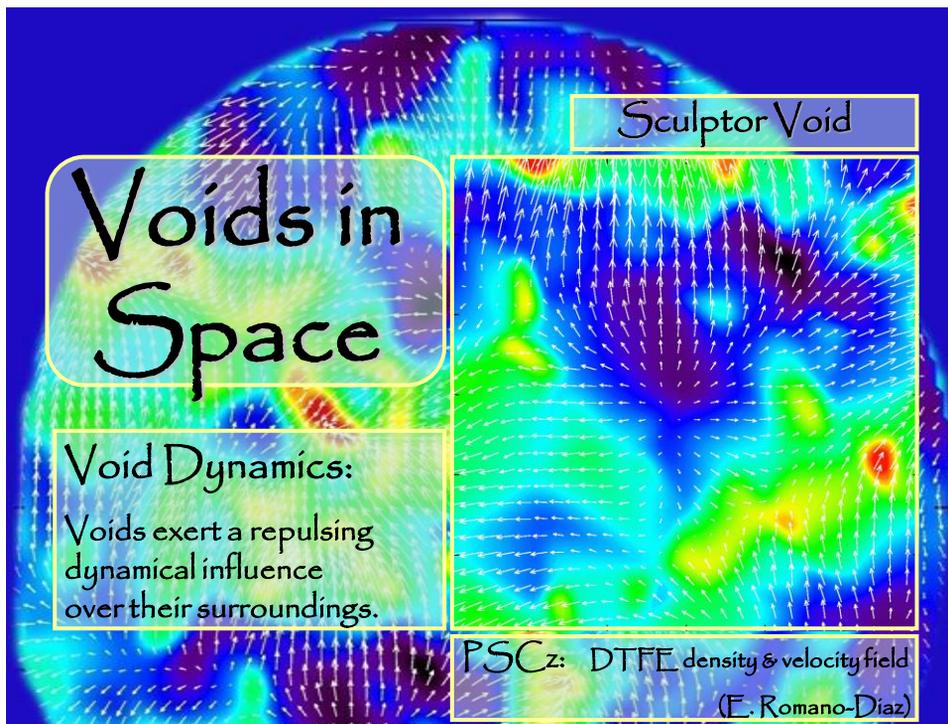
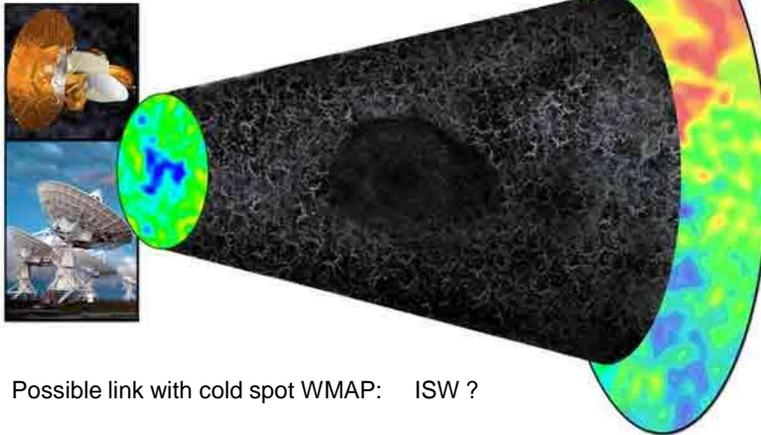
Comparison PSCz & models:

Plionis & Basilakos 2002

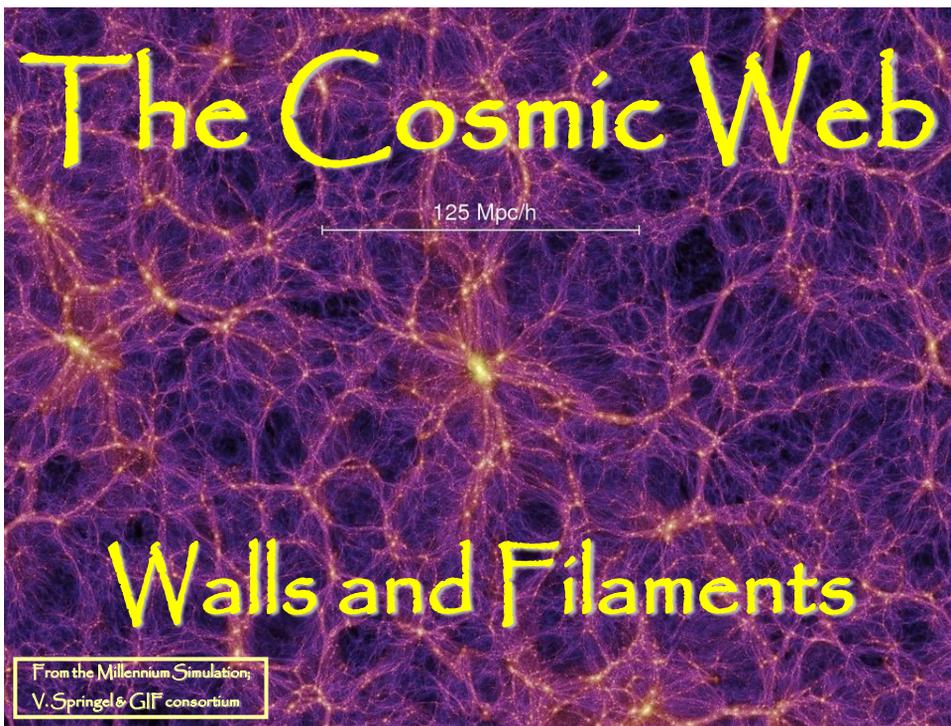


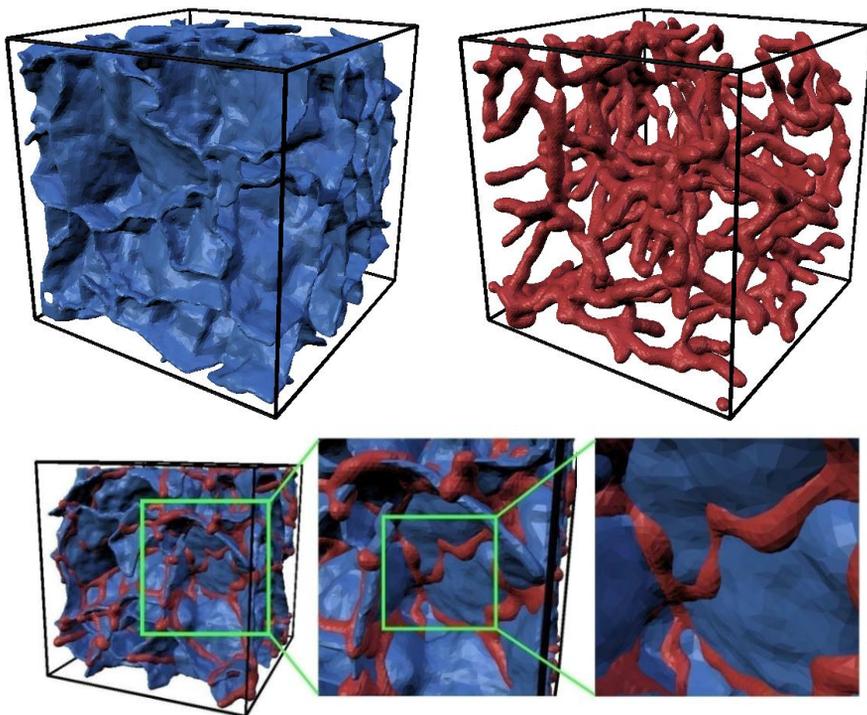
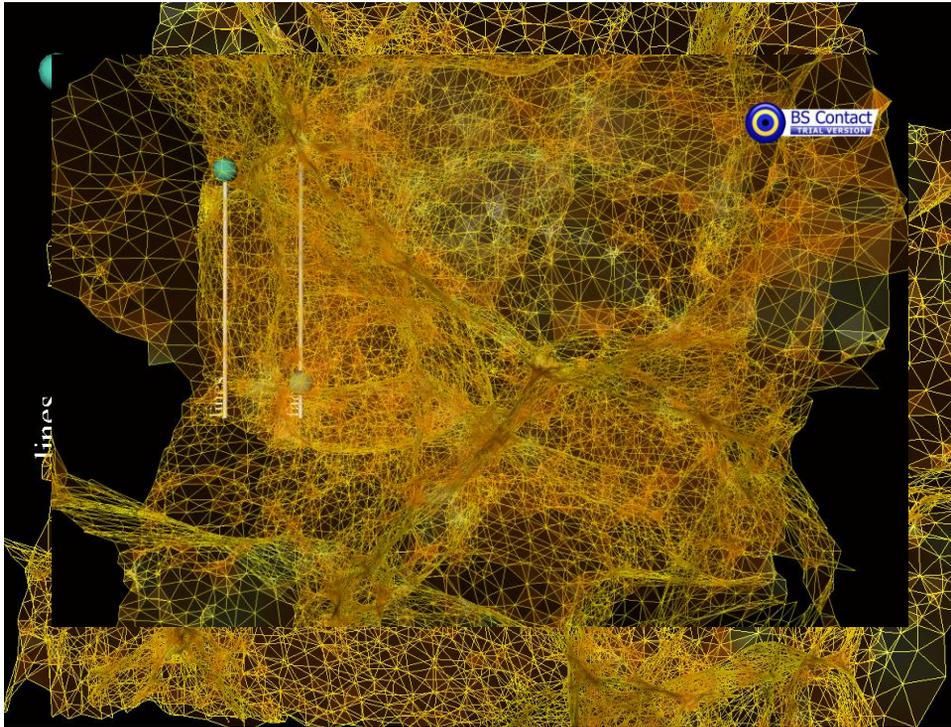
# Supervoids ???

