

Probes Dark Energy

- **Supernovae Ia**
probing luminosity distance – redshift relation
- **Clusters of Galaxies**
number counts $N(z)$,
formed clusters of galaxies as function of z sensitive to w & w'
- **Cosmic Shear/Weak Lensing**
measures angular diameter distance-redshift relation, in combination with structure growth
- **Baryonic Oscillations (BAO)**
cosmic yardstick, curvature: residual imprint in galaxy distribution
acoustic oscillations primordial baryon-photon plasma
- **Integrated Sachs Wolfe (ISW)**
imprint foreground large scale structure on CMB,
via evolving potential perturbations
- **Clustering**
clustering correlation function/power spectrum,
directly probing cosmological scenario, BAO wiggles
- **Growth of clustering:**
evolving growth rate $f(\Omega_m, z)$, probed via influence of
redshift distortions on correlation functions
- **Voids:**
evolving void shapes,
probing tidal force field generated by large scale mass distribution
- **Morphology and Topology**
sensitivity of topology, measured by homology (Betti numbers)

Dark Energy Probes: Comparison

Method	Strengths	Weaknesses	Systematics
Weak Lensing	Structure Growth + Geometric Statistical Power	CDM assumption	Image quality Photo-z
Supernovae SNIa	Purely Geometric Mature	Standard Candle assumption	Evolution Dust
BAO (Baryonic Acoustic Oscillation)	Largely Geometric Low systematics	Large samples required	Bias Nonlinearity
Cluster Population N(z)	Structure Growth + Geometric Xray+SZ+optical	CDM assumption	Determining mass Selection function

Standard Candle & Cosmic Distances

Robertson-Walker Metric

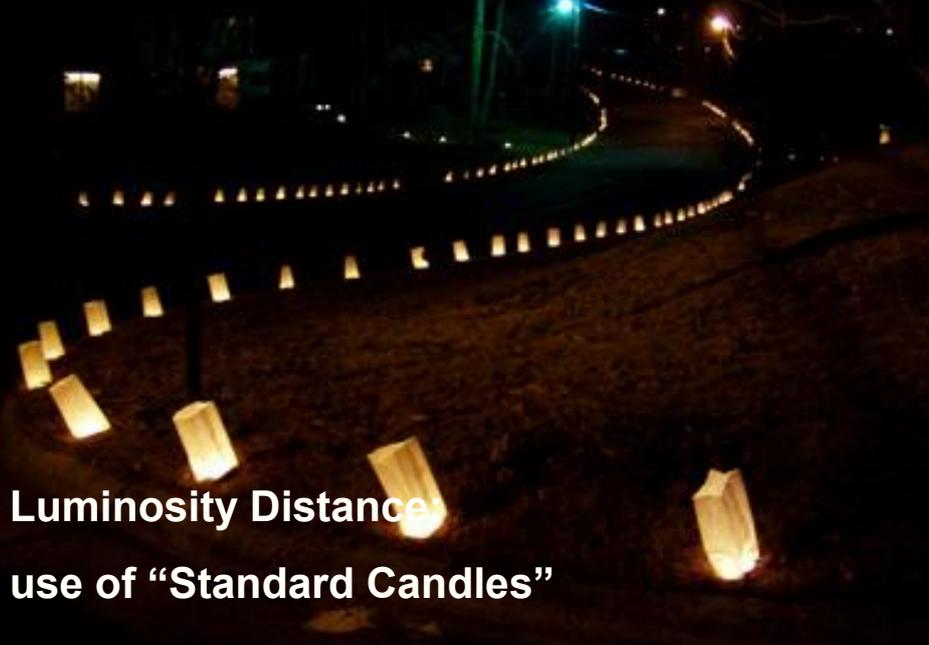
Distances in a uniformly curved spacetime is specified in terms of the Robertson-Walker metric. The spacetime distance of a point at coordinate (r, θ, ϕ) is:

$$ds^2 = c^2 dt^2 - a(t)^2 \left\{ dr^2 + R_c^2 S_k^2 \left(\frac{r}{R_c} \right) \left[d\theta^2 + \sin^2 \theta d\phi^2 \right] \right\}$$

where the function $S_k(r/R_c)$ specifies the effect of curvature on the distances between points in spacetime

$$S_k \left(\frac{r}{R_c} \right) = \begin{cases} \sin \left(\frac{r}{R_c} \right) & k = +1 \\ \frac{r}{R_c} & k = 0 \\ \sinh \left(\frac{r}{R_c} \right) & k = -1 \end{cases}$$

Cosmic Distance Measurements





Luminosity Distance

Definition cosmological luminosity distance:

$$l = \frac{L}{4\pi D_L^2}$$

for a source with INTRINSIC luminosity L
OBSERVED brightness l

In a Robertson-Walker geometry, luminosity distance is

$$D_L = (1+z)D(z)$$

where $D(z)$ is the cosmological distance measure

Luminosity Distance

Cosmological distance measure:

$$D(z) = R_0 S_k \left(\frac{r}{R_0} \right)$$

with curvature term $S_k(x) = \sin(x)$, x , or $\sinh(x)$

$$r(z) = \frac{c}{H_0} \int_0^z dz' \left[\sum_i \Omega_i (1+z')^{3+3w_i} - \frac{kc}{H_0 R_0} (1+z')^2 \right]^{-1/2}$$

Comoving radial distance $r(z)$ at redshift z

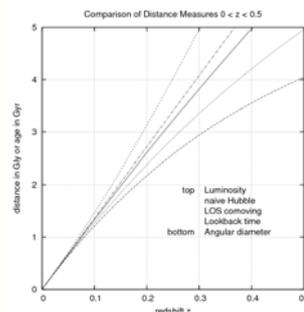
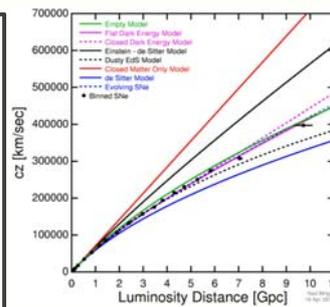
Luminosity Distance

Luminosity Distance at low redshift:

$$D_L = \frac{c}{H_0} \left\{ z + z^2 \left(\frac{1-q_0}{2} \right) + O(z^3) \right\}$$

- with first term the linear Hubble expansion term
- second term the first acceleration/deceleration term:

$$q = \frac{1}{2} \sum_i \Omega_i (1+3w_i)$$



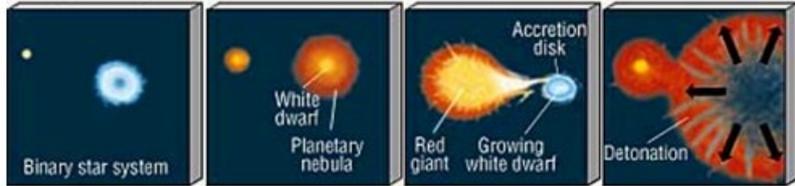
Type Ia Supernovae

Supernova Explosion & Host Galaxy

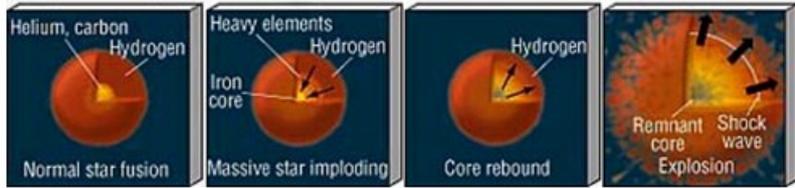


Supernovae

(a) Type- I Supernova



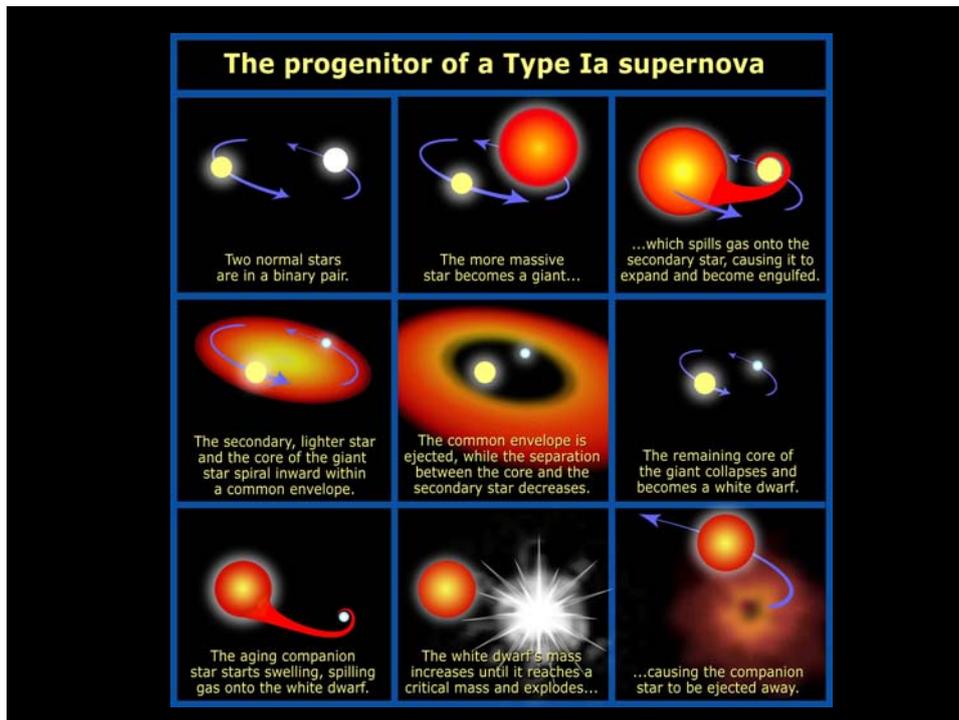
(b) Type- II Supernova



- | | |
|---|---|
| <p>Supernovae:</p> <ul style="list-style-type: none"> • gigantic stellar explosions • within few months more radiation than Sun over entire lifetime • shockwaves 5,000-30,000 km/s • enrichment interstellar medium • triggers star formation in surrounding ISM | <p>Supernovae, 4 types (spectral absorption lines):</p> <ul style="list-style-type: none"> • SN II • SN Ia - no hydrogen • SN Ib • SN Ic - no helium |
|---|---|

Type Ia Supernova Explosion



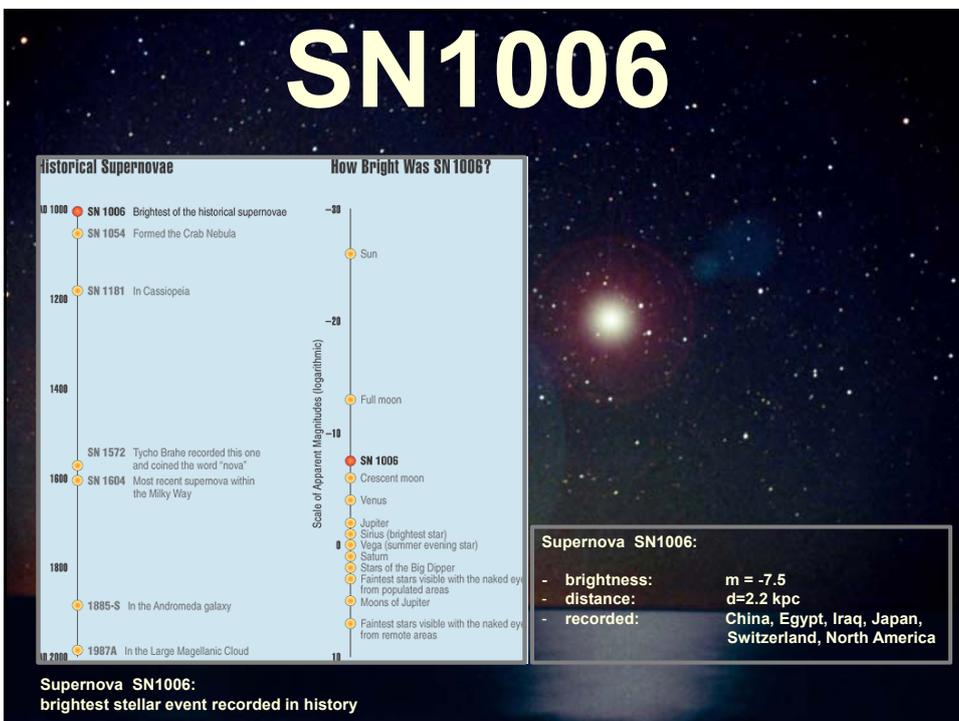


Type Ia Supernova

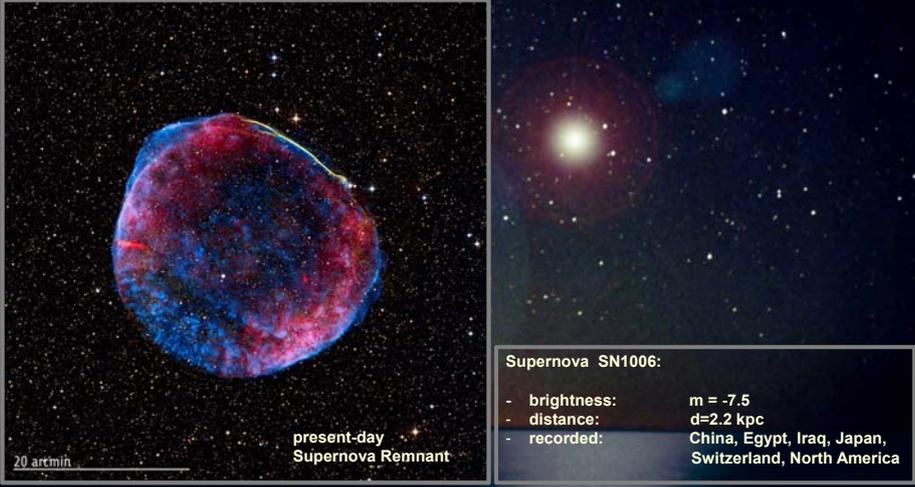
- Amongst the most energetic explosions in our Universe:
 $E \sim 10^{54}$ ergs
- During explosion the star is as bright as entire galaxy ! (ie. 10^{11} stars)

