

# The Born Investigator of the Heavens

## Jacobus Cornelius Kapteyn (1851–1922)

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Groningen, February 2015

Background

Short biography

Born investigator of the heavens?

Accidental astronomer?

First Groningen years

Cape Photographic Durchmusterung

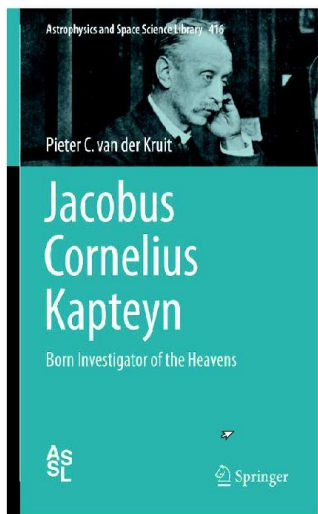
The Kapteyn Universe

# Background



- ▶ What I will be presenting is based on my [biography](#) of Kapteyn.
- ▶ Appeared in November 2014 ([©2015](#)) in the [Astrophysics and Space Science Library](#) of Springer.
- ▶ This makes it very expensive; unless your library subscribes to the relevant 'collection' of Springer.





2015, XXIV, 698 p. 296 illus., 99 illus. in color.

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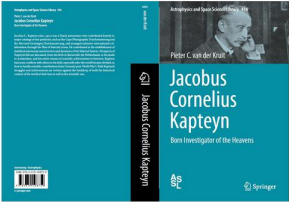
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university of Groningen / Faculty of Science and Engineering / Groningen Institute of Sciences / Institute for Astronomy / Kapteyn Institute  
working at the frontiers of knowledge / members van de Groninger van het wetten

## Jacobus Cornelius Kapteyn (1851 - 1922)



This Webpage accompanies a biography:

### Jacobus Cornelius Kapteyn: Born investigator of the Heavens

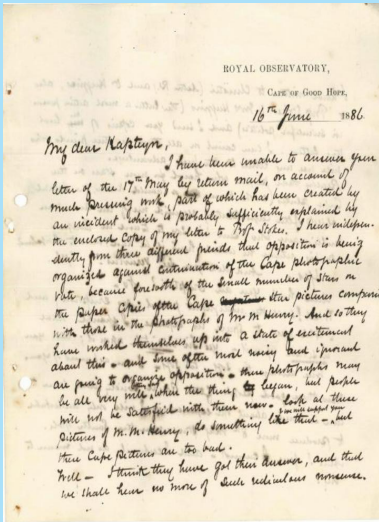
by Pieter C. van der Kruit,

to appear as 416 in the **Astrophysics and Space Science Library** of Springer Publishers, due November, 2014 (ISBN 978-3-319-10875-9). See also the [product flyer](#).

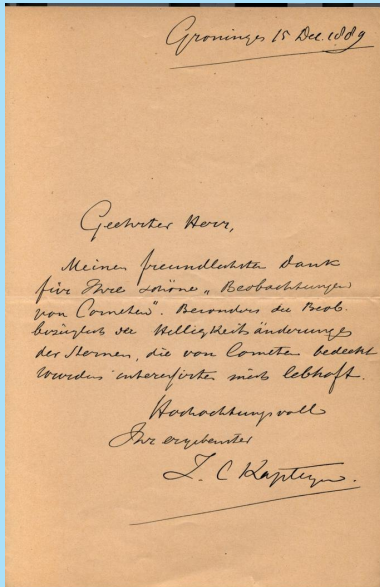
The biography and this Website are dedicated to Professor Adriaan Blaauw (1914–2010), who brought the Kapteyn Astronomical Laboratory as its third director back to the national and international forefront and encouraged me over a long period to write this biography after my formal retirement and –last but not least– to my wife Corry for her love and support and for her understanding that active professional life should not end at 65.

This page has been developed and is maintained by  
Prof. dr P.C. van der Kruit,  
Jacobus C. Kapteyn Distinguished Professor of Astronomy  
Kapteyn Astronomical Institute.

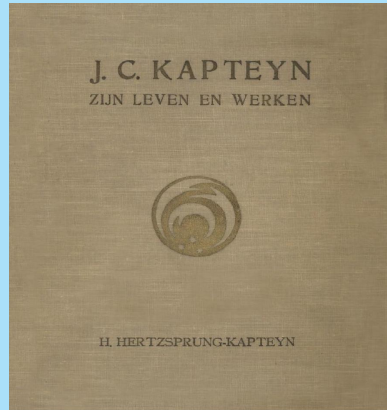
- ▶ I have designed a **special Webpage** to accompany the book.
- ▶ It provides access to any material on Kapteyn not protected by copyrights.
- ▶ Papers and publications of and about Kapteyn, Henriette Hertzsprung-Kapteyn's biography, letters from David Gill, etc.
- ▶ The URL is:  
[www.astro.rug.nl/JCKapteyn](http://www.astro.rug.nl/JCKapteyn)



- ▶ Almost all correspondence of Kapteyn is lost.
- ▶ Willem de Sitter and Johan Huizinga were contemplating writing a biography, but never did.
- ▶ Maybe Aernout de Sitter wanted to do this and shipped papers to Lembang.
- ▶ Everything presumable lost in Rotterdam bombing in 1940.
- ▶ We do have all letters by David Gill.
- ▶ And there are some Kladboeken left with his notes.



- ▶ There is correspondence of Kapteyn in [archives elsewhere](#).
- ▶ In 1999, [Petra van der Heijden](#) has made an inventory of this and obtained [copies](#).
- ▶ Some of this is also on the [Web](#).
- ▶ Mostly letters [by](#) Kapteyn rather than [to](#).
- ▶ Sometimes [drafts](#) or [carbon copies](#) of letters to Kapteyn.



- ▶ **Henriette Hertzsprung-Kapteyn** has written a **biography** in **1928**.

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ASTROPHYSICS AND  
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## THE LEGACY OF J.C. KAPTEYN

Studies on Kapteyn and the Development of  
Modern Astronomy

P.C. VAN DER KRUIT  
K. VAN BERKEL  
Editors



KLUWER ACADEMIC PUBLISHERS

- ▶ In 1999 Klaas van Berkel and I organized a Legacy symposium on Kapteyn.
- ▶ There were participants from all over the world.
- ▶ This is an important source for studies on Kapteyn.
- ▶ But expensive: 209\$, 140£, 166€ at Springer-site.

# 'Lieve Lize'

*De minnebrieven*

*van de Groningse astronoom J.C. Kapteyn  
aan Elise Kalshoven, 1878-1879*



*Klaas van Berkel  
en Annelies Noordhof-Hoorn*

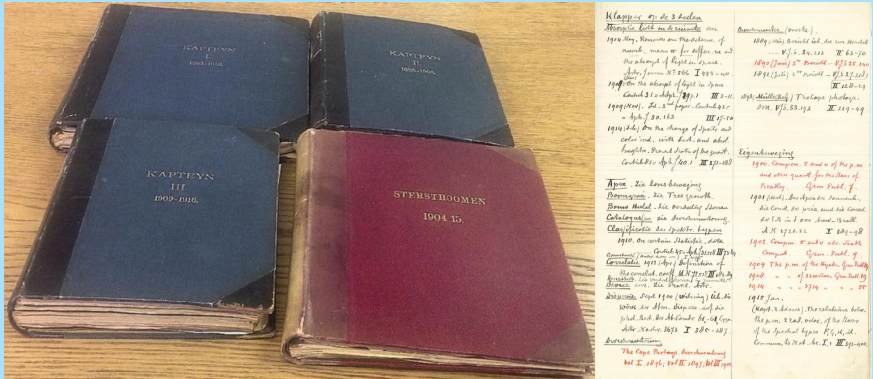
- ▶ **Klaas van Berkel** has found a set of **Love Letters** that Kapteyn wrote to his fiancée **Elise Kalshoven**.
- ▶ These started in **1878**, after Kapteyn was appointed professor in Groningen.
- ▶ It leads up to the time they married in **July 1879**.
- ▶ Most are transcribed in this book (in Dutch).