Claim: supervoid in NVVS radio galaxy distribution  
(Rudnick et al. 2007)

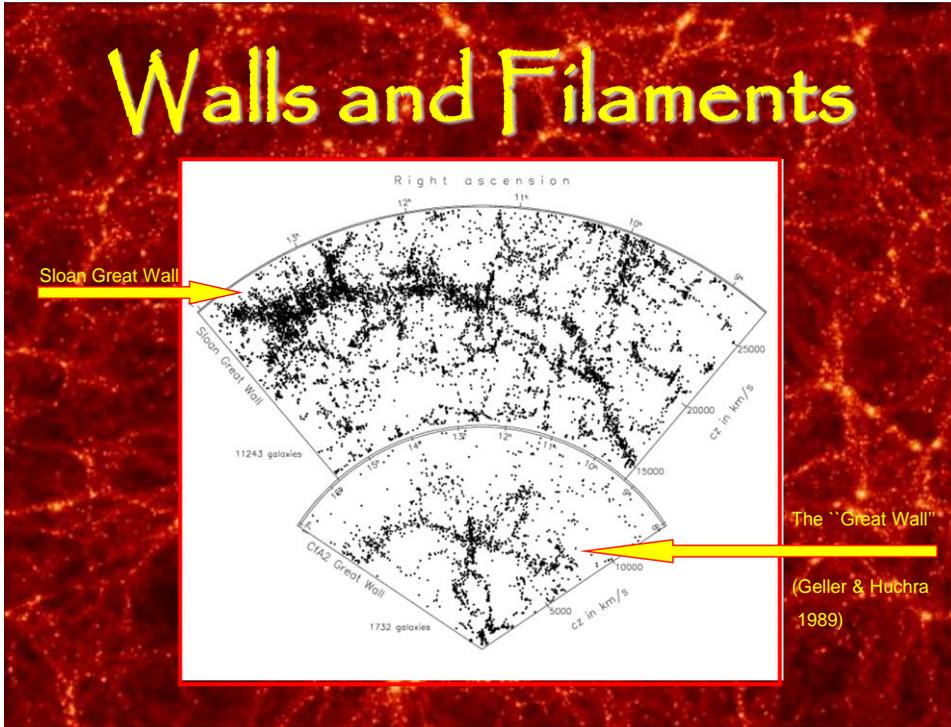


# Cosmic Web

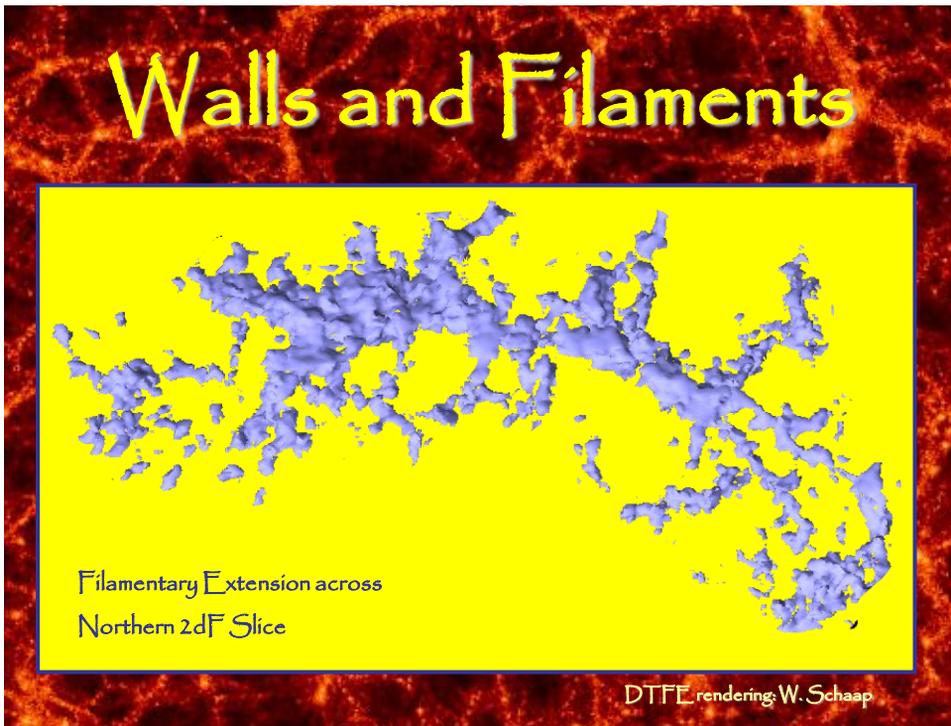




# Walls and Filaments



# Walls and Filaments



# Walls and Filaments

## Pisces-Perseus Supercluster

Canonic example of a strongly flattened supercluster consisting of

- sheet-like central region, dense filamentary boundary ridge
- Relative proximity ( $d \sim 55h^{-1}$  Mpc),
- Characteristic & salient filamentary morphology,
- Favourable orientation.

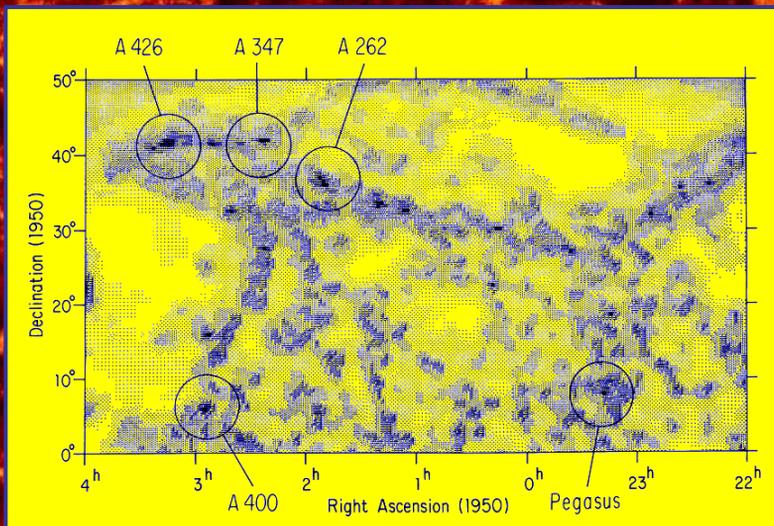
Northern boundary: ridge south-westward of Perseus cluster (A426)

Dimensions Ridge:  $5h^{-1}$  Mpc wide

$50h^{-1}$  Mpc length; possible  $140h^{-1}$  Mpc extension

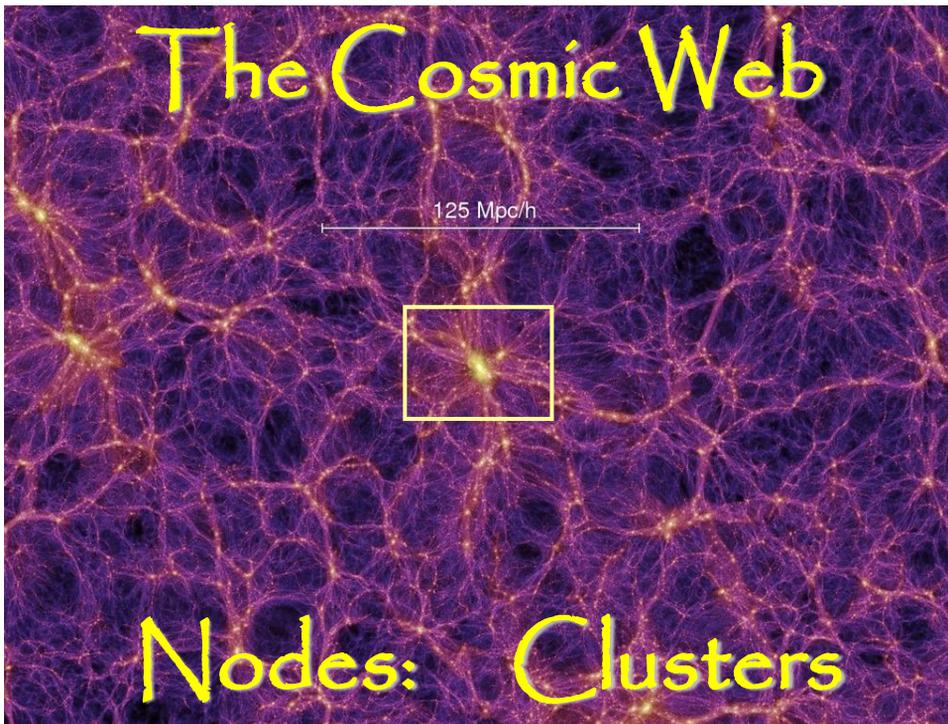
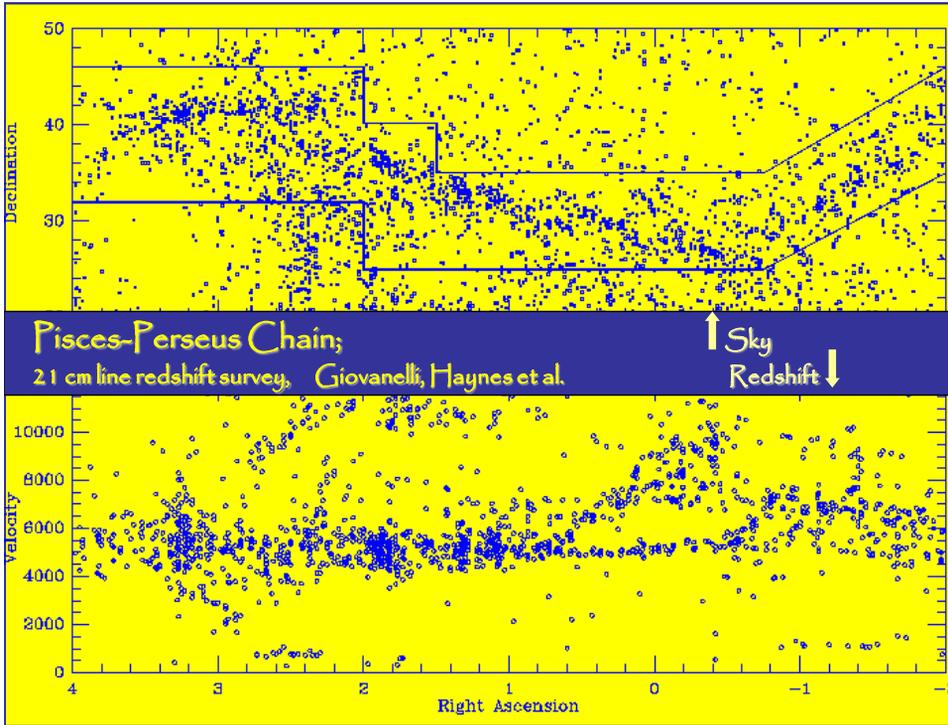
Along Ridge: high density clusters, incl. A462, A347, A262