- Violent explosion Carbon-Oxygen white dwarfs:
- Embedded in binary, mass accretion from companion star
- When nearing Chandrasekhar Limit ($1.38 M_{\odot}$), electron degeneracy pressure can no longer sustain star.
- while contracting under its weight, carbon fusion sets in, powering a catastrophic deflagration or detonation wave,
- leading to a violent explosion, ripping apart entire star

- Because exploding stars have nearly uniform progenitor ($\sim 1.38 M_{\odot}$ white dwarf), their luminosity is almost the same: $M \sim -19.3$
 Standard Candle



SN1006



20 arcmin

present-day
Supernova Remnant

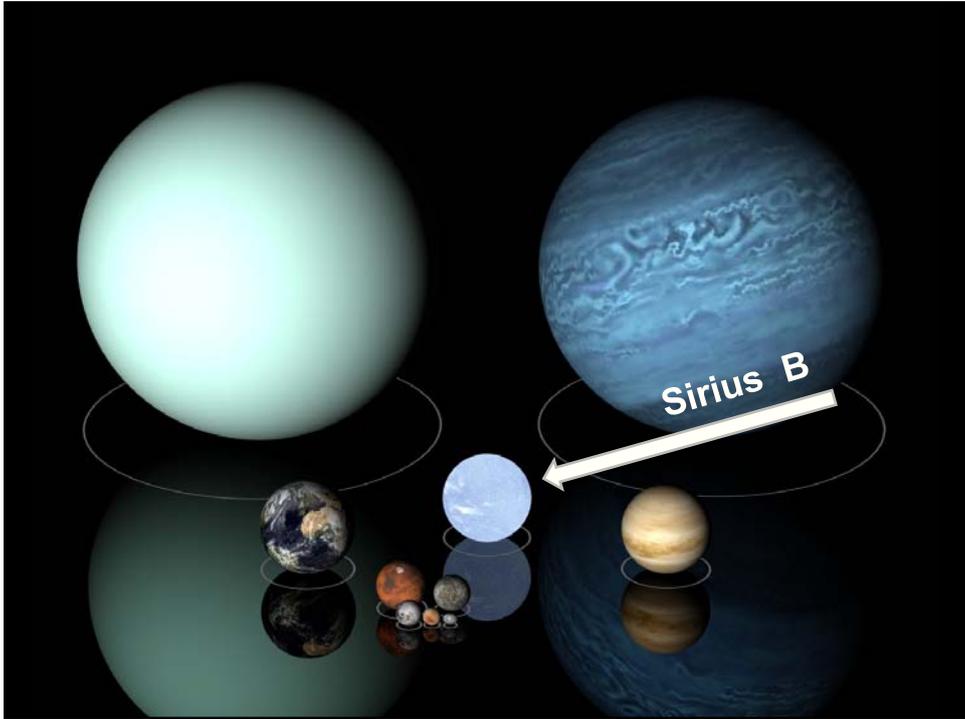
Supernova SN1006:

- brightness: $m = -7.5$
- distance: $d = 2.2 \text{ kpc}$
- recorded: China, Egypt, Iraq, Japan, Switzerland, North America

Supernova SN1006:
brightest stellar event recorded in history

White Dwarfs





Degenerate matter
(helium, carbon or other possible reaction products)

Normal gas
(50 km thick)

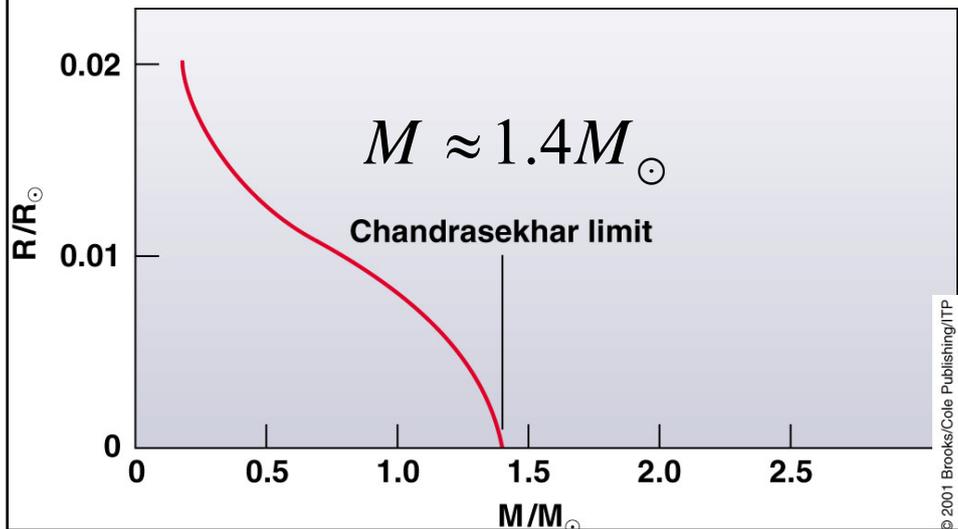
5000 to 6000 km

Regular gas: many unfilled energy levels. Particles free to move about and change energy levels.

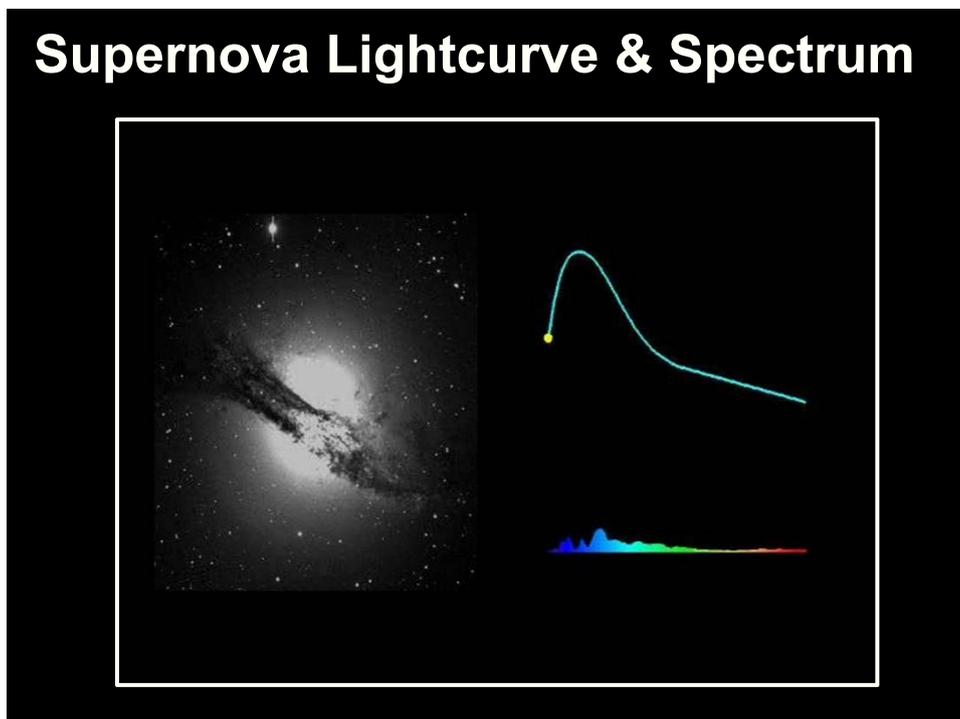
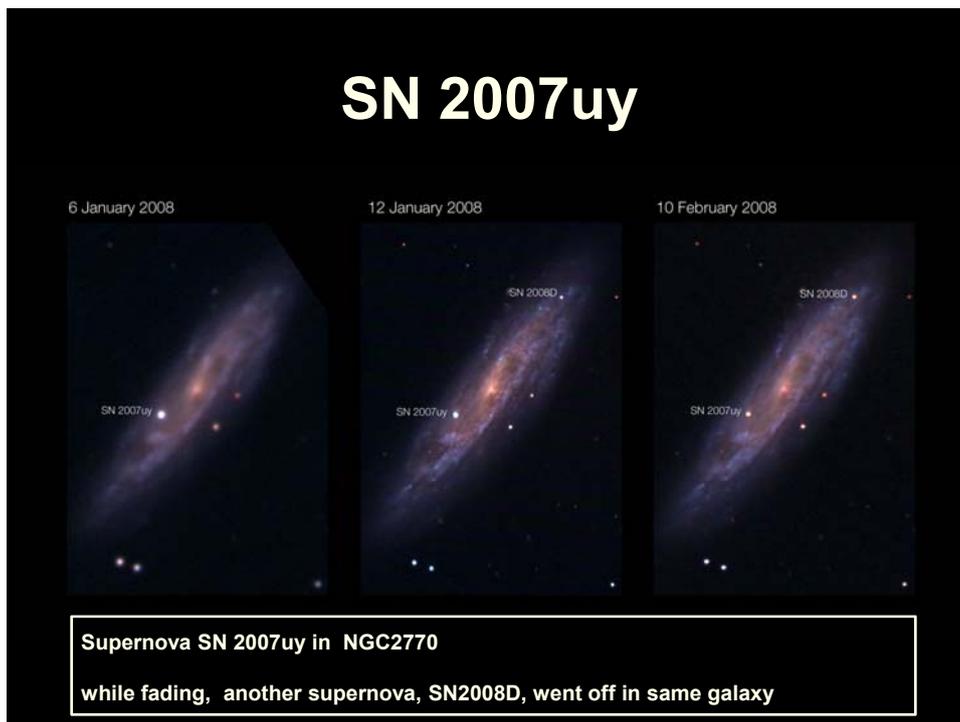
Degenerate gas: all lower energy levels filled with two particles each (opposite spins). Particles **locked** in place.

Chandrasekhar Mass Limit

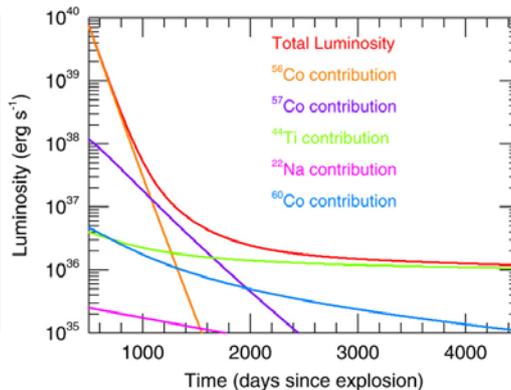
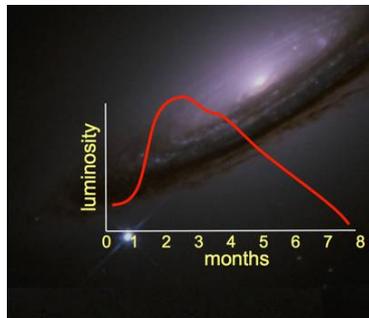
What is the maximum mass that can be supported by the dense compact material of a white dwarf star?



Supernova Lightcurves



Supernova Lightcurve

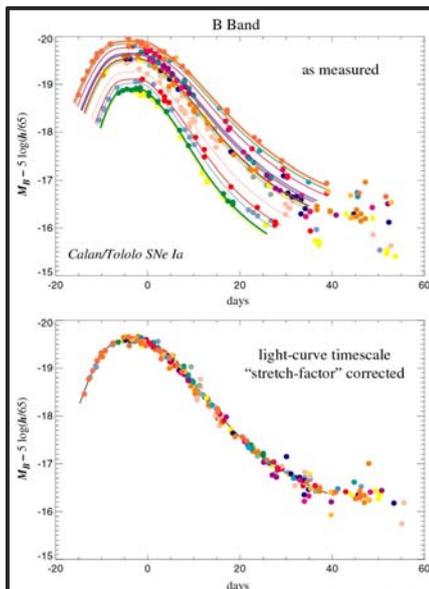


Type Ia supernovae follow a characteristic light curve—the graph of luminosity as a function of time—after the explosion.

This luminosity is generated by the radioactive decay of Nickel-56 through Cobalt-56 to Iron-56.

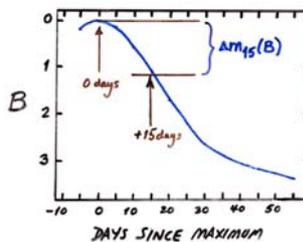
Maximum absolute magnitude of about -19.3.

the Phillips Relation



Relationship between

- peak luminosity of a Type Ia supernova
- speed of luminosity evolution after maximum light.



Mark Phillips (1993):

- on the basis of Calan/Tololo Supernova Survey
- the faster a supernova fades after peak,
- the fainter its intrinsic peak luminosity
- reduces scatter in Hubble diagram to $\sigma < 0.2$ mag
- heuristic relationship, as yet not theoretically “understood”

Supernova Teams: Practical Aspects

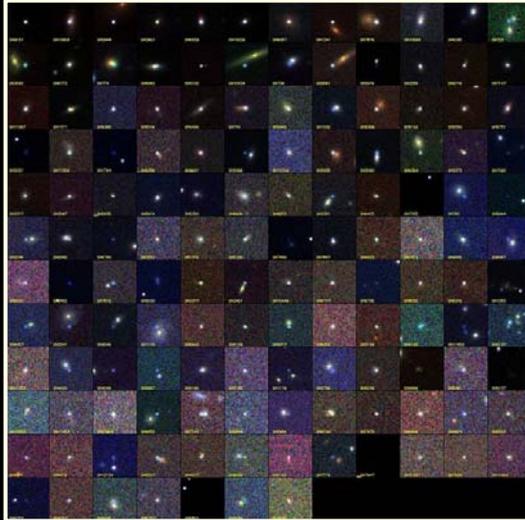
Supernova Cosmology Project

Success of Supernova Projects built on 3 major developments:

- **the introduction in the 1980s of large mosaic charge-coupled device (CCD) cameras on 4-meter class telescopes:**
 - systematic search of thousands of galaxies over large area of sky for rare supernova events
- **dramatic increase in computing power in the 1980s:**
 - enabling vast amount of data processing for automated search of supernovae amongst the huge number of galaxies monitored
- **Supernovae Ia as standard candles**
 - Calan/Tololo Supernova Search: accurate light curves & spectra
 - Phillips relation

High-z Supernova Search Team

Supernova Cosmology Project



diligently monitoring millions of galaxies, in search for that one explosion ...