- ▶ In the **Kapteyn Room** in the **Kapteyn Astronomical Institute** we have copies of all his publications.
- ▶ Many of these are in **book** form (Catalogues, Groningen Publications).



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► But Kapteyn collected his reprints in bound volumes together with a systematic index.

## The Born Investigator of the Heavens

Simon Newcomb, *The Stars: A study of the Universe*<sup>1</sup> (1901).

*'This work of Kapteyn offers a remarkable example of the spirit which animates the born investigator of the heavens. Although the work was officially that of the British Government, the years of toil devoted to it were, as the writer understands, expended without other compensation than the consciousness of making a noble contribution to knowledge, and the appreciation of his fellow astronomers of this and future generations.'*

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<sup>1</sup>Footnote on page 49.

# Short biography

(traditional version)



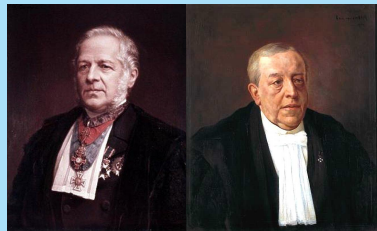
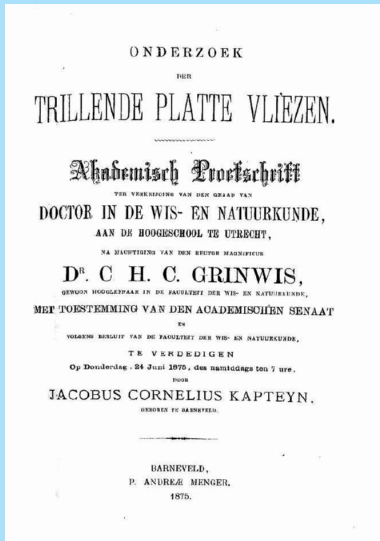
- ▶ Kapteyn was born on **January 19, 1851** in the municipality of **Barneveld**.
- ▶ In the middle of the '**Bible Belt**'.
- ▶ His parents were **Gerrit Jacobus Kapteyn** (1812–1879) and **Elisabeth Cornelia Koomans** (1814–1896).
- ▶ They ran a **boarding school** for boys.



- ▶ He was the tenth (not ninth) child of **fifteen**.
- ▶ This is a family reunion around **1877** or so.



- ▶ Kapteyn was educated at the boarding school of his parents.
- ▶ He always complained of a **lack of attention** by his parents.
- ▶ He enrolled at the **University of Utrecht** in **1868** to study **mathematics** and **physics**.



- ▶ He studied with C.H.D. Buys Ballot and C.H.C. Grinwis.
- ▶ And obtained his PhD in 1875 under Grinwis.
- ▶ The title was 'A study of vibrating, flat membranes'.



- ▶ In 1875 he was appointed observer at Leiden Observatory.
- ▶ The director was Hendricus G. van de Sande Bakhuyzen.
- ▶ The Observatory was mainly involved in positional astronomy.



- ▶ In 1877 he was appointed Professor of astronomy and theoretical mechanics at the University of Groningen.



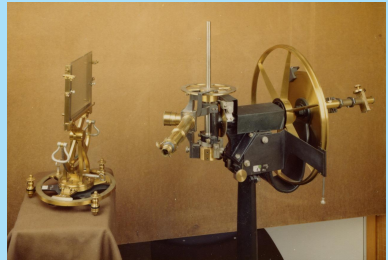
- ▶ The chair was a result of the Law on Higher Education of 1876.
- ▶ He took up his chair in 1878.
- ▶ He married Catharina Elisabeth Kalshoven (1855–1945) on July 16, 1879.



- ▶ In spite of many efforts he failed to obtain his own **observatory**.



- ▶ He heard about the efforts of **David Gill** at the **Royal Observatory at Cape of Good Hope** to produce a **photographic Durchmusterung**.
- ▶ He offered to **measure** Gill's plates and produce the **star positions and magnitudes**.
- ▶ The **Cape Photographic Durchmusterung** was published in three volumes in **1896, 1897** and **1900**.



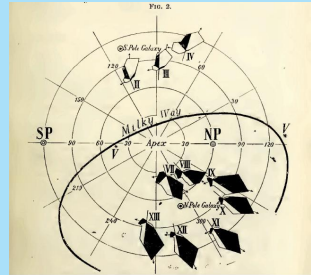
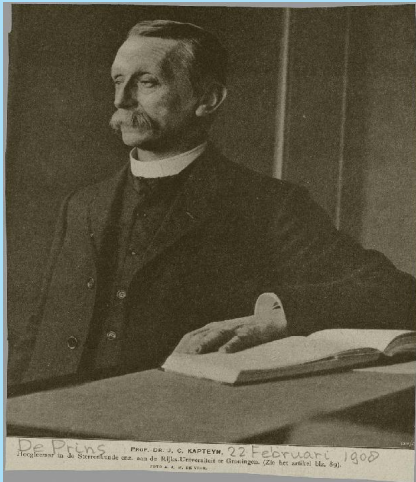
- ▶ He devised the **parallactic method** and measured the positions and magnitudes of **454,875** stars.
- ▶ He was given two small rooms in the laboratory of **G. Heymans**, professor of psychology and philosophy.



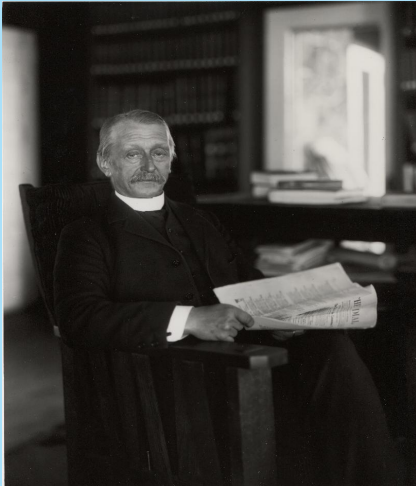
- ▶ Kapteyn devoted his career to the problem of the **Construction of the Heavens** or the **Structure of the Sidereal System**.
- ▶ He gave up measurement of direct **trigonometric parallaxes**.
- ▶ He used **proper motions** and made the assumptions that
  - ▶ **Luminosity curve everywhere the same.**
  - ▶ **Stellar motions in space have no preferred direction.**
  - ▶ **No interstellar absorption.**



- ▶ **Anders Donner** from **Helsingfors** provided him with many plates for both proper motions and parallax determinations.
- ▶ He had met Donner at the meeting of the **Carte du Ciel** in Paris in **1887**.

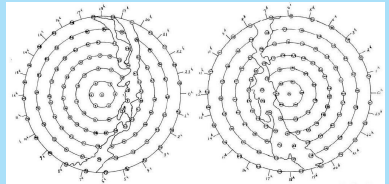
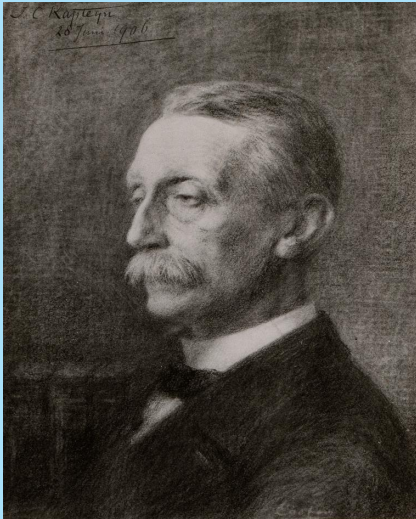


- ▶ However, Kapteyn discovered the **Two Star Streams**, showing two **preferred directions**.
- ▶ He first presented that at a Congress during the **1904 Louisiana Purchase Exposition**.