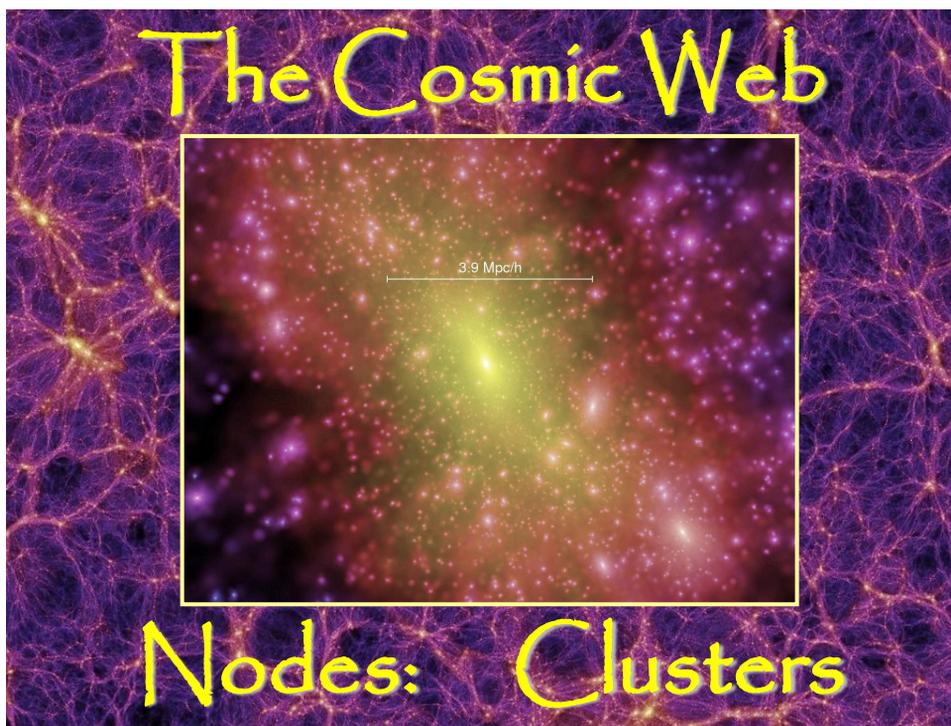
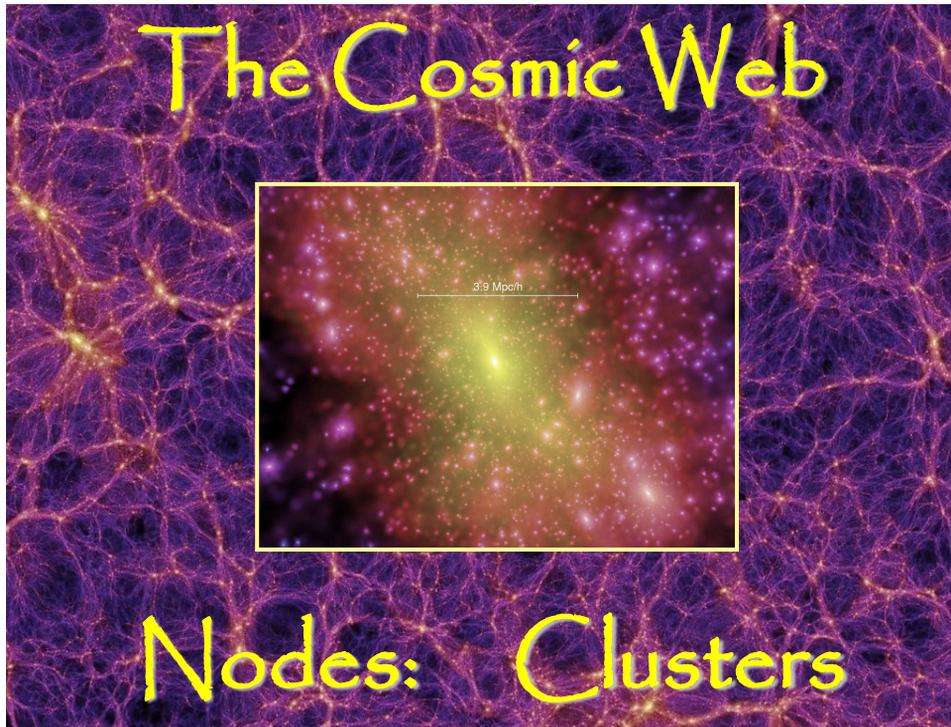
# Walls and Filaments

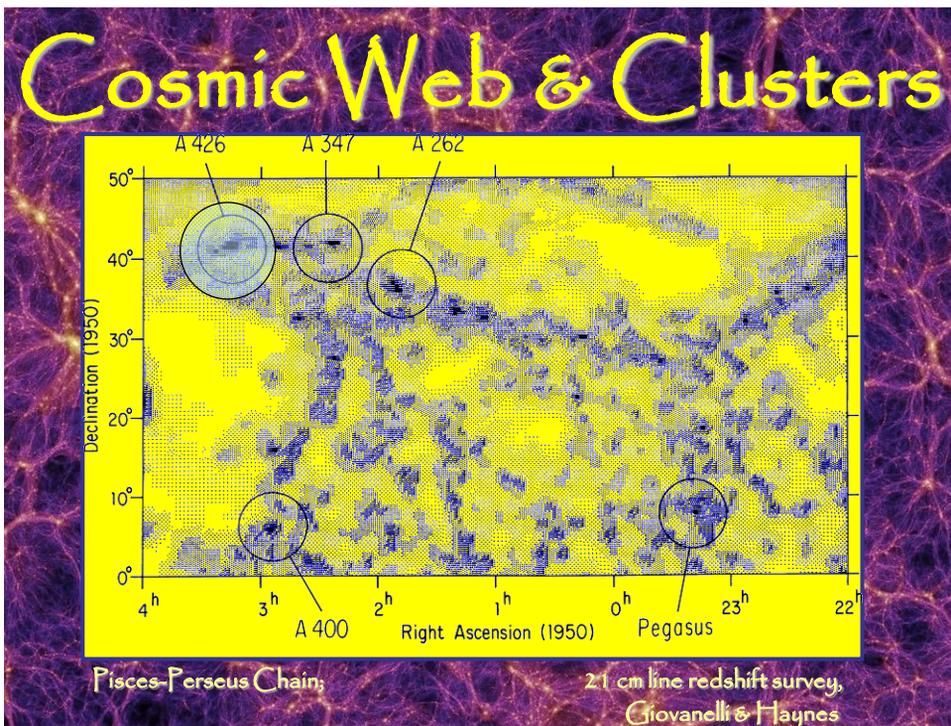
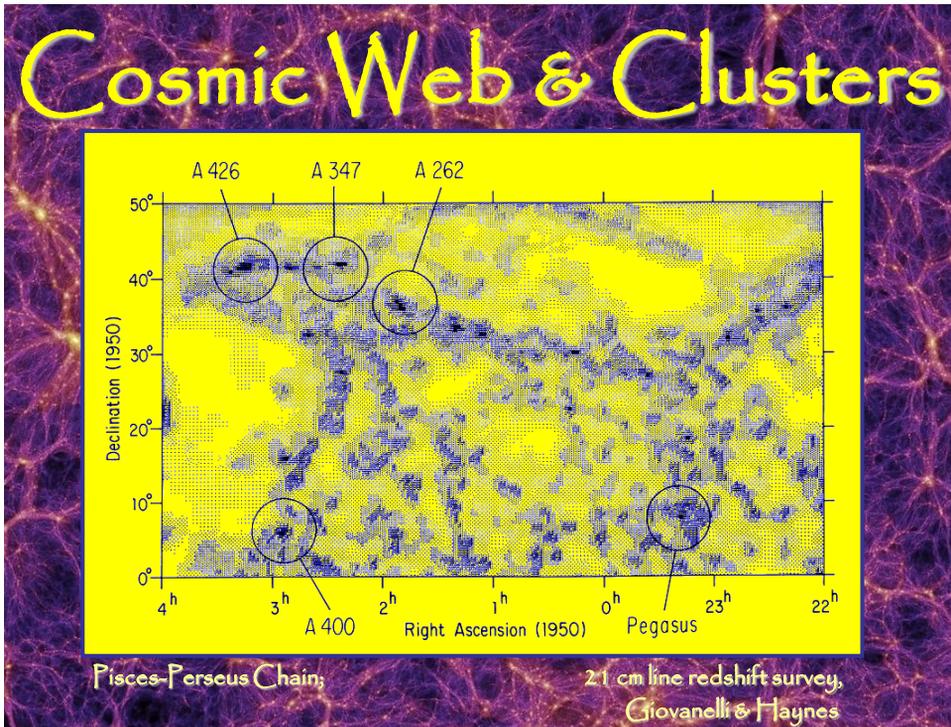


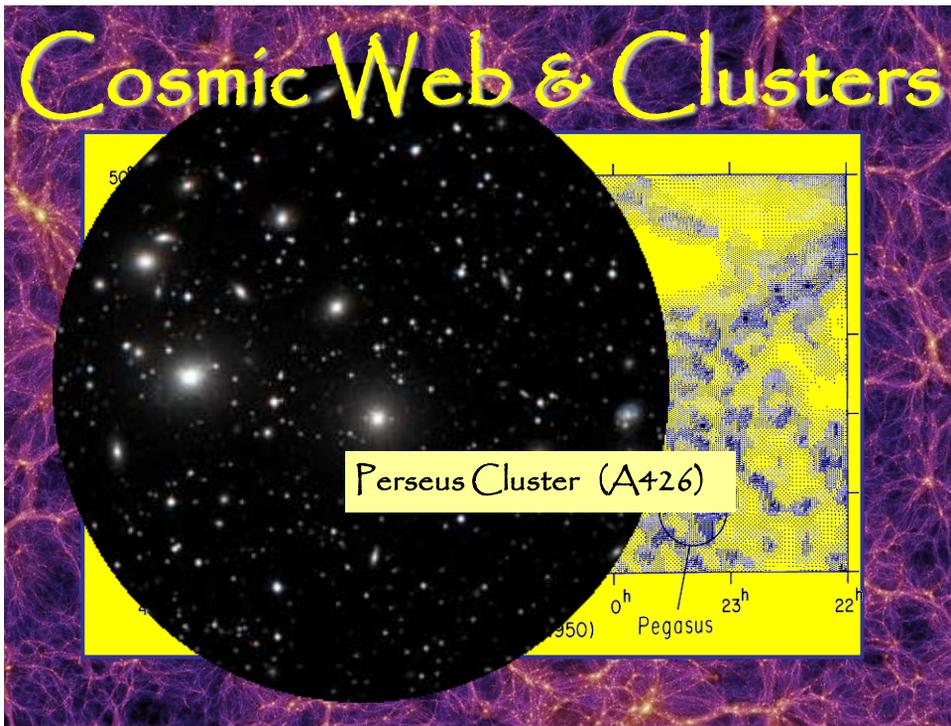
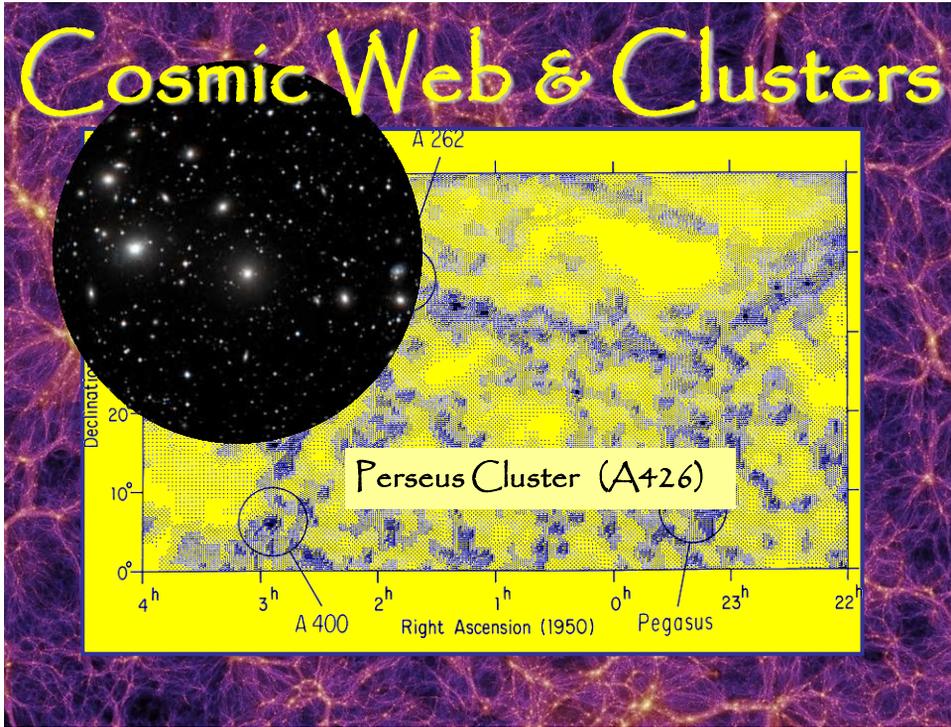
Pisces-Perseus Chain;