High-z Supernova Search Team

Supernova Cosmology Project

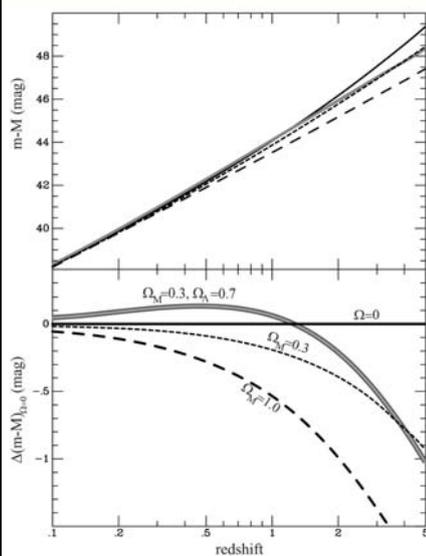
Challenges to be dealt with by Supernova Teams:

- Huge logistic (and political) issue of assuring vast amounts of (strongly contested) observing time on a range of telescopes (incl. 4-m ones for probing high-z universe)
- Dealing with a range of astronomical effects that would render any subtle cosmological signature insignificant:
 - Influence of dust: affecting brightness of supernovae
 - Abundance effects: poorly understood influence of heavy chemical elements on supernova lightcurves
 -
- Results put under heavy scrutiny through large range of tests dealing with each imaginable pitfall and artefact
- Absolutely crucial that two competing teams reached same conclusion independently !!!!

High-z Supernova Search Team

Cosmic Acceleration

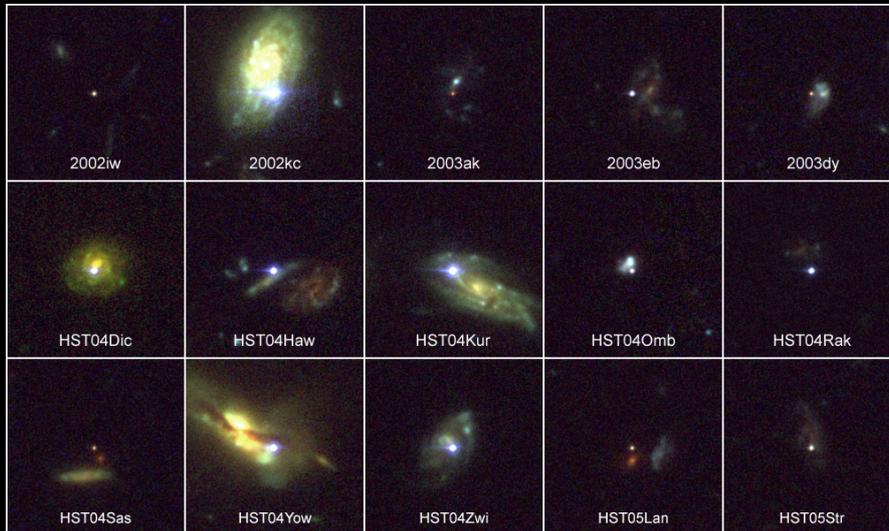
Cosmic Acceleration



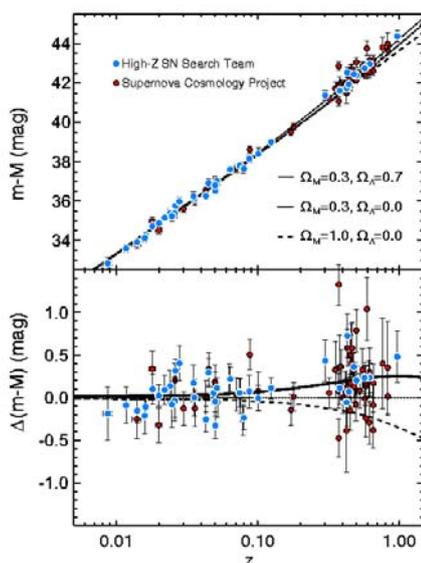
Hubble Diagram high-z SNIa

- distance vs. redshift z
 $m-M$ vs. redshift z
- determine:
 - absolute brightness of supernova Ia
 - from dimming rate (Phillips relation)
- measure:
 - apparent brightness of explosion
- translates into:
 - luminosity distance of supernova
 - dependent on acceleration parm. q

High-z SNIa: sample



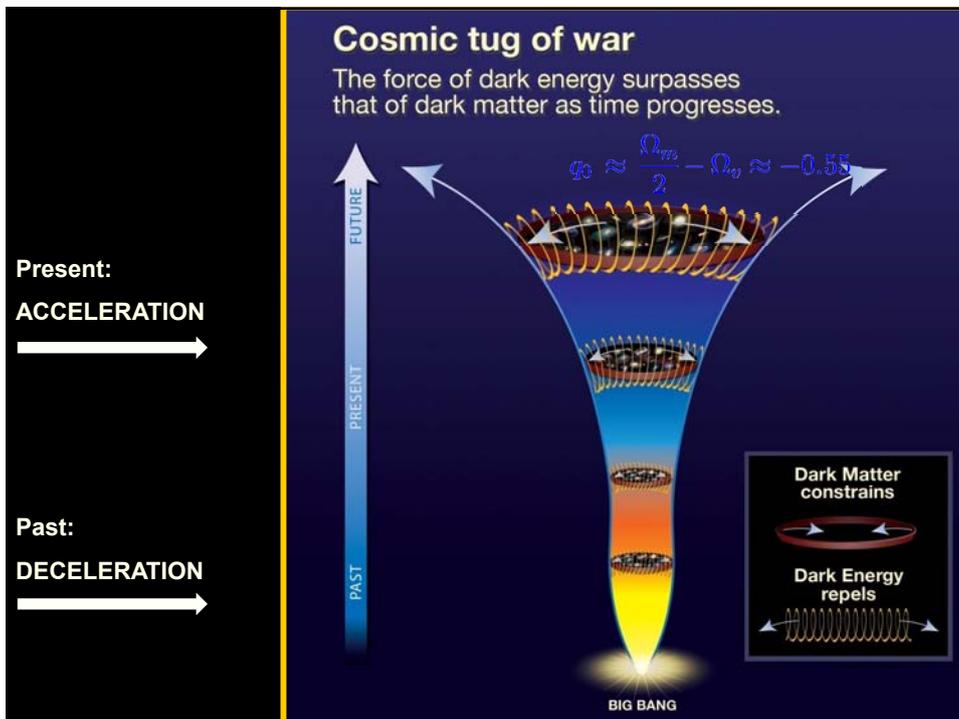
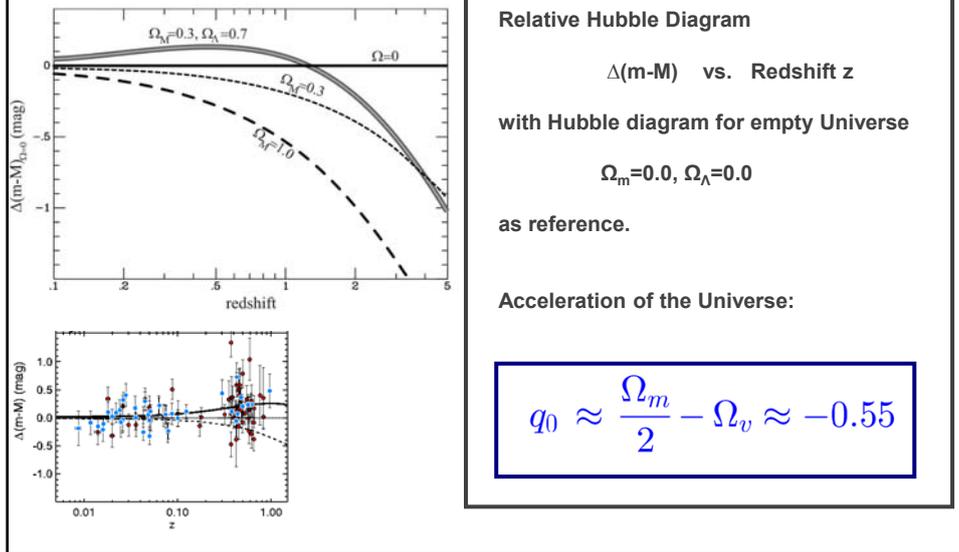
Cosmic Acceleration

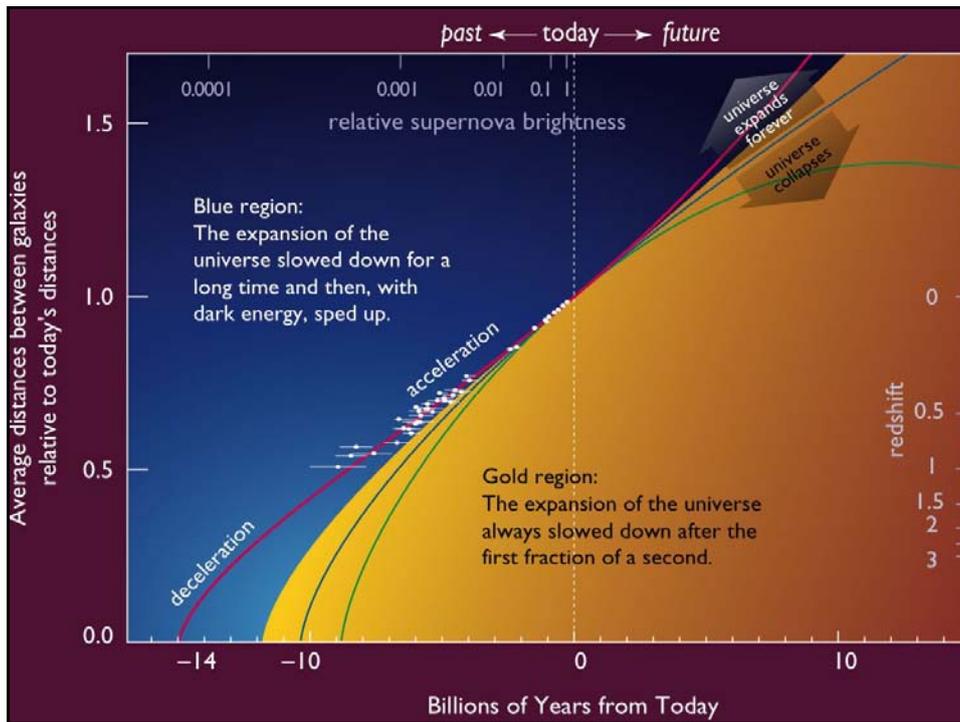


Hubble Diagram high-z SNIa

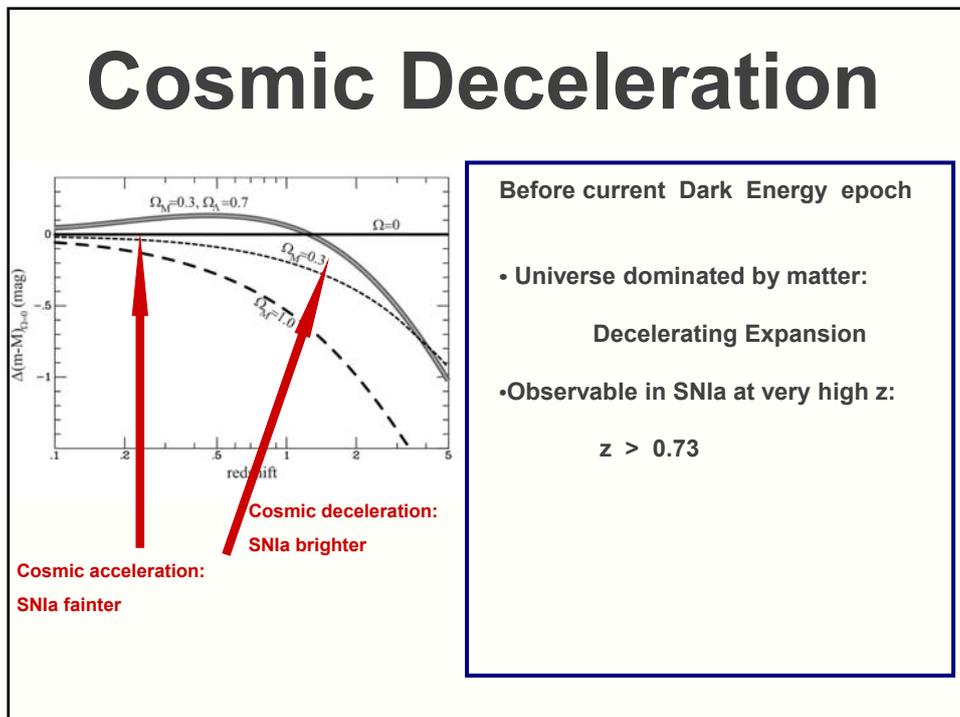
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Cosmic Acceleration