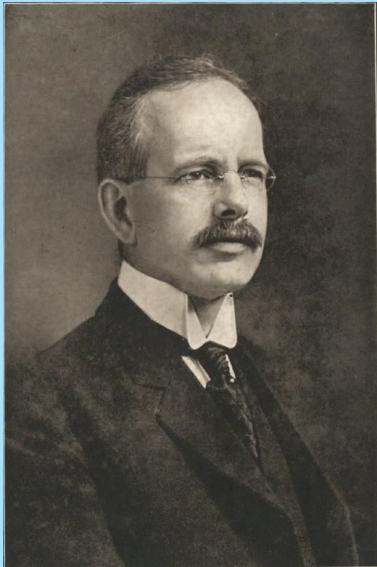


- ▶ The concept of Star Streams was quickly confirmed, a.o. by **Arthur Eddington**.
- ▶ **Karl Schwarzschild** proposed that the explanation was an **anisotropic velocity ellipsoid**.
- ▶ But the **stellar composition** of the two Streams was very different.
- ▶ The Streams had to be taken into account in the study of the distribution of stars in space.

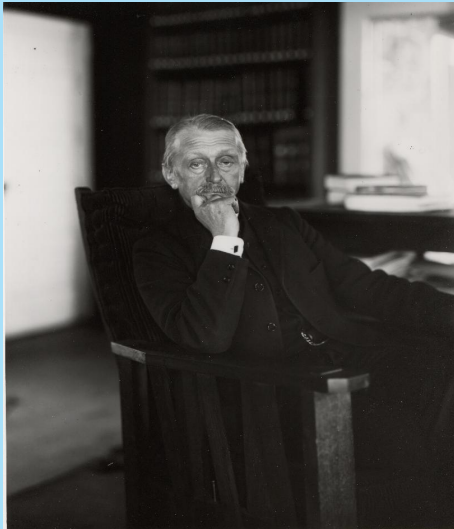




- ▶ He devised the **Plan of Selected Areas** after discussion with many colleagues.
- ▶ Eventually it became **220** areas in the '**Systematic Plan**' (+**46** in the '**Special Plan**').
- ▶ All **measurable** properties of stars should be determined.



- ▶ In St. Louis he met **George E. Hale** of the **Mount Wilson Observatory**
- ▶ Kapteyn was appointed **staff associate** for three months/year.
- ▶ He went to Mt. Wilson each year from **1908** to **1914**.



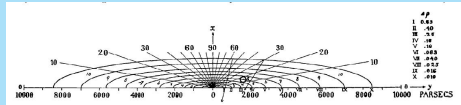
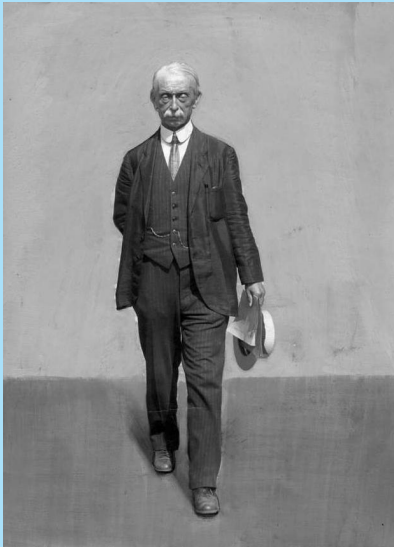
- ▶ **Hale** adopted the Plan as the prime program for his new Mount Wilson **60-inch**.
- ▶ The **star counts** in the Selected Areas project did come along well.
  - ▶ **Harvard-Groningen** with **Pickering** (1918/23/24): all sky down to **mag. 16**.
  - ▶ **Mt. Wilson-Groningen** with **Seares** (1930): north down to **mag. 19**.
- ▶ Supplemented with **radial velocity studies** by **Adams** (MtW).



JACOBUS CORNELIUS KAPTEYN

(Fotografie door ALBERT KAPTEYN)

- ▶ The problem Kapteyn worried about very much was that of **extinction** or **absorption** by interstellar dust.
- ▶ He deduced it would produce **reddening** and found (**1909**) a reasonable  $\sim 0.3 \text{ mag/kpc}$  (also **van Rhijn's** PhD thesis).
- ▶ Could be due to correlation **color-absolute magnitude**.
- ▶ **Shapley** showed (**1916**) space was **transparent** towards **M13**.



- ▶ In the end he produced the **Kapteyn Universe**, which had the Sun close to the center.
- ▶ He did derive a correct **vertical** distribution.
- ▶ Using velocities he laid the foundations for studies of **galactic dynamics**.
- ▶ First determination of **local mass density**.



- ▶ Kapteyn introduced the concept of the **astronomical laboratory**.
- ▶ This was listed by **Baillaud**, first IAU president in **Rome** in **1922** as **one of the three most important recent developments**.
- ▶ The other two were **astronomical photography** and **giant telescopes**.
- ▶ This was quoted by **de Sitter**, but rather overinterpreted.



- ▶ After retirement, Kapteyn became parttime adjunct-director in Leiden.
- ▶ The Kapteyns first stayed with their daughter in Amsterdam and bought a house in Hilversum.

- ▶ Kapteyn never lived there; after a prolonged illness he died in Amsterdam on June 18, 1922.

# Born investigator of the heavens?

(Misconceptions about Kapteyn)



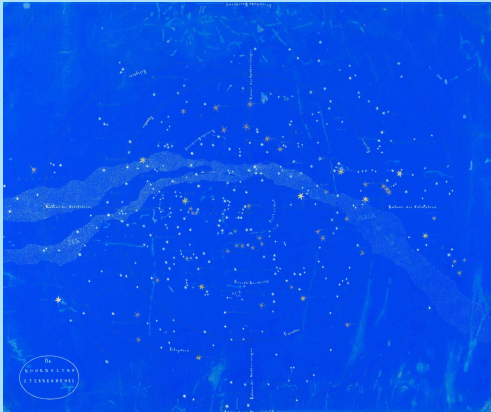
## Accidental astronomer?

- ▶ It is usually stated that Kapteyn by **accident** entered astronomy.
- ▶ **Adriaan van Maanen**<sup>2</sup> in his obituary:
  - ▶ *'... his doctoral thesis was in physics: "Onderzoek der Trillende Platte Vliezen".*  
*Just at this time, however, the position of observer at the Leiden Observatory was vacant, and Kapteyn applied for and obtained the position.*  
*By this accidental circumstance astronomy secured the privilege of counting Kapteyn as one of its workers and before long as one of its foremost leaders.'*
- ▶ Or **Sir James Jeans**<sup>3</sup>:
  - ▶ *'It would appear that during his student days Kapteyn was not particularly attracted to astronomy, ...'*

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<sup>2</sup>Astrophysical Journal 56, 145-153 (1922).

<sup>3</sup>Monthly Notices Royal Astronomical Society 83, 250 (1923).