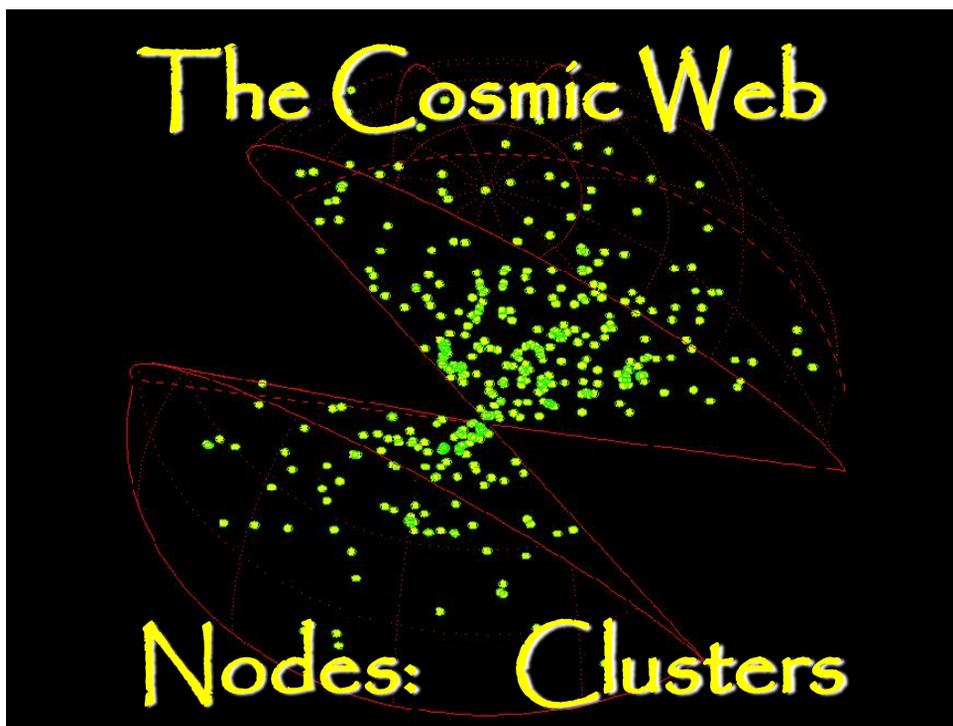
21 cm line redshift survey,  
Giovanelli & Haynes



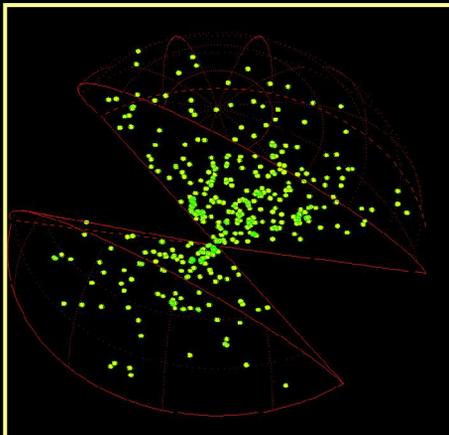








# The Cosmic Web



## The spatial cluster distribution.

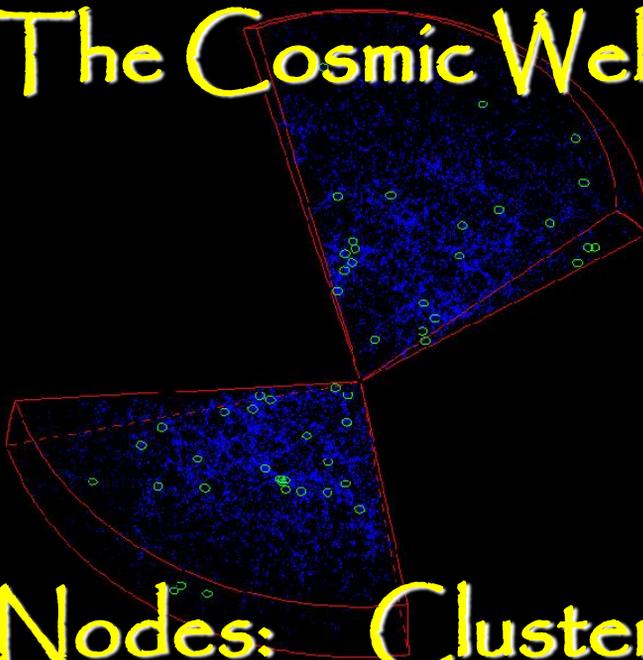
The full volume of the X-ray cluster REFLEX cluster survey within a distance of  $600h^{-1}$  Mpc. The REFLEX galaxy cluster catalogue contains all clusters brighter than an X-ray flux of  $3 \times 10^{-16}$  ergs  $\text{cm}^{-2}$  over a large part of the in the southern sky. The missing part of hemisphere delineates the region highly obscured by the Galaxy.

REFLEX: Boehringer et al. (2001)

Courtesy: Borgani & Guzzo (2001)

Nodes: Clusters

# The Cosmic Web



Nodes: Clusters

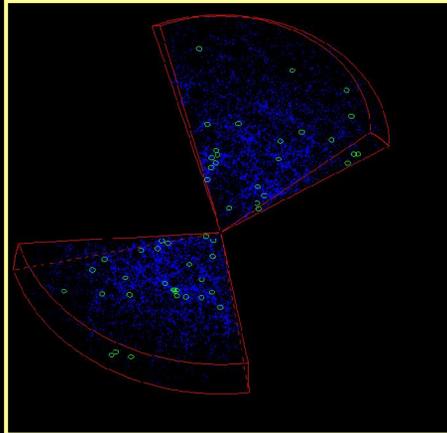
# The Cosmic Web

## The spatial cluster distribution and relation to Cosmic Web.

The green circles mark the positions of REFLEX X-ray clusters in the northern and southern slices of the Las Campanas redshift survey (LCRS, Shectman et al. 1996), out to a maximum distance of  $600h^{-1}$  Mpc. Underlying, in blue, the galaxies in the LCRS delineate a foaml like distribution of filaments, walls and voids.

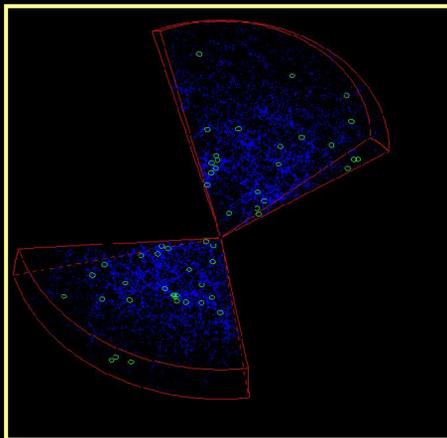
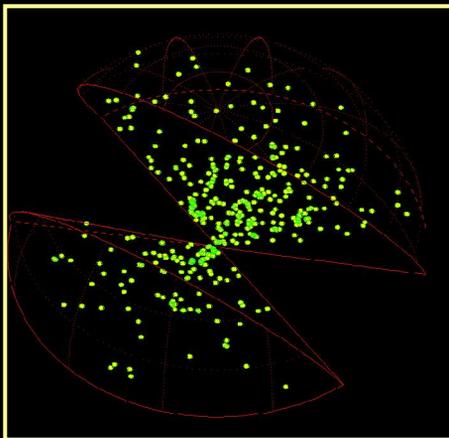
REFLEX: Boehringer et al. (2001)

Courtesy: Borgani & Guzzo (2001)