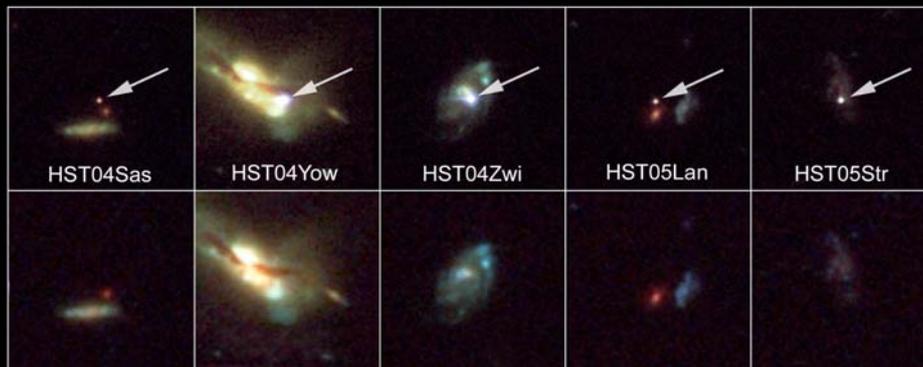




Cosmic Deceleration



Beyond Acceleration: SNe Ia at $z > 0.7$



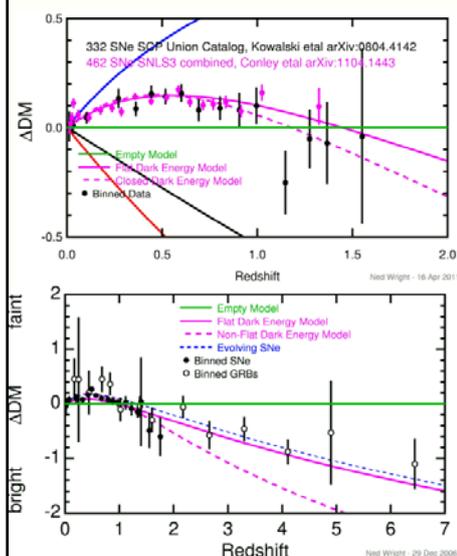
Five high-z SNIa, images HST-ACS camera

SNIa and host galaxies

lower panel: before

top panel: after explosion)

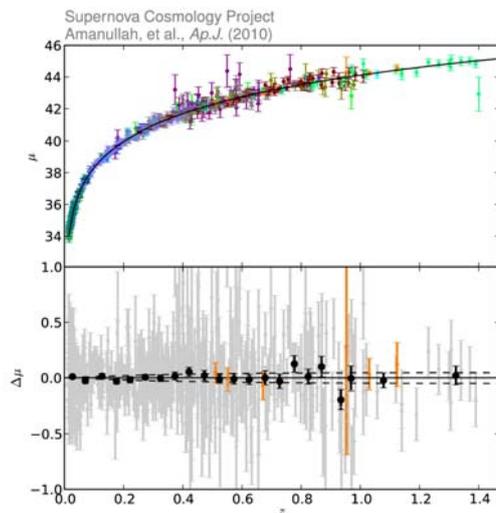
Cosmic Deceleration



Before current Dark Energy epoch

- Universe dominated by matter:
Decelerating Expansion
- Observable in SNIa at very high z :
 $z > 0.73$

Union2: state-of-the-art SNIa compilation



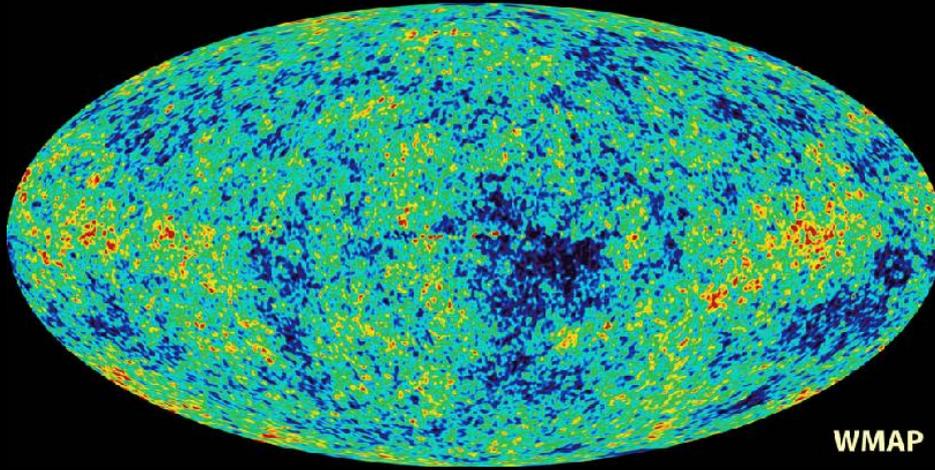
SCP Union2.1 SN Ia
compilation:

719 SNe, 17 datasets
(557 used)
6 $z > 1$ SN Ia

Amanullah et al. 2010

Cosmic Curvature

Cosmic Microwave Background



Map of the Universe at Recombination Epoch (WMAP, 2003):

- 379,000 years after Big Bang
- Subhorizon perturbations: primordial sound waves
- $\Delta T/T < 10^{-5}$

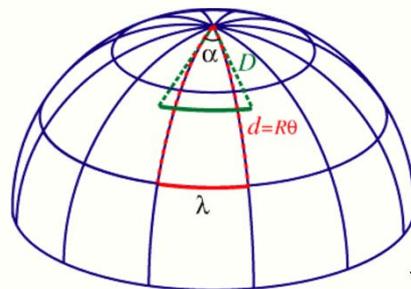
Measuring Curvature

Measuring the Geometry of the Universe:

- Object with known physical size, at large cosmological distance
- Measure angular extent on sky
- Comparison yields light path, and from this the curvature of space



Geometry of Space



W. Hu

In a FRW Universe:
lightpaths described by
Robertson-Walker metric

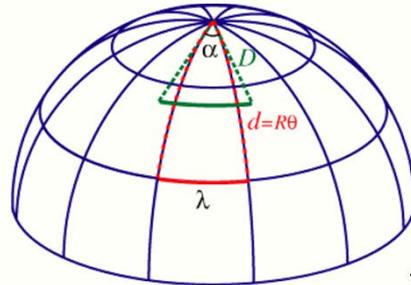
$$ds^2 = c^2 dt^2 - a(t)^2 \left\{ dr^2 + R_c^2 S_k^2 \left(\frac{r}{R_c} \right) \left[d\theta^2 + \sin^2 \theta d\phi^2 \right] \right\}$$

Measuring Curvature

- Object with known physical size, at large cosmological distance:
- Sound Waves in the Early Universe !!!!



**Temperature Fluctuations
CMB**

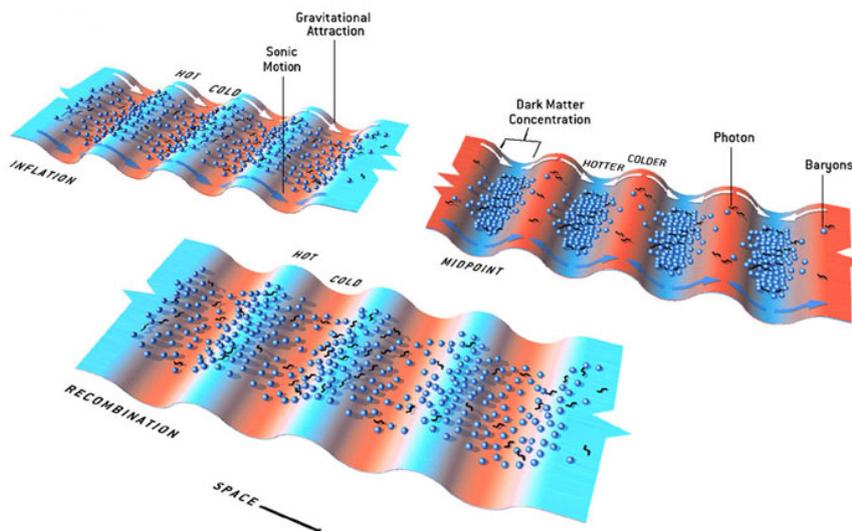


Y. Hu

**In a FRW Universe:
lightpaths described by
Robertson-Walker metric**

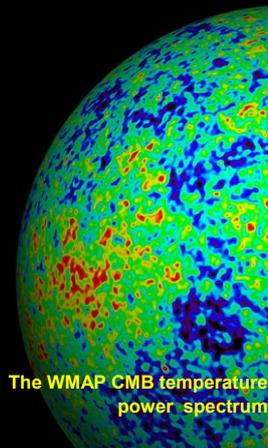
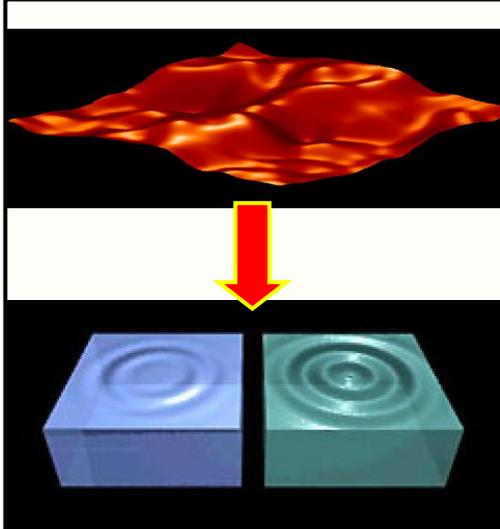
$$ds^2 = c^2 dt^2 - a(t)^2 \left\{ dr^2 + R_c^2 S_k^2 \left(\frac{r}{R_c} \right) \left[d\theta^2 + \sin^2 \theta d\phi^2 \right] \right\}$$

Fluctuations-Origin



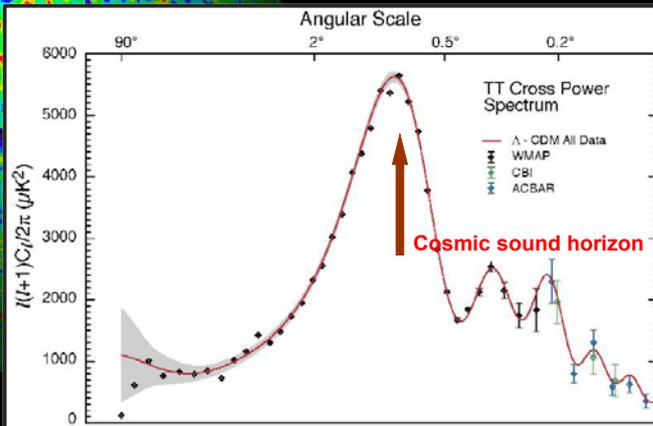
Music of the Spheres

- small ripples in primordial matter & photon distribution
- gravity:
 - compression primordial photon gas
 - photon pressure resists
- compressions and rarefactions in photon gas: sound waves
- sound waves not heard, but seen:
 - compressions: (photon) T higher
 - rarefactions: lower
- fundamental mode sound spectrum
 - size of "instrument":
 - (sound) horizon size last scattering
- Observed, angular size: $\theta \sim 1^\circ$
 - exact scale maximum compression, the "cosmic fundamental mode of music"

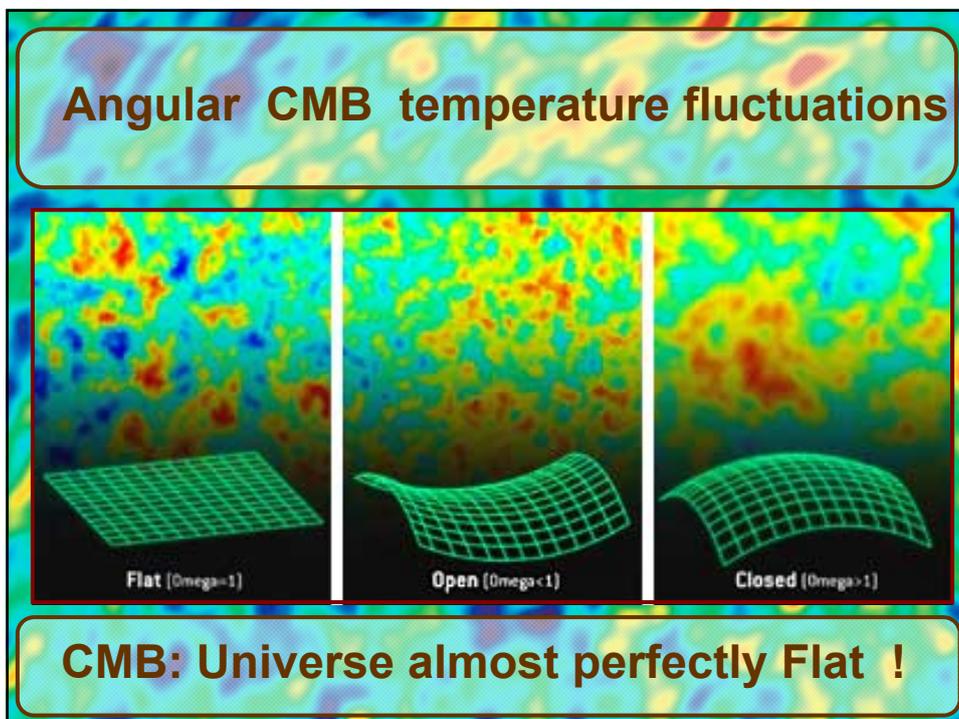
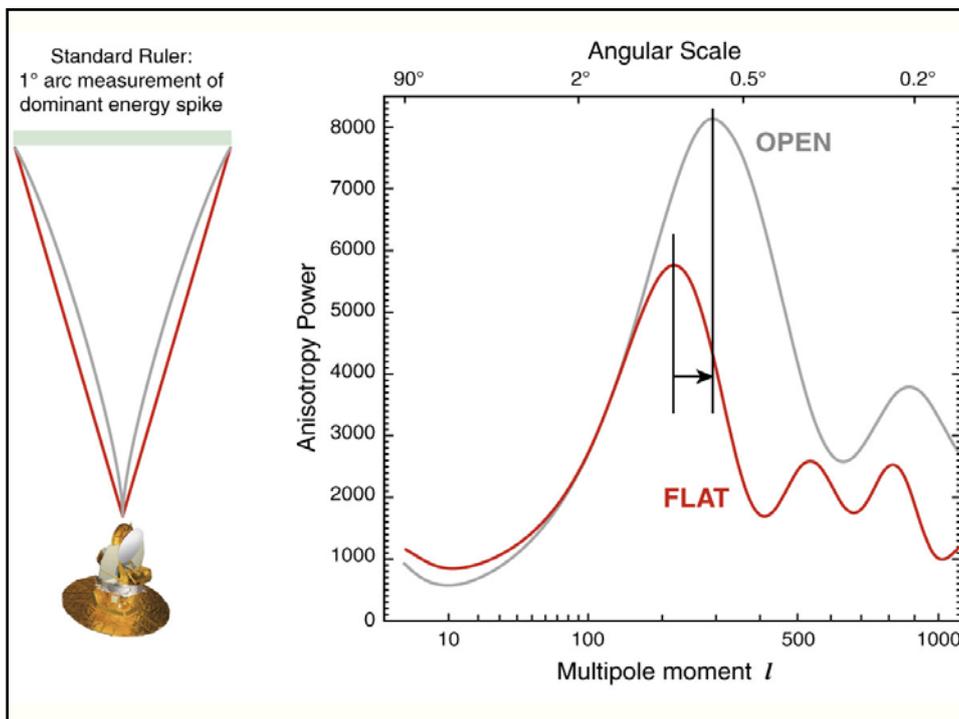