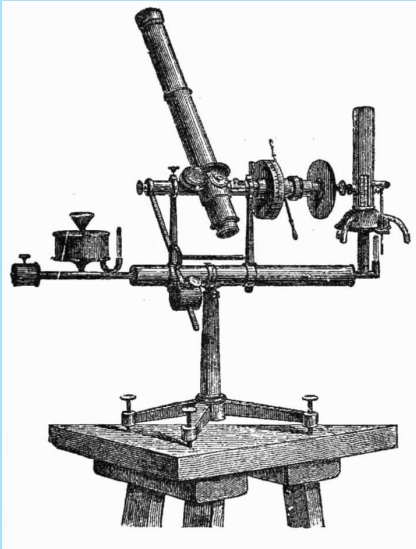


- ▶ There is evidence that Kapteyn as a **child** already had a special interest in astronomy.
- ▶ As a boy of **14** he made a **starmap** after his older sister had given him a star globe.
- ▶ HHK says:  
*‘When his father noted how seriously he studied the stars, he bought a large telescope for him, that was erected in the attic room and with which he very diligently observed the stars.’*

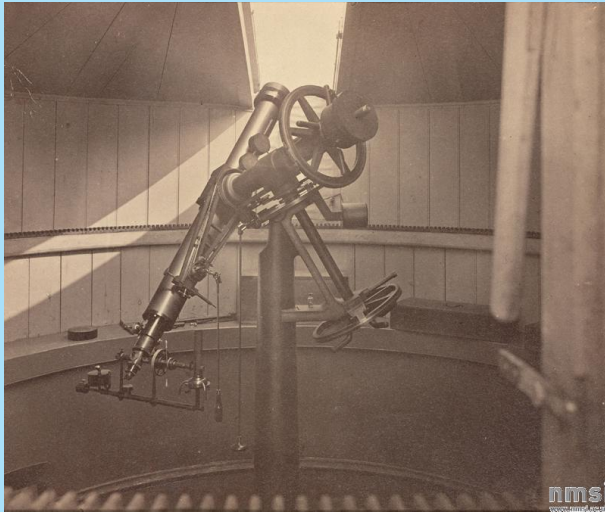


- ▶ Various sources, including a brochure of the boarding school, mention that 'Benno' had an 'observatory'.

- ▶ His PhD thesis had 18 'Stellingen' (propositions); no less than 7 of these are on astronomy.
- ▶ For example:
  - ▶ *'XV. The average proper motion of stars of different magnitude is not inversely proportional to their distance.'*
- ▶ He must have read about this or hypothesized about it and probably tried it on real data.
  - ▶ *'X. The best photometer is that of Zöllner.'*
- ▶ So he knew what a Zöllner photometer was and might even have used one.



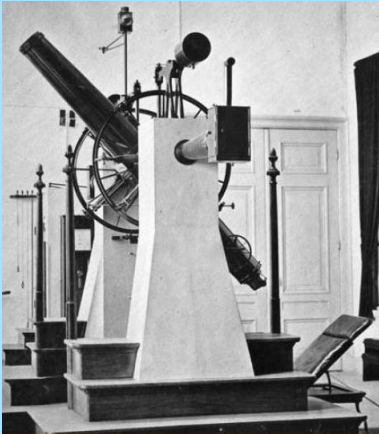
- ▶ The photometer was developed in 1858 by J.K.F. Zöllner and widely used from the 1860s onwards.
- ▶ It projected the light of a Bunsen burner through an adjustable set of polarizing plates.
- ▶ Utrecht Observatory had one, probably already at Kapteyn's time.



- ▶ A Zöllner photometer on the telescope at Pulkovo Observatory.



- ▶ **Buys Ballot** was first responsible for astronomy teaching and supervised one astronomical thesis (1871).
- ▶ In **1856 J.A.C. Oudemans** was appointed, but he left to Dutch Indies (as geographer) in **1857**.
- ▶ Eventually **M. Hoek** was appointed for astronomy teaching (**1859**).
- ▶ He was mostly interested in ether experiments and had **no PhD students**.
- ▶ He also had a poor health and died in **1873**.
- ▶ Oudemans came back as professor of astronomy in **1875**.



- ▶ So, Kapteyn had **no option** for an astronomy thesis in Utrecht.
- ▶ How did he get appointed in Leiden?
- ▶ The 'Sterrewacht' had **H.G. van de Sande Bakhuyzen** as director, and **K.W. Valentiner** and **E.F. van de Sande Bakhuyzen** as 'observator'.
- ▶ In **1875** Valentiner became director in Mannheim, creating a **vacancy** in Leiden.





- ▶ The course of events is as follows:
  - ▶ **June 22, 1875.** Van de Sande Bakhuyzen informs curators that Valentiner will be leaving.
  - ▶ **July 28, 1875.** Curators write that Minister awaits his proposals.
  - ▶ **August 10, 1875.** Van de Sande Bakhuyzen proposes that his brother become first and **J.C. Kapteyn** second observer.
  - ▶ **September 29, 1875.** Curators write that Minister has given honorable **discharge** to Valentiner and **appoints** the two observers as requested.
- ▶ Apparently not much happened between August 10 and September 29.

- ▶ From van de Sande Bakhuyzen's letter to Leiden University Curators of **August 10, 1875**:
  - ▶ *'... Dr. J.C. Kapteyn has been working for some time at my request at the Observatory, so that what he accomplishes here would make it possible to form an opinion on his suitability for the duties of an observator at the Observatory. As a result of the experience I had with him, I believe I can decide that, although he is not capable yet in all cases to perform the tasks that can be demanded from an observator, this will be the case in not too long a period, so that from the various candidates that are considered for this position, he should be recommended as the best.'*
- ▶ Apparently there were **more candicates** and Kapteyn had been on **trial on a temporary basis**.

- ▶ There is an unusual exchange of letters *directly* between the Minister and van de Sande Bakhuyzen.
- ▶ **September 21, 1875.** The Minister suggests that maybe **Dr. W. Gleuns** should be considered as well for the position.
- ▶ After all, Gleuns had been involved in calculations for van de Sande Bakhuyzen and was looking for a job.
- ▶ Curators have proposed Kapteyn *without argumentation*, *'which for a nomination like this is really very little'*.
- ▶ **September 22, 1875.** Van de Sande Bakhuyzen writes back *immediately*.
- ▶ Draft unreadable, but original in **National Archives**.

Afgestaan D. G. Glans staat D. J. Kapteyn. Gedrukt  
op schooltijd te Utrecht heeft hij niet daer, vooral de gelegenheid  
niet te hebben, op de Sterrenkunde te volgen en met de instrumenten  
op de Sterrenwacht te Groningen, zodat hij later bij zijn opvoeding was  
in het gebruik der kleine ~~instrumenten~~ astronomische metho-  
den. Het vorig jaar had hij plan om tot voortzetting zijner  
studien aan de Sterrenwacht te Leiden te komen werken, doch  
financieel bemannende beletten dit, de Heer Kapteyn bleef toen te  
Utrecht en promoveerde aldaar in Januari dit jaar op een  
veel <sup>dat niet over de sterren</sup> goede disputati. Toen nu door de benoeming van D. Valentijn  
een vacature ontstond door de afdeling van de Heer Kapteyn  
als een de-candidaten voor de betrekking van observator, en de  
zeer gunstig berichten, die ik om zijn bevoentens de Hoogleraar  
Bouys Ballot en Grunow ontbreekt hem vernamen, brachten en  
my verhoer toe om den Heer Kapteyn uit te noodigen hier  
enigen tijd aan de Sterrenwacht te komen werken, ten einde

- ▶ Van de Sande Bakhuyzen strongly **opposes** Gleuns as being a mathematician with no affiliation to astronomy.
- ▶ From **September 22, 1875** letter:
  - ▶ *'Vis-a-vis Dr. Gleuns we have Dr. Kapteyn. During his studies in Utrecht he has, as much as opportunities allowed, devoted himself to astronomy and has observed with instruments at the observatory so that he obtained considerable familiarity with the use of astronomical apparatus. Last year he took up the plan to continue his studies at the Observatory in Leiden, but financial considerations prevented this. Mr. Kapteyn did stay in Utrecht and obtained his degree there in June of this year with a very good thesis.'*
- ▶ So, Kapteyn had earlier contacted van de Sande Bakhuyzen and even tried to do an **astronomical PhD thesis in Leiden**.