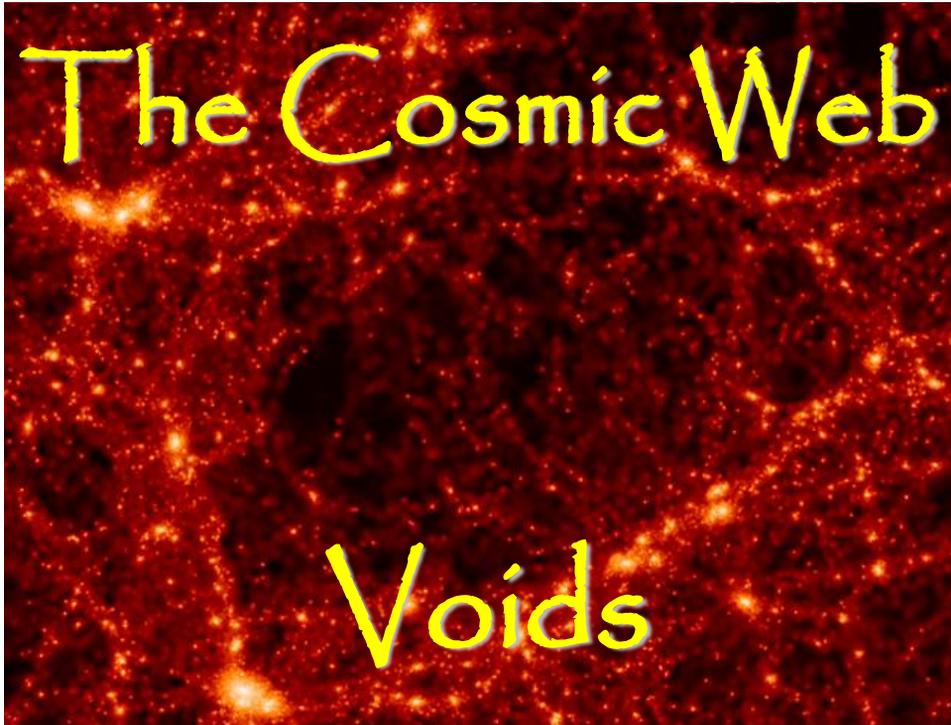


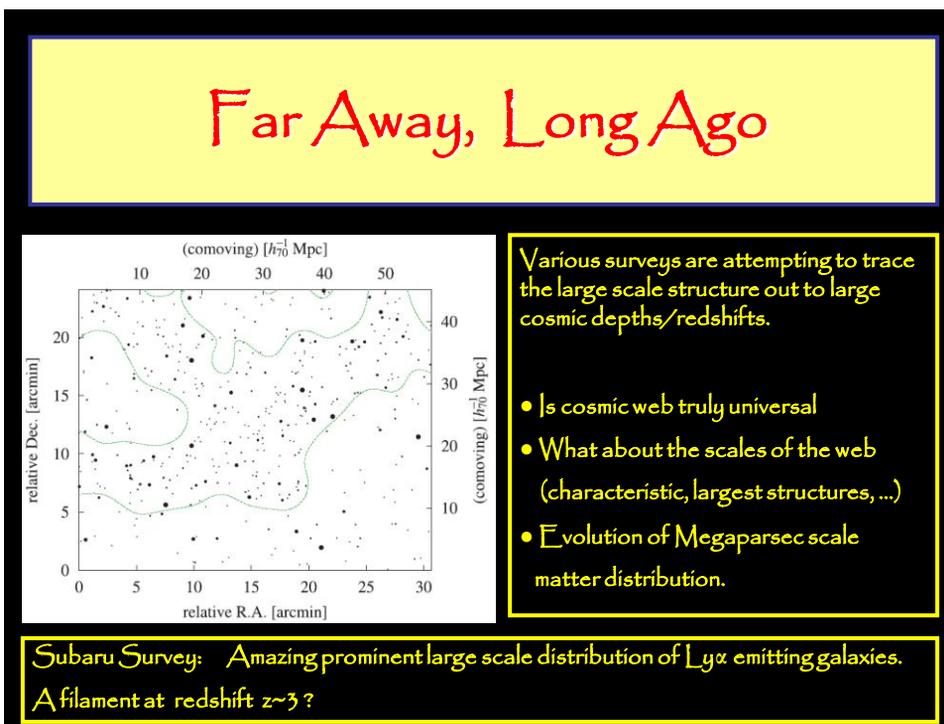
Nodes: Clusters

# The Cosmic Web

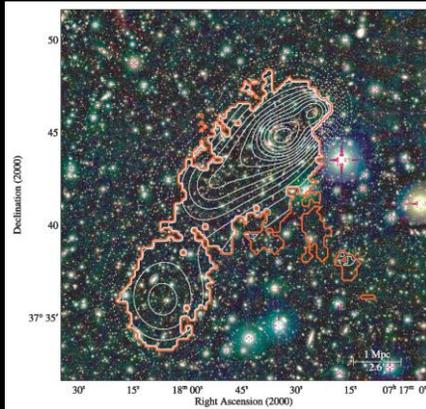


Nodes: Clusters





## Far Away, Long Ago



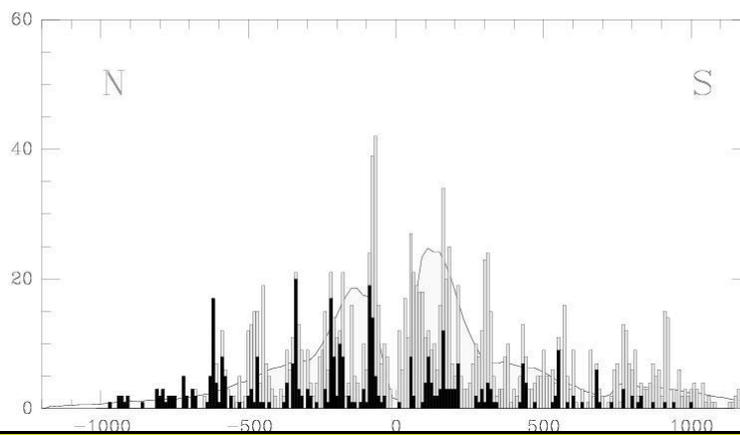
Various surveys are attempting to trace the large scale structure out to large cosmic depths/redshifts.

- Is cosmic web truly universal ?
- What about the scales of the web (characteristic, largest structures, ...)
- Evolution of Megaparsec scale matter distribution.

Ebeling et al. (2004):

A filamentary structure in between two rich clusters.

## Far Away, Long Ago

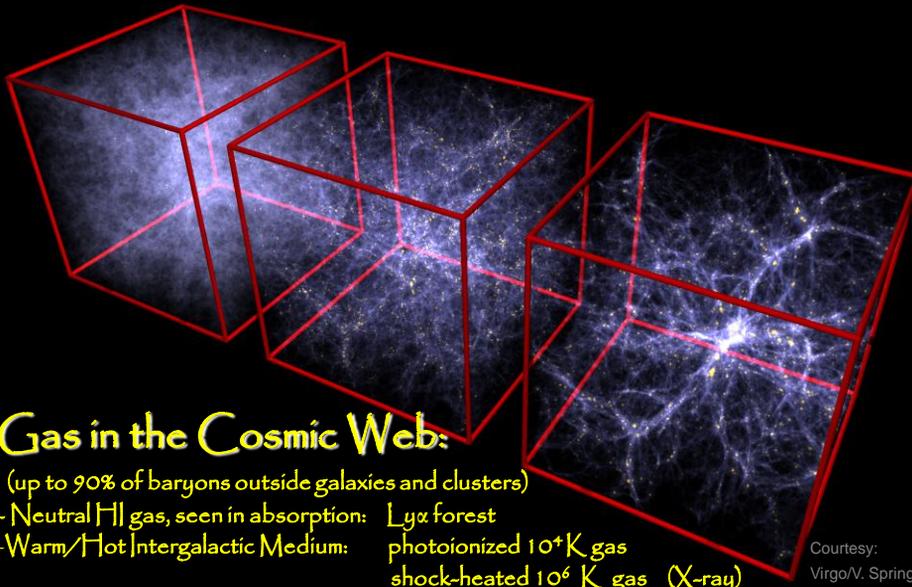


Deep pencil beam survey (Broadhurst et al):

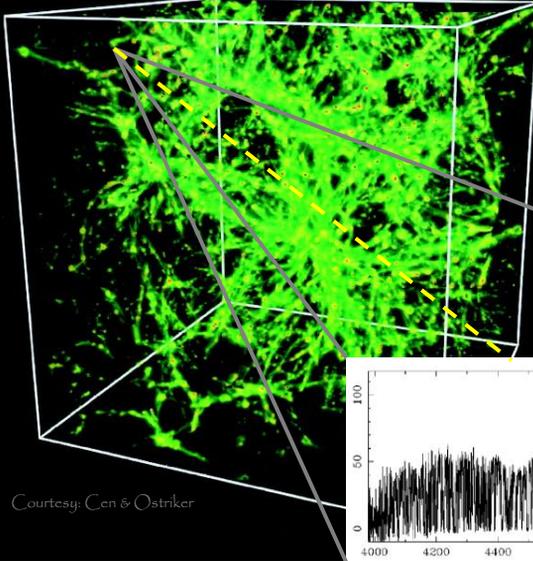
A semi-regular pattern of redshift spikes along line of sight, indicating the passage of l.o.s. through sheets, filaments and clusters. Suggestions for a characteristic scale of  $\sim 120h^{-1}$  Mpc should be ascribed to the 1-D character of the redshift skewer through 3-D structure.

# The Gastrophysical Web

## The Gastrophysical Web



# The Astrophysical Web



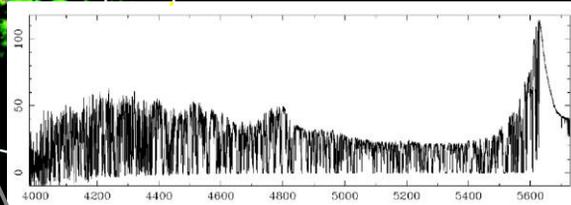
Courtesy: Cen & Ostriker

## The Ly $\alpha$ forest:

HI gas in the intergalactic medium closely traces the density fluctuations in the dark matter distribution.

QSO absorption lines arise due to the line of sight intersection by the neutral hydrogen component

Low column density absorption lines associated with sheets and filaments in the "Cosmic Web"



# Web Dynamics

# Cosmic Migration Flows

CMB Dipole:

We move wrt Universe:  $v \sim 620$  km/s

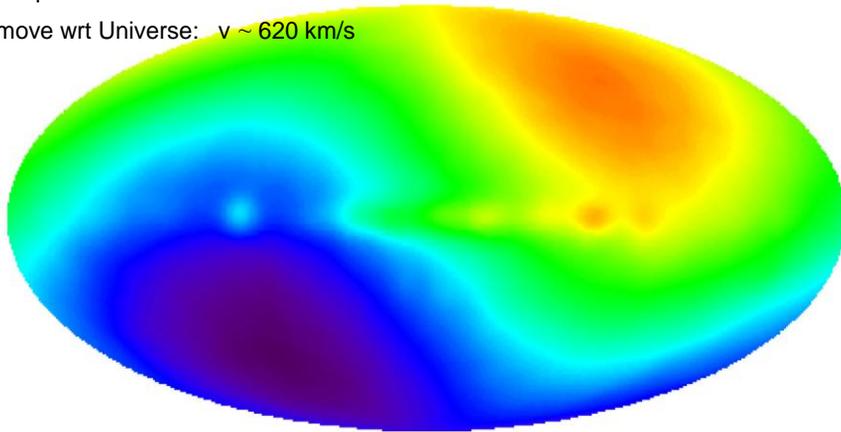
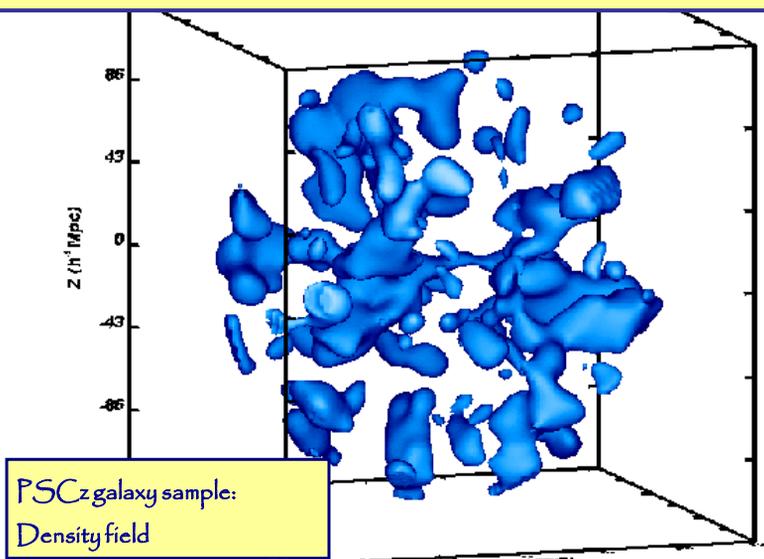