The WMAP CMB temperature power spectrum

The Cosmic Tonal Ladder

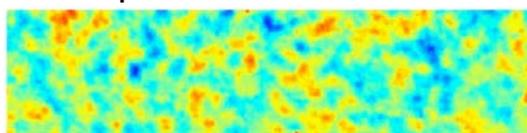


The Cosmic Microwave Background Temperature Anisotropies: Universe is almost perfectly flat

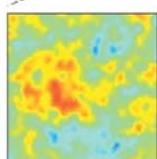
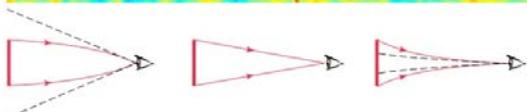


Flat universe from CMB

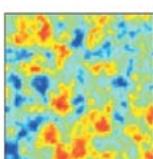
- First peak: flat universe



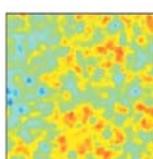
We know the redshift and the time it took for the light to reach us: from this we know the length of the legs of the triangle and the angle at which we are measuring and the sound horizon.



Closed: hot spots appear larger



Flat: appear as big as they are

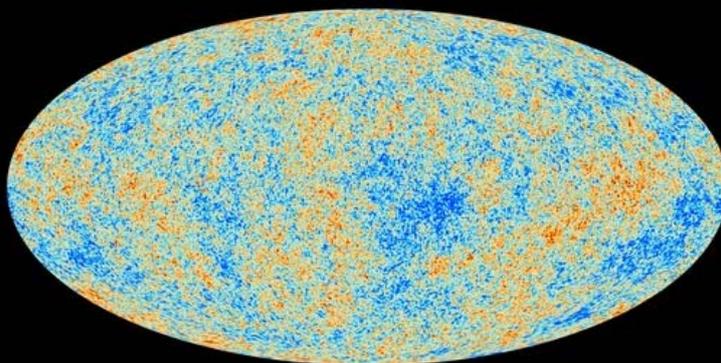


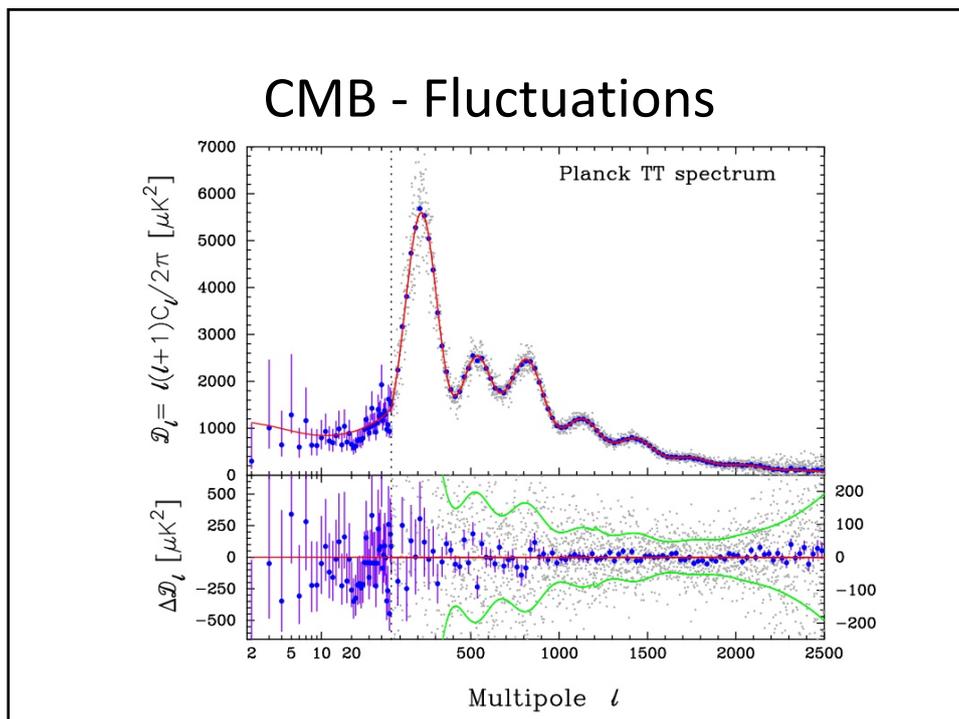
Open: spots appear smaller

$$v \approx \frac{c}{\sqrt{3}}$$

$$\ell \approx 200/\sqrt{1 - \Omega_k}$$

CMB, l up to 2500





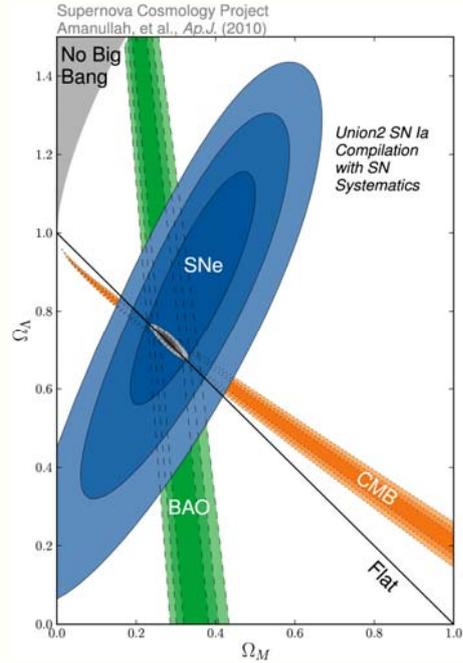
**Probes
Combined**

Ω_m vs. Ω_Λ

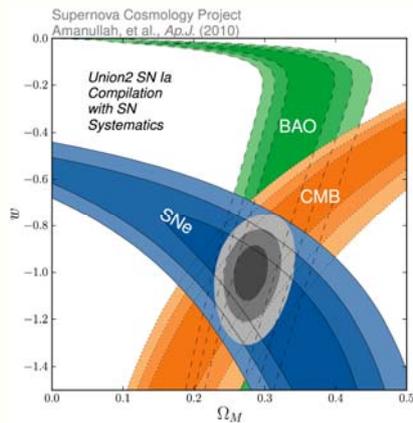
$$q \approx \frac{\Omega_m}{2} - \Omega_\Lambda$$

$$k = \frac{H^2 R^2}{c^2} (\Omega_m + \Omega_\Lambda - 1)$$

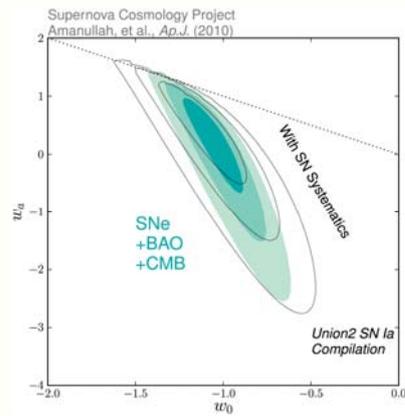
SCP Union2 constraints (2010)
 on values of matter density Ω_m
 dark energy density Ω_Λ



Dark Energy Eqn.State



SCP Union2 constraints (2010)
 on values of matter density Ω_m
 dark energy eqn. state w



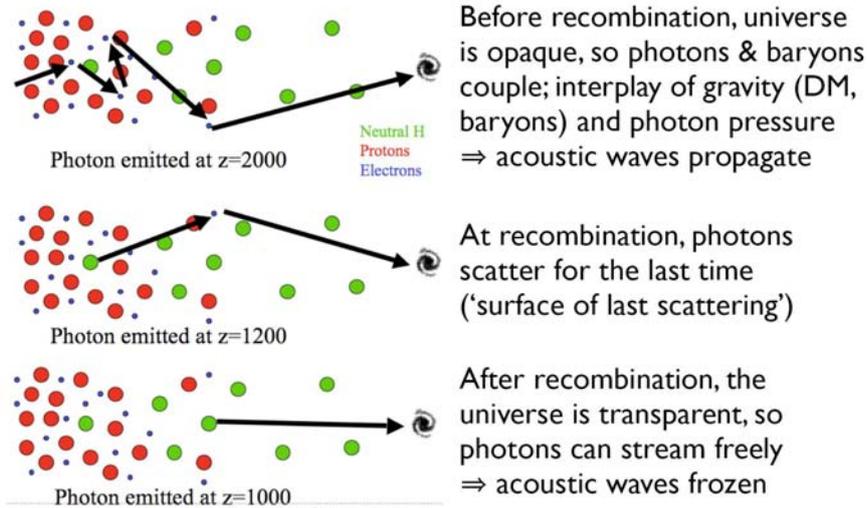
on dynamical evolution dark energy:
 eqn. state parameters w_0
 w_a

BAO: Baryonic Acoustic Oscillations

What are BAO?

- Sound waves traveling in the primordial plasma.
- The resonant wavelengths are selected by the time when recombination takes place.
- Signature of these waves in the matter distribution in the present universe.

BAO explained



BAO explained

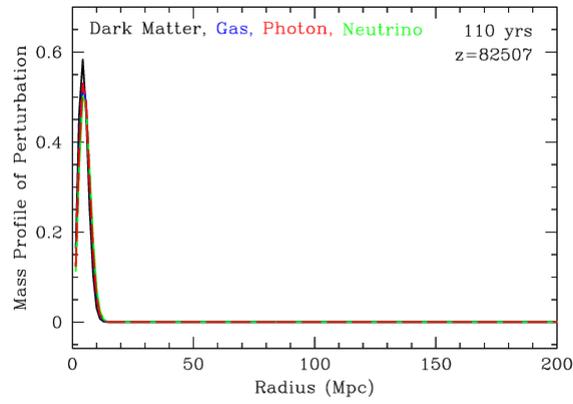
- The early universe is a hot plasma in which baryonic matter and radiation are tightly coupled.
- The density is not uniform, but there are small variations that oscillate due to gravity and radiation pressure.

$$c_s = \frac{c}{\sqrt{3 \left(1 + \frac{3\rho_b}{4\rho_\gamma}\right)}}$$

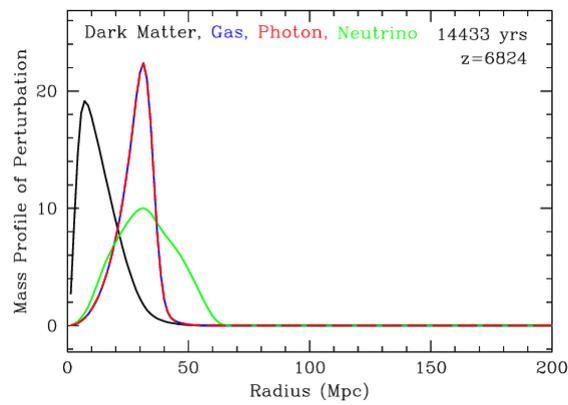
- The waves stop propagating at recombination, since the photons stop interacting with baryons.