- ▶ Van de Sande Bakhuyzen continues:
  - ▶ *'When the appointment of Dr. Valentiner created a vacancy, I immediately thought of Mr. Kapteyn as one of the candidates for the position of observator and the very positive words I received from his professors Buys Ballot and Grinwis about him made me decide to invite Mr. Kapteyn to work at the Observatory in order to decide to what extent he was a suitable candidate for the position of observator. Mr. Kapteyn accepted this offer and worked here for about 3 months, during which time he has completely confirmed the favorable expectations I initially had of him. Although he is not yet familiar with all the observing techniques he will have to perform, he has shown not to be second to any more experienced astronomer.'*
- ▶ Van de Sande Bakhuyzen had invited Kapteyn to come to Leiden for a **trial period**.

- ▶ Kapteyn had an interest in astronomy from a **young age** onward.
- ▶ Kapteyn did **as much astronomy as possible** in Utrecht, but could not do a PhD thesis there.
- ▶ Kapteyn tried to **move to Leiden** to do a thesis, but was prohibited by finances.
- ▶ Van de Sande Bakhuyzen thought of Kapteyn, when **Valentiner** left.
- ▶ Kapteyn actually worked **on trial** basis in Leiden for a few months.
- ▶ **Kapteyn certainly did not enter astronomy 'by accident'.**

## First Groningen years

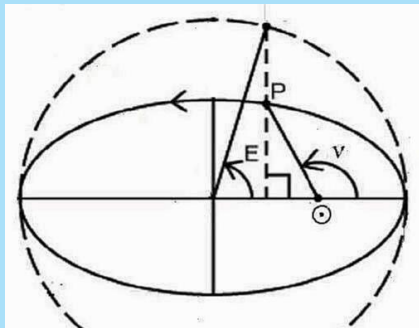
- ▶ It is often implied that Kapteyn, after going to Groningen, produced **little original, astronomical work**.
- ▶ Again **Adriaan van Maanen**:
  - ▶ *'Lack of an opportunity for observational work was, however, keenly felt by Kapteyn during the early years of his professorship, and he requested Professor H.G. van de Sande Bakhuyzen to let him use the meridian circle of Leiden Observatory during his vacations. The request was granted and Kapteyn planned a careful program for the observation of stellar parallax.'*
- ▶ But that was only 1885 (while appointed 1878).
- ▶ Other obituaries also leave the impression **nothing worth mentioning** was accomplished in this interval.



- ▶ From the **HHK biography**:
  - ▶ *'Kapteyn suffered under the impossibility to bring his scientific plans to reality and was always looking for things to do with his hands or his head. He collaborated in those days with his brother Willem, the mathematician from Utrecht.'*
  - ▶ *'He was also busy with meteorologic studies and he traveled to Worms and to Paris in order to do research on the growth of trees in relation to the climatic circumstances.'*
  - ▶ *'But all this did not satisfy him. It was only child's play and he wanted to do something much greater and he knew he was able to do that. Then, suddenly the solution came and it gave a entirely new direction to his life.'*

## 1. Kepler's equation

Solve for  $E$  in  $M = E - e \sin E$ .



- ▶ For orbits in the Solar System:

$$M = \frac{2\pi}{P}(t - T_0),$$

$$\tan\left(\frac{E}{2}\right) = \sqrt{\frac{1-e}{1+e}} \tan\left(\frac{\nu}{2}\right)$$

- ▶ This was **very time consuming**.
- ▶ But important not to lose newly discovered **asteroids** and **comets**.

## UEBER DAS KEPLERSCHE PROBLEM.

VON PROFESSOR J. C. KAPTEYN.

In diesem Aufsätze wird eine Reihe entwickelt für die Lösung des Keplerschen Problems, die für alle Planetenbahnen, auch die am meisten excentrischen, ausserordentlich convergent ist. Diese Convergenz ist so gross, dass eine *directe* Berechnung der excentrischen Anomalie, mit Zuhilfenahme einer mässig grossen Tafel eben so bequem, oder sogar noch etwas bequemer wird, als nach den gebräuchlichen Näherungsverfahren. Aber auch abgesehen von der Frage, in wiefern diese Lösung für den Praxis zu empfehlen ist, möchte die Reihe vielleicht nicht ohne Interesse sein.

Es sei  $M$  die mittlere,  $E$  die excentrische Anomalie,  $e$  die Excentricität,  $\Delta E = E - M$ ,

$$R = \frac{e \sin M}{1 - e \cos M}, \quad T = \frac{e \cos M}{1 - e \cos M}.$$

Die erwähnte Reihe wird dann erhalten, wenn man  $E - M$  entwickelt nach den steigenden Potenzen entweder von  $\cotang M$  oder von  $T$ . Das Ergebnis der ersten Entwicklungslart wird man in die folgende Form bringen können—

$$(1) E - M = a + \cotg M \left[ -\frac{1}{6} a^3 + \frac{11}{120} a^5 - \frac{337}{3040} a^7 + \frac{16711}{362880} a^9 - \frac{1273301}{39316800} a^{11} + \frac{139633707}{6227037600} a^{13} - \dots \right] \\ + \cot^3 M \left[ +\frac{1}{12} a^3 - \frac{13}{176} a^5 + \frac{7517}{60480} a^7 - \frac{228199}{1814400} a^9 + \frac{9528949}{79332000} a^{11} - \dots \right] \\ + \cot^5 M \left[ -\frac{1}{48} a^5 + \frac{161}{864} a^7 - \frac{166349}{507200} a^9 + \dots \right] \\ + \cot^7 M \left[ +\frac{55}{1296} a^7 - \frac{403}{3240} a^9 + \dots \right] \\ + \dots$$

wo—

$$(2) a = R \cos a$$

Es ist daher  $a$  immer kleiner (in absoluten Werth) als  $\frac{e \sin M}{1 - e \cos M}$ .

In eine Reihe entwickelt ergibt sich für  $a$ —

$$(3) a = R - \frac{1}{3} R^3 + \frac{13}{24} R^5 - \frac{541}{720} R^7 + \frac{9509}{8604} R^9 - \frac{7231801}{3693800} R^{11} + \dots$$

Wird dieser Werth für  $a$  in (1) eingeführt, so ist die erhaltene Reihe in Wirklichkeit nicht verschieden von einer Reihe, die schon von Keill

- ▶ Kapteyn proposed a new series expansion.
- ▶ He published it in *Copernicus* in 1883.
- ▶ However, gain was modest (if there was any gain at all).

## 2. Higher order sine functions.



- ▶ His older brother **Willem Kapteyn** also studied in Utrecht under Grinwis (but thesis on vibrating **plates**).
- ▶ Appointed same day **professor of mathematics** in Utrecht.
- ▶ Together they extensively studied **higher order sine functions**.
- ▶ That was more Willem's interest, so Jacobus' contribution probably small.
- ▶ Ironic: **Kapteyn series** useful for Kepler's equation.