Figure 11. The Cosmic Microwave Background dipole as measured by the DMR instrument of the COBE microwave background satellite (see also Kogut et al. 1993)

# Cosmic Migration Flows



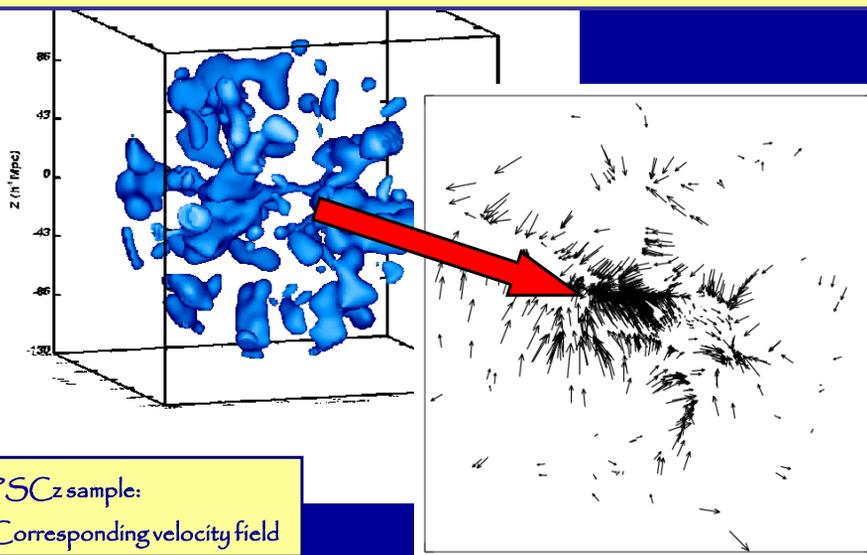
# Cosmic Migration Flows

$$\mathbf{v} = \frac{H f}{4\pi G \rho_u} \mathbf{g} = \frac{2 f}{3H\Omega} \mathbf{g}$$

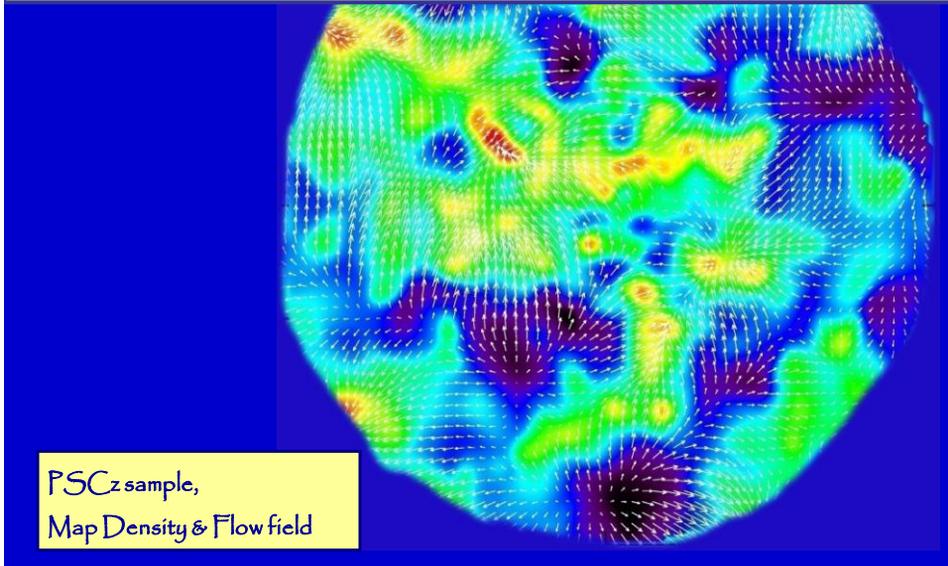


$$\mathbf{v}(\mathbf{x}, t) = \frac{H}{4\pi} \frac{f(\Omega_m)}{b} a \int d\mathbf{x}' \delta_{gal}(\mathbf{x}', t) \frac{(\mathbf{x}' - \mathbf{x})}{|\mathbf{x}' - \mathbf{x}|^3} \quad (158)$$

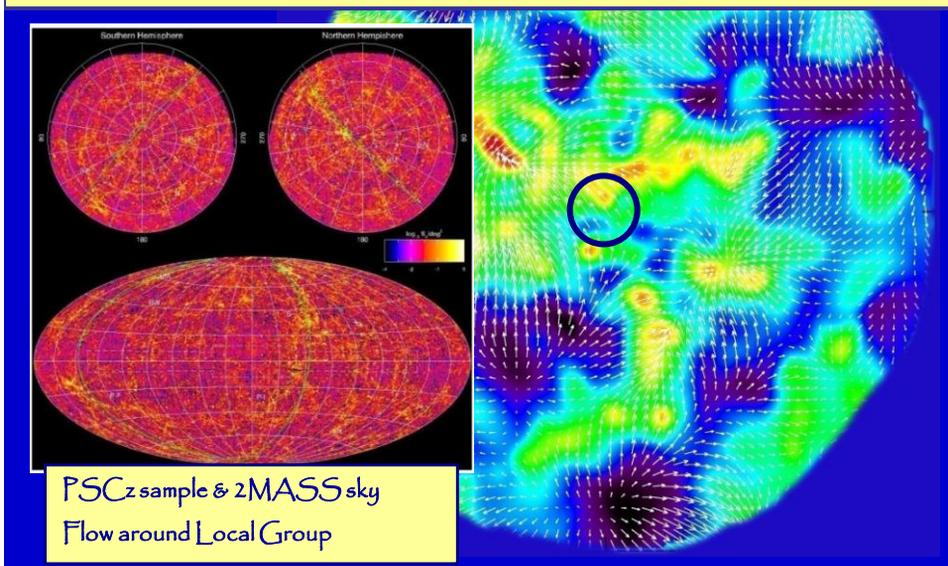
# Cosmic Migration Flows



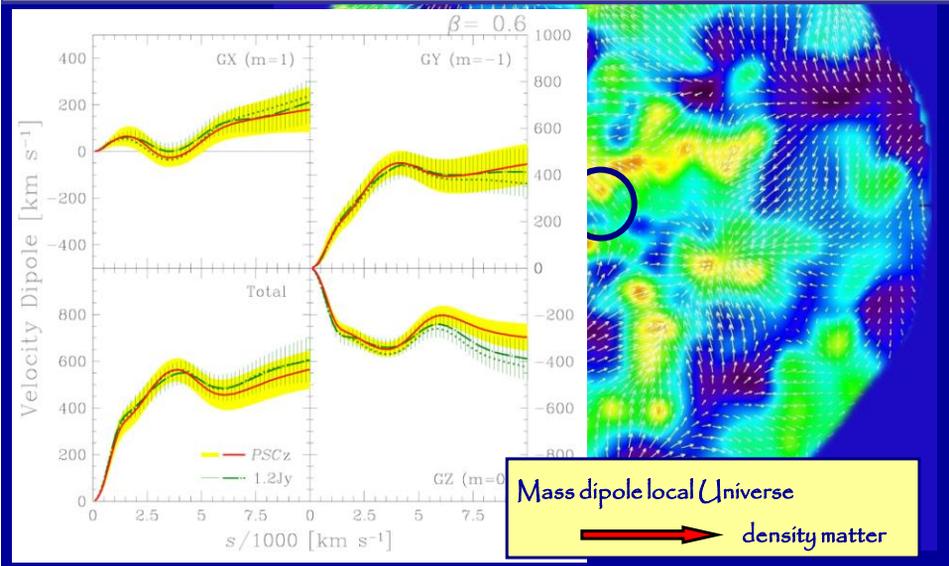
# Cosmic Migration Flows



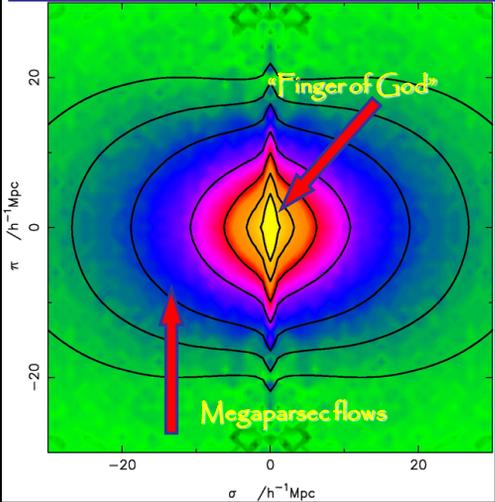
# Cosmic Migration Flows



# Cosmic Migration Flows



# the Web: Migration Flows



Large scale flows lead to redshift distortions:

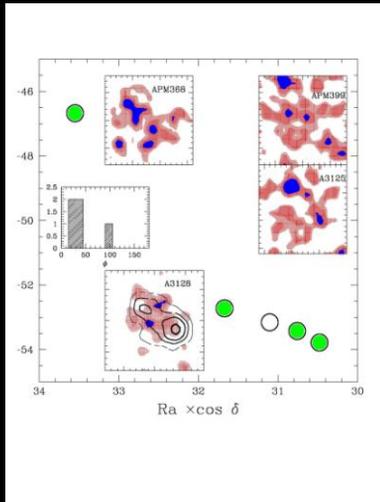
$$cz = Hr + v_{pec}$$

These flows are part of the assembly of large scale structures, and reach largest values as matter is transported along the filaments into the clusters.

When mapping the galaxy distribution in redshift space, this induces a distortion:

- Flattening along  $z$  as matter flows into Megaparsec features ( $v < 600 \text{ km/s}$ ).
- Extension due to thermal motions inside cluster ( $v \sim 1000 \text{ km/s}$ ): "Fingers of God"

## Web Dynamics: Alignments



Plionis 2005

Of utmost importance for understanding the dynamical origin of the cosmic web is that of alignments between and around clusters of galaxies.

The presence of such alignments is an indication for the tidal origin of the cosmic web with the clusters as the dominant tidal agents.

This forms an essential ingredient of the "Cosmic Web" theory of Bond et al.

Work by various groups, most notably Plionis and collaborators, indicate that indeed clusters, and galaxies around them, reveal significant alignments.

## Cosmic Shear & Gravitational Lensing

# Gravitational Lensing

A highly promising method to determine the amount and distribution of matter in the Universe does not concentrate on the way in which Dark Matter affects

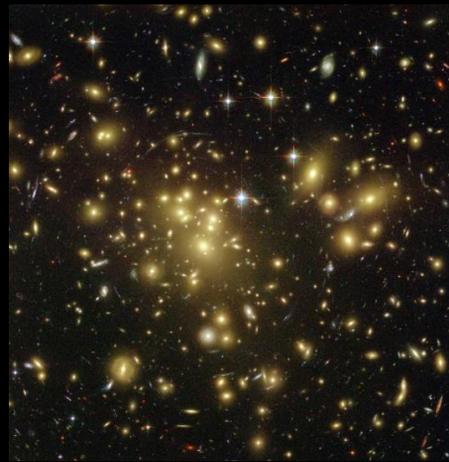
- the motions of galaxies and the intracluster gas,

but instead looks at the way it affects

- the trajectories of photons.