$$r_s \approx c_s t_{rec}$$

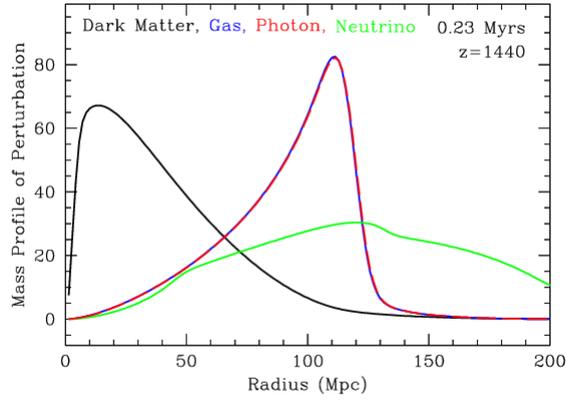
BAO explained



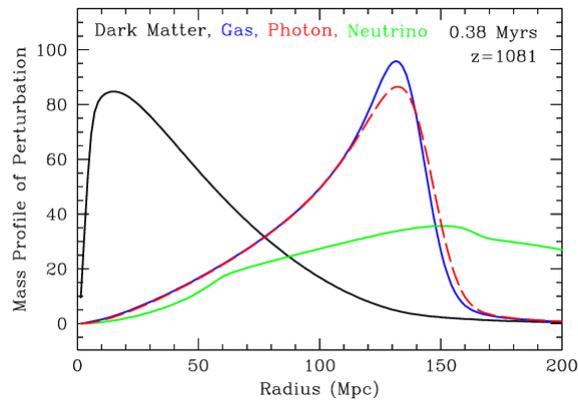
BAO explained



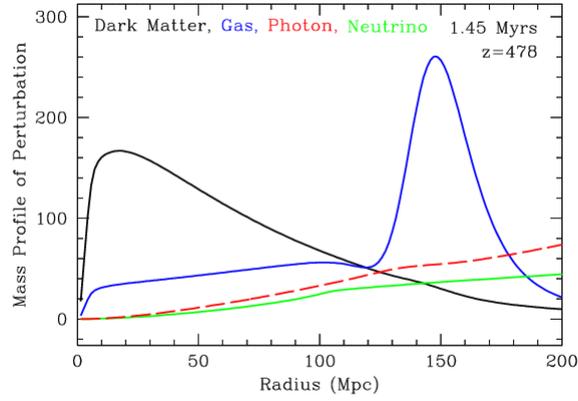
BAO explained



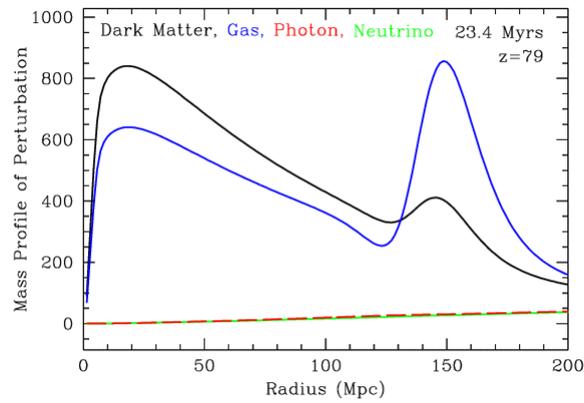
BAO explained



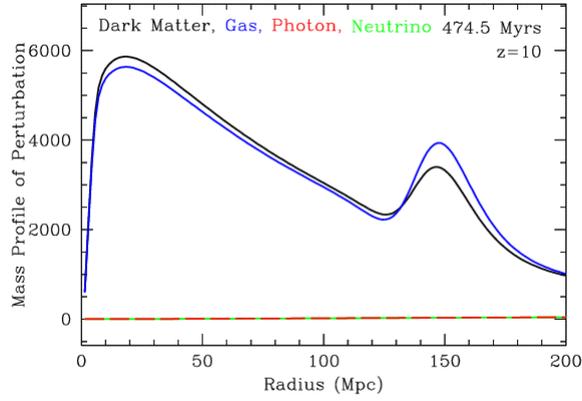
BAO explained



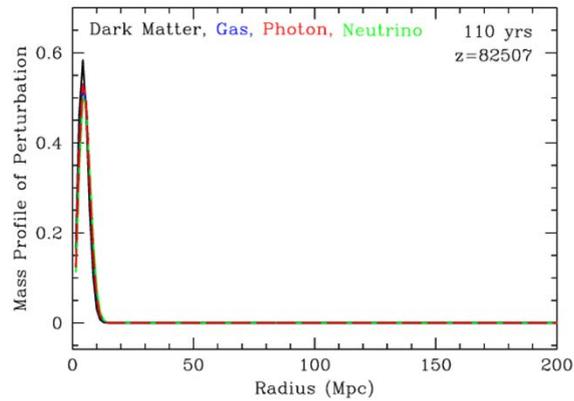
BAO explained



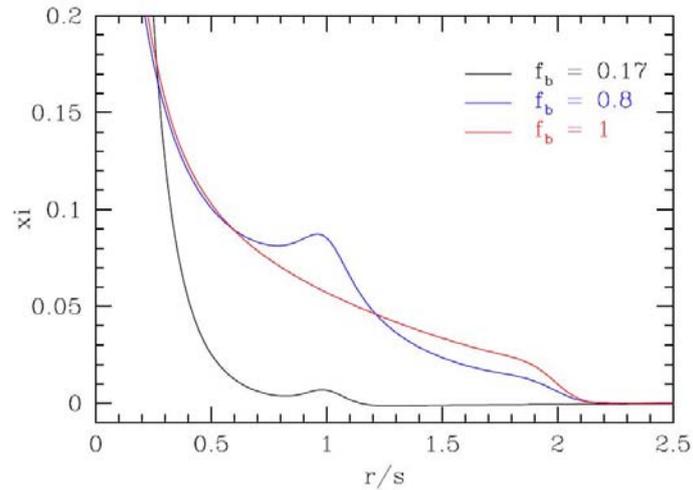
BAO explained



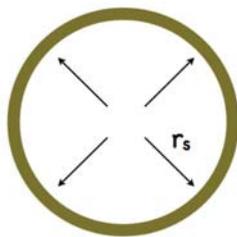
BAO explained



BAO explained

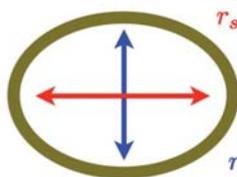


BAO as cosmological tools



Until recombination, the sound wave travels a distance of:

$$r_s = \int_{z_{rec}}^{\infty} \frac{c_s(z)}{H(z)} dz$$



This distance can be accurately determined from the CMB power spectrum, and was found to be 147 ± 2 Mpc.

BAO as cosmological tools

If we know the radius \mathbf{r}_s , then we can compute both the Hubble factor $\mathbf{H}(\mathbf{z})$ and the angular distance $\mathbf{D}_A(\mathbf{z})$:

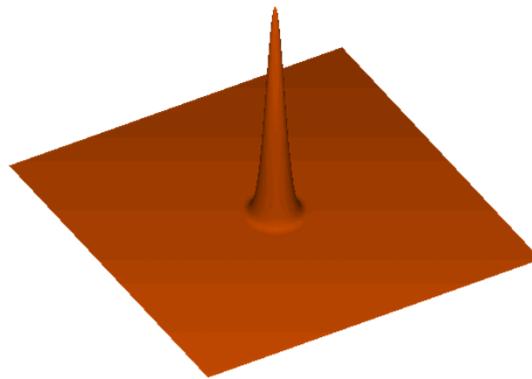
$$H(z) = H_0 \sqrt{\Omega_{rad}(1+z)^4 + \Omega_m(1+z)^3 + \Omega_k(1+z)^2 + \Omega_\Lambda f(z)}$$

$$D_A(z) = \frac{c}{1+z} \int_0^z \frac{dz'}{H(z')}$$

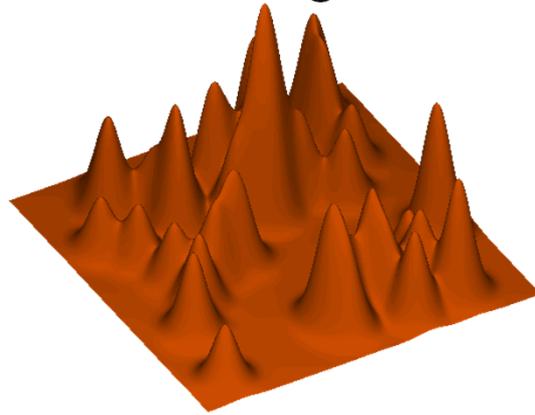
$$f(z) = (1+z)^{3(w+1)}, \text{ for constant } w$$

$$f(z) = (1+z)^3 \exp\left(3 \int_0^z \frac{w(z')}{1+z'} dz'\right), \text{ for } w(z)$$

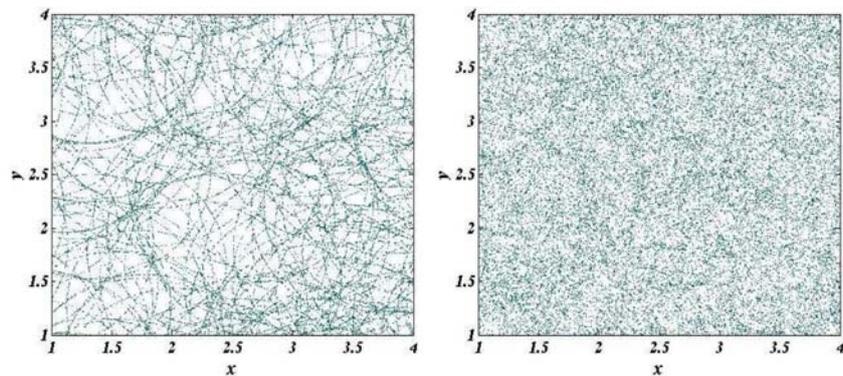
Measuring BAO

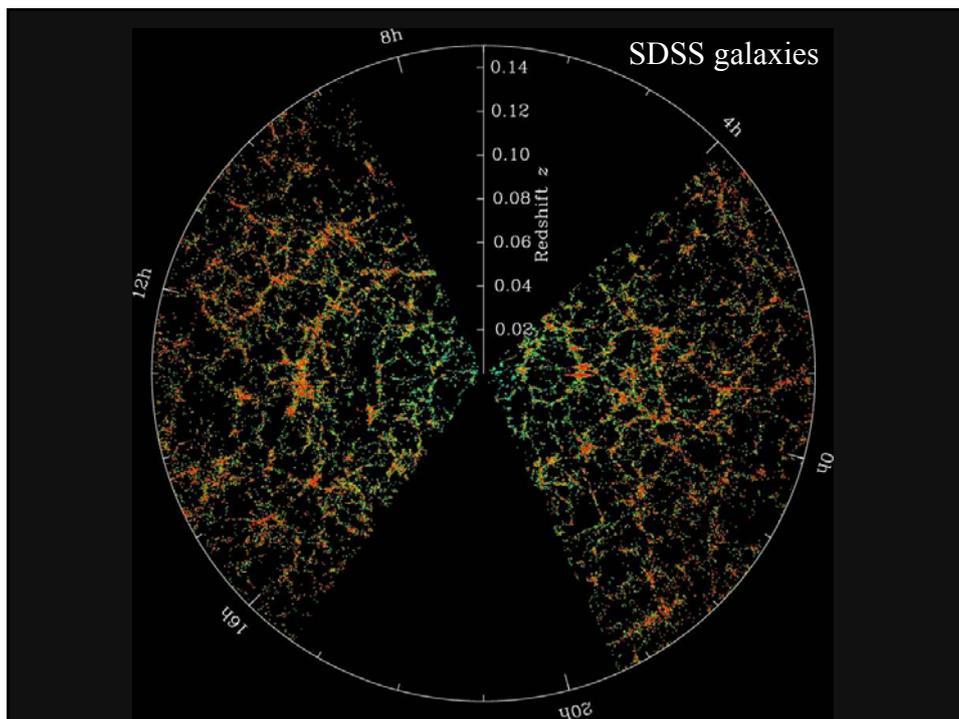


Measuring BAO



Measuring BAO





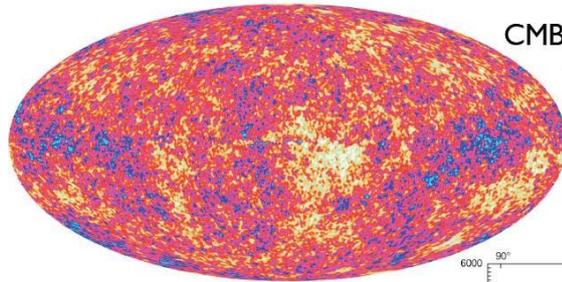
Measuring BAO

Must use statistical tools to find the acoustic peak!

In the CMB, the acoustic peak is found by computing the power spectrum of the temperature fluctuations across the sky. This determines the distance r_s traveled by the sound waves until recombination.

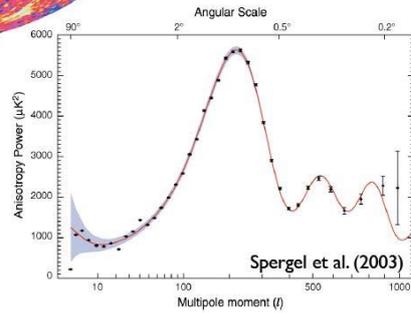
In the baryon distribution, the acoustic peak is computed from the 2-point correlation function or the power spectrum. (The 2-point correlation function quantifies the excess of clustering on a given scale relative to a uniform distribution of matter with the same mean density.)

Measuring BAO

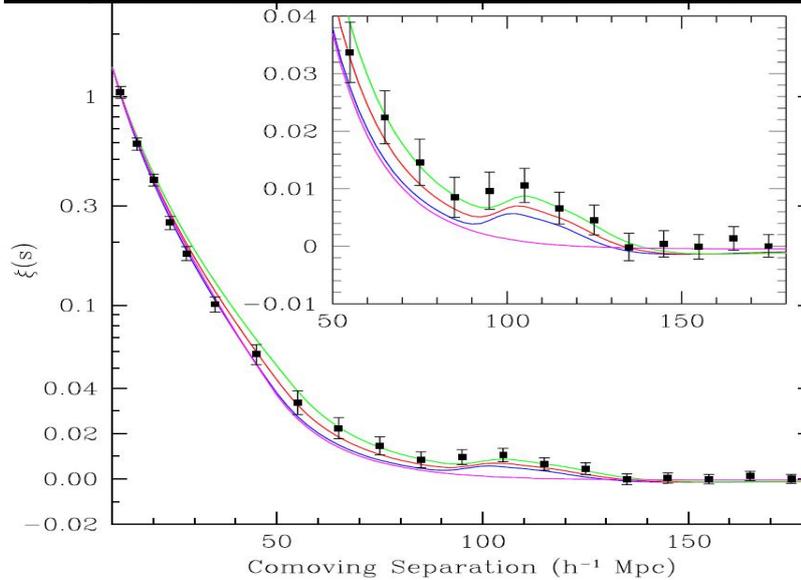


CMB anisotropies from WMAP

CMB power spectrum gives a very precise measurement of the BAO scale at $z=1100$:
 $r_s = 147 \pm 2$ Mpc