## Regular sine functions.

$$\sin x = \sum_{n=0}^{\infty} \frac{(-1)^n x^{2n+1}}{(2n+1)!} = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \dots$$

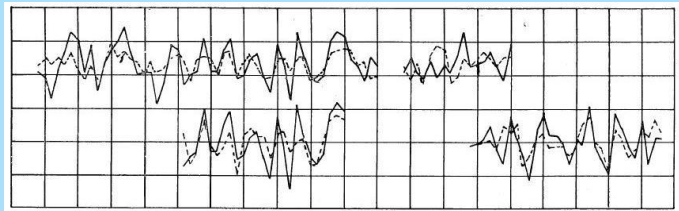
$$\cos x = \sum_{n=0}^{\infty} \frac{(-1)^n x^{2n}}{(2n)!} = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \dots$$

## Higher order sine functions.

$$\varphi_{\mu}(x) = \sum_{n=0}^{\infty} \frac{x^{kn+\mu}}{(kn+\mu)!} = \frac{x^{\mu}}{\mu!} + \frac{x^{\mu+k}}{(\mu+k)!} + \dots$$

$$\psi_{\mu}(x) = \sum_{n=0}^{\infty} \frac{(-1)^n x^{kn+\mu}}{(kn+\mu)!} = \frac{x^{\mu}}{\mu!} - \frac{x^{\mu+k}}{(\mu+k)!} + \dots$$

### 3. Tree rings.



1770

1880

- ▶ He looked for meteorological equivalents of **Saros cycles**.
- ▶ However, **meteorological records** were very too sparse and too recent, so he used **tree rings** to extend time sequence.
- ▶ He did find a correlation with number of **wet days** and periodicity of **12.4 years** (unrelated to solar cycle).
- ▶ First published in **1909** in *Pasadena Star News*.

## 4. Absolute declinations.

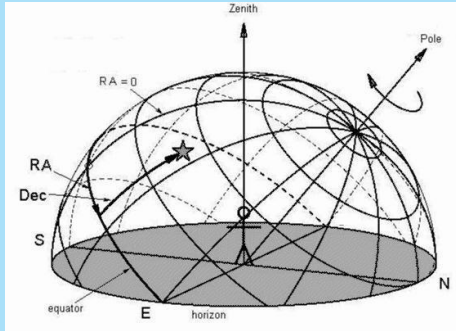
- ▶ Declinations (and polar height) were very inaccurate.
- ▶ Due to unknown amounts of flexure in the telescope and refraction ('bending') of light in the atmosphere.
- ▶ Another *Copernicus* paper in 1883:

UEBER EINE METHODE DIE POLHÖHE MÖGLICHEST FREI VON  
SYSTEMATISCHEN FEHLERN ZU BESTIMMEN.

VON PROFESSOR J. C. KAPTEYN.

### I. Einleitung.

Es ist eine sehr bekannte Sache, dass zwischen den Resultaten für die Declinationen der Fundamentalsterne, welche an verschiedenen, auch der best ausgestatteten Sternwarten, erhalten werden, Unterschiede bestehen, die weit ausser den Grenzen liegen, welche man, in Rücksicht auf die Uebereinstimmung der einzelnen, an der nämlichen Sternwarte angestellten Beobachtungen, erwarten müsste. Diese Erscheinung ist vermuthlich dem Zusammenwirken mehrerer Ursachen zuzuschreiben, und es verdienen hier wahrscheinlich das Mangelhafte unserer Kenntniss der Strahlenbrechung und der Biegung des Rohres und der Kreise in erster Linie genannt zu werden. Besonders auch in den letzten Jahren



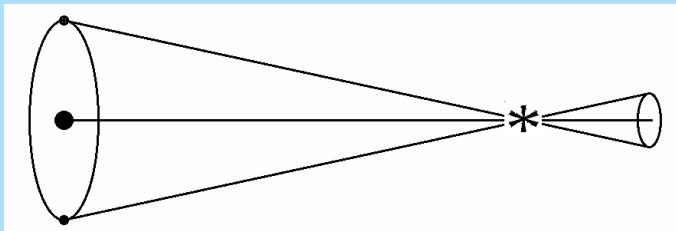
- ▶ Classical method; Measure **declination** (Decl) and **right ascension** (RA) from altitude and time of **meridian passage**.
  - ▶ **Height (altitude) of the pole** from altitude of two passages of **circumpolar stars**.
- ▶ Kapteyn's method involved measuring only **azimuths** and **timing of prime vertical passage** or altitude **differences** of two stars with roughly same altitude at the meridian.



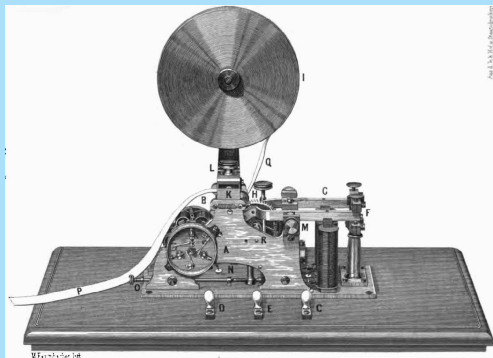


- ▶ Van de Sande Bakhuyzen allowed Kapteyn test the idea with the **Universal Instrument** at Leiden.
- ▶ This was during the summer of **1882**.
- ▶ The method was shown to work and paper was published in **1883**.

## 5. Trigonometric parallaxes.



- ▶ Kapteyn started a program to measure **annual parallaxes** by **differential meridian timing** measurements.
- ▶ This was felt to be too difficult.
- ▶ If **parallax** is **0.1 arcsec** and its **declination** **50°**, then parallax corresponds to **time difference** of **0.02 seconds of time**.



- ▶ So you need **extremely accurate** timings.
- ▶ Only possible with **many repeated** measurements.
- ▶ Kapteyn used a 'Registrier-Apparat' or strip recorder on the Leiden meridian circle (spring **1885**, Christmas 1885 & **1886**, and spring **1887**).

- ▶ He selected **15** stars with high **proper motion** that may be not too distant.
- ▶ Results published in **Astronomische Nachrichten** (preliminary) in **1889** and in **Annalen van de Sterrewacht te Leiden** in **1891**.

Star	$\rho_{\text{Kapteyn}}$ milli-arcsec	HD	$\rho_{\text{modern}}$ milli-arcsec	Remarks
BB VII 81 (pr.)	$74 \pm 27$	79210	$172.06 \pm 6.31$	Flare star; binary
		79211	$156.45 \pm 8.58$	Flare star; binary
$\theta$ Ursa. Maj.	$52 \pm 26$	82328	$74.19 \pm 0.16$	Spectroscopic binary
BB VII 85	$64 \pm 22$	84031	$54.89 \pm 0.92$	Variable star
20 Leon. Min.	$62 \pm 29$	86728	$66.46 \pm 0.32$	High proper-motion star
BB VII 89	$176 \pm 24$	88230	$205.21 \pm 0.34$	Flare star
BB VII 94	$101 \pm 26$	90508	$43.65 \pm 0.43$	High proper-motion star
BB VII 95	$38 \pm 27$	91347	$26.48 \pm 0.59$	High proper-motion star
Lal. 20670	$-6 \pm 28$	92855	$26.84 \pm 0.50$	Star in double system
BB VII 104	$428 \pm 30$	95735	$392.64 \pm 0.67$	Flare star
BB VII 105	$168 \pm 27$	–	$206.27 \pm 1.00$	High proper-motion star
BB VII 110	$30 \pm 27$	101177	$43.01 \pm 0.73$	Spectroscopic binary
BB VII 111	$16 \pm 32$	102158	$20.29 \pm 0.70$	Star in double system
BB VII 112	$139 \pm 26$	103095	$109.99 \pm 0.41$	High proper-motion star
BB VII 114	$-28 \pm 42$	104556	$17.5 \pm 0.51$	High proper-motion star
BB VII 119	$56 \pm 34$	105631	$40.77 \pm 0.66$	High proper-motion star

This really is very, very good!!