According to Einstein's theory of general relativity, gravitational potential wells will bend and focus light. Dark matter concentrations will therefore act

Gravitational Lens



A1689, HST, Broadhurst et al.

# Gravitational Lensing

Illustration:

Mass passing in front of background of galaxies, distorting their received images.

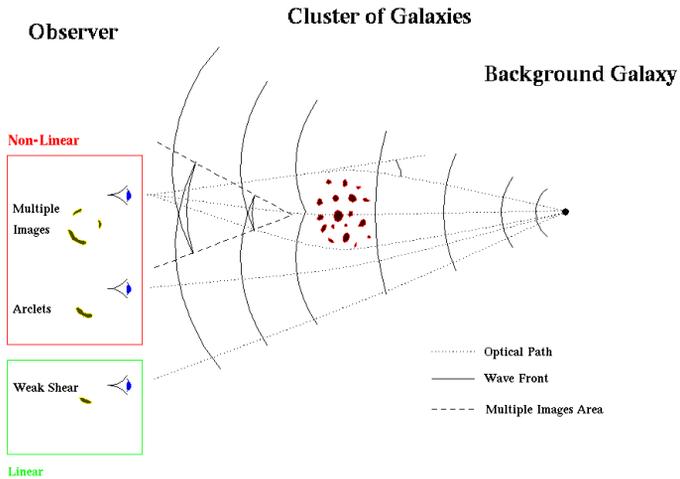


# Clusters: Gravitational Lensing

Illustration:

Dependent on whether the light passes within Einstein radius or outside, we deal with:

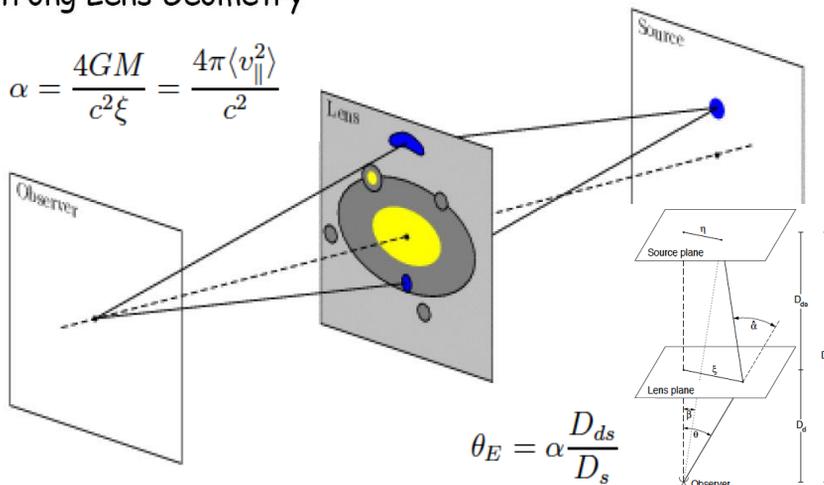
- **Strong Lensing:**  
nonlinear distortions
- **Weak Lensing:**  
linear distortions



## Gravitational Strong Lensing

Strong Lens Geometry

$$\alpha = \frac{4GM}{c^2\xi} = \frac{4\pi\langle v_{\parallel}^2 \rangle}{c^2}$$



# Clusters: Gravitational Lensing



Strong Lensing Arcs:

Abell 2218

$z=0.175$

Galaxy Cluster Abell 2218

HST • WFPC2

NASA, A. Fruchter and the ERO Team (STScI) • STScI-PRC00-08

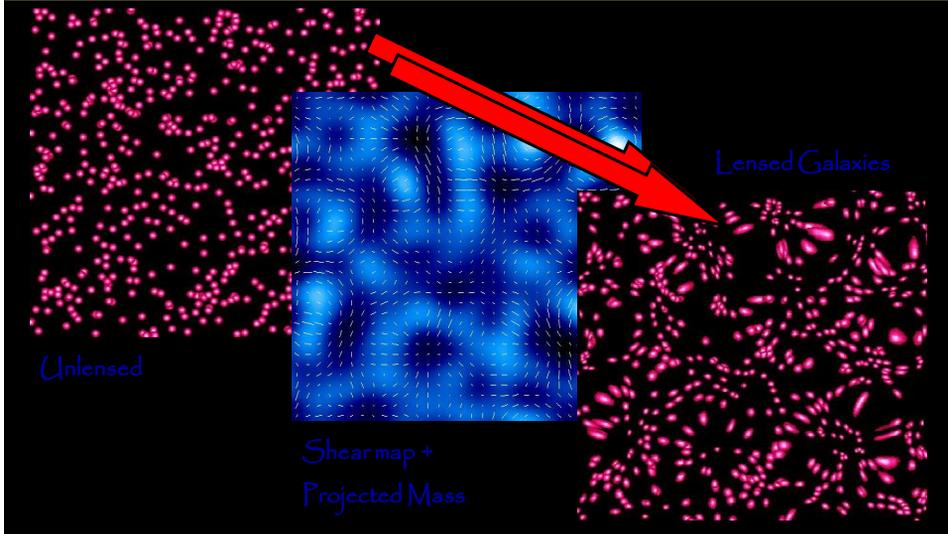
# Clusters: Gravitational Weak Lensing

Weak Lensing:

MS1054

- $z=0.83$  one of the highest  $z$  clusters
- Weak Lensing study by
  - Clowe et al. Keck
  - Hoekstra et al. HST

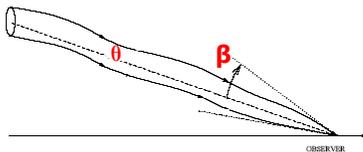
# Gravitational Weak Lensing



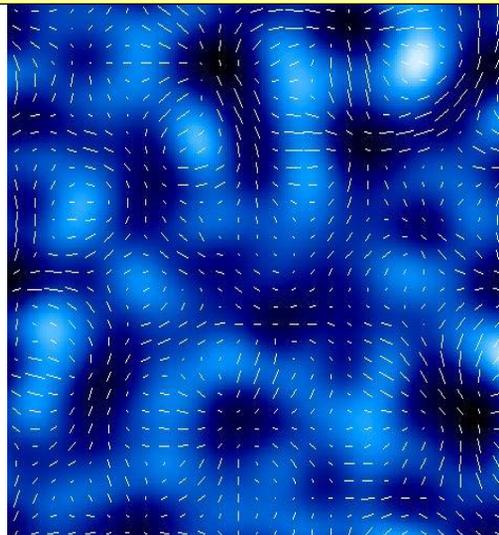
# Gravitational Lensing

$$A_{ij} \equiv \frac{\partial \beta_i}{\partial \theta_j} = \begin{pmatrix} 1 - \kappa & 0 \\ 0 & 1 - \kappa \end{pmatrix} + \begin{pmatrix} -\gamma_1 & \gamma_2 \\ \gamma_2 & \gamma_1 \end{pmatrix}$$

Magnification                  Shear



$$\begin{aligned} \kappa &= \frac{1}{2} (\phi_{,11} + \phi_{,22}) \\ \gamma_1 &= \frac{1}{2} (\phi_{,11} - \phi_{,22}) \\ \gamma_2 &= \phi_{,12} \\ \phi_{,ij} &= \frac{\partial^2 \phi}{\partial \theta_i \partial \theta_j} \end{aligned}$$



# Gravitational Lensing

$$\kappa = \frac{1}{2}(\phi_{,11} + \phi_{,22})$$

$$\gamma_1 = \frac{1}{2}(\phi_{,11} - \phi_{,22})$$

$$\gamma_2 = \phi_{,12}$$

$$\phi_{,ij} = \frac{\partial^2 \phi}{\partial \theta_i \partial \theta_j}$$

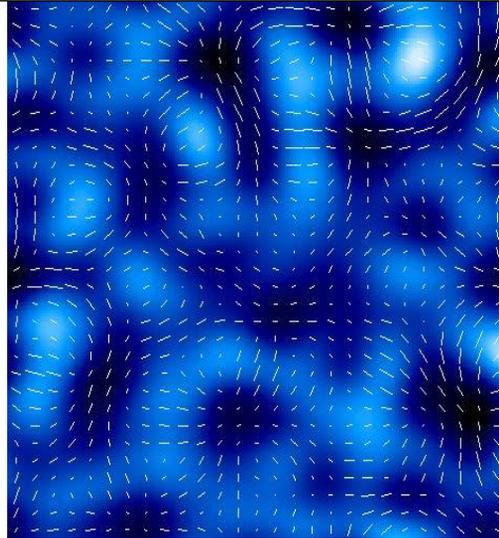


Lensing Potential

related to

Peculiar Gravitational Potential

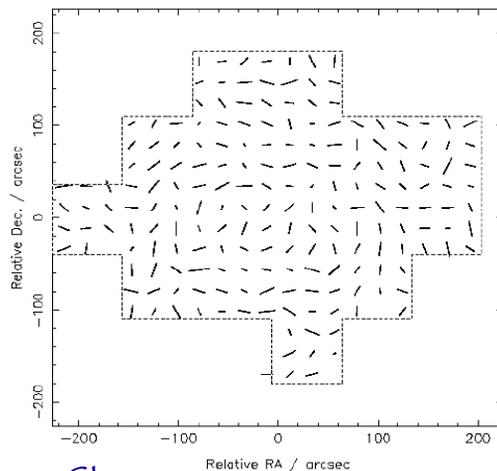
$$\phi(\mathbf{r}) = \frac{2}{c^2} \int_0^r dr' \Phi(r') \left( \frac{1}{r} - \frac{1}{r'} \right)$$



# Clusters: Gravitational Lensing

MS1054

- $z=0.83$  one of the highest  $z$  clusters
- Studied by
  - Clowe et al. Keck
  - Hoekstra et al. HST