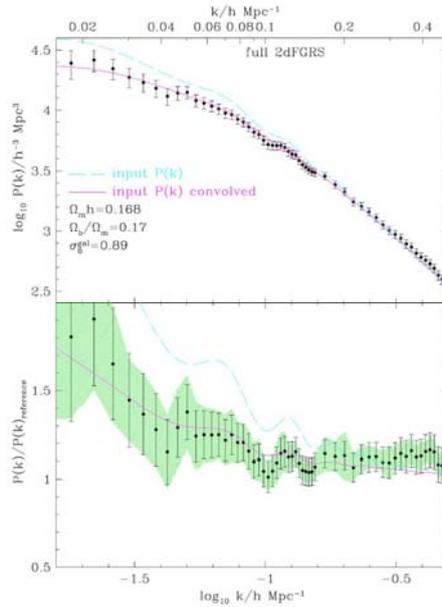


Green, red and blue: increasing $\Omega_m h^2$ from 0.12 to 0.14
 Magenta: Only CDM



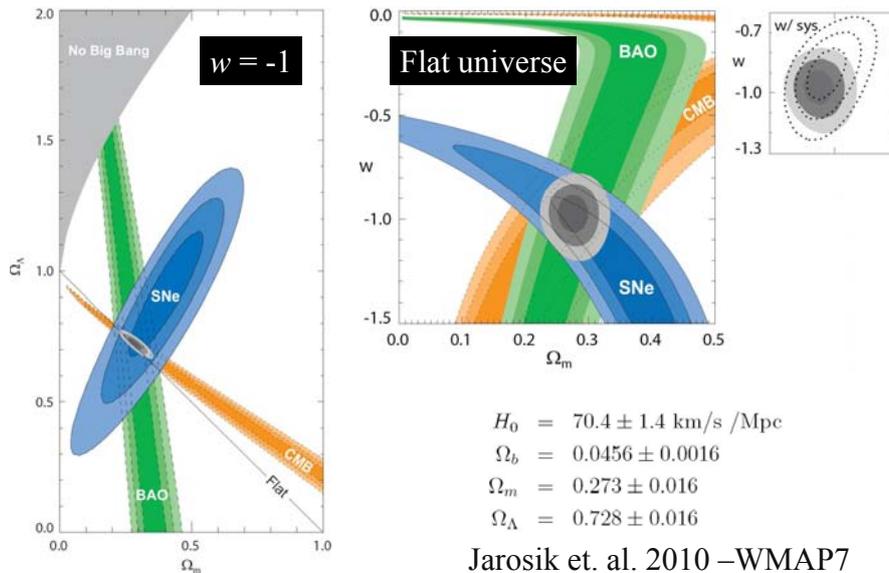
2dFGRS results

Cole et al. 2005



BAO Results

Kowalski et al. 2008

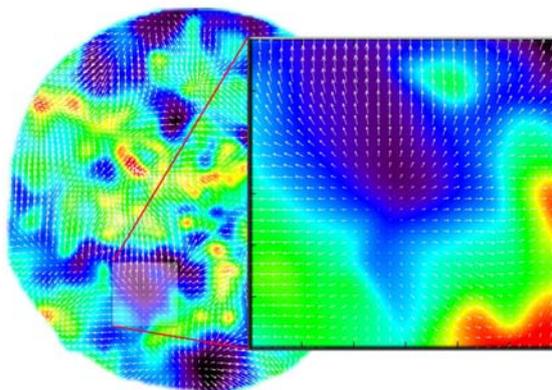


Structure Growth Factor

Large Scale Flows

Large-Scale Flows:

- On large (Mpc) scales, structure formation still in linear regime
- Structure buildup accompanied by displacement of matter:
 - Cosmic flows
- Directly related to cosmic matter distribution



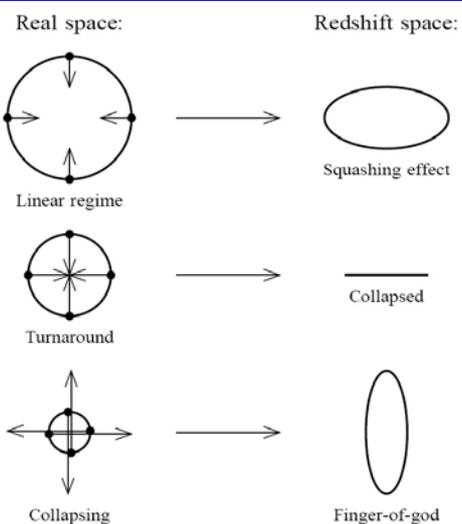
$$\mathbf{v}(\mathbf{x}, t) = \frac{H}{4\pi} \frac{f(\Omega_m)}{b} a \int d\mathbf{x}' \delta_{gal}(\mathbf{x}', t) \frac{(\mathbf{x}' - \mathbf{x})}{|\mathbf{x}' - \mathbf{x}|^3}$$

Redshift Distortions

Origin of peculiar velocities:

three regimes

- very high-density virialized cluster (core) regions: "thermal" motion in cluster, up to > 1000 km/s
- "Fingers of God"
- collapsing overdensity (forming cluster): inflow/infall velocity
- Large scales: (linear, quasi-linear) cosmic flow, manifestation of structure growth

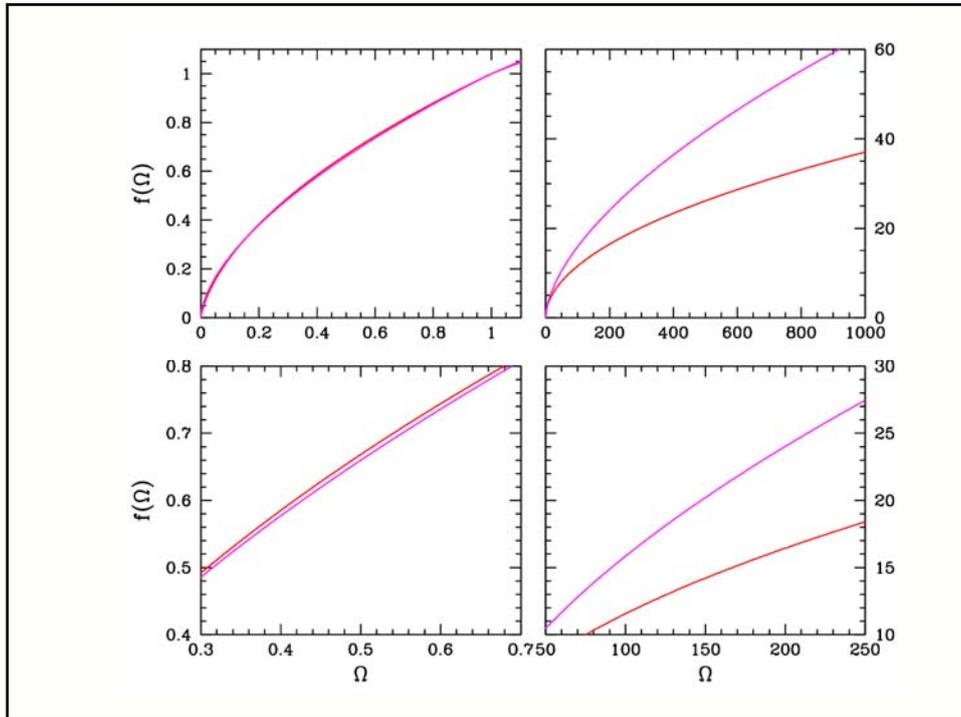


$$\mathbf{v} = \frac{H f}{4\pi G \rho_u} \mathbf{g} = \frac{2 f}{3H\Omega} \mathbf{g} \quad (142)$$

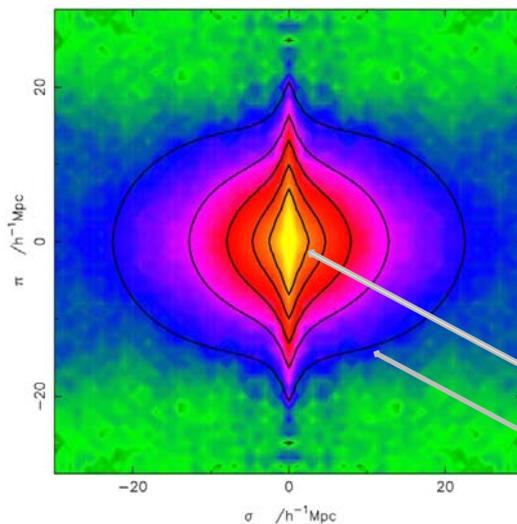
10.3.5. Dimensionless Linear Velocity Growth Factor $f(\Omega)$

In the above we found that the dimensionless linear velocity growth factor is a very important concept in the linear theory of structure formation,

$$f \equiv \frac{a}{D} \frac{dD}{da} = \frac{d \log D}{d \log a} \quad (143)$$



sky-redshift space 2-pt correlation function $\xi(\sigma, \pi)$



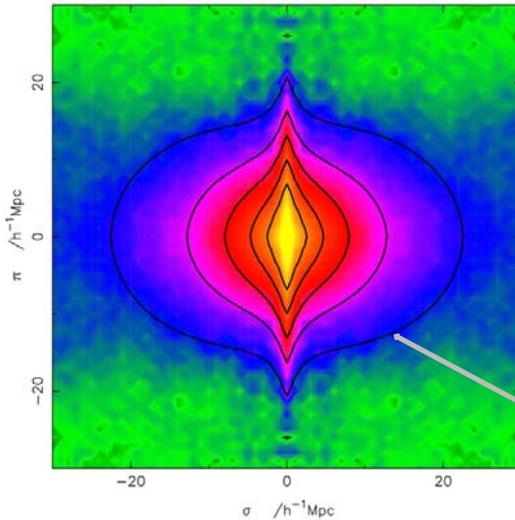
Correlation function determined in sky-redshift space:

$$\xi(\sigma, \pi)$$

sky position: $\sigma = (\alpha, \delta)$
redshift coordinate: $\pi = cz$

Close distances:
distortion due to non-linear
Finger of God
Large distances:
distortions due to large-scale
flows

Redshift Space Distortions Correlation Function



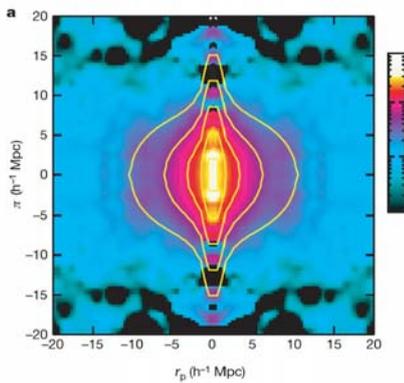
On average, $\xi_s(s)$ gets amplified wrt. $\xi_r(r)$

Linear perturbation theory (Kaiser 1987):

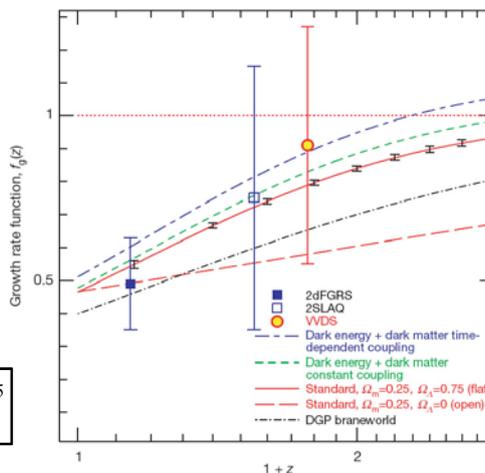
$$\xi_s(s) = \left(1 + \frac{2}{3}\Omega^{0.6} + \frac{1}{5}\Omega^{1.2}\right)\xi_r(s)$$

Large distances: distortions due to large-scale flows

Evolution Growth Rate



Linder 2008
Guzzo et al. 2008

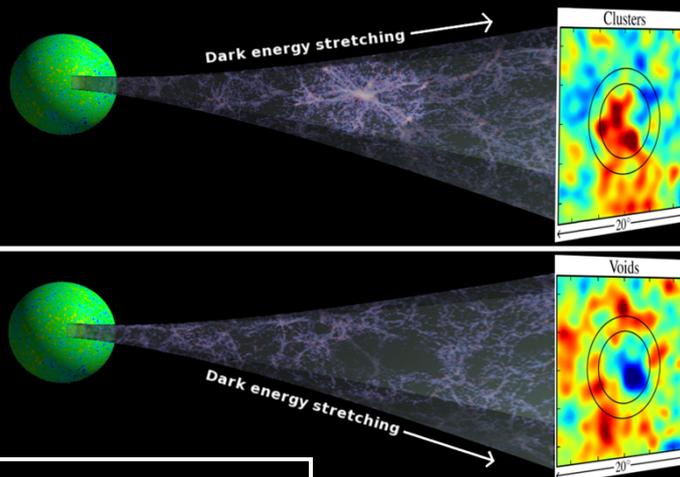


$$f(\Omega_m, \Omega_\Lambda) = \frac{a}{D} \frac{dD}{da} \approx \Omega_m^{0.55}$$

Peebles growth rate factor

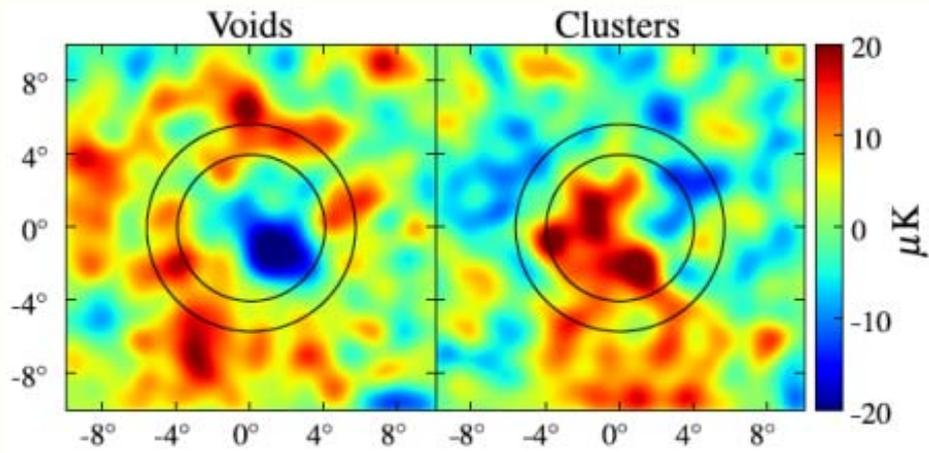
ISW: Integrated Sachs Wolfe Effect

Dark Energy: ISW



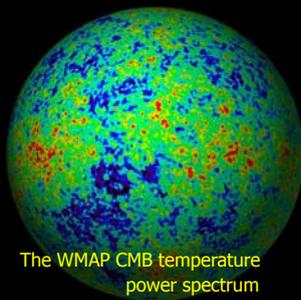
Dark Energy modifies evolution potential wells