## Cape Photographic Durchmusterung

- ▶ The usual view is that Kapteyn one day read a paper by David Gill, who was planning a southern photographic Durchmusterung from the Cape, and that this made him decide impulsively to offer his help, and that this, for Gill, came completely out of the blue.
- ▶ **Henriette Hertzsprung-Kapteyn:**
  - ▶ *'During the Christmas holidays of 1885 he read in Leiden in an astronomical journal an article by David Gill, Her Majesty's astronomer at Cape of Good Hope, about a major project he wanted to undertake. He was planning to produce a catalog of the stars in the southern hemisphere down to magnitude 10 and using photographic methods.'*
  - ▶ *'Instantly, the thought occurred to Kapteyn: 'Here is my chance!' He immediately wrote to Gill and offered to collaborate with him.'*



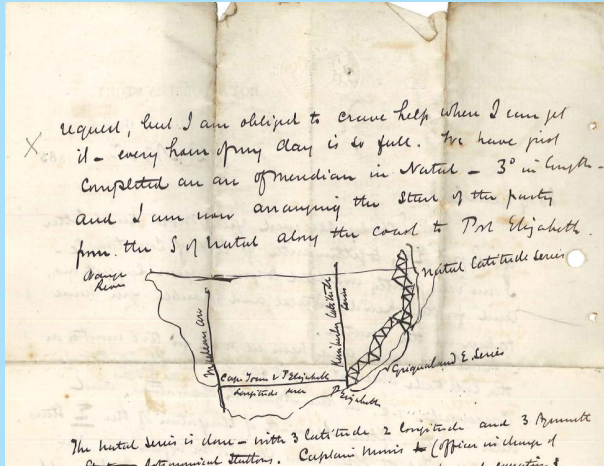
## Actually:

- ▶ On **April 30, 1884** Kapteyn had written to Gill and sent him his *Copernicus* paper on polar height and Gill answered on **September 12, 1884**.
- ▶ Kapteyn asked Gill to **work together** on a project to measure the altitude of the pole from the Cape.
- ▶ Gill agreed and Kapteyn sent a list of suitable stars on **December 10, 1884** and Gill answered on **January 18, 1885** (18 pages) laying out an observing strategy.
- ▶ The **Annual reports of the Royal Observatory at Cape of Good Hope** mentions ongoing observations between **1885** and **1890**.
- ▶ No real publication has resulted, but they corresponded and collaborated **well before the CPD**.

- ▶ Gill early on discusses his plans for a Durchmusterung with Kapteyn.
- ▶ On April 3, 1885:
  - ▶ *'I shall, I hope, write you next mail on some other points. Meanwhile I send you some of our first attempts in producing a photographic Durchmusterung of the southern Heavens. I hope to improve very greatly on this attempt. If you have any suggestions to give me on the best plans of measurement I shall be glad and grateful to have them. An accuracy of  $\pm 0.2$  would be ample.'*

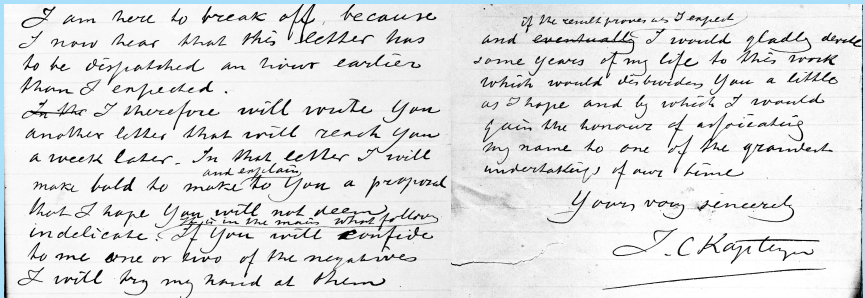


- ▶ On **May 15, 1885**:
  - ▶ *'We have now nearly 200 pictures towards a photographic Durchmusterung, each about  $6^\circ$  on the side. The plans of measurement & reduction I am still considering, and should greatly value your suggestions. I have not yet decided whether to adopt a system of position angles and distances or rectangular coordinates. I should be glad if you could think this matter over as to which presents the simplest method for converting measures into RA & Decl. with an accuracy of  $0'.2$  on the great circle.'*
- ▶ This is all really very close to **solliciting Kapteyn's help**.



- ▶ Gill on **November 2, 1885**:
  - ▶ *'I would ask you a great favour, to enter all your alterations, corrections and suggestions in red ink upon the lists I sent you, and return them to me. I will then send you a clean copy of the finally adopted list. It may seem to you absurd to make such a request, but I am obliged to crave help where I can get it – every hour of the day is so full.'*
  - ▶ *'So do not think I am neglecting astronomy. I am only rather overbusy at present, and would ask you to assist me in the way I propose.'*

- ▶ Kapteyn took the bait on **December 16, 1885**:



The image shows two pages of handwritten text. The left page contains the main body of a letter, and the right page contains a postscript and a signature. The handwriting is in cursive and appears to be from the late 19th century.

I am here to break off, because I now hear that this letter has to be despatched an hour earlier than I expected.

~~In the~~ I therefore will write you another letter that will reach you a week later. In that letter I will make bold to <sup>and explain</sup> make to you a proposal that I hope you will not deem indelicate. <sup>It is in the main what follows</sup> If you will confide to me one or two of the negatives I will try my hand at them.

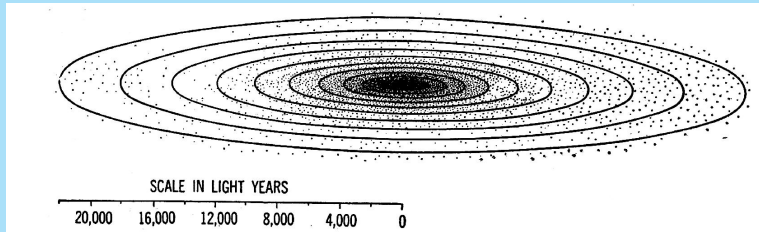
*if the result proves as I expect and eventually I would gladly devote some years of my life to this work which would disturb you a little as I hope and by which I would gain the honour of associating my name to one of the greatest undertakings of our time*

Yours very sincerely  
J. C. Kapteyn

- ▶ Kapteyn wrote:
  - ▶ *'If you will confide to me one or two of the negatives I will try my hand at them, and, if the result proves as I expect, I would gladly devote some years of my life to this work, which would disburden you a little, as I hope, and by which I would gain the honour of associating my name with one of the grandest undertakings of our time.'*
- ▶ This was written in a hurry and he promises to write more very soon.
- ▶ He asked van de Sande Bakhuyzen for advice, who tried to **discourage** Kapteyn.

- ▶ Kapteyn wrote Gill again on **December 23, 1885**:
  - ▶ *'Now, after your success in Stellar photography, and especially after your letter in which you tell me "I am obliged to crave help where I can get it," it has occurred to me that by measuring and reducing your photographs I could contribute very effectually towards the success of an enormous and eminently useful undertaking.'*
- ▶ Kapteyn's astronomical work on **absolute declinations and polar altitudes** was the key in establishing collaboration with Gill.
- ▶ Gill then succeeded in enlisting Kapteyn for his photographic Durchmusterung.

# The Kapteyn Universe



The **Kapteyn Universe** (coined by Jeans) was presented in two papers in **1920** and **1922**:

- ▶ **On the Distribution of the Stars in Space Especially in the High Galactic Latitudes** by Kapteyn and van Rhijn.<sup>4</sup>
- ▶ **First Attempt at a Theory of the Arrangement and Motion of the Sidereal System** by Kapteyn.<sup>5</sup>

<sup>4</sup>Ap.J. 52, 23-38, 1920; also Contr. Mt. Wilson Obs., No. 188.