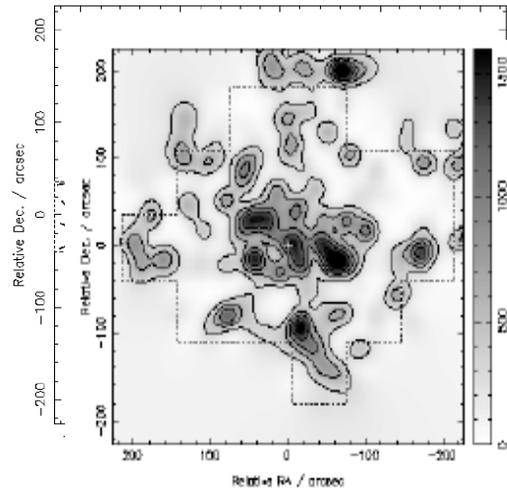


Shear map

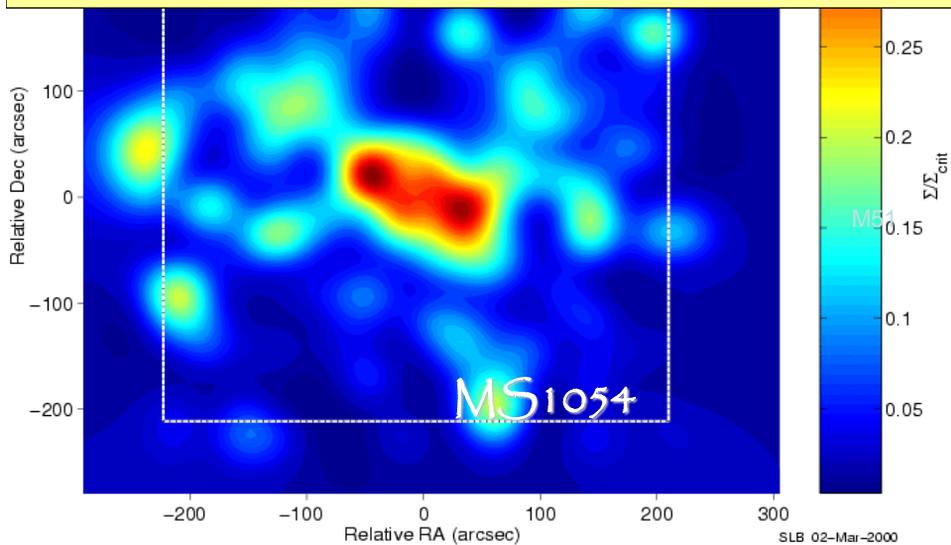
# Clusters: Gravitational Lensing

## MS1054

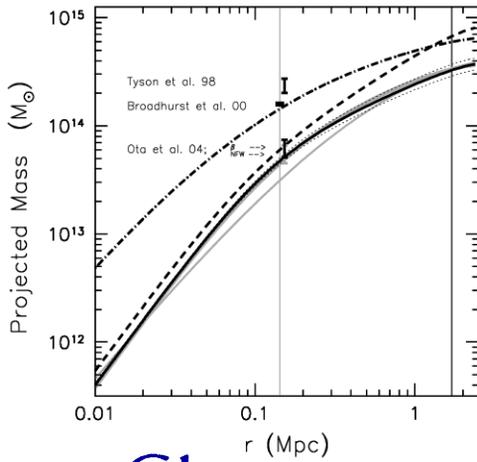
- $z=0.83$  one of the highest  $z$  clusters
- Studied by
  - Clowe et al. Keck
  - Hoekstra et al. HST



# Clusters: Gravitational Lensing

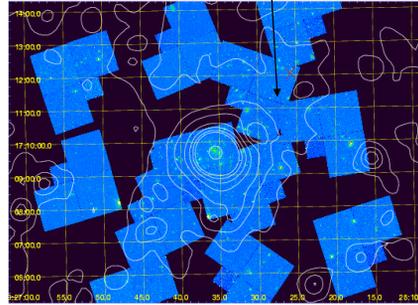


# Clusters: Comparison Lensing & X-ray



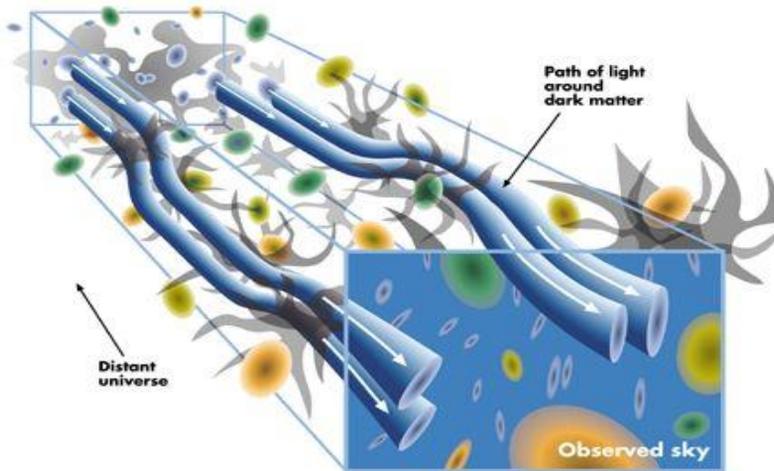
CL0024+17

Same substructure seen in  
weak lensing and X-rays

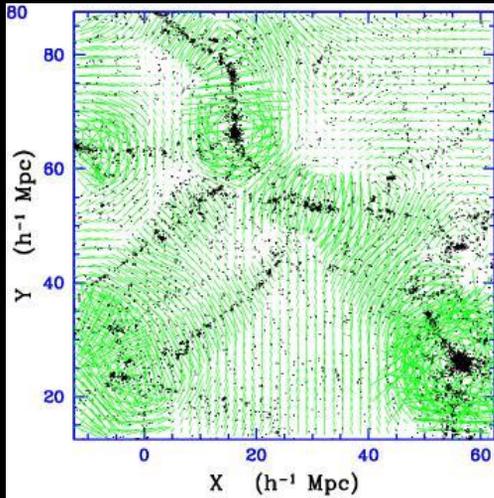


X-ray overlay on HST image

# Cosmic Shear



## the Web: Shear Distortions & Lensing



Large scale tidal shear distorts the paths of photons as they travel from their source to the observer.

This effect is known as "gravitational lensing". For moderate distortions, outside the Einstein radius ("weak lensing"),

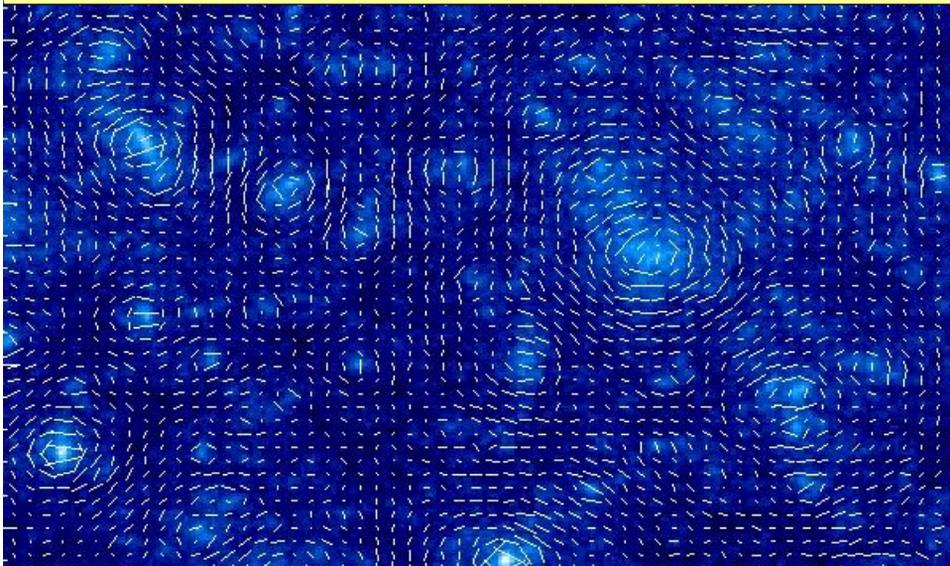
the distortions of galaxy shapes can be measured and inverted to yield the (projected) distorting mass distribution.

Clusters are outstanding, representing major potential wells.

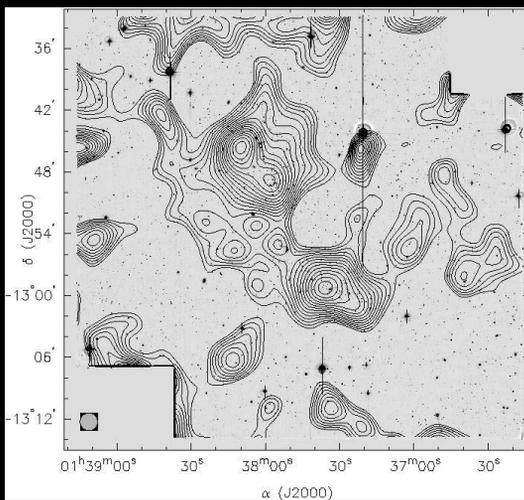
But also the generic Megaparsec matter distribution "lenses":

Cosmic Shear

## Cosmic Shear



## the Web: Shear Distortions & Lensing



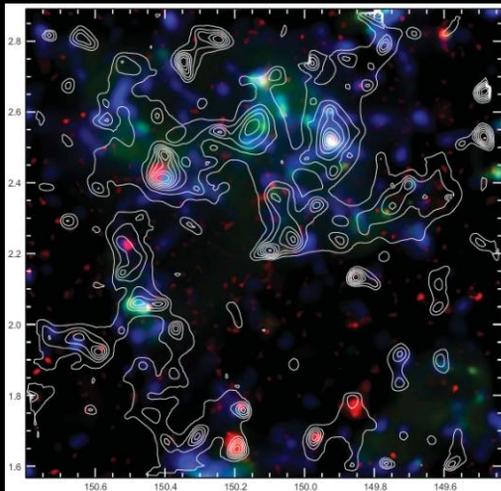
Although the cosmic shear due to a filament is considerably weaker than that of the clusters, recently

Dietrich, Schneider & Romano-Díaz (2004)

succeeded in mapping the filament between A222 and A333 on the basis of the measured lensing.

This shows that filaments are shown to be genuine dynamical entities.

## the Web: Shear Distortions & Lensing



First genuine map

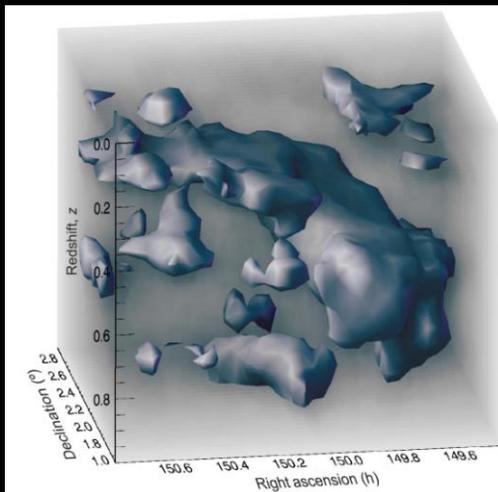
Large Scale

Cosmic Dark Matter distribution  
by means of weak lensing:

Clearly visible is the filamentary  
Weblike nature of the mass  
Distribution.

Massey et al. 2007

# the Web: Shear Distortions & Lensing



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