Dark Energy: ISW

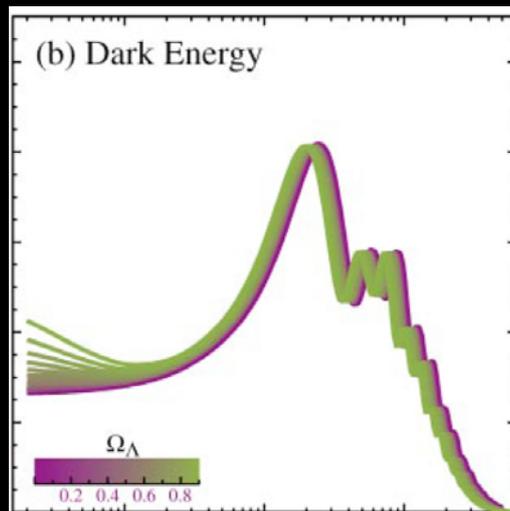


Dark Energy modifies evolution potential wells

Dark Energy & CMB: ISW

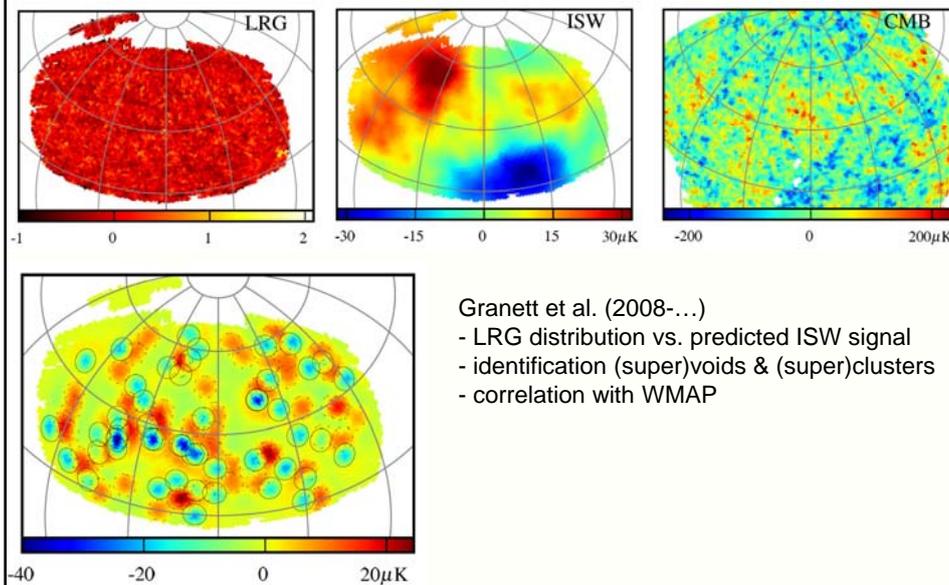


The WMAP CMB temperature power spectrum

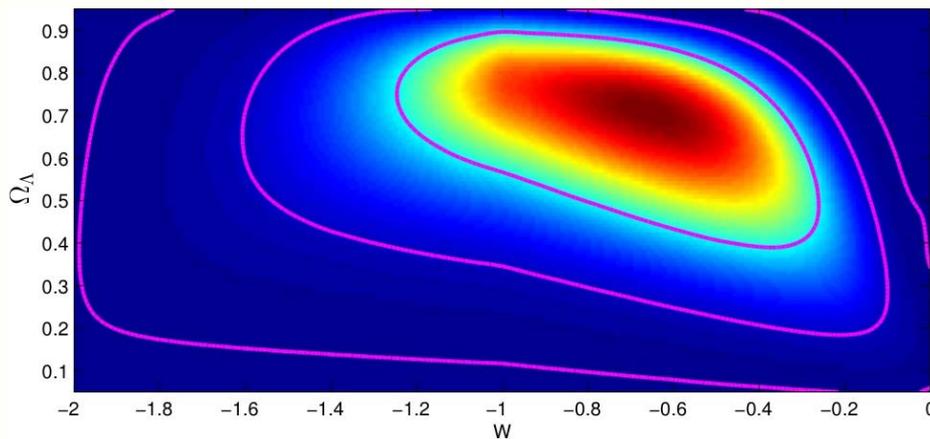


Dark Energy modifies evolution potential wells

ISW & identified voids/clusters

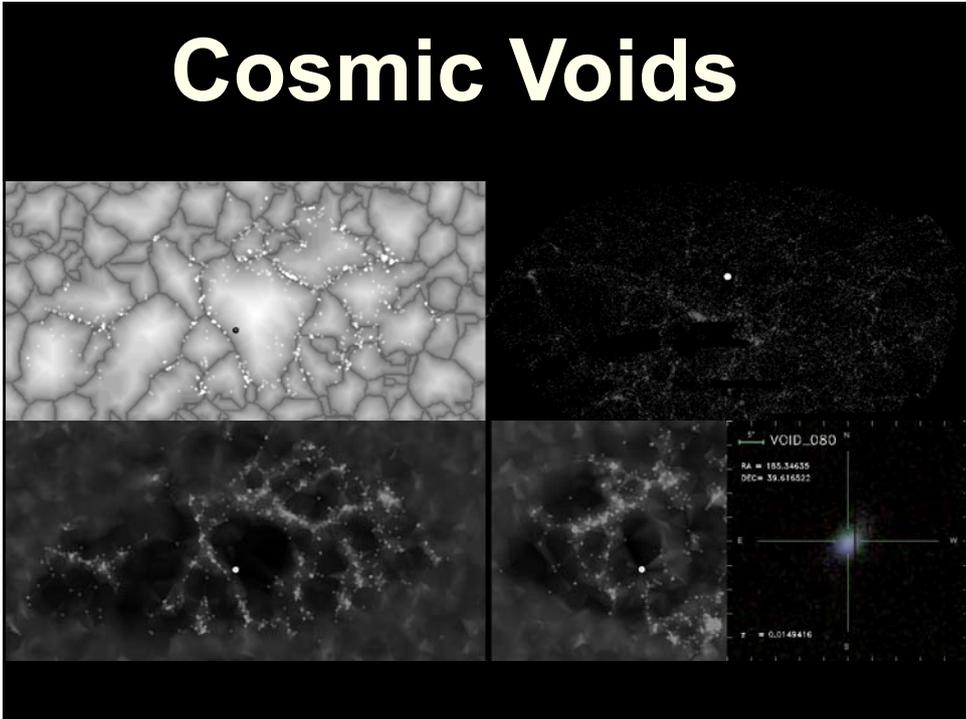


Dark Energy: ISW

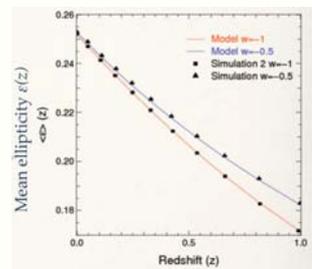
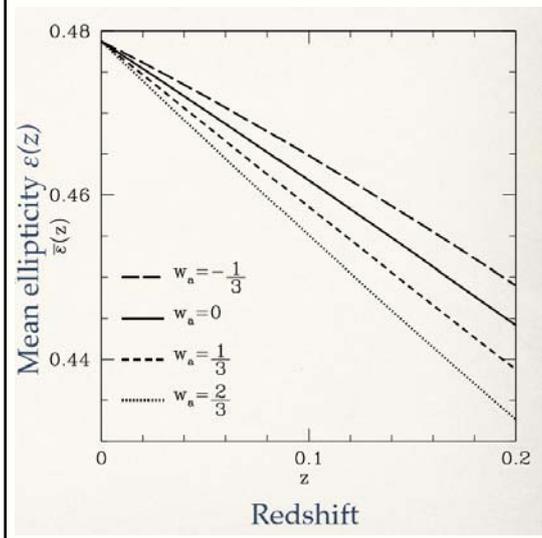


Dark Energy modifies evolution
potential wells

Cosmic Voids: Shape of Voids



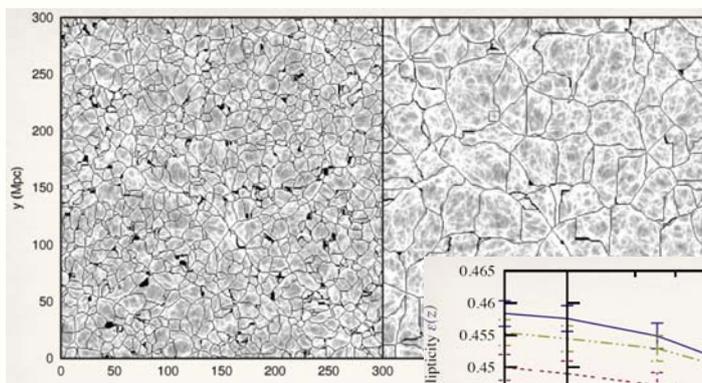
Evolving Void Shapes



Evolution of void shape
sensitive probe of dark energy:

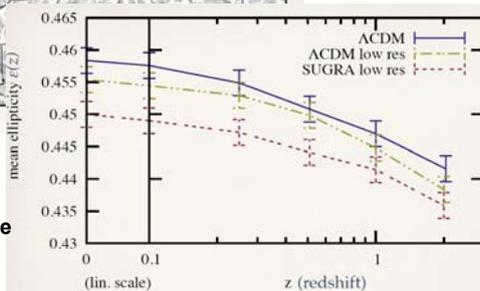
Park & Lee 2007
Lavaux & Wandelt 2010

Evolving Void Shapes



Bos et al. 2011:

Trend of evolving void shape
as function of dark energy eqn.state
confirmed.



Future Experiments

Euclid

Euclid:
father of geometry



ESA
Cosmic Vision
2020-2025

- 1.2 m Korsch telescope
- visible light:
 - m=24.5 CCD imaging
- IR (Y,J,H) band photometer
- spectrometer 108 bright gals

- 15,000 sq. deg. survey
- 40 sq. deg. deep survey

- Combination:
 - DUNE grav. Lensing
 - SPACE BAO

Euclid



ESA
Cosmic Vision
2020-2025

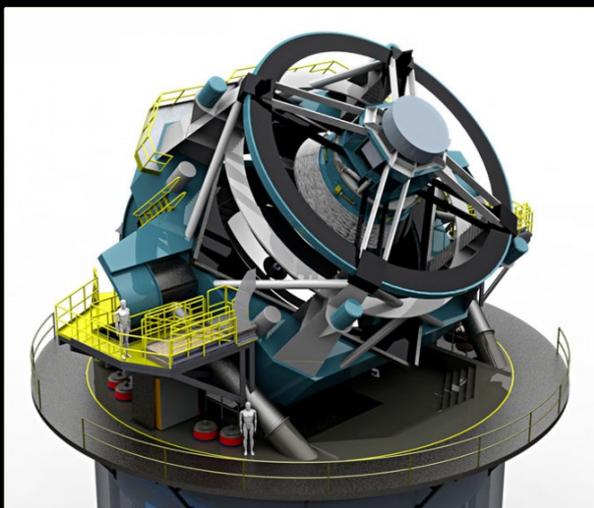
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- spectrometer 108 bright gals

- 15,000 sq. deg. survey
- 40 sq. deg. deep survey

- Combination:
 - DUNE grav. Lensing
 - SPACE BAO

LSST:

Large Synoptic Survey Telescope



8.4 m primary mirror
widefield survey telescope

- El Penon, Chile
2682 m. mountain
- start operation: 2015
- 3.5 deg. angle of view
- 3.2 Gigapixel prime focus
digital camera
- 200,000 images per year
- 30 Tbyte per night
- partial funding Bill Gates

Summary

Take-Home Facts

1. Strong evidence Accelerated Expansion

- since supernova discovery, 100s SNIa observed over broader range redshifts
- based solely upon supernova Hubble diagram, independent of General Relativity, very strong evidence expansion Universe accelerated recently

2. Dark energy as cause cosmic acceleration

- within general relativity, accelerated expansion cannot be explained by any known form of matter or energy
- it can be accommodated by a nearly smooth form of energy with large negative pressure, Dark Energy, that accounts for about 73% of the universe.

3. Independent evidence dark energy

- Cosmic Microwave Background and Large Scale Structure data provide independent evidence, within context of CDM model of structure formation, that the universe is filled with a smooth medium accounting for 73% of the total energy content of the universe.
- that came to dominate the dynamics of the universe once all observed structure had formed

Take-Home Facts

4. Vacuum energy as dark energy

- simplest explanation for dark energy is the energy associated with the vacuum
- mathematically equivalent to a cosmological constant
- However, most straightforward calculations of vacuum energy density from zero-point energies of all quantum fields lead to estimates which are a bit too large, in the order of $\sim 10^{120}$

5. Dark theories of Dark Energy

- There is no compelling theory of dark energy
- Beyond vacuum energy, many intriguing ideas: light scalar fields, additional spatial dimensions, etc.
- Many models involve time-varying dark energy

6. New Gravitational Theories ?

- alternatively, cosmic acceleration could be a manifestation of gravitational physics beyond General Relativity
- however, as yet there is no self-consistent model for new gravitational physics that is consistent with large body of data that constrains theories of gravity.

Take-Home Facts

7. Dark destiny

8. At the nexus of many physical mysteries

9. Two big questions

- a) Is dark energy something different than vacuum energy
- b) Does General Relativity self-consistently describe cosmic acceleration ?

10. Probing Dark Energy