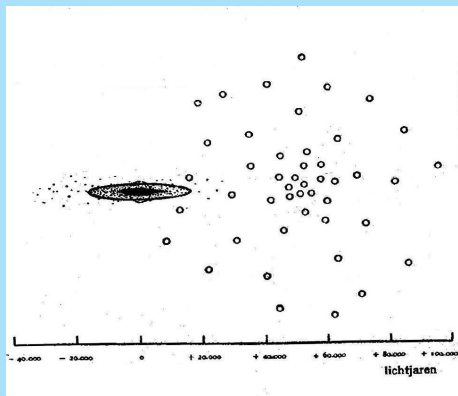
<sup>5</sup>Ap.J. 55, 302- 328, 1922; also Contr. Mt. Wilson Obs., No. 230.





- ▶ Kapteyn and van Rhijn (1920) presented a model for the distribution of stars in space.
- ▶ Kapteyn (1922) presented a model for its dynamics ('mechanics').

- ▶ Vertical dynamics based on random motions: correct.
- ▶ Horizontal based on rotation + random motions: incorrect.



(Figure from de Sitter, attributed to Oort.)

- ▶ This contrasted with Harlow Shapley's globular cluster distribution
- ▶ Kapteyn had neglected interstellar absorption; system had diameter of  $\sim 15$  kpc.
- ▶ But Shapley's distances too large also because of absorption; center at  $\sim 20$  kpc.
- ▶ Often seen as winner-loser:

- ▶ Kapteyn's Universe was wrong because of his unfounded neglect of interstellar extinction, in contrast to Harlow Shapley's brilliant work on globular clusters.

- ▶ Jan Hendrik Oort's 1926 acceptance lecture as 'privaat-docent' in Leiden: *Non-light-emitting matter in the Stellar System.*<sup>a</sup>
- ▶ Assumption of absorption in space the 'least contrived' solution to Shapley – Kapteyn disagreement.

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<sup>a</sup>Openbare les: '*Niet-lichtgevende materie in het sterrenstelsel*'.



Jan and Mieke Oort after thesis defense.

- ▶ Oort found differential rotation and the Oort constants in 1928.
- ▶ Improved Kapteyn's analysis to derive the Oort limit in 1932.

What would have happened had Kapteyn lived an extra 10 years?

- ▶ Kapteyn worried very much about **extinction**, and wrote **four papers** on this (1 in A.J. and 3 in Ap.J.)
- ▶ In **1904** **George Comstock** had deduced from the **star ratio** that absorption was very strong.
- ▶ He deduced **0.18 mag per unit distance** (corresponds to parallax of  $0''.1$ ), or **18 mag/kpc**.
- ▶ Kapteyn **agreed** there was extinction.
- ▶ From luminosity curve as a function of distance he found much **less** than Comstock.
- ▶ Sun in **special position** (local **minimum**) if Comstock were right.
- ▶ In **1909** Kapteyn proposed that **scattering means reddening**.
- ▶ Deduced **0.003 mag per unit distance** in photographic band.
- ▶ Actually **not too bad** compared to present.



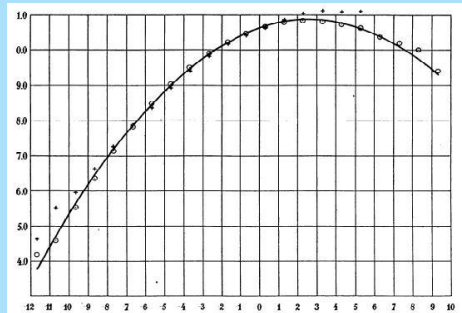
Piet van der Kruit

- ▶ The turning point came with Shapley's 1916 work on M13.
- ▶ If Kapteyn were correct, the stars should be 2.5 magnitudes redder than observed.
- ▶ Shapley concluded that space was transparent.
- ▶ This was widely accepted as the final word.

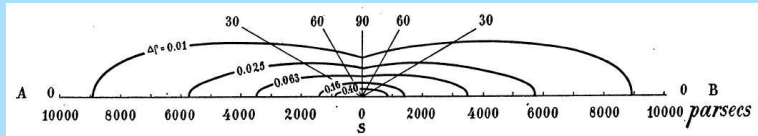
► Kapteyn & van Rhijn  
(1920):

*'Now that, after so many years of preparation, our data seem at last to be sufficient for the purpose, we have been unable to restrain our curiosity and have resolved to carry through completely a small part of the work ...'*

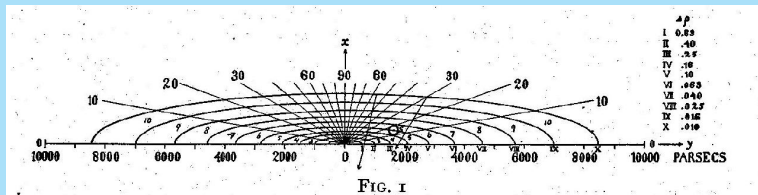
► First determined the **luminosity curve**.



Kapteyn hated the 'ugly' term **parsec**, but did adopt it and redefined **absolute magnitude** to distance of 1 pc.

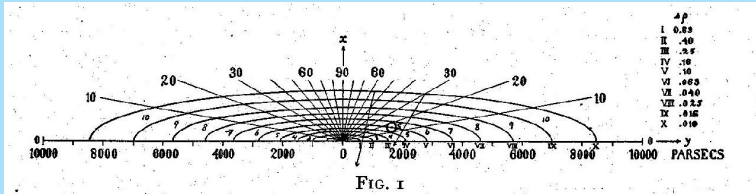


- ▶ Kapteyn & van Rhijn (1920):
- ▶ Solved counts for star density as function of distance from Sun.
- ▶ Performed this process for latitudes  $0^\circ$ ,  $30^\circ$ ,  $60^\circ$  and  $90^\circ$ .
- ▶ Resulting system had radius of **9 kpc**, but based on extrapolations..



- ▶ Kapteyn's (1922): *'First attempt at a theory of the arrangement and motion of the Sidereal System'*:
- ▶ First he fitted ellipsoids and then calculated **gravitational potential**.
- ▶ In the vertical direction assumed **hydrostatic equilibrium** with velocity dispersion **12 km/s**.
- ▶ *'Mass of dark matter in the Universe' ... 'cannot be excessive'*.
- ▶ Fit Kapteyn data with isothermal sheet:  $z_0 = 650$  pc.
- ▶ Modern:  $z_0 \sim 700$  pc and velocity dispersion about **17 km/s**.





- ▶ Kapteyn (1922) in the horizontal direction.
- ▶ Add centrifugal force: between 0.5 and 1.5 kpc from center rotation of 20 km/s required.
- ▶ That meant that the rotation was seen in the Star Streams!
- ▶ Sun cannot be in center; chose 650 pc radial displacement.
- ▶ From (son-in-law) Ejnar Hertzsprung from distribution of Cepheids: vertical displacement 38 pc.

- ▶ Kapteyn's Universe was a **consistent, dynamical system**.
- ▶ It explained both the **distribution** and the **motions**.
- ▶ What was wrong were **two** parts:
  1. **Transparency of space** – Observational evidence was Shapley's colors of M13 stars.
  2. **Star Streams versus velocity ellipsoid** – Observational evidence was very different make-up in terms of spectral types.
- ▶ Kapteyn constructed his model just before retirement and died soon afterwards,
- ▶ Important developments occurred only a few years later.
- ▶ He left Dutch astronomy in the hands of protégés like **van Rhijn** in Groningen and **de Sitter** and **Hertzsprung** (and later **Oort**) in Leiden.

The Kapteyn Astronomical Laboratory and the Mt. Wilson Kapteyn Cottage.



THE END